

Actuarial symbols of life contingencies and financial mathematics *

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Abstract

Package `actuarialsymbol` provides facilities to compose actuarial symbols of life contingencies and financial mathematics characterized by subscripts and superscripts on both sides of a principal symbol. The package also features commands to easily and consistently position precedence numbers above or below statuses in symbols for multiple lives contracts.

Since actuarial notation can get quite involved, the package defines a number of shortcut macros to ease entry of the most common elements. [Appendix A](#) lists the commands to typeset a large selection of life contingencies symbols.

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1 Introduction

Actuaries denote various quantities of life contingencies like present values of life insurances and life annuities, annual premiums, or reserves using a whole array of symbols. The highly descriptive, yet compact, notation was standardized as far back as in 1898 (Wolthuis, 2004). Figure 1 shows a creative use of the notation by the graduating class of 1972 in Actuarial Science at Université Laval.

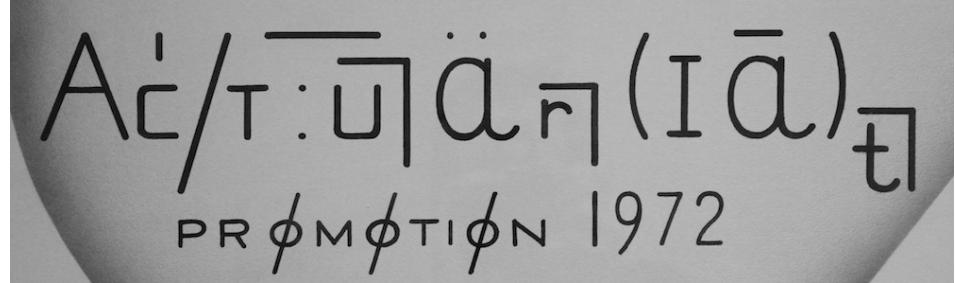


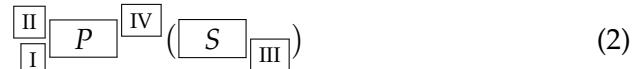
Figure 1: “Actuariat” (French for Actuarial Science) written using actuarial symbols on the 1972 graduating class mosaic at Université Laval

Bowers et al. (1997, Appendix 4) offer an excellent overview of the composition rules for symbols of actuarial functions. In a nutshell, a principal symbol, say S , is combined with auxiliary symbols positioned in subscript or in superscript, to the left or to the right. Schematically, we thus have:



The principal symbol is in general a single letter. The letter may be “accented” with a bar (\bar{A}), double dots (\ddot{a}) or a circle (\circ). When the principal symbol consists of two letters, they are grouped between parentheses, as in (IA) or $(D\bar{A})$. Most commonly, there are alphanumeric statuses in the lower-right position $\boxed{\text{III}}$. Numerals can be placed above or below the individual statuses to show the order of failure; we will refer to these numerals as *precedence numbers*. Otherwise, auxiliary symbols appear lower-left $\boxed{\text{I}}$, upper-left $\boxed{\text{II}}$ and upper-right $\boxed{\text{IV}}$, in that order of frequency.

Principle symbols for benefit premiums, reserves and amount of reduced paid-up insurance, P , V and W , are combined with benefit symbols unless the benefit is a level unit insurance payable at the end of the year of death. In such cases, we have the following symbol structure (replace P by V or W as needed):



Perhaps the most commonly used auxiliary symbol not readily available in L^AT_EX is the “angle” denoting a duration n , as in \overline{n} . Package *actuarialangle* (Goulet, 2017) provides commands to create this symbol, as

well as an overhead angle bracket¹ (or “roof”) used to emphasize joint status when ambiguity is possible: \overline{xy} . This package is imported at load time by `actuarialsymbol`.

Package `actuarialsymbol` provides a generic command to position all subscripts and superscripts easily and consistently around a principal symbol; a command to create two-letter symbols; and two commands to position precedence numbers above and below statuses. Since entering actuarial symbols can get quite involved, the package also defines a number of shortcuts to create the most common actuarial functions of financial mathematics and life contingencies.

2 For the impatient

The hurried reader may jump to [section 4](#) for tables of shortcut macros defined by the package, and to [Appendix A](#) for a comprehensive list of symbols of life contingencies along with the `LATEX` code to compose them with `actuarialsymbol` loaded. That said, in our highly biased view, it remains worth reading along the fine documentation below.

3 Package features

This section describes the generic commands provided by the package to compose actuarial symbols. On a daily basis, one should use the shortcuts of [section 4](#) to ease entry of symbols.

3.1 Actuarial symbol

`\actsymb` The generic command `\actsymb` typesets a principal symbol with surrounding subscripts and superscripts. Its syntax is somewhat unusual for `LATEX`, but it serves well the natural order of the building blocks of a symbol and their relative prevalence:

```
\actsymb[\langle ll \rangle][\langle ul \rangle]{\langle symbol \rangle}{\langle lr \rangle}[\langle ur \rangle]
```

Above, $\langle ll \rangle$ identifies the auxiliary symbol in the lower left subscript position \boxed{I} (following the notation in the schematic representation (1)); $\langle ul \rangle$ is the upper left superscript \boxed{II} ; $\langle symbol \rangle$ is the principal symbol S ; $\langle lr \rangle$ is the lower right subscript \boxed{III} ; $\langle ur \rangle$ is the upper right superscript

¹Starting with version 2.0 dated 2017/04/10.

IV. The principal symbol and the right subscript are required, the other arguments are optional.

\actsymbol{A}{x}	A_x
\actsymbol[n]{A}{x}	$n A_x$
\actsymbol[n][2]{A}{x}	${}^2_n A_x$
\actsymbol[n][2]{A}{x}[(m)]	${}^2_n A_x^{(m)}$

The command actually admits one more optional argument to compose symbols for premiums, reserves and paid-up insurance. The extended command

`\actsymbol[⟨ll⟩][⟨ul⟩][⟨principle⟩]{⟨symbol⟩}{⟨lr⟩}[⟨ur⟩]`

puts symbol $\langle principle \rangle$ outside the parentheses in the schematic representation (2).

\actsymbol[]{}[P]{\bar{A}}{x:\bar{n}}	$P(\bar{A}_{x:\bar{n}})$
\actsymbol[k]{}[V]{\bar{A}}{x}[{}^1]	${}_k V^{\{1\}}(\bar{A}_x)$
\actsymbol[k]{}[\bar{W}]{\bar{A}}{x}	${}_k \bar{W}(\bar{A}_x)$

Remark. TeX adjusts the position of a subscript downward when a superscript is present:

$$A_x \quad A_x^2.$$

The package maintains this behaviour. Therefore, entering the symbols above using the standard operators `^` and `_` or with `\actsymbol` yields the same result.

A_x \quad A_x^2	$A_x \quad A_x^2$
\actsymbol{A}{x} \quad \actsymbol{A}{x}[2]	$A_x \quad A_x^2$

Furthermore, the package also ensures that the left and right subscripts, when both present, are at the same level, something popular ad hoc constructions do not provide.

{ }_t A_x \quad { }_t A_x^2	${}_t A_x \quad {}_t A_x^2$
\actsymbol[t]{A}{x} \quad \actsymbol[t]{A}{x}[2]	${}_t A_x \quad {}_t A_x^2$

In symbols for premiums, reserves and paid-up insurance, subscripts and superscripts are aligned only around the principle symbol. Authors who would prefer a uniform subscript position *throughout their document* should load package `subdepth` (Robertson, 2007).

3.2 Two-letter principal symbols

`\twoletsymb` Entering two-letter principal symbols like (DA) as $$(DA)$$ results in letters that are too distant from one another: (DA) . To unify presentation, the package provides the command

```
\twoletsymb[<length>]{<symbol_1>}{<symbol_2>}
```

to group $\langle symbol_1 \rangle$ and $\langle symbol_2 \rangle$ between parentheses with kerning² reduced by length `\twoletkern` (see below). One can also reduce spacing by $\langle length \rangle$ for a specific symbol.

<code>\twoletsymb{\bar{D}}{\bar{A}}</code>	$(\bar{D}\bar{A})$
<code>\twoletsymb{I}{\ddot{a}}</code>	$(I\ddot{a})$
<code>\twoletsymb[0.8pt]{I}{\ddot{a}}</code>	$(I\ddot{a})$

We expect authors to use `\twoletsymb` to define commands, not directly in equations. The package already defines a number of shortcuts for the main two-letter actuarial symbols; see [section 4](#).

`\twoletkern` The standard kerning between mathematical symbols defined with `\twoletsymb` is *reduced* by the length `\twoletkern`, by default 1.2pt. This value can be changed as usual using `\setlength`.

3.3 Precedence numbers

`\nthtop` Precedence numbers appear above or below individual statuses in the right subscript `[III]` of a symbol. Commands

```
\nthtop[<length>]{<number>}{<status>}
\nthtop*[<length>]{<number>}{<status>}
```

put a precedence $\langle number \rangle$ above a $\langle status \rangle$, smashed so that the apparent height of the status is its normal height. This is normally used in the right subscript `[III]` of a symbol. With `\nthtop`, the spacing between the precedence number and the status is a constant `\nthtopsep` (see below). This can result in precedence numbers placed at different heights if one status contains an horizontal rule.

<code>\actsymb{A}{\nthtop{1}{x}}{\angln}</code>	$A_{x:\overline{n}}^1$
<code>\actsymb{A}{x:\nthtop{1}{\angln}}</code>	$A_{x:\overline{n}}^1$
<code>\actsymb{A}{\nthtop{1}{x}y:\nthtop{2}{\angln}}</code>	$A_{xy:\overline{n}}^{1,2}$

²Spacing adjustment between the characters

Conversely, `\nthtop*` always leaves enough space `\nthtopskip` for intervening horizontal rules, resulting in vertically aligned precedence numbers.

<code>\actssymb{A}{\nthtop*{1}{x}:\angln}</code>	$A_{x:\bar{n}}^1$
<code>\actssymb{A}{x:\nthtop*{1}{\angln}}</code>	$A_{x:\bar{n}}^1$
<code>\actssymb{A}{\nthtop*{1}{x}y:\nthtop*{2}{\angln}}</code>	$A_{xy:\bar{n}}^{1 \atop 2}$

The optional argument `<length>` changes the default spacing for one symbol. The package also defines shortcuts for first, second and third top precedence; see [section 4](#).

`\nthbottom` In the same vein as the above two commands,

`\nthbottom*`

<code>\nthbottom[<length>]{<number>}{<status>}</code>
<code>\nthbottom*{<length>}{<number>}{<status>}</code>

put a precedence `<number>` below a `<status>`. With `\nthbottom` the spacing between the status and the number is a constant `\nthbottomsep`, whereas with `\nthbottom*` enough spacing `\nthbottomskip` is left to bottom align the precedence numbers. The `*` variant is most useful in cases involving more than one bottom precedence numbers and statuses with descenders.

<code>\actssymb{A}{\nthtop{3}{x}%</code>	A_{xyz}^3
<code> \nthbottom{1}{y}\nthbottom{2}{z}}</code>	$_{12}$

<code>\actssymb{A}{\nthtop{3}{x}%</code>	A_{xyz}^3
<code> \nthbottom*{1}{y}\nthbottom*{2}{z}}</code>	$_{12}$

The optional argument `<length>` changes the default spacing for one symbol. The package also defines shortcuts for first, second and third bottom precedence; see [section 4](#).

Remark. The fact that top precedence numbers have zero height means they will clash with a right superscript `[IV]`:

<code>\actssymb{A}{\nthtop{1}{x}:\angln}[{(m)}]</code>	$A_{x:\bar{n}}^{(m)}$
--	-----------------------

In such rare circumstances, one needs to insert a *strut* (an invisible vertical rule) in the subscript to push it downward as needed:

<code>\actssymb{A}{\rule{0pt}{2.3ex}%</code>	$A_1^{(m)}$
<code> \nthtop{1}{x}:\angln}[{(m)}]</code>	$_{x:\bar{n}}$

`\nhtopsep` The constant spacing between a top precedence number and the status underneath when using `\nhtop` is `\nhtopsep`, by default 2.0pt. The constant height of top precedence numbers when using `\nhtop*` is achieved by setting the baseline skip to `\nhtopskip`, by default 7.0pt.
`\nhtopskip`
`\nhtbottomsep`
`\nhtbottomskip`

Similarly, the constant spacing between a bottom precedence number and the status above when using `\nhtbottom` is `\nhtbottomsep`, by default 2.0pt, and the constant height of bottom precedence numbers when using `\nhtbottom*` is achieved by setting the baseline skip to `\nhtbottomskip`, by default 9.0pt.

These values can be changed as usual using `\setlength`.

4 Shortcuts

Composing actuarial symbols from scratch using `\actssymb` can easily get quite involved. For this reason, the package defines a large number of shortcut macros to ease entry of the most common symbols. We encourage authors to define their own shortcuts for cases we did not consider. The package provides powerful facilities to define shortcuts.

4.1 Basic symbols of life tables, insurance and annuities

[Table 1](#) lists shortcuts to compose complete symbols of life tables and benefits of insurance and annuities. For space considerations only the mandatory arguments are given, but it should be noted that all commands of Table 1 accept the optional arguments $\langle ll \rangle$, $\langle ul \rangle$ and $\langle ur \rangle$ of `\actssymb`.

One will note that shortcuts for insurance benefits come in two variants: one for the benefit payable at the end of the year of death (standard shortcut) and one for the benefit payable at the time of death (* variant). Shortcuts for annuity benefits have three variants: payable at the end of the period (standard), continuously (* variant) and at the beginning of the period (** variant).

`\@actinssc`
`\@actannsc`
`\@actothersc`
`\@actinssc{\symbol{}}`
`\@actannsc{\symbol{}}`
`\@actothersc{\symbol{}}`

Table 1: Shortcuts for life table, insurance and annuity symbols. All commands accept the optional arguments $\langle ll \rangle$, $\langle ul \rangle$ and $\langle ur \rangle$ of `\actssymb`.

Definition	Example	Output
<code>\lx{\langle age \rangle}</code>	<code>\lx{x}</code>	ℓ_x
<code>\Lx{\langle age \rangle}</code>	<code>\Lx{x}</code>	\mathcal{L}_x^+
<code>\dx{\langle age \rangle}</code>	<code>\dx[n]{x}</code>	$n d_x$
<code>\Dx{\langle age \rangle}</code>	<code>\Dx[n]{x}</code>	$n \mathcal{D}_x^+$
<code>\px{\langle age \rangle}</code>	<code>\px[t]{x}</code>	$t p_x$
<code>\qx{\langle age \rangle}</code>	<code>\qx[t]{x}</code>	$t q_x$
<code>\eringx{\langle lr \rangle}</code>	<code>\eringx{x:\angln}</code>	$\dot{e}_{x:\bar{n}}$
<code>\Ax{\langle lr \rangle}</code>	<code>\Ax{x:\angln}</code>	$A_{x:\bar{n}}$
<code>\Ax*\{\langle lr \rangle\}</code>	<code>\Ax*[x:\angln]</code>	$\bar{A}_{x:\bar{n}}$
<code>\Ex{\langle lr \rangle}</code>	<code>\Ex[n]{x}</code>	$n E_x$
<code>\ax{\langle lr \rangle}</code>	<code>\ax{x:\angln}</code>	$a_{x:\bar{n}}$
<code>\ax*\{\langle lr \rangle\}</code>	<code>\ax*[x:\angln]</code>	$\bar{a}_{x:\bar{n}}$
<code>\ax**{\langle lr \rangle}</code>	<code>\ax**{x:\angln}</code>	$\ddot{a}_{x:\bar{n}}$
<code>\sx{\langle lr \rangle}</code>	<code>\sx{x:\angln}</code>	$s_{x:\bar{n}}$
<code>\sx*\{\langle lr \rangle\}</code>	<code>\sx*[x:\angln]</code>	$\bar{s}_{x:\bar{n}}$
<code>\sx**{\langle lr \rangle}</code>	<code>\sx**{x:\angln}</code>	$\ddot{s}_{x:\bar{n}}$
<code>\aringx{\langle lr \rangle}</code>	<code>\aringx{x:\angln}</code>	$\dot{a}_{x:\bar{n}}$

[†] Calligraphic letters obtained using `\mathcal{}`. These specific versions of \mathcal{L} and \mathcal{D} require package `rsfso` (Sharpe, 2015). Standard versions are \mathcal{L} and \mathcal{D} .

Command `\actinssc` automatically provides the two shortcuts for insurance benefits, command `\actannsc` provides the three shortcuts for annuity benefits and command `\actothersc` provides a single shortcut for $\langle symbol \rangle$.

For example, the package defines the shortcut `\px` with the equivalent of

```
\newcommand{\px}{\@actothersc{p}}
```

shortcuts `\Ax` and `\Ax*` with

```
\newcommand{\Ax}{\@actinssc{A}}
```

and shortcuts `\ax`, `\ax*` and `\ax**` with

```
\newcommand{\ax}{\@actannsc{a}}
```

Remark. When used in the preamble of a document, the above commands need to be protected by a `\makeatletter ... \makeatother` pair since they make use of the reserved character `@`. Therefore, to define shortcuts, say, `\Bx` and `\Bx*` to the imaginary benefits B and \bar{B} , one would write in the preamble

```
\makatletter
\newcommand{\Bx}{\@actinssc{B}}
\makeatother
```

4.2 Symbols for premiums, reserves and paid-up insurance

Symbols for premiums, reserves and paid-up insurance come in two main variants: without an explicit benefit between parentheses for insurances payable at the end of the year of death, and with the type of benefit specified for all other insurances and annuities.

[Table 2](#) lists two sets of shortcuts to compose symbols for premiums, reserves and paid-up insurance. Shortcuts from the first set take in mandatory argument the content of the $\langle lr \rangle$ subscript of actuarial symbols. Those from the second set require a complete benefit symbol in argument. One may use the shortcuts of [Table 1](#) to this effect. Again, only the mandatory arguments are given in the table, but all commands accept the optional arguments $\langle ll \rangle$, $\langle ul \rangle$ and $\langle ur \rangle$ of `\actsymb`.

`\@actpremres` The package eases definition of additional shortcut macros similar to the second set of [Table 2](#) using the internal command

```
\@actpremres{\langle principle \rangle}
```

It defines shortcuts for discrete (default) or continuous (* variant) premiums, reserves and paid-up insurance. For example, the package defines shortcuts `\premium` and `\premium*` with

```
\newcommand{\premium}{\@actpremres{P}}
```

The remark at the end of [section 4.1](#) also applies here.

4.3 Auxiliary symbols

[Table 3](#) lists shortcuts for a few common auxiliary symbols used in the lower right subscript $\boxed{\text{III}}$.

Table 2: Shortcuts for premiums, reserves and paid-up insurance. All commands accept the optional arguments $\langle ll \rangle$, $\langle ul \rangle$ and $\langle ur \rangle$ of `\actssymb`.

Definition	Example	Output
<code>\Px{\langle lr \rangle}</code>	<code>\Px[h]{x}</code>	${}_h P_x$
<code>\Vx{\langle lr \rangle}</code>	<code>\Vx[k]{x}</code>	${}_k V_x$
<code>\Wx{\langle lr \rangle}</code>	<code>\Wx[k]{x}</code>	${}_k W_x$
<code>\premium{\langle benefit \rangle}</code>	<code>\premium[t]{\Ax*x}</code>	${}_t P(\bar{A}_x)$
<code>\premium*{\langle benefit \rangle}</code>	<code>\premium*[t]{\Ax*x:\angln}</code>	${}_t \bar{P}(\bar{A}_{x:\bar{n}})$
<code>\reserve{\langle benefit \rangle}</code>	<code>\reserve[t]{\ax**x}</code>	${}_t V(\ddot{a}_x)$
<code>\reserve*{\langle benefit \rangle}</code>	<code>\reserve*[t]{\ax*x}</code>	${}_t \bar{V}(\bar{a}_x)$
<code>\paidup{\langle benefit \rangle}</code>	<code>\paidup[k]{\Ax*x}</code>	${}_k W(\bar{A}_x)$
<code>\paidup*{\langle benefit \rangle}</code>	<code>\paidup*[k][h]{\Ax*x}</code>	${}_k^h \bar{W}(\bar{A}_x)$

4.4 Symbols for varying benefit insurance and annuities

[Table 4](#) lists shortcuts for common two-letter symbols of varying benefit insurance and annuities. These shortcuts can be used as principal symbol in `\actssymb` or in the commands of [Table 1](#).

`\@twoletinssc`
`\@twoletannsc`

One may define additional shortcuts for two-letter insurance and annuity benefit symbols using the internal commands

```
\@twoletinssc[\langle length \rangle]{\langle symbol_1 \rangle}{\langle symbol_2 \rangle}
\@twoletannsc[\langle length \rangle]{\langle symbol_1 \rangle}{\langle symbol_2 \rangle}
```

These commands are similar to those of [section 4.1](#): `\@twoletinssc` provides two shortcuts (standard and * variant), whereas `\@twoletannsc` provides three (standard, * and ** variants).

4.5 First, second and third precedence

[Table 5](#) lists shortcuts and aliases for the first, second and third precedence numbers, top and bottom. These shortcuts can be used in auxiliary symbols in `\actssymb` or in the commands of [Table 1](#).

Table 3: Shortcuts for auxiliary symbols

Definition	Example	Output
\term{<age>}{<duration>}	\Ax{\term{x}{n}}	$A_{x:\bar{n}}^1$
\termxn	\Ax{\term{x}{n}}	$A_{x:\bar{n}}^1$
\pureendow{<age>}{<duration>}	\Ax{\pureendow{x}{n}}	$A_{x:\bar{n}}^1$
\pureendowxn	\Ax{\pureendow{x}{n}}	$A_{x:\bar{n}}^1$
\endow{<age>}{<duration>}	\ax**{\endow{x}{n}}	$\ddot{a}_{x:\bar{n}}$
\endowxn	\ax**{\endow{x}{n}}	$\ddot{a}_{x:\bar{n}}$
\joint{ages}†	\Ax*{\joint{xy}z}	$\bar{A}_{\bar{x}\bar{y}z}$

† alias for \overline

Table 4: Shortcuts for varying benefit insurance and annuities

Definition	Output	Definition	Output
\IA	(IA)	\DA	(DA)
\IA*	(I\bar{A})	\DA*	(D\bar{A})
\IbA	(\bar{I}A)	\DbA	(\bar{D}A)
\IbA*	(\bar{I}\bar{A})	\DbA*	(\bar{D}\bar{A})
\ImA	(I^{(m)}A)	\DmA	(D^{(m)}A)
\ImA*	(I^{(m)}\bar{A})	\DmA*	(D^{(m)}\bar{A})
\Ia	(Ia)	\Da	(Da)
\Ia*	(I\bar{a})	\Da*	(D\bar{a})
\Ia**	(I\ddot{a})	\Da**	(D\ddot{a})
\Is	(Is)	\Ds	(Ds)
\Is*	(I\bar{s})	\Ds*	(D\bar{s})
\Is**	(I\ddot{s})	\Ds**	(D\ddot{s})

Table 5: Shortcuts and aliases for precedence numbers

Definition	Alias	Output
<code>\firsttop{<status>}</code>	<code>\itop{<status>}</code>	$A_{x:\bar{n}}^1$
<code>\secondtop{<status>}</code>	<code>\iitop{<status>}</code>	A_{xyz}^2
<code>\thirdtop{<status>}</code>	<code>\iiitop{<status>}</code>	A_{xyz}^3
<code>\firsttop*{<status>}</code>	<code>\itop*{<status>}</code>	$A_{x:\bar{n}}^1$
<code>\secondtop*{<status>}</code>	<code>\iitop*{<status>}</code>	A_{xyz}^2
<code>\thirdtop*{<status>}</code>	<code>\iiitop*{<status>}</code>	A_{xyz}^3
<code>\firstbottom{<status>}</code>	<code>\ibottom{<status>}</code>	A_{xyz}^1
<code>\secondbottom{<status>}</code>	<code>\iibottom{<status>}</code>	A_{xyz}^2
<code>\thirdbottom{<status>}</code>	<code>\iiibottom{<status>}</code>	A_{xyz}^3
<code>\firstbottom*{<status>}</code>	<code>\ibottom*{<status>}</code>	A_{xyz}^1
<code>\secondbottom*{<status>}</code>	<code>\iibottom*{<status>}</code>	A_{xyz}^2
<code>\thirdbottom*{<status>}</code>	<code>\iiibottom*{<status>}</code>	A_{xyz}^3

5 Package options

The package offers two options to control the placement of precedence numbers:

`alignpreced` always align top and bottom precedence numbers; makes `\nthtop` and `\nthbottom` equivalent to `\nthtop*` and `\nthbottom*`, respectively;

`compactpreced` always put precedence numbers close to the corresponding status; makes `\nthtop*` and `\nthbottom*` equivalent to `\nthtop` and `\nthbottom`, respectively.

Option `alignpreced` can be useful to simplify entry of uniformly positioned precedence numbers. On the other hand, option `compactpreced` is merely included as a complement to `alignpreced`. We do not recommended — nor see a reason — to use it as it basically renders inoperative commands `\nthtop*` and `\nthbottom*`.

A Comprehensive life contingencies symbol list

This appendix was inspired by Trivedi (2004). The title is a nod to the immensely useful *Comprehensive L^AT_EX Symbol List* of Pakin (2015).

The table below contains all the life contingencies symbols listed in Appendix 3 of Bowers et al. (1997) along with the code to compose them with `actuarialsymbol` (and therefore `actuarialangle`) loaded. Often times there are various ways to obtain a symbol; we tried to always present the most compact and legible option. Not all symbols require features of `actuarialsymbol`.

Calligraphic letters are typeset using `\mathcal{}`. The specific versions of \mathcal{L} and \mathcal{D} that appear in this table require package `rsfso` (Sharpe, 2015), which is *not* loaded by `actuarialsymbol`. Standard versions of the calligraphic letters are \mathcal{L} and \mathcal{D} . See Table 299 of Pakin (2015) for other options.

Symbol	Code to compose the symbol
a	<code>a</code>
$a(x)$	<code>a(x)</code>
a_x	<code>a_x</code>
$a_{\bar{K}}$	<code>\ax{\angl{K}}</code>
$\bar{a}_{\bar{n}}$	<code>\ax*{\angln}</code>
\bar{a}_{P_t}	<code>\ax*{P_t}</code>
$\bar{a}_{\bar{T}}$	<code>\ax*{\angl{T}}</code>
\bar{a}_x	<code>\ax*{x}</code>
\bar{a}_r^h	<code>\ax*{r}[h]</code>
\bar{a}_{x+t}^i	<code>\ax*{x + t}[i]</code>
\bar{a}_{x+t}^r	<code>\ax*{x + t}[r]</code>
$\ddot{a}_{\bar{K+1}}$	<code>\ax**{\angl{K + 1}}</code>
$\ddot{a}_x^{(m)}$	<code>\ax**{x}[(m)]</code>
$\mathring{a}_x^{(m)}$	<code>\aringx{x}[(m)]</code>
$\ddot{a}_x^{\{m\}}$	<code>\ax**{x}[\{m\}]</code>
$j\ddot{a}_x$	<code>\ax**[j]{x}</code>
$*\ddot{a}_x$	<code>\ax**[*]{x}</code>
$a_{x:\bar{n}}$	<code>\ax{\endowxn}</code>
$\bar{a}_{x:\bar{n}}$	<code>\ax*{\endowxn}</code>

Symbol	Code to compose the symbol
$\ddot{a}_{x:\bar{n}}$	<code>\ax**{\endowxn}</code>
$\ddot{a}_{x:\bar{n}}^{(m)}$	<code>\ax**{\endowxn}[(m)]</code>
$\dot{a}_{x:\bar{n}}^{(m)}$	<code>\aringx{\endowxn}[(m)]</code>
$\ddot{a}_{x:\bar{n}}^{\{m\}}$	<code>\ax**{\endowxn}[\{m\}]</code>
$\bar{a}_{\bar{x}:\bar{n}}$	<code>\ax*\{\joint\endowxn}</code>
${}^2\bar{a}_{x:\bar{n}}$	<code>\ax*[2]{\endowxn}</code>
$n a_x$	<code>\ax[n]{x}</code>
$n \bar{a}_x$	<code>\ax*[n]{x}</code>
$n \ddot{a}_x$	<code>\ax**[n]{x}</code>
$n \ddot{a}_x^{(m)}$	<code>\ax**[n]{x}[(m)]</code>
$\bar{a}_{xy z}^1$	<code>\ax*\{xy z\}[1]</code>
$\ddot{a}_{xy}^{(m)}$	<code>\ax**{\xy}{(m)}</code>
$\ddot{a}_{xy:\bar{n}}$	<code>\ax**[\bar{n}]{xy:\angln}</code>
${}^2\ddot{a}_{xy:\bar{n}}$	<code>\ax**[2]{xy:\angln}</code>
$\bar{a}_{x y}$	<code>\ax*\{x y\}</code>
$\bar{a}_{\bar{x}_1\bar{x}_2\bar{x}_3}$	<code>\ax*\{\joint{x_1 x_2 x_3}\}</code>
$(aA)(x)$	<code>\twoletsymb[0.6pt]{a}{A}(x)</code>
$(aA)_t$	<code>\twoletsymb[0.6pt]{a}{A}_t</code>
$(aC)_t$	<code>\twoletsymb[0.3pt]{a}{C}_t</code>
$(aF)_t$	<code>\twoletsymb[0.6pt]{a}{F}_t</code>
$(aU)_t$	<code>\twoletsymb[0.6pt]{a}{U}_t</code>
$(aV)(x)$	<code>\twoletsymb[0.6pt]{a}{V}(x)</code>
$(aV)_t$	<code>\twoletsymb[0.6pt]{a}{V}_t</code>
$A(h)$	<code>A(h)</code>
A_t	<code>A_t</code>
A_x	<code>\Ax{x}</code>
\bar{A}_x	<code>\Ax*x</code>
$A_x^{(m)}$	<code>\Ax{x}[(m)]</code>
\bar{A}_x^{PR}	<code>\Ax*x[\text{PR}]</code>
$A_{x:\bar{n}}^1$	<code>\Ax{\termxn}</code>
$A_{x:\bar{n}}$	<code>\Ax{\endowxn}</code>

Symbol	Code to compose the symbol
$\bar{A}_{x:\bar{n}}$	<code>\Ax*\{\endowxn\}</code>
$A_{x:\bar{n}}^1$	<code>\Ax{\pureendowxn}</code>
$_j A_x$	<code>\Ax[j]{x}</code>
$* A_x$	<code>\Ax[*]{x}</code>
$\bar{A}_{x:\bar{n}}^1$	<code>\Ax*\{\termxn\}</code>
$\tilde{A}_{x:\bar{n}}^1$	<code>\actssymb{\tilde{A}}{\termxn}</code>
${}^2 A_{x:\bar{n}}^1$	<code>\Ax[]{}[2]{\pureendowxn}</code>
${}^2 A_{x:\bar{n}}^1$	<code>\Ax[]{}[2]{\termxn}</code>
${}_{m } \bar{A}_x$	<code>\Ax*[m]{x}</code>
${}_{m n} \bar{A}_x$	<code>\Ax*[m n]{x}</code>
A_{xy}	<code>\Ax{xy}</code>
$A_{\overline{xy}}$	<code>\Ax{\joint{xy}}</code>
$A_{xy}^{(m)}$	<code>\Ax{xy}[(m)]</code>
\bar{A}_{xy}^2	<code>\Ax*\{x\itop{y}\}</code>
\bar{A}_{xy}^1	<code>\Ax*\{\itop{x}y\}</code>
$A_{xy:\bar{n}}$	<code>\Ax{xy:\angln}</code>
$\bar{A}_{xy:\bar{n}}^1$	<code>\Ax*\{\itop{\joint{xy}}:\angln\}</code>
${}^2 A_{xy:\bar{n}}$	<code>\Ax[]{}[2]{xy:\angln}</code>
\bar{A}_{wxy}^2	<code>\Ax*\{wx\itop{y}\}</code>
$\bar{A}_{x_1 x_2 x_3}$	<code>\Ax*\{\joint{x_1 x_2 x_3}\}</code>
${}_k AS$	<code>\actssymb[k]{\mathit{AS}}{}</code>
$\widehat{k AS}$	<code>\actssymb[k]{\widehat{\mathit{AS}}}{}</code>
$(AS)_{x+h}$	<code>\twoletsymb[0pt]{A}{S}_{x+h}</code>
(AAI)	<code>(\mathit{AAI})</code>
β	<code>\beta</code>
$\bar{\beta}$	<code>\bar{\beta}</code>
$\Gamma(\alpha)$	<code>\Gamma(\alpha)</code>
$b(u)$	<code>b(u)</code>
b_j	<code>b_j</code>
b_t	<code>b_t</code>
$b_f(t)$	<code>b_f(t)</code>

Symbol	Code to compose the symbol
B_t	<code>B_t</code>
\hat{B}_{x+k}	<code>\hat{B}_{x+k}</code>
$\hat{B}_{x+t}^{(3)}$	<code>\hat{B}_{x+t}^{(3)}</code>
$\hat{B}_{x+t}^{(j)}$	<code>\hat{B}_{x+t}^{(j)}</code>
$_hBP$	<code>\actsymbol[h]{\mathit{BP}}</code>
c	<code>c</code>
c_k	<code>c_k</code>
\hat{c}_k	<code>\hat{c}_k</code>
$c(t)$	<code>c(t)</code>
C_1	<code>C_1</code>
C_2	<code>C_2</code>
C_3	<code>C_3</code>
C_h	<code>C_h</code>
$_kCV$	<code>\actsymbol[k]{\mathit{CV}}</code>
$d_x^{(j)}$	<code>\dx{x}{(j)}</code>
$_n d_x$	<code>\dx[n]{x}</code>
$_n d_x^{(j)}$	<code>\dx[n]{x}{(j)}</code>
$_n d_x^{(\tau)}$	<code>\dx[n]{x}{(\tau)}</code>
$_t D_j$	<code>\actsymbol[t]{D}{j}</code>
$_{k+1}D$	<code>\actsymbol[k+1]{D}</code>
$(DA)_{x:\bar{n}}^1$	<code>\DA_{\term{x}{n}}</code>
$(D\bar{A})_{x:\bar{n}}^1$	<code>\DA*_{\term{x}{n}}</code>
$_n \mathcal{D}_x$	<code>\Dx[n]{x}</code>
$_n \mathcal{D}_x^{(j)}$	<code>\Dx[n]{x}{(j)}</code>
$_n \mathcal{D}_x^{(\tau)}$	<code>\Dx[n]{x}{(\tau)}</code>
e	<code>e</code>
e_{h-1}	<code>e_{h-1}</code>
e_x	<code>e_x</code>
\mathring{e}_x	<code>\ering{x}</code>
\hat{e}_k	<code>\hat{e}_k</code>

Symbol	Code to compose the symbol
$\dot{e}_{x:\bar{n}}$	<code>\er{ing}{\endow{x}{n}}</code>
e_{xy}	<code>e_{xy}</code>
$e_{\bar{x}\bar{y}}$	<code>e_{\joint{xy}}</code>
E	<code>\mathrm{E}</code>
E	<code>E</code>
E_0	<code>E_0</code>
nE_x	<code>\Ex[n]{x}</code>
$(ES)_{x+h+t}$	<code>\twoletsymb[0.6pt]{E}{S}_{x + h + t}</code>
$ELRA$	<code>\mathit{ELRA}</code>
f	<code>f</code>
$f(u, t)$	<code>f(u, t)</code>
$f_S(s)$	<code>f_S(s)</code>
$F_X(x)$	<code>F_X(x)</code>
F_t	<code>F_t</code>
$F^{(k)}$	<code>F^{(k)}</code>
$F_S(s)$	<code>F_S(s)</code>
$_kF$	<code>\actsymbol[k]{F}()</code>
G	<code>G</code>
\hat{G}	<code>\hat{G}</code>
$G(b)$	<code>G(b)</code>
$G(b)$	<code>G(b)</code>
$G(x; \alpha, \beta)$	<code>G(x; \alpha, \beta)</code>
$h(x)$	<code>h(x)</code>
$H(r)$	<code>H(r)</code>
$H(x; \alpha, \beta, x_0)$	<code>H(x; \alpha, \beta, x_0)</code>
${}_u(hp)_{x+t}^{(\tau)}$	<code>\actsymbol[u]{\twoletsymb{h}{p}}{x + t}[(\tau)]</code>
$(h\mu)_{x+t}^{(j)}(u)$	<code>\actsymbol{\twoletsymb{h}{\mu}}{x + t}[(j)](u)</code>
i'_{k+1}	<code>i'_{k + 1}</code>
\hat{i}_{k+1}	<code>\hat{i}_{k + 1}</code>
$i(s, s + t)$	<code>i(s, s + t)</code>

Symbol	Code to compose the symbol
I_k	I_k
I_d	I_d
$I_d(x)$	I_d(x)
$j_i k$	\actsymbol{j}{i}{k}
$(IA)_x$	\IA_x
$(I\bar{A})_x$	\IA*_x
$(\bar{I}\bar{A})_x$	\IBA*_x
$(I^{(m)}\bar{A})_x$	\ImA*_x
$(IA)_{x:\bar{n}}^1$	\IA_{\termxn}
J	J
$j(s, s + t, s + u)$	j(s, s + t, s + u)
$t\bar{k}_x$	\actsymbol{t}{\bar{k}}{x}
K	K
$K(x)$	K(x)
$K(xy)$	K(xy)
$K(\overline{xy})$	K(\joint{xy})
ℓ_x	\lx{x}
$\ell_{[x]+k}$	\lx{[x] + k}
$\ell_x^{(\tau)}$	\lx{x}[(\tau)]
$l(x, u)$	l(x, u)
$l_f(x, u)$	l_f(x, u)
L	L
L_1	L_1
L_x	L_x
$L(h)$	L(h)
tL	\actsymbol{t}{L}{}{}
tL^2	\actsymbol{t}{L}{}{}[\underline{2}]
tL_e	\actsymbol{t}{L}{e}{}{}
tL_e^2	\actsymbol{t}{L}{e}{}[\underline{2}]
$\mathcal{L}(x)$	\mathcal{L}(x)

Symbol	Code to compose the symbol
$\mathcal{L}_x^{(\tau)}$	<code>\Lx{x}[(\tau)]</code>
$m(x)$	<code>m(x)</code>
m_x	<code>m_x</code>
$m_x^{(j)}$	<code>m_x^{(j)}</code>
$m_x^{(\tau)}$	<code>m_x^{(\tau)}</code>
$m_x'{}^{(j)}$	<code>m_x^{\prime(j)}</code>
$M_X(t)$	<code>\mathrm{M}_X(t)</code>
$M(x)$	<code>M(x)</code>
$n(u)$	<code>n(u)</code>
N	<code>N</code>
$N(t)$	<code>N(t)</code>
$p(j)$	<code>p(j)</code>
$p(x)$	<code>p(x)</code>
p_k	<code>p_k</code>
$p_{[x]+r}$	<code>\px{x} + r</code>
$p^{*n}(x)$	<code>p^{*n}(x)</code>
$t p_x$	<code>\px[t]{x}</code>
$t p_x^{(\tau)}$	<code>\px[t]{x}[(\tau)]</code>
$t p_x'{}^{(j)}$	<code>\px[t]{x}[\prime(j)]</code>
$t p_{xy}$	<code>\px[t]{xy}</code>
$t p_{\bar{x}\bar{y}}$	<code>\px[t]{\joint{xy}}</code>
$u p_{\bar{x}\bar{y}+t}$	<code>\px[u]{\joint{xy} + t}</code>
$t p_{\bar{x}_1 \bar{x}_2 \bar{x}_3}^k$	<code>\px[t]{\joint{x_1 x_2} \nhtop{k}{\joint{x_3}}}</code>
$P(x)$	<code>P(x)</code>
$P(s, t)$	<code>P(s, t)</code>
P_t	<code>P_t</code>
${}^T P_t$	<code>\actsymbol[T]{P}{t}</code>
P^a	<code>P^a</code>
P_x	<code>P_x</code>
$j P_x$	<code>\Px[j]{x}</code>

Symbol	Code to compose the symbol
$*P_x$	\Px[*]{x}
$P_{x:\bar{n}}^A$	\Px{\endowxn}[A]
$P_{x:\bar{n}}$	\Px{\endowxn}
$P_{\bar{x}\bar{y}}$	\Px{\joint{xy}}
$P_{x:\bar{n}}^1$	\Px{:}{\termxn}
$P_{x:\bar{n}}^{\frac{1}{n}}$	\Px{\pureendowxn}
$P^{*n}(x)$	\P^{\star n}(x)
${}_h P_x$	\Px[h]{x}
${}_h P_{x:\bar{n}}$	\Px[h]{\endowxn}
$(Pa)(x)$	\twoletsymb[0.6pt]{P}{a}(x)
$(Pa)_t$	\twoletsymb[0.6pt]{P}{a}_t
$P(\bar{A}_{x:\bar{n}})$	\premium{\Ax{\endowxn}}
$P(n \ddot{a}_x)$	\premium{\ax{\n }{x}}
$P(n \bar{a}_x)$	\premium{\ax{\n }{x}}
$P^{(m)}(\bar{A}_x)$	\premium{\Ax{x}}[(m)]
$P^{\{m\}}(\bar{A}_x)$	\premium{\Ax{x}}[\{m\}]
$P(\bar{A}_x^{\text{PR}})$	\premium{\Ax{x}}[\text{PR}]
$\bar{P}(\bar{A}_{x:\bar{n}})$	\premium{\Ax{\endowxn}}
$\bar{P}(\bar{A}_{x:\bar{n}}^1)$	\premium{\Ax{\termxn}}
$\bar{P}(\bar{A}_{x:\bar{n}}^{\frac{1}{n}})$	\premium{\Ax{\pureendowxn}}
$P^{(m)}(\bar{A}_{x:\bar{n}})$	\premium{\Ax{\endowxn}}[(m)]
$P^{(m)}(\bar{A}_{x:\bar{n}}^1)$	\premium{\Ax{\termxn}}[(m)]
${}_h \bar{P}(\bar{A}_x)$	\premium[h]{\Ax{x}}
${}_h \bar{P}(\bar{A}_{x:\bar{n}})$	\premium[h]{\Ax{\endowxn}}
${}_h P^{(m)}(\bar{A}_x)$	\premium[h]{\Ax{x}}[(m)]
${}_h P^{(m)}(\bar{A}_{x:\bar{n}})$	\premium[h]{\Ax{\endowxn}}[(m)]
${}_h P^{\{m\}}(\bar{A}_{x:\bar{n}})$	\premium[h]{\Ax{\endowxn}}[\{m\}]
$P(\bar{A}_{\bar{x}\bar{y}\bar{z}}^2)$	\premium{\Ax{\joint{xy}}\iitop{\joint{z}}}}
$P(\bar{A}_{xyz}^2)$	\premium{\Ax{\ibottom{x}}\iitop{yz}}
$\tilde{P}_{x:\bar{n}}^1$	\tilde{P}{\bar{n}}_1{:}{\termxn}

Symbol	Code to compose the symbol
$q_{[x]+r}^{(d)}$	\qx{[x]} + r}
$q_x^{(i)}$	\qx{x}[(d)]
$q_x^{(r)}$	\qx{x}[(i)]
$q_x^{(w)}$	\qx{x}[(r)]
$q_x^{(j)}$	\qx{x}[(w)]
$\hat{q}_{x+k}^{(j)}$	\actsymbol{\hat{q}}{x+k}{(j)}
q_{xy}	\qx{xy}
$k q_x$	\qx[k]{x}
tq_x	\qx[t]{x}
$tq_x^{(j)}$	\qx[t]{x}{(j)}
$tq_x^{(\tau)}$	\qx[t]{x}{(\tau)}
$tq_x'^{(j)}$	\qx[t]{x}{\prime}{(j)}
$t uq_x$	\qx[t u]{x}
nq_{xy}^1	\qx[n]{\itop{xy}}
nq_{xy}^2	\qx[n]{x\itop{y}}
$k q_{xy}$	\qx[k]{xy}
nq_{xyz}^2	\qx[n]{\ibottom{xyz}\itop{yz}}
∞q_{xyz}^3	\qx[\infty]{\ibottom*{xyz}\ibottom*{y}\itop{z}}
r	r
r_C	r_C
r_F	r_F
r_N	r_N
$(rA)_t$	\twoletsymbol[0.6pt]{r}{A}_t
$(rF)_t$	\twoletsymbol[0.6pt]{r}{F}_t
$(rV)_t$	\twoletsymbol[0.6pt]{r}{V}_t
R	R
\tilde{R}	\tilde{R}
$R(x, h, y)$	R(x, h, y)
$s(x)$	s(x)

Symbol	Code to compose the symbol
$\ddot{s}_{\bar{n}}$	<code>\sx**{\angln}</code>
$s(x, u)$	<code>s(x,u)</code>
$\bar{s}_{x:\bar{n}}$	<code>\sx*{\endowxn}</code>
$\ddot{s}_{x:\bar{n}}$	<code>\sx**{\endowxn}</code>
S	<code>S</code>
$S(t)$	<code>S(t)</code>
S_y	<code>S_y</code>
${}_kSC$	<code>\actsymbol{k}{\mathit{SC}}{}</code>
T	<code>T</code>
\tilde{T}	<code>\tilde{T}</code>
T_x	<code>T_x</code>
T_{xy}	<code>T_{xy}</code>
$T_{\overline{xy}}$	<code>T_{\joint{xy}}</code>
$U(t)$	<code>U(t)</code>
U_t	<code>U_t</code>
$\hat{U}t$	<code>\hat{U}\{t\}</code>
v_t	<code>v_t</code>
\tilde{v}_n	<code>\tilde{v}_n</code>
V_i	<code>V_i</code>
V_t	<code>V_t</code>
${}_kV_x$	<code>\Vx{k}{x}</code>
${}_kV_{x:\bar{n}}$	<code>\Vx{k}{\endowxn}</code>
${}_kV_{x:\bar{n}}^1$	<code>\Vx{k}{\text{:}\term{x}}</code>
${}_kV_{x:\bar{n}}^1$	<code>\Vx{k}{\pureendowxn}</code>
${}_kV_x^{\text{FPT}}$	<code>\Vx{k}{x}{\text{FPT}}</code>
${}_tV_{\overline{xy}:\bar{n}}^1$	<code>\Vx{t}{\itop{\group{xy}}:\angln}</code>
${}_hV_x$	<code>\Vx{k}{h}{x}</code>
${}_hV_{x:\bar{n}}$	<code>\Vx{k}{h}{\endowxn}</code>
${}_hV_{x:\bar{n}}^{(m)}$	<code>\Vx{k}{h}{\endowxn}{(m)}</code>
${}_hV_{x:\bar{n}}^{\text{Mod}}$	<code>\Vx{k}{h}{\endowxn}{\text{Mod}}</code>

Symbol	Code to compose the symbol
$_k V(n \ddot{a}_x)$	\reserve[k]{\ax**[n]{x}}
$_t \bar{V}(n \bar{a}_x)$	\reserve*[t]{\ax*[n]{x}}
$_t \bar{V}(\bar{A}_x)$	\reserve*[t]{\Ax*x}
$_t \bar{V}(\bar{A}_{x:\bar{n}})$	\reserve*[t]{\Ax*\{\endowxn\}}
$_t \bar{V}(\bar{A}_{x:\bar{n}}^1)$	\reserve*[t]{\Ax*\{\termxn\}}
$_t \bar{V}(\bar{A}_{x:\bar{n}}^1)$	\reserve*[t]{\Ax*\{\pureendowxn\}}
$_t \bar{V}(\bar{A}_x)^{\text{Mod}}$	\reserve*[t]{\Ax*x}^{\text{\text{Mod}}}
$_t V(\bar{A}_{\bar{x}\bar{y}})$	\reserve[t]{\Ax*\{\joint{xy}\}}
$_t V^{\{1\}}(\bar{A}_x)$	\reserve[t]{\Ax*x}[\{1\}]
$_k V(\bar{A}_x^{\text{PR}})$	\reserve[k]{\Ax*x}[\text{PR}]
${}_k^h V(A_{x:\bar{n}}^1)$	\reserve[k][h]{\Ax*\{\termxn\}}
${}_t^h \bar{V}(\bar{A}_x)$	\reserve*[t][h]{\Ax*x}
${}_t^h \bar{V}(\bar{A}_{x:\bar{n}})$	\reserve*[t][h]{\Ax*\{\endowxn\}}
${}_t^h \bar{V}^{(m)}(\bar{A}_{x:\bar{n}})$	\reserve*[t][h]{\Ax*\{\endowxn\}}[(m)]
$w(x)$	w(x)
W_i	W_i
W_t	W_t
$_k W$	\Wx[k]{}{}
$_k W_x$	\Wx[k]{x}
$_k W_{x:\bar{n}}$	\Wx[k]{\endowxn}
$_k^h W_x$	\Wx[k][h]{x}
$(Wa)_t$	\twoletsymb{W}{a}_t
$_k \bar{W}(A_x)$	\paidup*[k]{\Ax{x}}
$_k \bar{W}(A_{x:\bar{n}})$	\paidup*[k]{\Ax{\endowxn}}
$_k \bar{W}(A_x)$	\paidup*[k][h]{\Ax{x}}
(x)	(x)
$(x_1 x_2 \cdots x_m)$	(x_1 x_2 \dots x_m)
$(\overline{x_1 x_2 \cdots x_m})$	(\joint{x_1 x_2 \dots x_m})
$\frac{k}{x_1 x_2 \cdots x_m}$	\joint{x_1 x_2 \dots x_m}\nthtop{k}{\joint{x_m}}

Symbol	Code to compose the symbol
$\overline{x_1 x_2 \cdots x_m}^{[k]}$	<code>\joint{x_1}{x_2}{\dots}{\nthtop{[k]}{\joint{x_m}}}</code>
X_i	<code>X_i</code>
$X(\theta)$	<code>X(\theta)</code>
Y	<code>Y</code>
$y(s, s + m)$	<code>y(s, s + m)</code>
$Y(t, n)$	<code>Y(t, n)</code>
z_t	<code>z_t</code>
Z	<code>Z</code>
$_m Z_t$	<code>\actsymbol{m}{Z}{t}</code>
α	<code>\alpha</code>
$\alpha(m)$	<code>\alpha(m)</code>
$\bar{\alpha}$	<code>\bar{\alpha}</code>
α^{CRVM}	<code>\alpha^{\text{CRVM}}</code>
β	<code>\beta</code>
$\beta(m)$	<code>\beta(m)</code>
$\bar{\beta}$	<code>\bar{\beta}</code>
β^{CRVM}	<code>\beta^{\text{CRVM}}</code>
$\beta(x, u)$	<code>\beta(x, u)</code>
$\Gamma(\alpha)$	<code>\Gamma(\alpha)</code>
δ	<code>\delta</code>
δ_t	<code>\delta_t</code>
θ	<code>\theta</code>
$\lambda(t)$	<code>\lambda(t)</code>
$\lambda(t, n)$	<code>\lambda(t, n)</code>
Λ	<code>\Lambda</code>
Λ_h	<code>\Lambda_h</code>
$\mu(x)$	<code>\mu(x)</code>
$\mu_x(t)$	<code>\mu_x(t)</code>

Symbol	Code to compose the symbol
$\mu_x^{(d)}$	<code>\mu_x^{(d)}</code>
$\mu_x^{(i)}$	<code>\mu_x^{(i)}</code>
$\mu_x^{(w)}$	<code>\mu_x^{(w)}</code>
$\mu_x^{(j)}(t)$	<code>\mu_x^{(j)}(t)</code>
$\mu_x^{(\tau)}(t)$	<code>\mu_x^{(\tau)}(t)</code>
$\mu_{xy}(t)$	<code>\mu_{xy}(t)</code>
$\mu_{\overline{xy}}(t)$	<code>\mu_{\overline{xy}}(t)</code>
$\mu(x, u)$	<code>\mu(x, u)</code>
π_h	<code>\pi_h</code>
π_t	<code>\pi_t</code>
ρ	<code>\rho</code>
τ	<code>\tau</code>
$\phi(x)$	<code>\phi(x)</code>
$\phi(x, u)$	<code>\phi(x, u)</code>
$\Psi(u)$	<code>\Psi(u)</code>
$\tilde{\Psi}(u)$	<code>\tilde{\Psi}(u)</code>
$\Psi(u, t)$	<code>\Psi(u, t)</code>
$\Psi(u; w)$	<code>\Psi(u; w)</code>
$\tilde{\Psi}(u; w)$	<code>\tilde{\Psi}(u; w)</code>
ω	<code>\omega</code>

B Implementation

This appendix contains the annotated source code of the package. Most readers can stop reading here.

B.1 Required packages

RequirePackage The package depends on packages amsmath (American Mathematical Society, 2002) and actuarialangle (Goulet, 2017).

```
1 \RequirePackage{amsmath}
2 \RequirePackage{actuarialangle}
```

B.2 Package options

\ifacts@alignpreced We define two flags to keep track of the type of alignment for precedence numbers. Both are false by default.

```
1 \newif\ifacts@alignpreced
2 \newif\ifacts@compactpreced
```

\DeclareOption Declaration of the package options and processing.

```
5 \DeclareOption{alignpreced}{\acts@alignprecedtrue}
6 \DeclareOption{compactpreced}{\acts@compactprecedtrue}
7 \ProcessOptions
```

B.3 Actuarial symbol

We face three main challenges when trying to compose actuarial symbols: position a subscript and a superscript to the left of a main symbol; ensure that the left and right subscripts and superscripts are vertically aligned; maintain consistency with the placement of subscripts and superscripts elsewhere in the document.

B.3.1 User level and parsing commands

actsymb We first define the user level command.

```
8 \DeclareRobustCommand{\actsymb}{\acts@actsymb}
```

\acts@actsymb With its unusual syntax, \actsymb requires four parsing macros to pass the arguments to the actual workhorse \@actsymbol.

\acts@@@actsymb 9 \newcommand{\acts@actsymb}{%

\acts@@@@actsymb 10 \@ifnextchar[{\acts@@@actsymb}{%

```

11          {\acts@@actssymb[]}}
12 \newcommand\acts@@actssymb{}
13 \def\acts@@actssymb[#1]{%
14   \@ifnextchar[{\acts@@@actssymb[#1]}{%
15     {\acts@@@actssymb[#1][]}}}
16 \newcommand\acts@@@actssymb{}
17 \def\acts@@@actssymb[#1][#2]{%
18   \@ifnextchar[{\acts@@@@actssymb[#1][#2]}{%
19     {\acts@@@@actssymb[#1][#2][]}}}
20 \newcommand\acts@@@@actssymb{}
21 \def\acts@@@@actssymb[#1][#2][#3]{%
22   \@ifnextchar[{\@actsymbol[#1][#2][#3]{#4}{#5}}{%
23     {\@actsymbol[#1][#2][#3]{#4}{#5}[]}}}

```

B.3.2 Symbol construction

\@actsymbol We now define the workhorse to compose an actuarial symbol allowing for auxiliary symbols on all four corners around a principal symbol. The macro \@actsymbol has the following six arguments, using the notation from of the schematics representations (1) and (2):

1. lower left subscript \boxed{I} ; may be empty;
2. upper left superscript \boxed{II} ; may be empty;
3. principle symbol P ; when empty a standard symbol is typeset;
4. principal symbol S ; assumed present;
5. lower right subscript \boxed{III} ; assumed present;
6. upper right superscript \boxed{IV} ; may be empty.

The definition below is heavily inspired by the code of \prescript from package mathtools ([Høgholm and Madsen, 2015](#)) which, as reported by the author, is itself based on a posting to comp. text by Michael J. Downes. Some of the comments below are still his.

```
24 \def\@actsymbol[#1][#2][#3]{#4}{#5}{#6}{
```

We put the principle symbol and all subscripts and superscript into horizontal boxes using \mathmeasure of package amsmath.

```

25  \mathmeasure{z@\displaystyle{#3}}
26  \mathmeasure{@ne@\scriptstyle{#1}}
27  \mathmeasure{tw@\scriptstyle{#2}}
28  \mathmeasure{thr@\scriptstyle{#5}}
29  \mathmeasure{4@\scriptstyle{#6}}
```

Do not let a preceding mathord symbol approach without any intervening space.

```
30  \mathord{}
```

Right align the left subscript and superscript (if there is a superscript) by adjusting the width of their horizontal boxes.

```

31 \ifdim \wd\tw@>\z@ \ifdim \wd\tw@>\wd\@ne
32   \setbox\@ne\hbox to\wd\tw@{\hfil\unhbox\@ne}
33 \else
34   \setbox\tw@\hbox to\wd\@ne{\hfil\unhbox\tw@}
35 \fi\fi

```

Bottom align the left and right subscripts by making their heights equal.

```

36 \ifdim \ht\@ne>\ht\thr@@
37   \ht\thr@@=\ht\@ne
38 \else
39   \ht\@ne=\ht\thr@@
40 \fi

```

Actual symbol construction. First the case where there is at least one superscript (the nested conditionals emulate an OR condition).

```

41 \ifnum\ifdim \wd\tw@>\z@ 1\else\ifdim \wd4>\z@ 1\else 0\fi\fi
42 =1

```

To ensure equal spacing with the subscripts on both sides of the principal symbol, make the depths of the left and right supercripts equal.

```
43 \ifdim \dp\tw@>\dp4 \dp4=\dp\tw@\else \dp\tw@=\dp4\fi
```

Typesetting of the left subscript and superscript. Use `\mathopen` to suppress space between those and the principal symbol even when the latter is not of type ord. (We use `\textstyle` inside `\vphantom` to avoid bad positioning of subscripts with X_ET_EX; see [the discussion](#) on StackExchange for details.)

```
44 \mathopen{\vphantom{\textstyle #4}{\box\tw@}\sb{\box\@ne}}%
```

Typesetting of the principal symbol and the right subscript and superscript. The principal symbol is either a principal symbol alone or a principle symbol and a benefit symbol between parentheses. In the latter case, we make sure to align the subscripts and superscripts only around the principle symbol.

```

45 \ifdim\wd\z@=\z@
46   #4^{\box4}\sb{\box\thr@@}%
47 \else
48   #3^{\box4}\sb{\vphantom{\copy\thr@@}(#4\sb{\box\thr@@})}%
49 \fi
50 \else

```

Same ideas as above in the simpler case without superscripts. That way, T_EX's default placement of subscripts and superscripts is maintained.

```

51   \mathopen{\vphantom{\textstyle #4}\sb{\box@ne}}%
52   \ifdim\wd\z@=\z@
53     #4\sb{\box\thr@@}%
54   \else
55     #3(#4\sb{\box\thr@@})%
56   \fi
57 \fi
58 }

```

B.3.3 Shortcuts for basic symbols of life tables, insurance and annuities

\@actinssc We first define the internal macros and parsing macros used to define shortcuts for insurance benefits (\@actinssc), annuity benefits (\@actannsc) and simple symbols (\@actothersc).

```

59 \newcommand{\@actinssc}[1]{%
60   \@ifstar{\acts@actsc{\bar{#1}}}{%
61     {\acts@actsc{#1}}}
62 \newcommand{\@actannsc}[1]{%
63   \@ifstar{\@ifstar{\acts@actsc{\ddot{#1}}}{%
64     {\acts@actsc{\bar{#1}}}}}{%
65     {\acts@actsc{#1}}}
66 \newcommand{\acts@actsc}[1]{%
67   \@ifnextchar[{\acts@actsc{#1}}{%
68     {\acts@actsc{#1}[]}}
69 \let\@actothersc\acts@actsc
70 \newcommand{\acts@actsc}{}
71 \def\acts@actsc#1[#2]{%
72   \@ifnextchar[{\acts@actsc{#1}[#2]}{%
73     {\acts@actsc{#1}[#2]}}
74 \newcommand{\acts@@actsc}{}
75 \def\acts@@actsc#1[#2][#3][#4]{%
76   \@ifnextchar[{\@actsymbol{#2}[#3][#1][#4]}{%
77     {\@actsymbol{#2}[#3][#1][#4]}}}

```

\DeclareRobustCommand We can now define all the shortcuts of [Table 1](#).

```

78 \DeclareRobustCommand{\lx}{\@actothersc {\ell}}
79 \DeclareRobustCommand{\Lx}{\@actothersc {\mathcal{L}}}
80 \DeclareRobustCommand{\dx}{\@actothersc d}
81 \DeclareRobustCommand{\Dx}{\@actothersc {\mathcal{D}}}
82 \DeclareRobustCommand{\px}{\@actothersc p}
83 \DeclareRobustCommand{\qx}{\@actothersc q}
84 \DeclareRobustCommand{\Ax}{\@actinssc A}
85 \DeclareRobustCommand{\Ex}{\@actinssc E}

```

```

86 \DeclareRobustCommand{\ax}{\@actannsc a}
87 \DeclareRobustCommand{\sx}{\@actannsc s}
88 \DeclareRobustCommand{\aringx}{\@actothersc{\mathring{a}}}
89 \DeclareRobustCommand{\erinx}{\@actothersc{\mathring{e}}}

```

B.3.4 Shortcuts for premiums, reserves and paid-up insurance

\@actpremres Not unlike above, we first define the internal and parsing macros used to create shortcut for premiums, reserves and paid-up insurance symbols.

```

90 \newcommand{\actpremres}[1]{%
91   \@ifstar{\acts@actpremres{\bar{#1}}}{%
92     {\acts@actpremres{#1}}}
93 \newcommand{\acts@actpremres}[1]{%
94   \@ifnextchar[{\acts@@actpremres{#1}}{%
95     {\acts@@actpremres{#1}[]}}
96 \newcommand{\acts@actpremres}{}%
97 \def{\acts@actpremres#1[#2]}{%
98   \@ifnextchar[{\acts@@actpremres{#1}[#2]}{%
99     {\acts@@actpremres{#1}[#2][]}}
100 \newcommand{\acts@@actpremres}{}%
101 \def{\acts@@actpremres#1[#2][#3]}{%
102   \@ifnextchar[{\actsymbol{#2}[#3][#1]{#4}}{%
103     {\actsymbol{#2}[#3][#1]{#4}[]}}}

```

\DeclareRobustCommand Then we can define the shortcuts of [Table 2](#).

```

104 \DeclareRobustCommand{\Px}{\@actothersc P}
105 \DeclareRobustCommand{\Vx}{\@actothersc V}
106 \DeclareRobustCommand{\Wx}{\@actothersc W}
107 \DeclareRobustCommand{\premium}{\@actpremres P}
108 \DeclareRobustCommand{\reserve}{\@actpremres V}
109 \DeclareRobustCommand{\paidup}{\@actpremres W}

```

B.3.5 Shortcuts for auxiliary symbols

\DeclareRobustCommand Here we define the shortcuts for common auxiliary symbols listed in [Table 3](#). Command \joint is simply defined as an alias of \overline.

```

110 \DeclareRobustCommand{\term}[2]{\itop{#1}:\angl{#2}}
111 \DeclareRobustCommand{\termxn}{{\itop{x}}:\angln}
112 \DeclareRobustCommand{\pureendow}[2]{#1:\itop{\angl{#2}}}
113 \DeclareRobustCommand{\pureendowxn}{{x:\itop{\angln}}}
114 \DeclareRobustCommand{\endow}[2]{#1:\angl{#2}}
115 \DeclareRobustCommand{\endowxn}{{x:\angln}}
116 \let{\joint}{\overline}

```

B.4 Two-letter symbols

\twoletkern	The definition of the user level command \twoletsymb is pretty straightforward.
\twoletsymb	
	117 \newlength{\twoletkern} 118 \setlength{\twoletkern}{1.2pt} 119 \DeclareRobustCommand{\twoletsymb}[3][\twoletkern]{(#2\kern-#1#3)}
\@twoletinssc	Following the same lines as above, we define two internal macros to create
\@twoletannsc	shortcuts for two-letter insurance and annuity benefit symbols.
	120 \newcommand{\@twoletinssc}[3][\twoletkern]{% 121 \@ifstar{\twoletsymb[#1]{#2}{\bar{#3}}}{% 122 {\twoletsymb[#1]{#2}{#3}}} 123 \newcommand{\@twoletannsc}[3][\twoletkern]{% 124 \@ifstar{\@ifstar{\twoletsymb[#1]{#2}{\ddot{#3}}}{% 125 {\twoletsymb[#1]{#2}{\bar{#3}}}}}{% 126 {\twoletsymb[#1]{#2}{#3}}}
\newcommand	Follow the shortcuts of Table 4 . Note that we used a smaller negative kerning adjustment for symbols annuity symbols.
	127 \newcommand{\IA}{\@twoletinssc IA} 128 \newcommand{\IBA}{\@twoletinssc{\bar{I}}A} 129 \newcommand{\ImA}{\@twoletinssc{I^{(m)}}A} 130 \newcommand{\DA}{\@twoletinssc DA} 131 \newcommand{\DbA}{\@twoletinssc{\bar{D}}A} 132 \newcommand{\DmA}{\@twoletinssc{D^{(m)}}A} 133 \newcommand{\Ia}{\@twoletannsc[0.5\twoletkern]Ia} 134 \newcommand{\Is}{\@twoletannsc[0.5\twoletkern]Is} 135 \newcommand{\Da}{\@twoletannsc[0.5\twoletkern]Da} 136 \newcommand{\Ds}{\@twoletannsc[0.5\twoletkern]Ds}

B.5 Precedence numbers

The system of precedence numbers builds on a backbone that used to be part of package `actuarialangle`. The author of the code is unknown. Some of the comments on \@precedence, below, are his or hers.

B.5.1 User level lengths and commands

\nthtopsep	Let us start by defining the lengths needed to position the precedence
\nthtopskip	numbers above or below the statuses.
\nthbottomsep	137 \newlength{\nthtopsep}
\nthbottomskip	138 \setlength{\nthtopsep}{2\p@}

```

139 \newlength{\nthtopskip}
140 \setlength{\nthtopskip}{7\p@}
141 \newlength{\nthbottomsep}
142 \setlength{\nthbottomsep}{2\p@}
143 \newlength{\nthbottomskip}
144 \setlength{\nthbottomskip}{9\p@}

```

\nthtop Next up are the two user level commands and the internal commands that
\nthbottom call the workhorse \@precedence.

```

145 \DeclareRobustCommand{\nthtop}{\@ifstar\varnthtop\@nthtop}
146 \DeclareRobustCommand{\nthbottom}{\@ifstar\varnthbottom\@nthbottom}
147 \newcommand{\@nthtop}[3][\nthtopsep]{%
148   \mathpalette{\@precedence t{#1}{#2}}{#3}}
149 \newcommand{\@varnthtop}[3][\nthtopskip]{%
150   \mathpalette{\@precedence t{#1}{z{#2}}}{#3}}
151 \newcommand{\@nthbottom}[3][\nthbottomsep]{%
152   \mathpalette{\@precedence b{#1}{z{#2}}}{#3}}
153 \newcommand{\@varnthbottom}[3][\nthbottomskip]{%
154   \mathpalette{\@precedence b{#1}{z{#2}}}{#3}}

```

\@nthtop With the internal commands defined we can now process the package
\@nthbottom options. Option alignpreced makes the internal macros \@nthtop and
\@nthbottom equivalent to \@varnthtop and \@varnthbottom, respectively.

```

155 \iffacts@alignpreced
156   \let\@nthtop\varnthtop
157   \let\@nthbottom\varnthbottom
158 \fi

```

\@varnthtop Option compactpreced does the opposite.

```

159 \iffacts@compactpreced
160   \let\@varnthtop\nthtop
161   \let\@varnthbottom\nthbottom
162 \fi

```

B.5.2 Number and status positioning

\@precedence We now define the workhorse to position precedence numbers above
or below statuses, smashed so that the height of the auxiliary symbol
containing the call remains unaffected. The macro \@precedence has the
following six arguments:

1. t for top or b for bottom;
2. baseline skip between the top and bottom symbols;
3. spacing between the top and bottom symbols;

4. first argument from the user;
5. one of math style selecting commands (`\displaystyle`, `\textstyle`, `\scriptstyle`, `\scriptscriptstyle`) from `\mathpalette`;
6. second argument given by the user.

This peculiar ordering of the arguments is done to work around the restriction of `\mathpalette` that it only reads two arguments.

```

163 \def\@precedence#1#2#3#4#5#6{%
164   \setbox\tw@\hbox{$\m@th#5#4$}%
165   \setbox\z@\hbox{$\m@th#5#6$}%
166   \dimen@\wd\z@
167   \vbox to\ht\z@{%
168     \baselineskip=#2
169     \lineskip=#3
170     \lineskiplimit\lineskip
171     \if b#1\relax\box\z@\else\vss\fi
172     \hbox to\dimen@{\hss\unhbox\tw@\hss}%
173     \if t#1\relax\box\z@\else\vss\fi
174   }
175 }
```

B.5.3 Shortcuts and aliases

`\DeclareRobustCommand` We finish off by defining the shortcuts and aliases of [Table 5](#).

```

176 \DeclareRobustCommand{\firsttop}{%
177   \@ifstar{\@varnthtop{1}}{\@nthtop{1}}}
178 \DeclareRobustCommand{\secondtop}{%
179   \@ifstar{\@varnthtop{2}}{\@nthtop{2}}}
180 \DeclareRobustCommand{\thirdtop}{%
181   \@ifstar{\@varnthtop{3}}{\@nthtop{3}}}
182 \DeclareRobustCommand{\firstbottom}{%
183   \@ifstar{\@varnthbottom{1}}{\@nthbottom{1}}}
184 \DeclareRobustCommand{\secondbottom}{%
185   \@ifstar{\@varnthbottom{2}}{\@nthbottom{2}}}
186 \DeclareRobustCommand{\thirdbottom}{%
187   \@ifstar{\@varnthbottom{3}}{\@nthbottom{3}}}
188 \let\itop\firsttop
189 \let\iitop\secondtop
190 \let\iiitop\thirdtop
191 \let\ibottom\firstbottom
192 \let\iibottom\secondbottom
193 \let\iiibottom\thirdbottom
```

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Version history

1.0	1.0a
General: Initial release.	1
	\@actsymbol: Fix left subscript positioning with xetex.
	29