# The sTEX3 Manual * 

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2022-02-26


#### Abstract

$\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ is a collection of $\mathrm{E}^{\mathrm{A}} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ package that allow to markup documents semantically without leaving the document format, essentially turning ${ }^{\mathrm{E}} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ into a document format for mathematical knowledge management (MKM). STEX augments $\mathrm{A}_{\mathrm{E}} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ with - Semantic macros that denote and distinguish between mathematical concepts, operators, etc. independent of their notational presentation, - A powerful module system that allows for authoring and importing individual fragments containing document text and/or semantic macros, independent of - and without hard coding - directory paths relative to the current document, - A mechanism for exporting STEX documents to (modular) XHTML, preserving all the semantic information for semantically informed knowledge management services.


This is the user manual for the $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ package and associated software. It is primarily directed at end-users who want to use $\mathrm{ST}_{\mathrm{E}}$ to author semantically enriched documents. For the full documentation, see the $S_{\mathrm{T}} \mathrm{X}$ documentation

[^0]
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## Chapter 1

## What is $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ ?

Formal systems for mathematics (such as interactive theorem provers) have the potential to significantly increase both the accessibility of published knowledge, as well as the confidence in its veracity, by rendering the precise semantics of statements machine actionable. This allows for a plurality of added-value services, from semantic search up to verification and automated theorem proving. Unfortunately, their usefulness is hidden behind severe barriers to accessibility; primarily related to their surface languages reminiscent of programming languages and very unlike informal standards of presentation.

STEX minimizes this gap between informal and formal mathematics by integrating formal methods into established and widespread authoring workflows, primarily $\mathrm{LAT}_{\mathrm{E}} \mathrm{X}$, via non-intrusive semantic annotations of arbitrary informal document fragments. That way formal knowledge management services become available for informal documents, accessible via an IDE for authors and via generated active documents for readers, while remaining fully compatible with existing authoring workflows and publishing systems.

Additionally, an extensible library of reusable document fragments is being developed, that serve as reference targets for global disambiguation, intermediaries for content exchange between systems and other services.

Every component of the system is designed modularly and extensibly, and thus lay the groundwork for a potential full integration of interactive theorem proving systems into established informal document authoring workflows.

The general $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ workflow combines functionalities provided by several pieces of software:

- The $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ package to use semantic annotations in $\mathrm{ET}_{\mathrm{E}} \mathrm{X}$ documents,
- RusTEX to convert tex sources to (semantically enriched) xhtml,
- The Mmt software, that extracts semantic information from the thus generated xhtml and provides semantically informed added value services.


## Chapter 2

## Quickstart

### 2.1 Setup

### 2.1.1 The STEX ID $^{2}$ IDE

TODO: VSCode Plugin

### 2.1.2 Manual Setup

Foregoing on the STEX IDE, we will need several pieces of software; namely:

- The $\mathbf{S T}_{\mathbf{E}} \mathbf{X}-$ Package available here ${ }^{1}$. Note, that the CTAN repository for $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$ packages may contain outdated versions of the $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ package, so make sure, that your TEXMF system variable is configured such that the packages available in the linked repository are prioritized over potential default packages that come with your $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ distribution.
- The Mmt System available here ${ }^{2}$. We recommend following the setup routine documented here.

Following the setup routine (Step 3) will entail designating a MathHub-directory on your local file system, where the MmT system will look for $\mathrm{ST}^{\mathrm{E} X} / \mathrm{MmT}$ content archives.

- To make sure that $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ too knows where to find its archives, we need to set a global system variable MATHHUB, that points to your local MathHub-directory (see chapter 4).
- $\mathbf{S T}_{\mathbf{E}} \mathbf{X}$ Archives If we only care about $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$ and generating pdfs, we do not technically need Ммт at all; however, we still need the MATHHUB system variable to be set. Furthermore, Mmt can make downloading content archives we might want to use significantly easier, since it makes sure that all dependencies of (often highly interrelated) $\mathrm{S}^{\mathrm{T}} \mathrm{E}$ archives are cloned as well.
Once set up, we can run mmt in a shell and download an archive along with all of its dependencies like this: lmh install <name-of-repository>, or a whole group of archives; for example, 1 mh install smglom will download all smglom archives.

[^1]- RUSTEX The Mmt system will also set up RuSTEX for you, which is used to generate (semantically annotated) xhtml from tex sources. In lieu of using MmT, you can also download and use RusTEX directly here.


### 2.2 A First $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ Document

Having set everything up, we can write a first $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ document. As an example, we will use the smglom/calculus and smglom/arithmetics archives, which should be present in the designated MathHub-folder.

The document we will consider is the following:

```
documentclass{article}
usepackage{stex}
usepackage{xcolor}
\def\compemph#1{\textcolor{blue}{#1}}
\begin{document}
    \usemodule[smglom/calculus]{series}
    \usemodule[smglom/arithmetics]{realarith}
    The \symref{series }{series} $\infinitesum {n}{1}{
        realdivide[frac]{1}
    $}}\symref{converges}{converges} towards $1$.
\end {document }
```

Compiling this document with pdflatex should yield the output
The series $\sum_{n=1}^{\infty} \frac{1}{2^{n}}$ converges towards 1.
Note that the $\sum$ and $\infty$-symbols are highlighted in blue, and the words "series" and "converges" in bold. This signifies that these words and symbols reference $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ symbols formally declared somewhere; associating their presentation in the document with their (formal) definition - i.e. their semantics. The precise way in which they are highlighted (if at all) can of course be customized (see ${ }^{3}$ ).
\usemodule The command \usemodule[some/archive] \{modulename\} finds some module in the appropriate archive - in the first case (\usemodule[smglom/calculus]\{series\}), $\mathrm{S}^{\mathrm{T}} \mathrm{EX}$ looks for the archive smglom/calculus in our local MathHub-directory (see chapter 4), and in its source-folder for a file series.tex. Since no such file exists, and by default the document is assumed to be in english, it picks the file series.en.tex, and indeed, in here we find a statement \begin\{smodule\}\{series\}. }
$\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ now reads this file and makes all semantic macros therein available to use, along with all its dependencies. This enables the usage of \infinitesum later on.

Analogously, \usemodule[smglom/arithmetics]\{realarith\} opens the file realarith.en.tex in the .../smglom/arithmetics/source-folder and makes its contents available, e.g. \realdivide and \realpower.

[^2]\symref
\symname

The command \symref\{symbolname\}\{text\} marks the text in the second argument as representing the symbolname in the first argument - which is why the word "series" is set in boldface. In the pdf, this is all that happens. In the xhtml (which we will investigate shortly) however, we will note that the word "series" is now annotated with the full URI of the symbol denoting the mathematical concept of a series. In other words, the word is associated with an unambiguous semantics.

Notably, in both cases above (series and converges) the text that references the symbol and the name of the symbol are identical. Since this occurs quite often, the shorthand \symname\{converges\} would have worked as well, where \symname\{foo-bar\} behaves exactly like \symref\{foo-bar\}\{foo bar\}-i.e. the text is simply the name of the symbol with "-" replaced by a space.
\importmodule If you investigated the contents of the imported modules (realarith and series) more closely, you'll note that none of them contain a symbol "converges". Yet, we can use \symref to refer to "converges". That is because the symbol converges is found in smglom/calculus/source/sequenceConvergence.en.tex, and series.en.tex contains the line \importmodule\{sequenceConvergence\}. The \importmodule-statement makes the module referenced available to all documents that include the current module. As such, a "current module" has to exist for \importmodule to work, which is why the command is only allowed within a module-environment.

TODO explain xhtml conversion, MMT compilation (requires an archive...?).

## Chapter 3

## Using $\mathbf{S T}_{\mathbf{E}} \mathrm{X}$

Both the stex package and document class offer the following options:
lang ( $\langle$ language $\rangle *$ ) Languages to load with the babel package.
mathhub ( $\langle$ directory $\rangle$ ) MathHub folder to search for repositories.
sms (〈boolean $\rangle$ ) use persisted mode (not yet implemented).
image ( $\langle$ boolean $\rangle$ ) passed on to tikzinput.
debug ( $\langle l o g$-prefix $\rangle *)$ Logs debugging information with the given prefixes to the terminal, or all if all is given

TODO: terms documentation
TODO: references documentation

## Chapter 4

## STEX Archives

### 4.1 The Local MathHub-Directory

\usemodule, \importmodule, \inputref etc. allow for including content modularly without having to specify absolute paths, which would differ between users and machines. Instead, $\mathrm{ST}_{\mathrm{EX}}$ uses archives that determine the global namespaces for symbols and statements and make it possible for $\mathrm{S}^{\mathrm{T}} \mathrm{EX}$ to find content referenced via such URIs.

All $S_{\mathrm{S}} \mathrm{X}$ archives need to exist in the local MathHub-directory. $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ knows where this folder is via one of three means:

1. If the $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ package is loaded with the option mathhub=/path/to/mathhub, then $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ will consider /path/to/mathhub as the local MathHub-directory.
2. If the mathhub package option is not set, but the macro stswhenthe${}_{ST}\mathrm{E}_{\mathrm{E}}\mathrm{X}$-packageisloaded,thenthismacroisassumedtopointtothelocalMathHubdirectory;i.e.$\backslash$def$\backslash$mathhub\{/path/to/mathhub\}\usepackage\{stex\}willsettheMathHub-directoryaspath/to/mathhub.undefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefined
3. Otherwise, $\mathrm{STEX}^{2}$ will attempt to retrieve the system variable MATHHUB, assuming it will point to the local MathHub-directory. Since this variant needs setting up only once and is machine-specific (rather than defined in tex code), it is compatible with collaborating and sharing tex content, and hence recommended.

### 4.2 The Structure of $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ Archives

$\mathrm{An} \mathrm{ST}_{\mathrm{E}} \mathrm{X}$ archive group/name needs to be stored in the directory /path/to/mathhub/group/name; e.g. assuming your local MathHub-directory is set as /user/foo/MathHub, then in order for the smglom/calculus-archive to be found by the $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ system, it needs to be in /user/foo/MathHub/smglom/calculus.

Each such archive needs two subdirectories:

- /source - this is where all your tex files go.
- /META-INF - a directory containing a single file MANIFEST.MF, the content of which we will consider shortly

An additional lib-directory is optional, and is where STEX will look for files included via \libinput.

Additionally a group of archives group/name may have an additional archive group/meta-inf. If this meta-inf-archive has a /lib-subdirectory, it too will be searched by \libinput from all tex files in any archive in the group/*-group.

### 4.3 MANIFEST.MF-Files

The MANIFEST.MF in the META-INF-directory consists of key-value-pairs, instructing STEX (and associated software) of various properties of an archive. For example, the MANIFEST.MF of the smglom/calculus-archive looks like this:

```
id: smglom/calculus
source-base: http://mathhub.info/smglom/calculus
narration-base: http://mathhub.info/smglom/calculus
dependencies: smglom/arithmetics,smglom/sets,smglom/topology,
    smglom/mv,smglom/linear-algebra,smglom/algebra
responsible: Michael.Kohlhase@FAU.de
title: Elementary Calculus
teaser: Terminology for the mathematical study of change.
description: desc.html
```

Many of these are in fact ignored by $\mathrm{S}_{\mathrm{E}} \mathrm{X}$, but some are important:
id: The name of the archive, including its group (e.g. smglom/calculus),
source-base or
ns: The namespace from which all symbol and module URIs in this repository are formed, see (TODO),
narration-base: The namespace from which all document URIs in this repository are formed, see (TODO),
url-base: The URL that is formed as a basis for external references, see (TODO),
dependencies: All archives that this archive depends on. $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ ignores this field, but Mmт can pick up on them to resolve dependencies, e.g. for lmh install.

## Chapter 5

## Creating New Modules and Symbols

TODO
Example 1
\begin \{smodule\} \{assoctest \} }
$\backslash$ symdef $\{$ foo $\}[\operatorname{args=iia]}\{\backslash \operatorname{comp}\{\mathrm{a}:\} \# 1 \backslash \operatorname{comp}\{; \mathrm{b}:\} \# 2 \backslash \operatorname{comp}\{; \mathrm{c}:\} \# 3\}\{\backslash \operatorname{comp}[\# 1 \backslash \operatorname{comp}\{;\} \# \# 1 \backslash \operatorname{comp+\# \# 2} \mathbf{c o m p} ; \# 2 \backslash \operatorname{comp}]\}$
lend \{smodule $\}$

Module 1: $\quad a: w_{1} ; b: w_{2} ; c:\left[w_{1} ; x+\left[w_{1} ; y+z ; w_{2}\right] ; w_{2}\right]$

TODO: modules documentation
TODO: symbols documentation
TODO: inheritance documentation

### 5.1 Advanced Structuring Mechanisms

Given modules:
Example 2
\begin \{smodule\}\{magma\} }
$\backslash$ symdef $\{$ universe $\}\{\backslash \operatorname{comp}\{\backslash$ mathcal U $\}\}$
\symdef\{operation $\}$ [args=2,op=\circ]\{\#1 \comp\circ \#2\}
lend $\{$ smodule $\}$
\imegin\{smodule $\}\{$ monoid
symdef\{unit\} \{magma\}
lend \{smodule\}
lbegin\{smodule $\}$ \{group $\}$
\importmodule\{monoid $\}$
$\$ symdef $\{$ inverse $\}[\operatorname{args}=1]\left\{\{\# 1\}^{\wedge}\{\backslash \operatorname{comp}\{-1\}\}\right\}$
end $\{$ smodule $\}$

Module 2:
Module
Module 4

We can form a module for rings by "cloning" an instance of group (for addition) and monoid (for multiplication), respectively, and "glueing them together" to ensure they share the same universe:

## Example 3

\begin \{smodule\}\{ring\} }
\begin \{copymodule\} \{group\}\{addition\} }
$\backslash r e n a m e d e c l[n a m e=u n i v e r s e]\{$ universe $\}\{r u n i v e r s e\}$
\renamedecl[name=plus]\{operation\}\{rplus\}
Yrenamedecl[name=uminus]\{inverse\}\{ruminus
lend \{copymodule \}
$\backslash$ notation* $\{$ rplus $\}[$ plus, op=+, prec $=60]\{\# 1$ $\backslash$ comp+ \#2\}
\notation*\{rzero\}[zero]\{ $\backslash$ compo $\}$
\notation*\{ruminus $\}[$ uminus,op $=-]\{$ comp- $\# 1\}$
\begin \{copymodule } \} \{ monoid \} \{ m u l t i p l i c a t i o n \}
\assign \{universe\} $\} \backslash r u n i v e r s e\}$
\renamedecl[name=times]\{operation\}\{rtimes\}
\renamedecliname

notation $\boldsymbol{\text { notrone }}$ [one] $\{\backslash$ compl $\}$
Test: \$ \rtimes a\{ \rplus c\{\rtimes de\}\}\$
lend \{smodule \}

TODO: explain donotclone
Example 4

```
\begin{smodule}{int}
\symdef{Integers}{\comp{\mathbb Z }}
\symdef{Integerrs}{\comp{\mathbb Z }}
\symdef{plus }[args=2,op
\symdef{uminus}[args=1,op=-]{\comp-#1}
\begin{interpretmodule}{group}{intisgroup}
\assign{universe}{\Integers}
assign{operation}{\plus!}
lassign{unit}{\zero}
\assign{inverse}{\uminus!}
end{interpretmodule}
lend{smodule}
```


### 5.2 Primitive Symbols (The $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ Metatheory)

TODO: metatheory documentation

## Chapter 6

## $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ Statements (Definitions, Theorems, Examples, ...)

TODO: statements documentation<br>TODO: sproofs documentation

## Chapter 7

# Additional Packages 

TODO: tikzinput documentation

### 7.1 Modular Document Structuring

TODO: document-structure documentation

### 7.2 Slides and Course Notes

TODO: notesslides documentation

### 7.3 Homework, Problems and Exams

TODO: problem documentation
TODO: hwexam documentation

## Chapter 8

## Stuff

### 8.1 Modules

## \sTeX

\stex

### 8.1.1 Semantic Macros and Notations

Semantic macros invoke a formally declared symbol.
To declare a symbol (in a module), we use \symdecl, which takes as argument the name of the corresponding semantic macro, e.g. \symdecl\{foo\} introduces the macro $\backslash$ foo. Additionally, \symdecl takes several options, the most important one being its arity. foo as declared above yields a constant symbol. To introduce an operator which takes arguments, we have to specify which arguments it takes.

Module 7: For example, to introduce binary multiplication, we can do \symdecl\{mult\}[args=2]. We can then supply the semantic macro with arbitrarily many notations, such as \notation\{mult\}\{\#1 \#2\}.

## Example 5

```
\symdecl{mult}[args=2]
\notation{mult}{#1 #2}
$\mult{a}{b}$
```


## $a b$

Since usually, a freshly introduced symbol also comes with a notation from the start, the \symdef command combines \symdecl and \notation. So instead of the above, we could have also written
\symdef $\{$ mult $\}$ [args=2] \{\#1 \#2\}

Adding more notations like \notation\{mult\}[cdot]\{\#1 \comp\{\cdot\} \#2\} or \notation\{mult\}[times]\{\#1 \comp\{\times\} \#2\} allows us to write $\$ \backslash \operatorname{mult}[c \operatorname{dot}]\{a\}\{b\} \$$ and \$ mmult [times] $\{\mathrm{a}\}\{\mathrm{b}\} \$$ :

## Example 6

\notation $\{$ mult $\}[\operatorname{cdot}]\{\# 1 \quad \backslash \operatorname{comp}\{\backslash \operatorname{cdot}\} \# 2\}$
notation $\{$ mult $\}[$ times $]\{\# 1 \quad \backslash$ comp $\{\backslash$ times $\} ~ \# 2\}$
S $\backslash$ mult [cdot] $\{\mathrm{a}\}\{\mathrm{b}\}$ \$ and $\mathbb{S} \backslash \mathrm{mult}[$ times $]\{\mathrm{a}\}\{\mathrm{b}\}$

```
\(a \cdot b\) and \(a \times b\)
```

Not using an explicit option with a semantic macro yields the first declared notation, unless changed ${ }^{4}$.

Outside of math mode, or by using the starred variant \foo*, allows to provide a custom notation, where notational (or textual) components can be given explicitly in square brackets.

## Example 7

```
\mult{\comp{product of}\arg{$a$} \comp{and} \arg{$b$}}
```

$$
a * b \text { is the product of } a \text { and } b
$$

In custom mode, prefixing an argument with a star will not print that argument, but still export it to OMDoc:

## Example 8

```
\mult{\comp{Multiplying} \arg*{$\mult {a}{b}$} again by \arg{$b$}} yields
```

```
Multiplying again by b yields...
```

-The syntax $*[\langle i n t\rangle]$ allows switching the order of arguments. For example, given a 2-ary semantic macro \forevery with exemplary notation \forall \#1. \#2, we can write

Example 9
\symdecl\{forevery\}[args=2]
$\backslash$ forevery $\{\backslash \arg [2]\{$ The proposition $\$ P \$\} \backslash \operatorname{comp}\{$ holds for every $\} \backslash \arg [1]\{\$ x \backslash i n$ A $\$\}$

$$
\text { The proposition } P \text { holds for every } x \in A
$$

[^3]When using $*[n]$, after reading the provided ( $n$ th) argument, the "argument counter" automatically continues where we left off, so the $*[1]$ in the above example can be omitted.

For a macro with arity $>0$, we can refer to the operator itself semantically by suffixing the semantic macro with an exclamation point ! in either text or math mode. For that reason \notation (and thus \symdef) take an additional optional argument $o p=$, which allows to assign a notation for the operator itself. e.g.

Example 10
\symdef $\{\operatorname{add}\}[\operatorname{args}=2, o p=\{+\}]\{\# 1 \quad \backslash$ comp $+\# 2\}$
The operator $\$ \backslash$ add! $\$$ adds two elements, as in $\$ \backslash a d d$ ab $\$$.

```
The operator + adds two elements, as in a+b
```

* is composable with ! for custom notations, as in:


## Example 11

$$
\backslash \text { mult! }\{\backslash \operatorname{comp}\{\text { Multiplication }\}\} \text { (denoted by } \$ \backslash m u l t!*\{\backslash \operatorname{comp} \backslash c d o t\} \$ \text { ) is defined by }
$$

```
Multiplication (denoted by .) is defined by...
```

The macro \comp as used everywhere above is responsible for highlighting, linking, and tooltips, and should be wrapped around the notation (or text) components that should be treated accordingly. While it is attractive to just wrap a whole notation, this would also wrap around e.g. the arguments themselves, so instead, the user is tasked with marking the notation components themself.

The precise behaviour of \comp is governed by the macro \@comp, which takes two arguments: The tex code of the text (unexpanded) to highlight, and the URI of the current symbol. \@comp can be safely redefined to customize the behaviour.

The starred variant \symdecl*\{foo\} does not introduce a semantic macro, but still declares a corresponding symbol. foo (like any other symbol, for that matter) can then be accessed via \STEXsymbol\{foo\} or (if foo was declared in a module Foo) via \STEXModule\{Foo\}?\{foo\}.
both \STEXsymbol and \STEXModule take any arbitrary ending segment of a full URI to determine which symbol or module is meant. e.g. \STEXsymbol\{Foo?foo\} is also valid, as are e.g. \STEXModule\{path?Foo\}?\{foo\} or \STEXsymbol\{path?Foo?foo\}

There's also a convient shortcut \symref\{?foo\}\{some text\} for \STEXsymbol\{?foo\}! [some text]

## Other Argument Types

So far, we have stated the arity of a semantic macro directly. This works if we only have "normal" (or more precisely: i-type) arguments. To make use of other argument types, instead of providing the arity numerically, we can provide it as a sequence of characters representing the argument types - e.g. instead of writing args=2, we can equivalently write args=ii, indicating that the macro takes two i-type arguments.

Besides i-type arguments, $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ has two other types, which we will discuss now. The first are binding (b-type) arguments, representing variables that are bound by the operator. This is the case for example in the above \forevery-macro: The first argument is not actually an argument that the forevery "function" is "applied" to; rather, the first argument is a new variable (e.g. $x$ ) that is bound in the subsequent argument. More accurately, the macro should therefore have been implemented thusly:
\symdef\{forevery\}[args=bi]\{\forall \#1. \; \#2\}
Module 8: b-type arguments are indistinguishable from i-type arguments within $S_{\mathrm{E}} \mathrm{E} \mathrm{X}$, but are treated very differently in OMDoc and by Mmt. More interesting within STEX are a-type arguments, which represent (associative) arguments of flexible arity, which are provided as comma-separated lists. This allows e.g. better representing the \mult-macro above:

## Example 12

\symdef\{mult $\}[\operatorname{args=a}]\{\# 1\}\{\# \# 1 \quad \backslash \operatorname{comp} \backslash \operatorname{cdot} \# \# 2\}$
S $\backslash \mathrm{mult}\left\{a, b, c,\left\{d^{\wedge} \mathrm{e}\right\}, f\right\} \mathrm{S}$
$a \cdot b \cdot c \cdot d^{e} \cdot f$
-As the example above shows, notations get a little more complicated for associative arguments. For every a-type argument, the \notation-macro takes an additional argument that declares how individual entries in an a-type argument list are aggregated. The first notation argument then describes how the aggregated expression is combined into the full representation.

For a more interesting example, consider a flexary operator for ordered sequences in ordered set, that taking arguments $\{\mathrm{a}, \mathrm{b}, \mathrm{c}\}$ and $\backslash$ mathbb $\{\mathrm{R}\}$ prints $a \leq b \leq c \in \mathbb{R}$. This operator takes two arguments (an a-type argument and an i-type argument), aggregates the individuals of the associative argument using \leq, and combines the result with \in and the second argument thusly:

Example 13
\symdef\{numseq $\}[\operatorname{args=ai]\{ \# 1~\backslash comp\backslash in\# 2\} \{ \# \# 1~\ comp\backslash leq~\# \# 2\} ~}$
\numseq $\{\mathrm{a}, \mathrm{b}, \mathrm{c}\}\{\backslash$ mathbb R$\}$ \$

```
a<b<c\in\mathbb{R}
```

Finally, B-type arguments combine the functionalities of a and b, i.e. they represent flexary binding operator arguments.

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[^4]
## Precedences

Every notation has an (upwards) operator precedence and for each argument a (downwards) argument precedence used for automated bracketing. For example, a notation for a binary operator $\backslash$ foo could be declared like this:

```
\notation{foo}[prec=200;500x600]{#1 \comp{+} #2}
```

assigning an operator precedence of 200, an argument precedence of 500 for the first argument, and an argument precedence of 600 for the second argument.
$\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ insert brackets thusly: Upon encountering a semantic macro (such as \foo), its operator precedence (e.g. 200) is compared to the current downwards precedence (initially \neginfprec). If the operator precedence is larger than the current downwards precedence, parentheses are inserted around the semantic macro.

Notations for symbols of arity 0 have a default precedence of $\operatorname{infprec}$, i.e. by default, parentheses are never inserted around constants. Notations for symbols with arity $>0$ have a default operator precedence of 0 . If no argument precedences are explicitly provided, then by default they are equal to the operator precedence.

Consequently, if some operator $A$ should bind stronger than some operator $B$, then $A$ s operator precedence should be smaller than $B$ s argument precedences.

For example:

## Module 9:

## Example 14

notation $\{$ plus $\}[$ prec $=100]\{\# 1 \quad \backslash \operatorname{comp}\{+\} \quad \# 2\}$
notation $\{$ times $\}[$ prec $=50]\{\# 1 \quad \backslash \operatorname{comp}\{\backslash \mathrm{cdot}\} \# 2\}$


```
a+b\cdotc and a
```


### 8.1.2 Archives and Imports

## Namespaces

Ideally, $\mathrm{ST}_{\mathrm{E}} \mathrm{X}$ would use arbitrary URIs for modules, with no forced relationships between the logical namespace of a module and the physical location of the file declaring the module - like Mmт does things.

Unfortunately, $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ only provides very restricted access to the file system, so we are forced to generate namespaces systematically in such a way that they reflect the physical location of the associated files, so that $\mathrm{S}_{\mathrm{E}} \mathrm{X}$ can resolve them accordingly. Largely, users need not concern themselves with namespaces at all, but for completenesses sake, we describe how they are constructed:

- If \begin\{module\}\{Foo\} occurs in a file/path/to/file/Foo[. } \langle lang \rangle ].tex which does not belong to an archive, the namespace is file://path/to/file.
- If the same statement occurs in a file /path/to/file/bar[. $\langle$ lang $\rangle$ ].tex, the namespace is file://path/to/file/bar.

In other words: outside of archives, the namespace corresponds to the file URI with the filename dropped iff it is equal to the module name, and ignoring the (optional) language suffix ${ }^{1}$.

If the current file is in an archive, the procedure is the same except that the initial segment of the file path up to the archive's source-folder is replaced by the archive's namespace URI.

## Paths in Import-Statements

Conversely, here is how namespaces/URIs and file paths are computed in import statements, examplary \importmodule:

- \importmodule\{Foo\} outside of an archive refers to module Foo in the current namespace. Consequently, Foo must have been declared earlier in the same document or, if not, in a file Foo[. $\langle$ lang $\rangle$ ]. tex in the same directory.
- The same statement within an archive refers to either the module Foo declared earlier in the same document, or otherwise to the module Foo in the archive's toplevel namespace. In the latter case, is has to be declared in a file Foo [. 〈lang〉] .tex directly in the archive's source-folder.
- Similarly, in \importmodule\{some/path?Foo\} the path some/path refers to either the sub-directory and relative namespace path of the current directory and namespace outside of an archive, or relative to the current archive's top-level namespace and source-folder, respectively.
The module Foo must either be declared in the file $\langle$ top-directory $\rangle /$ some/path/Foo [. $\langle l a n g\rangle$ ].tex, or in $\langle$ top-directory $\rangle /$ some/path [. $\langle$ lang $\rangle$ ].tex (which are checked in that order).
- Similarly, \importmodule[Some/Archive]\{some/path?Foo\} is resolved like the previous cases, but relative to the archive Some/Archive in the mathhub-directory.
- Finally, \importmodule\{full://uri?Foo\} naturally refers to the module Foo in the namespace full://uri. Since the file this module is declared in can not be determined directly from the URI, the module must be in memory already, e.g. by being referenced earlier in the same document.

Since this is less compatible with a modular development, using full URIs directly is discouraged.

[^5]
[^0]:    *Version 3.0 (last revised 2022-02-26)

[^1]:    ${ }^{1}$ EdNote: For now, we require the latex3-branch
    ${ }^{2}$ EdNote: For now, we require the sTeX-branch, requiring manually compiling the MMT sources

[^2]:    ${ }^{3}$ EdNote: somewhere later

[^3]:    ${ }^{4}$ EdNote: TODO

[^4]:    ${ }^{5}$ EdNote: what about e.g. \int _x $x$ int _ $y \backslash$ int $\_z \mathrm{f} d x \mathrm{dy} \mathrm{dz}$ ?
    ${ }^{6}$ EdNote: "decompose" a-type arguments into fixed-arity operators?

[^5]:    ${ }^{1}$ which is internally attached to the module name instead, but a user need not worry about that.

