# The calc package Infix notation arithmetic in $IAT_FX^*$

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### Abstract

The calc package reimplements the  $L^{A}T_{E}X$  commands <code>\setcounter</code>, <code>\addtocounter</code>, <code>\setlength</code>, and <code>\addtolength</code>. Instead of a simple value, these commands now accept an infix notation expression.

### 1 Introduction

Arithmetic in  $T_EX$  is done using low-level operations such as **\advance** and **\multiply**. This may be acceptable when developing a macro package, but it is not an acceptable interface for the end-user.

This package introduces proper infix notation arithmetic which is much more familiar to most people. The infix notation is more readable and easier to modify than the alternative: a sequence of assignment and arithmetic instructions. One of the arithmetic instructions (\divide) does not even have an equivalent in standard LATEX.

The infix expressions can be used in arguments to macros (the calc package doesn't employ category code changes to achieve its goals).<sup>1</sup>

# 2 Informal description

Standard IATEX provides the following set of commands to manipulate counters and lengths [2, pages 194 and 216].

<sup>\*</sup>We thank Frank Mittelbach for his valuable comments and suggestions which have greatly improved this package.

 $<sup>^1\</sup>mathrm{However},$  it therefore assumes that the category codes of the special characters, such as (\*/) in its syntax do not change.

- $\content ctr \{num\}\$  increments the value of the counter ctr by (the value of) num. (Fragile)
- \setlength{cmd}{len} sets the value of the length command cmd equal to (the
  value of) len. (Robust)
- \addtolength{cmd}{len} sets the value of the length command cmd equal to its
   current value plus (the value of) len. (Robust)

(The \setCounter and \addtocounter commands have global effect, while the \setlength and \addtolength commands obey the normal scoping rules.) In standard LATEX, the arguments to these commands must be simple values. The calc package extends these commands to accept infix notation expressions, denoting values of appropriate types. Using the calc package, *num* is replaced by (integer expression), and *len* is replaced by (glue expression). The formal syntax of (integer expression) and (glue expression) is given below.

In addition to these commands to explicitly set a length, many IATEX commands take a length argument. After loading this package, most of these commands will accept a (glue expression). This includes the optional width argument of \makebox, the width argument of \parbox, minipage, and a tabular p-column, and many similar constructions. (This package does not redefine any of these commands, but they are defined by default to read their arguments by \setlength and so automatically benefit from the enhanced \setlength command provided by this package.)

In the following, we shall use standard TEX terminology. The correspondence between TEX and LATEX terminology is as follows: LATEX counters correspond to TEX's count registers; they hold quantities of type (number). LATEX length commands correspond to TEX's dimen (for rigid lengths) and skip (for rubber lengths) registers; they hold quantities of types (dimen) and (glue), respectively.

 $T_{E}X$  gives us primitive operations to perform arithmetic on registers as follows:

- addition and subtraction on all types of quantities without restrictions;
- multiplication and division by an *integer* can be performed on a register of any type;
- multiplication by a *real* number (i.e., a number with a fractional part) can be performed on a register of any type, but the stretch and shrink components of a glue quantity are discarded.

The calc package uses these  $T_EX$  primitives but provides a more user-friendly notation for expressing the arithmetic.

An expression is formed of numerical quantities (such as explicit constants and IATEX counters and length commands) and binary operators (the tokens '+', '-', '\*', and '/' with their usual meaning) using the familiar infix notation; parentheses may be used to override the usual precedences (that multiplication/division have higher precedence than addition/subtraction).

Expressions must be properly typed. This means, e.g., that a dimen expression must be a sum of dimen terms: i.e., you cannot say '2cm+4' but '2cm+4pt' is valid.

In a dimen term, the dimension part must come first; the same holds for glue terms. Also, multiplication and division by non-integer quantities require a special syntax; see below. Evaluation of subexpressions at the same level of precedence proceeds from left to right. Consider a dimen term such as "4cm\*3\*4". First, the value of the factor 4cm is assigned to a dimen register, then this register is multiplied by 3 (using \multiply), and, finally, the register is multiplied by 4 (again using \multiply). This also explains why the dimension part (i.e., the part with the unit designation) must come first; T<sub>E</sub>X simply doesn't allow untyped constants to be assigned to a dimen register.

The calc package also allows multiplication and division by real numbers. However, a special syntax is required: you must use  $\real{\langle decimal constant \rangle}^2$  or  $\ratio{\langle dimen expression \rangle}{\langle dimen expression \rangle}$  to denote a real value to be used for multiplication/division. The first form has the obvious meaning, and the second form denotes the number obtained by dividing the value of the first expression by the value of the second expression.

A later addition to the package (in June 1998) allows an additional method of specifying a factor of type dimen by setting some text (in LR-mode) and measuring its dimensions: these are denoted as follows.

These calculate the natural sizes of the  $\langle \text{text} \rangle$  in exactly the same way as is done for the commands settowidth etc. on Page 216 of the manual [2]. In August 2005 the package was further extended to provide the command

```
\totalheightof{\langle text \rangle}
```

This command does exactly what you'd expect from its name. Additionally the package also provides the command

Note that there is a small difference in the usage of these two methods of accessing text dimensions. After \settowidth{\txtwd}{Some text} you can use:

\setlength{\parskip}{0.68\textwd}

whereas using the more direct access to the width of the text requires the longer form for multiplication, thus:

\setlength{\parskip}{\widthof{Some text} \* \real{0.68}}

T<sub>E</sub>X discards the stretch and shrink components of glue when glue is multiplied by a real number. So, for example,

\setlength{\parskip}{3pt plus 3pt \* \real{1.5}}

will set the paragraph separation to 4.5pt with no stretch or shrink. Incidentally, note how spaces can be used to enhance readability. When TEX is scanning for a  $\langle number \rangle$  etc. it is common to terminate the scanning with a space token or by inserting \relax. As of version 4.3 calc allows \relax tokens to appear in places where they would usually be used for terminating TEX's scanning. In short this is just before any of +-\*/) or at the end of the expression being evaluated.

<sup>&</sup>lt;sup>2</sup>Actually, instead of  $\langle \text{decimal constant} \rangle$ , the more general  $\langle \text{optional signs} \rangle \langle \text{factor} \rangle$  can be used. However, that doesn't add any extra expressive power to the language of infix expressions.

When  $T_EX$  performs arithmetic on integers, any fractional part of the results are discarded. For example,

```
\setcounter{x}{7/2}
\setcounter{y}{3*\real{1.6}}
\setcounter{z}{3*\real{1.7}}
```

will assign the value 3 to the counter  $\mathbf{x}$ , the value 4 to  $\mathbf{y}$ , and the value 5 to  $\mathbf{z}$ . This truncation also applies to *intermediate* results in the sequential computation of a composite expression; thus, the following command

 $\operatorname{x}{3 * \operatorname{real}{1.6} * \operatorname{real}{1.7}}$ 

will assign 6 to x.

As an example of the use of **\ratio**, consider the problem of scaling a figure to occupy the full width (i.e., **\textwidth**) of the body of a page. Assume that the original dimensions of the figure are given by the dimen (length) variables, **\Xsize** and **\Ysize**. The height of the scaled figure can then be expressed by

\setlength{\newYsize}{\Ysize\*\ratio{\textwidth}{\Xsize}}

Another new feature introduced in August 2005 was max and min operations with associated macros

```
\maxof{\type expression\}{\type expression\}
\minof{\type expression\}{\type expression\}
```

When type is either  $\langle glue \rangle$  or  $\langle dimen \rangle$  these macros are allowed only as part of addition or subtraction but when type is  $\langle integer \rangle$  they can also be used when multiplying and dividing. In the latter case they follow the same syntax rules as **\ratio** and **\real** which means they must come after the \* or the /. Thus

```
\table \table
```

will assign  $3 \times \max(9, 12) + \min(3, 4) = 39$  to x. Similarly

```
\setlength{\parindent}{%
    \minof{3pt}{\parskip}*\real{1.5}*\maxof{2*\real{1.6}}{2-1}}
```

will assign  $\min(13.5\text{pt}, 4.5\text{parskip})$  to parindent

## 3 Formal syntax

The syntax is described by the following set of rules. Note that the definitions of  $\langle \text{number} \rangle$ ,  $\langle \text{dimen} \rangle$ ,  $\langle \text{glue} \rangle$ ,  $\langle \text{decimal constant} \rangle$ , and  $\langle \text{plus or minus} \rangle$  are as in Chapter 24 of The T<sub>E</sub>Xbook [1]; and  $\langle \text{text} \rangle$  is LR-mode material, as in the manual [2]. We use *type* as a meta-variable, standing for 'integer', 'dimen', and 'glue'.<sup>3</sup>

```
\begin{array}{l} \langle type \; \mathrm{expression} \rangle \longrightarrow \langle type \; \mathrm{term} \rangle \\ & \mid \langle type \; \mathrm{expression} \rangle \langle \mathrm{plus} \; \mathrm{or} \; \mathrm{minus} \rangle \langle type \; \mathrm{term} \rangle \\ \langle type \; \mathrm{term} \rangle \longrightarrow \langle type \; \mathrm{term} \rangle \langle type \; \mathrm{scan} \; \mathrm{stop} \rangle \; \mid \langle type \; \mathrm{factor} \rangle \\ & \mid \langle type \; \mathrm{term} \rangle \langle \mathrm{multiply} \; \mathrm{or} \; \mathrm{divide} \rangle \langle \mathrm{integer} \rangle \end{array}
```

 $^{3}$ This version of the calc package doesn't support evaluation of muglue expressions.

 $|\langle type \ term \rangle \langle multiply \ or \ divide \rangle \langle real \ number \rangle$  $|\langle type \ term \rangle \langle multiply \ or \ divide \rangle \langle max \ or \ min \ integer \rangle$  $\langle type \text{ scan stop} \rangle \longrightarrow \langle empty \rangle \mid \langle optional space \rangle \mid \text{`relax}$  $\langle type | factor \rangle \longrightarrow \langle type \rangle | \langle text | dimen | factor \rangle | \langle max | or min | type \rangle$  $| (_{12} \langle type \text{ expression} \rangle)_{12}$  $\langle \text{integer} \rangle \longrightarrow \langle \text{number} \rangle$  $\langle \max \text{ or } \min type \rangle$  $\rightarrow$  (max or min command) { (type expression) } { (type expression) }  $\langle \max \text{ or } \min \text{ command} \rangle \longrightarrow \backslash \max of | \backslash \min of$  $\langle \text{text dimen factor} \rangle \longrightarrow \langle \text{text dimen command} \rangle \{ \langle \text{text} \rangle \}$  $\langle \text{text dimen command} \rangle \longrightarrow \langle \text{widthof} | \rangle \langle \text{heightof} | \rangle \langle \text{depthof} \rangle$ \totalheightof (multiply or divide)  $\longrightarrow *_{12} | /_{12}$  $(real number) \longrightarrow \langle dimen expression \rangle \{ (dimen expression) \}$ | real(optional signs)(decimal constant) $\langle \text{plus or minus} \rangle \longrightarrow +_{12} \mid -_{12}$  $\langle \text{decimal constant} \rangle \longrightarrow ._{12} \mid ,_{12} \mid \langle \text{digit} \rangle \langle \text{decimal constant} \rangle$  $|\langle decimal constant \rangle \langle digit \rangle$  $\langle \text{digit} \rangle \longrightarrow 0_{12} \mid 1_{12} \mid 2_{12} \mid 3_{12} \mid 4_{12} \mid 5_{12} \mid 6_{12} \mid 7_{12} \mid 8_{12} \mid 9_{12}$  $\langle \text{optional signs} \rangle \longrightarrow \langle \text{optional spaces} \rangle$  $|\langle \text{optional signs} \rangle \langle \text{plus or minus} \rangle \langle \text{optional spaces} \rangle$ 

Relying heavily on  $T_EX$  to do the underlying assignments, it is only natural for calc to simulate  $T_EX$ 's parsing machinery for these quantities. Therefore it a) imposes the same restrictions on the catcode of syntax characters as  $T_EX$  and b) tries to expand its argument fully. a) means that implicit characters for the tokens  $*_{12}$ ,  $/_{12}$ ,  $(_{12}$ , and  $)_{12}$  will not work<sup>4</sup> but because of b), the expansion should allow you to use macros that expand to explicit syntax characters.

### 4 The evaluation scheme

In this section, we shall for simplicity consider only expressions containing '+' (addition) and '\*' (multiplication) operators. It is trivial to add subtraction and division.

An expression E is a sum of terms:  $T_1 + \cdots + T_n$ ; a term is a product of factors:  $F_1 * \cdots * F_m$ ; a factor is either a simple numeric quantity f (like  $\langle \text{number} \rangle$  as described in the T<sub>E</sub>Xbook), or a parenthesized expression (E').

Since the  $T_EX$  engine can only execute arithmetic operations in a machinecode like manner, we have to find a way to translate the infix notation into this 'instruction set'.

 $<sup>^4{\</sup>rm eT}_{\rm E\!X}$  also assumes these catcodes when parsing a <code>\numexpr</code>, <code>\dimexpr</code>, <code>\glueexpr</code>, or <code>\muglueexpr</code> and does not allow implicit characters.

Our goal is to design a translation scheme that translates X (an expression, a term, or a factor) into a sequence of TEX instructions that does the following [Invariance Property]: correctly evaluates X, leaves the result in a global register A (using a global assignment), and does not perform global assignments to the scratch register B; moreover, the code sequence must be balanced with respect to TEX groups. We shall denote the code sequence corresponding to X by [X].

In the replacement code specified below, we use the following conventions:

- A and B denote registers; all assignments to A will be global, and all assignments to B will be local.
- "\equiv "means global assignment to the register on the lhs.
- "
  —" means local assignment to the register on the lhs.
- " $_{\hookrightarrow[C]}$ " means "save the code C until the current group (scope) ends, then execute it." This corresponds to the T<sub>E</sub>X-primitive \aftergroup.
- "{" denotes the start of a new group, and "}" denotes the end of a group.

Let us consider an expression  $T_1+T_2+\cdots+T_n$ . Assuming that  $[\![T_k]\!]$   $(1 \le k \le n)$  attains the stated goal, the following code clearly attains the stated goal for their sum:

$$\begin{bmatrix} T_1 + T_2 + \dots + T_n \end{bmatrix} \implies \{ \begin{bmatrix} T_1 \end{bmatrix} \} B \leftarrow A \quad \{ \begin{bmatrix} T_2 \end{bmatrix} \} B \leftarrow B + A$$
$$\dots \quad \{ \begin{bmatrix} T_n \end{bmatrix} \} B \leftarrow B + A \quad A \Leftarrow B$$

Note the extra level of grouping enclosing each of  $[T_1], [T_2], \ldots, [T_n]$ . This will ensure that register B, used to compute the sum of the terms, is not clobbered by the intermediate computations of the individual terms. Actually, the group enclosing  $[T_1]$  is unnecessary, but it turns out to be simpler if all terms are treated the same way.

The code sequence "{  $\llbracket T_2 \rrbracket$ }  $B \leftarrow B + A$ " can be translated into the following equivalent code sequence: "{  ${ { }_{\hookrightarrow [B \leftarrow B + A]} \llbracket T_2 \rrbracket}$  }". This observation turns out to be the key to the implementation: The " ${ }_{\hookrightarrow [B \leftarrow B + A]}$ " is generated *before*  $T_2$  is translated, at the same time as the '+' operator between  $T_1$  and  $T_2$  is seen.

Now, the specification of the translation scheme is straightforward:

$$\begin{split} \llbracket f \rrbracket &\implies A \leftarrow f \\ \llbracket (E') \rrbracket &\implies \llbracket E' \rrbracket \\ \llbracket T_1 + T_2 + \dots + T_n \rrbracket &\implies \{ {}_{\hookrightarrow [B \leftarrow A]} \llbracket T_1 \rrbracket \} \quad \{ {}_{\hookrightarrow [B \leftarrow B + A]} \llbracket T_2 \rrbracket \} \\ & \dots \quad \{ {}_{\hookrightarrow [B \leftarrow B + A]} \llbracket T_n \rrbracket \} \quad A \leftarrow B \\ \llbracket F_1 * F_2 * \dots * F_m \rrbracket &\implies \{ {}_{\hookrightarrow [B \leftarrow A]} \llbracket F_1 \rrbracket \} \quad \{ {}_{\hookrightarrow [B \leftarrow B * A]} \llbracket F_2 \rrbracket \} \\ & \dots \quad \{ {}_{\hookrightarrow [B \leftarrow B * A]} \llbracket F_m \rrbracket \} \quad A \leftarrow B \end{split}$$

By structural induction, it is easily seen that the stated property is attained.

By inspection of this translation scheme, we see that we have to generate the following code:

• we must generate " $\{ {}_{{}_{\bigcirc}[B \leftarrow A]} \{ {}_{{}_{\bigcirc}[B \leftarrow A]} \}$ " at the left border of an expression (i.e., for each left parenthesis and the implicit left parenthesis at the beginning of the whole expression);

- we must generate "}A ⇐ B}A ⇐ B" at the right border of an expression (i.e., each right parenthesis and the implicit right parenthesis at the end of the full expression);
- '\*' is replaced by "} $\{ \subseteq B \in B \in A^{n} ]$ ";
- '+' is replaced by "} $A \leftarrow B$ { $\subseteq B \leftarrow B+A$ ]{ $\subseteq B \leftarrow A$ ]";
- when we see (expect) a numeric quantity, we insert the assignment code " $A \Leftarrow$ " in front of the quantity and let T<sub>E</sub>X parse it.

### 5 Implementation

For brevity define

 $\langle numeric \rangle \longrightarrow \langle number \rangle \mid \langle dimen \rangle \mid \langle glue \rangle \mid \langle muglue \rangle$ 

So far we have ignored the question of how to determine the type of register to be used in the code. However, it is easy to see that (1) '\*' always initiates an  $\langle \text{integer factor} \rangle$ , (2) all  $\langle \text{numeric} \rangle$ s in an expression, except those which are part of an  $\langle \text{integer factor} \rangle$ , are of the same type as the whole expression, and all  $\langle \text{numeric} \rangle$ s in an  $\langle \text{integer factor} \rangle$  are  $\langle \text{number} \rangle$ s.

We have to ensure that A and B always have an appropriate type for the  $\langle numeric \rangle$ s they manipulate. We can achieve this by having an instance of A and B for each type. Initially, A and B refer to registers of the proper type for the whole expression. When an  $\langle integer \ factor \rangle$  is expected, we must change A and B to refer to integer type registers. We can accomplish this by including instructions to change the type of A and B to integer type as part of the replacement code for '\*; if we append such instructions to the replacement code described above, we also ensure that the type-change is local (provided that the type-changing instructions only have local effect). However, note that the instance of A referred to in  $\hookrightarrow_{[B \leftarrow B*A]}$  is the integer instance of A.

We shall use **\begingroup** and **\endgroup** for the open-group and close-group characters. This avoids problems with spacing in math (as pointed out to us by Frank Mittelbach).

### 5.1 Getting started

Now we have enough insight to do the actual implementation in  $T_EX$ . First, we announce the macro package.<sup>5</sup>

```
1 \langle * \mathsf{package} \rangle
```

```
2 %\NeedsTeXFormat{LaTeX2e}
```

```
3 %\ProvidesPackage{calc}[\filedate\space\fileversion]
```

### 5.2 Assignment macros

\calc@assign@generic

The \calc@assign@generic macro takes four arguments: (1 and 2) the registers to be used for global and local manipulations, respectively; (3) the lvalue part; (4) the expression to be evaluated.

<sup>&</sup>lt;sup>5</sup>Code moved to top of file

The third argument (the lvalue) will be used as a prefix to a register that contains the value of the specified expression (the fourth argument).

In general, an lvalue is anything that may be followed by a variable of the appropriate type. As an example, \linepenalty and \global\advance\linepenalty may both be followed by an  $\langle \text{integer variable} \rangle$ .

The macros described below refer to the registers by the names \calcQA and \calc@B; this is accomplished by \let-assignments.

As discovered in Section 4, we have to generate code as if the expression is parenthesized. As described below, \calc@open is the macro that replaces a left parenthesis by its corresponding T<sub>F</sub>X code sequence. When the scanning process sees the exclamation point, it generates an \endgroup and stops. As we recall from Section 4, the correct expansion of a right parenthesis is " $A \leftarrow B A \leftarrow$ B". The remaining tokens of this expansion are inserted explicitly, except that the last assignment has been replaced by the lvalue part (i.e., argument #3 of \calc@assign@generic) followed by \calc@B.

```
4 \def\calc@assign@generic#1#2#3#4{\let\calc@A#1\let\calc@B#2%
```

```
5
      \calc@open(#4!%
```

```
6
     \global\calc@A\calc@B\endgroup#3\calc@B}
```

We need three instances of the \calc@assign@generic macro, corresponding to \calc@assign@count the types  $\langle \text{integer} \rangle$ ,  $\langle \text{dimen} \rangle$ , and  $\langle \text{glue} \rangle$ . \calc@assign@dimen

```
\calc@assign@skip
```

```
7 \def\calc@assign@count{\calc@assign@generic\calc@Acount\calc@Bcount}
8 \def\calc@assign@dimen{\calc@assign@generic\calc@Adimen\calc@Bdimen}
```

These macros each refer to two registers, one to be used globally and one to be used locally. We must allocate these registers.

10 \newcount\calc@Acount	\newcount\calc@Bcount
11 \newdimen\calc@Adimen	\newdimen\calc@Bdimen
12 \newskip\calc@Askip	\newskip\calc@Bskip

#### The LATEX interface 5.3

As promised, we redefine the following standard LATEX commands: \setcounter, \addtocounter, \setlength, and \addtolength.

```
13 \def\setcounter#1#2{\@ifundefined{c@#1}{\@nocounterr{#1}}%
14
```

```
{\calc@assign@count{\global\csname c@#1\endcsname}{#2}}}
```

```
15
    \def\addtocounter#1#2{\@ifundefined{c@#1}{\@nocounterr{#1}}%
```

```
{\calc@assign@count{\global\advance\csname c@#1\endcsname}{#2}}}%
16
```

We also fix \stepcounter to not go through the whole calc process.

- \def\stepcounter#1{\@ifundefined {c@#1}% 17
- {\@nocounterr {#1}}% 18
- {\global\advance\csname c@#1\endcsname \@ne 19
- 20\begingroup

21

- \let\@elt\@stpelt \csname cl@#1\endcsname
- 22\endgroup}}%

If the amstext package is loaded we must add the \iffirstchoice@ switch as well. We patch the commands this way since it's good practice when we know how many arguments they take.

\setcounter \addtocounter \steptocounter \setlength \addtolength

```
23 \@ifpackageloaded{amstext}{%
   \expandafter\def\expandafter\stepcounter
24
      \expandafter#\expandafter1\expandafter{%
25
      \expandafter\iffirstchoice@\stepcounter{#1}\fi
26
   }
27
   \expandafter\def\expandafter\addtocounter
28
      \expandafter#\expandafter1\expandafter#\expandafter2\expandafter{%
29
      \expandafter\iffirstchoice@\addtocounter{#1}{#2}\fi
30
31 }
32 }{}
33 \DeclareRobustCommand\setlength{\calc@assign@skip}
34 \DeclareRobustCommand\addtolength[1]{\calc@assign@skip{\advance#1}}
```

(\setlength and \addtolength are robust according to [2].)

### 5.4 The scanner

We evaluate expressions by explicit scanning of characters. We do not rely on active characters for this.

The scanner consists of two parts, \calc@pre@scan and \calc@post@scan; \calc@pre@scan consumes left parentheses, and \calc@post@scan consumes binary operator, \real, \ratio, and right parenthesis tokens.

\calc@pre@scan Note that this is called at least once on every use of calc processing, even when \@calc@pre@scan none of the extended syntax is present; it therefore needs to be made very efficient.

It reads the initial part of expressions, until some  $\langle \text{text dimen factor} \rangle$  or  $\langle \text{numeric} \rangle$  is seen; in fact, anything not explicitly recognized here is taken to be a  $\langle \text{numeric} \rangle$  of some sort as this allows unary '+' and unary '-' to be treated easily and correctly<sup>6</sup> but means that anything illegal will simply generate a T<sub>E</sub>X-level error, often a reasonably comprehensible one!

The \romannumeral-'\a part is a little trick which forces expansion in case #1 is a normal macro, something that occurs from time to time. A conditional test inside will possibly leave a trailing \fi but this remnant is removed later when \calc@post@scan performs the same trick.

The many \expandafters are needed to efficiently end the nested conditionals so that \calc@textsize and \calc@maxmin@addsub can process their argument.

```
35 \def\calc@pre@scan#1{%
    \expandafter\@calc@pre@scan\romannumeral-'\a#1}
36
  \def\@calc@pre@scan#1{%
37
    ifx(#1%)
38
      \expandafter\calc@open
39
    \else
40
41
      \ifx\widthof#1%
42
        \expandafter\expandafter\expandafter\calc@textsize
43
      \else
44
        \ifx\maxof#1%
          \expandafter\expandafter\expandafter\expandafter
45
          \expandafter\expandafter\calc@maxmin@addsub
46
47
        \else
          \calc@numeric% no \expandafter needed for this one.
48
```

<sup>&</sup>lt;sup>6</sup>In the few contexts where signs are allowed: this could, I think, be extended (CAR).

```
\fi
                 49
                       \fi
                 50
                     \fi
                 51
                     #1}
                 52
   \calc@open
                \calc@open is used when there is a left parenthesis right ahead. This parenthesis
                is replaced by TEX code corresponding to the code sequence "\{ \subseteq B \in A \} \{ \subseteq B \in A \}"
   \calc@initB
                derived in Section 4. Finally, \calc@pre@scan is called again.
                 53 \def\calc@open({\begingroup\aftergroup\calc@initB
                 54
                      \begingroup\aftergroup\calc@initB
                 55
                      \calc@pre@scan}
                 56 \def\calc@initB{\calc@B\calc@A}
                \calcOnumeric assigns the following value to \calcOA and then transfers control
\calc@numeric
                to \calc@post@scan.
                 57 \def\calc@numeric{\afterassignment\calc@post@scan \global\calc@A}
      \widthof
                These do not need any particular definition when they are scanned so, for effi-
     \heightof
                ciency and robustness, we make them all equivalent to the same harmless (I hope)
                unexpandable command.<sup>7</sup> Thus the test in \@calc@pre@scan finds any of them.
      \depthof
                   As we have to check for these commands explicitly we must ensure that our
\totalheightof
                definition wins. Using \newcommand gives an error when loading calc and may
                be mildly surprising. This should be a little more informative.
                 58 \@for\reserved@a:=widthof,heightof,depthof,totalheightof,maxof,minof\do
                 59 {\@ifundefined{\reserved@a}{}{%
                     \PackageError{calc}{%
                 60
                     The\space calc\space package\space reserves\space the\space
                 61
                     command\space name\space '\@backslashchar\reserved@a'\MessageBreak
                 62
                     but\space it\space has\space already\space been\space defined\space
                 63
                     with\space the\space meaning\MessageBreak
                 64
                     65
                     This\space original\space definition\space will\space be\space lost}%
                 66
                 67
                     {If\space you\space need\space a\space command\space with\space
                     this\space definition,\space you\space must\space use\space a\space
                 68
                     different\space name.}}%
                 69
                 70 }
                 71 \let\widthof\ignorespaces
                 72 \let\heightof\ignorespaces
                 73 \let\depthof\ignorespaces
                 74 \let\totalheightof\ignorespaces
                The presence of the above four commands invokes this code, where we must dis-
\calc@textsize
                tinguish them from each other. This implementation is somewhat optimized by
                using low-level code from the commands \settowidth, etc.<sup>8</sup>
```

Within the text argument we must restore the normal meanings of the four user-level commands since arbitrary material can appear in here, including further uses of calc.

```
75 \def\calc@textsize #1#2{%
76 \begingroup
77 \let\widthof\wd
```

<sup>&</sup>lt;sup>7</sup>If this level of safety is not needed then the code can be sped up: CAR.

 $<sup>^{8}\</sup>mathrm{It}$  is based on suggestions by Donald Arseneau and David Carlisle.

- 78 \let\heightof\ht
- 79 \let\depthof\dp
- 80 \def\totalheightof{\ht\dp}%

We must expand the argument one level if it's \totalheightof and it doesn't hurt the other three.

```
\expandafter\@settodim\expandafter{#1}%
81
82
         {\global\calc@A}%
         {%
83
          \let\widthof\ignorespaces
84
          \let\heightof\ignorespaces
85
          \let\depthof\ignorespaces
86
87
          \let\totalheightof\ignorespaces
88
          #2}%
89
    \endgroup
    \calc@post@scan}
90
```

\calc@post@scan \@calc@post@scan The macro  $\calc@post@scan</code> is called right after a value has been read. At this point, a binary operator, a sequence of right parentheses, an optional <math>\relax$ , and the end-of-expression mark ('!') is allowed.<sup>9</sup> Depending on our findings, we call a suitable macro to generate the corresponding T<sub>E</sub>X code (except when we detect the end-of-expression marker: then scanning ends, and control is returned to  $\calc@assign@generic$ ).

This macro may be optimized by selecting a different order of ifx-tests. The test for '!' (end-of-expression) is placed first as it will always be performed: this is the only test to be performed if the expression consists of a single (numeric). This ensures that documents that do not use the extra expressive power provided by the calc package only suffer a minimum slowdown in processing time.

```
91 \def\calc@post@scan#1{%
92
   \expandafter\@calc@post@scan\romannumeral-'\a#1}
93 \def\@calc@post@scan#1{%
94
     \ifx#1!\let\calc@next\endgroup \else
       \ifx#1+\let\calc@next\calc@add \else
95
         \ifx#1-\let\calc@next\calc@subtract \else
96
           \ifx#1*\let\calc@next\calc@multiplyx \else
97
             \ifx#1/\let\calc@next\calc@dividex \else
98
                \ifx#1)\let\calc@next\calc@close \else
99
                  \ifx#1\relax\let\calc@next\calc@post@scan \else
100
                    \def\calc@next{\calc@error#1}%
101
                  \fi
102
                \fi
103
             \fi
104
105
           \fi
106
         \fi
       \fi
107
     \fi
108
     calc@next
109
```

\calc@add \calc@subtract \calc@generic@add \calc@addAtoB \calc@subtractAfromB

The replacement code for the binary operators '+' and '-' follow a common pattern; the only difference is the token that is stored away by \aftergroup. After this replacement code, control is transferred to \calc@pre@scan.

<sup>9</sup>Is ! a good choice, CAR?

```
110 \def\calc@add{\calc@generic@add\calc@addAtoB}
111 \def\calc@subtract{\calc@generic@add\calc@subtractAfromB}
112 \def\calc@generic@add#1{\endgroup\global\calc@A\calc@B\endgroup
113 \begingroup\aftergroup#1\begingroup\aftergroup\calc@initB
114 \calc@pre@scan}
115 \def\calc@addAtoB{\advance\calc@B\calc@A}
116 \def\calc@subtractAfromB{\advance\calc@B-\calc@A}
```

\real \ratio \calc@ratio@x \calc@real@x The multiplicative operators, '\*' and '/', may be followed by a \real, \ratio, \minof, or \maxof token. The last two of these control sequences are defined by calc as they are needed by the scanner for addition or subtraction while the first two are not defined (at least not by the calc package); this, unfortunately, leaves them highly non-robust. We therefore equate them to \relax but only if they have not already been defined<sup>10</sup> (by some other package: dangerous but possible!); this will also make them appear to be undefined to a LATEX user (also possibly dangerous).

```
117 \ifx\real\@undefined\let\real\relax\fi
118 \ifx\ratio\@undefined\let\ratio\relax\fi
In order to test for \real or \ratio, we define these two.<sup>11</sup>
119 \def\calc@ratio@x{\ratio}
120 \def\calc@real@x{\real}
```

\calc@multiplyx Test which operator followed \* or /. If none followed it's just a standard multi-\calc@dividex plication or division.

```
121 \def\calc@multiplyx#1{\def\calc@tmp{#1}%
     \ifx\calc@tmp\calc@ratio@x \let\calc@next\calc@ratio@multiply \else
122
       \ifx\calc@tmp\calc@real@x \let\calc@next\calc@real@multiply \else
123
124
         \ifx\maxof#1\let\calc@next\calc@maxmin@multiply \else
125
           \let\calc@next\calc@multiply
         \fi
126
127
       \fi
     \fi
128
     \calc@next#1}
129
130 \def\calc@dividex#1{\def\calc@tmp{#1}%
     \ifx\calc@tmp\calc@ratio@x \let\calc@next\calc@ratio@divide \else
131
       \ifx\calc@tmp\calc@real@x \let\calc@next\calc@real@divide \else
132
         \ifx\maxof#1\let\calc@next\calc@maxmin@divide \else
133
           \let\calc@next\calc@divide
134
135
         \fi
       \fi
136
     \fi
137
     \calc@next#1}
138
```

\calc@multiply \calc@divide \calc@generic@multiply \calc@multiplyBbyA \calc@divideBbyA The binary operators '\*' and '/' also insert code as determined above. Moreover, the meaning of \calc@A and \calc@B is changed as factors following a multiplication and division operator always have integer type; the original meaning of these macros will be restored when the factor has been read and evaluated.

```
139 \def\calc@multiply{\calc@generic@multiply\calc@multiplyBbyA}
140 \def\calc@divide{\calc@generic@multiply\calc@divideBbyA}
141 \def\calc@generic@multiply#1{\endgroup\begingroup
```

```
<sup>10</sup>Suggested code from David Carlisle.
```

<sup>&</sup>lt;sup>11</sup>May not need the extra names, CAR?

```
142 \let\calc@A\calc@Acount \let\calc@B\calc@Bcount
143 \aftergroup#1\calc@pre@scan}
144 \def\calc@multiplyBbyA{\multiply\calc@B\calc@Acount}
145 \def\calc@divideBbyA{\divide\calc@B\calc@Acount}
```

Since the value to use in the multiplication/division operation is stored in the \calc@Acount register, the \calc@multiplyBbyA and \calc@divideBbyA macros use this register.

**\calc@close \calc@close** generates code for a right parenthesis (which was derived to be " $A \leftarrow B A \leftarrow B$ " in Section 4). After this code, the control is returned to **\calc@post@scan** in order to look for another right parenthesis or a binary operator.

146 \def\calc@close

```
147 {\endgroup\global\calc@A\calc@B
```

- 148 \endgroup\global\calc@A\calc@B
- 149  $\calc@post@scan$ }

### 5.5 Calculating a ratio

# \calc@ratio@multiply \calc@ratio@divide

When \calc@post@scan encounters a \ratio control sequence, it hands control to one of the macros \calc@ratio@multiply or \calc@ratio@divide, depending on the preceding character. Those macros both forward the control to the macro \calc@ratio@evaluate, which performs two steps: (1) it calculates the ratio, which is saved in the global macro token \calc@the@ratio; (2) it makes sure that the value of \calc@B will be multiplied by the ratio as soon as the current group ends.

The following macros call \calc@ratio@evaluate which multiplies \calc@B by the ratio, but \calc@ratio@divide flips the arguments so that the 'opposite' fraction is actually evaluated.

```
150 \def\calc@ratio@multiply\ratio{\calc@ratio@evaluate}
151 \def\calc@ratio@divide\ratio#1#2{\calc@ratio@evaluate{#2}{#1}}
```

\calc@Ccount We shall need two registers for temporary usage in the calculations. We can save \calc@numerator one register since we can reuse \calc@Bcount. \calc@denominator 152 \newcount\calc@Ccount

```
152 \newcount\calc@Ccount
153 \let\calc@numerator=\calc@Bcount
154 \let\calc@denominator=\calc@Ccount
```

\calc@ratio@evaluate Here is the macro that handles the actual evaluation of ratios. The procedure is this: First, the two expressions are evaluated and coerced to integers. The whole procedure is enclosed in a group to be able to use the registers \calc@numerator and \calc@denominator for temporary manipulations.

```
155 \def\calc@ratio@evaluate#1#2{%
```

156 \endgroup\begingroup

```
157 \calc@assign@dimen\calc@numerator{#1}%
```

158 \calc@assign@dimen\calc@denominator{#2}%

Here we calculate the ratio. First, we check for negative numerator and/or denominator; note that  $T_EX$  interprets two minus signs the same as a plus sign. Then, we calculate the integer part. The minus sign(s), the integer part, and a decimal point, form the initial expansion of the \calc@the@ratio macro.

159	\gdef\calc@the@ratio{}%
160	\ifnum\calc@numerator<0 \calc@numerator-\calc@numerator
161	\gdef\calc@the@ratio{-}%
162	\fi
163	\ifnum\calc@denominator<0 \calc@denominator-\calc@denominator
164	\xdef\calc@the@ratio{\calc@the@ratio-}%
165	\fi
166	\calc@Acount\calc@numerator
167	\divide\calc@Acount\calc@denominator
168	\xdef\calc@the@ratio{\calc@the@ratio\number\calc@Acount.}%

Now we generate the digits after the decimal point, one at a time. When  $T_EX$  scans these digits (in the actual multiplication operation), it forms a fixed-point number with 16 bits for the fractional part. We hope that six digits is sufficient, even though the last digit may not be rounded correctly.

```
169\calc@next@digit \calc@next@digit170\calc@next@digit \calc@next@digit
```

171 \endgroup

Now we have the ratio represented (as the expansion of the global macro  $\calc@the@ratio$ ) in the syntax (decimal constant) [1, page 270]. This is fed to  $\calc@multiply@by@real</code> that will perform the actual multiplication. It is important that the multiplication takes place at the correct grouping level so that the correct instance of the$ *B* $register will be used. Also note that we do not need the <math>\aftergroup$  mechanism in this case.

- 172 \calc@multiply@by@real\calc@the@ratio
- 173 \begingroup
- $174 \quad \calc@post@scan}$

The \begingroup inserted before the \calc@post@scan will be matched by the \endgroup generated as part of the replacement of a subsequent binary operator or right parenthesis.

\calc@next@digit			
	175 \def\calc@next@digit{%		
	176	\multiply\calc@Acount\calc@denominator	
	177	\advance\calc@numerator -\calc@Acount	
	178	\multiply\calc@numerator 10	
	179	\calc@Acount\calc@numerator	
	180	\divide\calc@Acount\calc@denominator	
	181	\xdef\calc@the@ratio{\calc@the@ratio\number\calc@Acount}}	
	T .1 (		

\calc@multiply@by@real In the following code, it is important that we first assign the result to a dimen register. Otherwise, TEX won't allow us to multiply with a real number.

182 \def\calc@Bultiply@by@real#1{\calc@Bdimen #1\calc@B \calc@Bdimen} (Note that this code wouldn't work if \calc@B were a muglue register. This is the real reason why the calc package doesn't support muglue expressions. To support muglue expressions in full, the \calc@multiply@by@real macro must use a muglue register instead of \calc@Bdimen when \calc@B is a muglue register; otherwise, a dimen register should be used. Since integer expressions can appear as part of a muglue expression, it would be necessary to determine the correct register to use each time a multiplication is made.)

# 5.6 Multiplication by real numbers

\calc@real@multiply \calc@real@divide \maxof \minof	This is similar to the \calc@ratio@evaluate macro above, except that it is con- siderably simplified since we don't need to calculate the factor explicitly. 183 \def\calc@real@multiply\real#1{\endgroup 184 \calc@multiply@by@real{#1}\begingroup 185 \calc@post@scan} 186 \def\calc@real@divide\real#1{\calc@ratio@evaluate{1pt}{#1pt}} 5.7 max and min operations With version 4.2, the max and min operators were added to calc. The user func- tions for them are \maxof and \minof respectively. These macros are internally similar to \widthof etc. in that they are unexpandable and easily recognizable by the scanner. 187 \let\maxof\@@italiccorr	
	188 \let\minof\@@italiccorr	
\calc@Cskip \ifcalc@count@	The max and min operations take two arguments so we need an extra (skip) register. We also add a switch for determining when to perform a (skip) or a (count) assignment. 189 \newskip\calc@Cskip 190 \newif\ifcalc@count@	
\calc@maxmin@addsub \calc@maxmin@generic	<pre>190 \newif\ifcalc@count@ When doing addition or subtraction with a max or min operator, we first check if \calc@A is a (count) register or not and then set the switch. Then call the real function which sets \calc@A to the desired value and continue as usual with \calc@post@scan. 191 \def\calc@naxmin@addsub#1#2#3{\begingroup 192 \ifr\calc@A\calc@A\count% 193 \calc@count@true 194 \else 195 \calc@count@false 196 \fi 197 \calc@maxmin@generic#1{#2}{#3}% 198 \endgroup 199 \calc@post@scan 200 } Check the switch and do either (count) or (skip) assignments. Note that \maxof and \minof are not set to &gt; and &lt; until after the assignments, which ensures we can nest them without problems. Then set \calc@A to the correct one. 201 \def\calc@maxmin@generic#1#2#3{% 202 \begingroup 203 \ifcalc@count@ 204 \calc@assign@count\calc@Ccount#1\calc@Bcount 205 \calc@assign@count\calc@Ccount#3% 206 \def\minof(&lt;}\def\maxof{&gt;}% 207 \global\calc@A\ifnum\calc@Ccount#1\calc@Bcount 208 \calc@assign@skip\calc@Cskip{#2}% 201 \calc@assign@skip\calc@Cskip{#3}% 202 \besime 203 \calc@assign@skip\calc@Bskip{#3}% 204 \calc@assign@skip\calc@Bskip{#3}% 205 \calc@assign@skip\calc@Bskip{#3}% 206 \calc@assign@skip\calc@Bskip{#3}% 207 \calc@assign@skip\calc@Bskip{#3}% 208 \calc@assign@skip\calc@Bskip{#3}% 209 \calc@assign@skip\calc@Bskip{#3}% 200 \calc@assign@skip\calc@Bskip{#3}% 201 \calc@assign@skip\calc@Bskip{#3}% 20</pre>	

```
212 \def\minof{<}\def\maxof{>}%
213 \global\calc@A\ifdim\calc@Cskip#1\calc@Bskip
214 \calc@Cskip\else\calc@Bskip\fi
215 \fi
216 \endgroup
217 }
```

\calc@maxmin@divmul \calc@maxmin@multiply \calc@maxmin@divide When doing division or multiplication we must be using (count) registers so we set the switch. Other than that it is almost business as usual when multiplying or dividing. #1 is the instruction to either multiply or divide \calc@B by \calc@A, #2 is either \maxof or \minof which is waiting in the input stream and #3 and #4 are the calc expressions. We end it all as usual by calling \calc@post@scan.

```
218 \def\calc@maxmin@divmul#1#2#3#4{%
```

```
220 \calc@count@true
221 \aftergroup#1%
```

```
222 \calc@maxmin@generic#2{#3}{#4}%
```

```
223 \endgroup\begingroup
```

```
224 \calc@post@scan
```

225 }

The two functions called when seeing a \* or a /.

```
226 \def\calc@maxmin@multiply{\calc@maxmin@divmul\calc@multiplyBbyA}
227 \def\calc@maxmin@divide {\calc@maxmin@divmul\calc@divideBbyA}
```

# 6 Reporting errors

```
\calc@error If \calc@post@scan reads a character that is not one of '+', '-', '*', '/', or ')', an error has occurred, and this is reported to the user. Violations in the syntax of (numeric)s will be detected and reported by T<sub>E</sub>X.
```

```
228 \def\calc@error#1{%
229 \PackageError{calc}%
230 {'#1' invalid at this point}%
231 {I expected to see one of: + - * / )}}
```

# 7 Other additions

\@settodim \settototalheight

Ddim The kernel macro \@settodim is changed so that it runs through a list containing \ht, \wd, and \dp and than advance the length one step at a time. We just have to use a scratch register in case the user decides to put in a \global prefix on the length register. A search on the internet confirmed that some people do that kind of thing.

```
232 \def\@settodim#1#2#3{%
```

233 \setbox\@tempboxa\hbox{{#3}}%

```
234 \dimen@ii=\z@
```

- 235 \@tf@r\reserved@a #1\do{%
- 236 \advance\dimen@ii\reserved@a\@tempboxa}%
- 237 **#2=\dimen@ii**
- 238 \setbox\@tempboxa\box\voidb@x}

Now the user level macro is straightforward.

```
239 \def\settototalheight{\@settodim{\ht\dp}}
```

That's the end of the package.  $_{240}\; \big< / {\sf package} \big>$ 

# References

- [1] D. E. KNUTH. The T<sub>E</sub>Xbook (Computers & Typesetting Volume A). Addison-Wesley, Reading, Massachusetts, 1986.
- [2] L. LAMPORT. HTEX, A Document Preparation System. Addison-Wesley, Reading, Massachusetts, Second edition 1994/1985.

# **Change History**

v4.0d	\@settodim: Changed kernel macro 16
$\calc@error: Use \PackageError$	<b>\addtocounter</b> : Fix to make
for error messages (DPC) $\dots$ 16	\addtocounter work with
General: Contributed to tools	amstext 8
distribution $\ldots \ldots \ldots \ldots 1$	\calc@assign@generic: Removed
v4.0e	a few redundant
$\calc@error: typo fixed \dots 16$	\expandafters7
v4.1a	\calc@dividex: Added max and
\@calc@pre@scan: Added code for	min operations $\ldots \ldots \ldots 12$
text sizes: CAR $\dots \dots 9$	\calc@maxmin@divide: Macros
\calc@error: Improved, I hope,	added $\dots \dots \dots$
error message: CAR 16	\calc@maxmin@generic: Macros
\calc@real@x: Added macro	added $\ldots$ 15
set-ups to make them robust	\calc@multiplyx: Added max and
but undefined: CAR 12	min operations $\dots \dots \dots$
\calc@textsize: Added macro:	\calc@textsize: Extended macro
CAR 10	with $\totalheight of \ldots 10$
\depthof: Added macros: CAR . 10	\minof: Added macros 15
General: Added text sizes: CAR 1	\settototalheight: Added macro 16
Attempt to make user-syntax	\steptocounter: Avoid redundant
robust: CAR 1 v4.1b	processing. $PR/3795$
\@calc@pre@scan: Correction to	\totalheightof: Added
ifx true case	informative message for
v4.2	reserved macros 10
\@calc@post@scan: Added macro	Added macro 10
and force expansion 11	v4.3
\@calc@pre@scan: Added \maxof	\@calc@post@scan: Discard
and \minof operations 9	terminating \relax tokens and
Added macro and force	avoid extra error message from
expansion	\calc@next 11
cirpunoion	(carosnono