The xint bundle: xint, xintfrac, xintexpr, xintbinhex, xintgcd, xintseries and xintcfrac.

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Abstract

The xint package implements with expandable TEX macros the basic arithmetic operations of addition, subtraction, multiplication and division, applied to arbitrarily long numbers represented as chains of digits with an optional minus sign. The xintfrac package extends the scope of xint to fractional numbers with arbitrarily long numerators and denominators.

xintexpr provides an expandable parser `\xintexpr . . . \relax` of expressions constructed with decimal numbers, fractions, numbers in scientific notation, the basic operations as infix operators, parentheses, sign prefixes, factorial symbol, and sub-expressions or macros expanding to the previous items.

The xintbinhex package is for conversions to and from binary and hexadecimal bases, xintseries provides some basic functionality for computing in an expandable manner partial sums of series and power series with fractional coefficients, xintgcd implements the Euclidean algorithm and its typesetting, and xintcfrac deals with the computation of continued fractions.

Most macros, and all of those doing computations, work purely by expansion without assignments, and may thus be used almost everywhere in TEX.

The packages may be used with any flavor of TEX supporting the ε-TEX extensions. LATEX users will use `\usepackage` and others `\input` to load the package components.

Contents

1 Presentation

1.1 Recent changes

Release 1.08b:

- Correction of a problem with spaces inside \xintexpr-essions.
- Additional improvements to the handling of floating point numbers.
- The macros of **xintfrac** allow to use count registers in their arguments in ways which were not previously documented. See Use of count registers.

Release 1.08a:

- Improved efficiency of the basic conversion from exact fractions to floating point numbers, with ensuing speed gains especially for the power function macros \xintFloatPow and \xintFloatPower,
- Better management by the **xintfrac** macros \xintCmp, \xintMax, \xintMin and \xintGeq of inputs having big powers of ten in them.
- Macros for floating point numbers added to the **xintseries** package.

Release 1.08:

- Extraction of square roots, for floating point numbers (\xintFloatSqrt), and also in a version adapted to integers (\xintiSqrt).
- New package **xintbinhex** providing conversion routines to and from binary and hexadecimal bases.

Release 1.07:

- The **xintfrac** macros accept numbers written in scientific notation, the \xintFloat command serves to output its argument with a given number D of significant figures. The value of D is either given as optional argument to \xintFloat or set with \xintDigits := D;. The default value is 16.
- The **xintexpr** package is a new core constituent (which loads automatically **xintfrac** and **xint**) and implements the expandable expanding parsers
  \xintexpr . . . \relax, and its variant \xintfloatexpr . . . \relax
  allowing on input formulas using the standard form with infix operators +, -, *, /, and ^, and arbitrary levels of parenthesizing. Within a float expression the operations are executed according to the current value of \xintDigits. Within an \xintexpr-ession the binary operators are computed exactly.

The floating point precision D is set (this is a local assignment to a \mathchar variable) with \xintDigits := D; and queried with \xinttheDigits. It may be set to anything up to 32767.[1] The macro incarnations of the binary operations admit an optional argument which will replace pointwise D; this argument may exceed the 32767 bound.

To write the \xintexpr parser I benefited from the commented source of the LaTeX3 parser; the \xintexpr parser has its own features and peculiarities. See its documentation.

[1] but values higher than 100 or 200 will presumably give too slow evaluations.

1.2 Overview

The main characteristics are:

1. exact algebra on arbitrarily big numbers, integers as well as fractions,
2. floating point variants with user-chosen precision,
3. implemented via macros compatible with expansion-only context.

'Arbitrarily big': this means with less than `2^31-1=2147483647` digits, as most of the macros will have to compute the length of the inputs and these lengths must be treatable as TEX integers, which are at most `2147483647` in absolute value. This is a distant theoretical upper bound, the true limitation is from the *time* taken by the expansion-compatible algorithms, this will be commented upon soon.

As just recalled, ten-digits numbers starting with a `3` already exceed the TEX bound on integers; and TEX does not have a native processing of floating point numbers (multiplication by a decimal number of a dimension register is allowed — this is used for example by the pgf basic math engine.)

TEX elementary operations on numbers are done via the non-expandable *advance, multiply,* and *divide* assignments. This was changed with ε-TEX's `\numexpr` which does expandable computations using standard infix notations with TEX integers. But ε-TEX did not modify the TEX bound on acceptable integers, and did not add floating point support.

The bigintcalc package by Heiko Oberdiek provided expandable operations (using some of `\numexpr` possibilities, when available) on arbitrarily big integers, beyond the TEX bound. The present package does this again, using more of `\numexpr` (**`xint`** requires the ε-TEX extensions) for higher speed, and also on fractions, not only integers. Arbitrary precision floating points operations are a derivative, and not the initial design goal.[2, 3]

The LATEX3 project has implemented expandably floating-point computations with 16 significant figures (l3fp), including special functions such as exp, log, sine and cosine.

The **`xint`** package can be used for 24, 40, etc... significant figures but one rather quickly (not much beyond 100 figures perhaps) hits against a 'wall' created by the constraint of expandability: currently, multiplying out two one-hundred digits numbers takes circa 80 or 90 times longer than for two ten-digits numbers, which is reasonable, but multiplying out two one-thousand digits numbers takes more than 500 times longer than for two one hundred-digits numbers. This shows that the algorithm is drifting from quadratic to cubic in that range. On my laptop multiplication of two 1000-digits numbers takes some seconds, so it can not be done routinely in a document.[4]

[2] currently (`v1.08`), the only non-elementary operation implemented for floating point numbers is the square-root extraction; furthermore no `NaN`'s nor error traps has been implemented, only the notion of 'scientific notation with a given number of significant figures'.

[3] multiplication of two floats with `P=\xinttheDigits` digits is first done exactly then rounded to `P` digits, rather than using a specially tailored multiplication for floating point numbers which would be more efficient (it is a waste to evaluate fully the multiplication result with `2P` or `2P-1` digits.)

[4] without entering into too much technical details, the source of this 'wall' is that when dealing with two long operands, when one wants to pick some digits from the second one, one has to jump above all digits constituting the first one, which can not be stored away: expandability forbids assignments to memory storage. One may envision some sophisticated schemes, dealing with this problem in less naive ways, trying to move big chunks of data higher up in the input stream and come back to it later, etc...; but each 'better' algorithm adds overhead for the smaller inputs. For example, I have another

The conclusion perhaps could be that it is in the end lucky that the speed gains brought by **xint** for expandable operations on big numbers do open some non-empty range of applicability in terms of the number of kept digits for routine floating point operations.

The second conclusion, somewhat depressing after all the hard work, is that if one really wants to do computations with *hundreds* of digits, one should drop the expandability requirement. And indeed, as clearly demonstrated long ago by the pi computing file by D. Roegel one can program TEX to compute with many digits at a much higher speed than what **xint** achieves: but, direct access to memory storage in one form or another seems a necessity for this kind of speed and one has to renounce at the complete expandability.[5] [6]

1.3 Missing things

'Arbitrary-precision' floating-point operations are currently limited to the basic four operations, the power function with integer exponent, and the extraction of square-roots.

1.4 Some examples

The main initial goal is to allow computations with integers and fractions of arbitrary sizes.

Here are some examples. The first one uses only the base module **xint**, the next two require the **xintfrac** package, which deals with fractions. Then two examples with the **xintgcd** package, one with the **xintseries** package, and finally a computation with a float. Some inputs are simplified by the use of the **xintexpr** package.

123456^99:

```
\xintiPow{123456}{99}: 114738181166266556633273330008454586747025480423426102975889545437359089469703202762264705426632058346902708682211681334152500324038762776168953222117634295872033762216088606915850757168019716710712087697033536507377487778737784987816067499997983665812517232752154970541659566738491153332674854107560766971890623518995832377826369998110953239399323518999222056458781270149587767914316773543725385844594871559412151974163986661258969837372587167573949494355201709502618658016651990307184144322311696783769 6
```

1234/56789 with 1500 digits after the decimal point:

```
\xintTrunc{1500}{1234/56789}\dots: 0.021729560302171195125816619415731919914067865255595273732589057740055292398175703041081899663667259504481501699272746482593460001056542640300058109845216503196041486907675782281779922168025497895719241402384264558277131134550705242212400288788321682015883357692510873584673088098047157019845392593636091496592649985032312595749176777192766204722745602141259751008117769286305446477310746799556252091073975593865009068657662575498776171441652432689429290883797918610998608885523604923488703798270791878708904893553328989769145433094437302998820194051664935110672841571431087006 2
```

version of addition which is twice faster on inputs with 500 digits or more, but it is slightly less efficient for 50 digits or less. This 'wall' dissuaded me to look into implementing 'intelligent' multiplication which would be sub-quadratic in a model where storing and retrieving from memory do not cost much.

[5] I could, naturally, be proven wrong!

[6] The LuaTEX project possibly makes endeavours such as **xint** appear even more insane that they are, in truth.

86428709785345753579038194016446847100670904576590536899751712479529
48634418637412174893025057669619116378171829051400799450597827043969
78288048741833805842680800859321347444047262674109422599447076018242
96958918100336332740495518498300727253517406539998943457359699941890
15478349680395851309232421771822007783197450210428075859761573544172
28688654492947577875997112116783179841166423074891264153269119019528
42980154607406363908503407350014967687404250823222807233795277254397
85874024899188223071369455352268925320044374790892602440613499093134
23374245012238285583475673105707091162020813890013911144763950765112
96201729208121291095106446671010230854566905562697001179805948335064
88932715842856891299371357129021465424642096180598355315289932909542
34094631002482875204705136558136258782510697494233038088362182817094
85992005494021729560302171195125816619415731919914067865255595273732
58905774005529239817570304108189966366 7...

0.99^{-100} with 200 digits after the decimal point:
\xintTrunc{200}{\xinttheexpr .99^-100\relax}\dots: 2.731999026429026003
84667172125783743550535164293857207083343057250824645551870534304481
43013784806140368055624765019253070342696854891531946166122710159206
71913840348851485747943086470963920731779793 03...

Computation of a Bezout identity with 7^200-3^200 and 2^200-1:
\xintAssign\xintBezout
{\xintNum{\xinttheexpr 7^200-3^200\relax}}
{\xintNum{\xinttheexpr 2^200-1\relax}}\to\A\B\U\V\D
\U$\times$(7^200-3^200)+\xintiOpp\V$\times$(2^200-1)=\D
-220045702773594816771390169652074193009609478853×(7^200-3^200)+1432
58949362763693185913068326832046547441686338771408915838167247899192
11328201191274624371580391777549768571912876931442406050669914563361
43205677696774891×(2^200-1)=1803403947125

The Euclide algorithm applied to 179,876,541,573 and 66,172,838,904:[7]
\xintTypesetEuclideAlgorithm {179876541573}{66172838904}

$$\begin{aligned}
179876541573 &= 2\times 66172838904 + 47530863765\\
66172838904 &= 1\times 47530863765 + 18641975139\\
47530863765 &= 2\times 18641975139 + 10246913487\\
18641975139 &= 1\times 10246913487 + 8395061652\\
10246913487 &= 1\times 8395061652 + 1851851835\\
8395061652 &= 4\times 1851851835 + 987654312\\
1851851835 &= 1\times 987654312 + 864197523\\
987654312 &= 1\times 864197523 + 123456789\\
864197523 &= 7\times 123456789 + 0
\end{aligned}$$

$\sum_{n=1}^{500}(4n^2-9)^{-2}$ with each term rounded to twelve digits, and the sum to nine digits:
\def\coeff #1%
{\xintiRound {12}{1/\xintiSqr{\the\numexpr 4*#1*#1-9\relax }[0]}}
\xintRound {9}{\xintiSeries {1}{500}{\coeff}[-12]}: 0.062366080

The complete series, extended to infinity, has value $\frac{\pi^2}{144}-\frac{1}{162}$ = 0.062,366,079,

[7] this example is computed tremendously faster than the other ones, but we had to limit the space taken by the output.

945,836,595,346,844,45... [8] I also used (this is a lengthier computation than the one above) **xintseries** to evaluate the sum with 100,000 terms, obtaining 16 correct decimal digits for the complete sum. The coefficient macro must be redefined to avoid a \numexpr overflow, as \numexpr inputs must not exceed 2^31-1; my choice was:

```
\def\coeff #1%
{\xintiRound {22}{1/\xintiSqr{\xintiMul{\the\numexpr 2*#1-3\relax}
                                      {\the\numexpr 2*#1+3\relax}}[0]}}
```

Computation of $2^{999,999,999}$ with 24 significant figures:
\xintFloatPow[24] {2}{999999999}: 2.30648800058453469655806e301029995

To see more of **xint** in action, jump to the section 19 describing the commands of the **xintseries** package, especially as illustrated with the traditional computations of π and $\log 2$, or also see the computation of the convergents of e made with the **xintcfrac** package.

Note that almost all of the computational results interspersed through the documentation are not hard-coded in the source of the document but just written there using the package macros, and were selected to not impact too much the compilation time.

1.5 Origins of the package

Package bigintcalc by Heiko Oberdiek already provides expandable arithmetic operations on "big integers", exceeding the TEX limits (of 2^{31}-1), so why another[9] one?

I got started on this in early March 2013, via a thread on the c.t.tex usenet group, where Ulrich Diez used the previously cited package together with a macro (\ReverseOrder) which I had contributed to another thread.[10] What I had learned in this other thread thanks to interaction with Ulrich Diez and GL on expandable manipulations of tokens motivated me to try my hands at addition and multiplication.

I wrote macros \bigMul and \bigAdd which I posted to the newsgroup; they appeared to work comparatively fast. These first versions did not use the ε-TEX \numexpr primitive, they worked one digit at a time, having previously stored carry-arithmetic in 1200 macros.

I noticed that the bigintcalc package used\numexpr if available, but (as far as I could tell) not to do computations many digits at a time. Using \numexpr for one digit at a time for \bigAdd and \bigMul slowed them a tiny bit but avoided cluttering TEX memory with the 1200 macros storing pre-computed digit arithmetic. I wondered if some speed could be gained by using \numexpr to do four digits at a time for elementary multiplications (as the maximal admissible number for \numexpr has ten digits).

The present package is the result of this initial questioning.

xint requires the ε-TEX extensions.

[8] This number is typeset using the numprint package, with \npthousandsep {,\hskip .05em plus .01em minus .01em}. But the breaking accross lines works only in text mode. The number itself was (of course...) computed initially with **xint**, with 30 digits of π as input. See how **xint** may compute π from scratch.

[9] this section was written before the **xintfrac** package; the author is not aware of another package allowing expandable computations with arbitrarily big fractions.

[10] the \ReverseOrder could be avoided in that circumstance, but it does play a crucial rôle here.

2 Expansions

Except for some specific macros dealing with assignments or typesetting, the bundle macros all work in expansion-only context. For example, with the following code snippet within `myfile.tex`:

```
\newwrite\outfile
\immediate\openout\outfile \jobname-out\relax
\immediate\write\outfile {\xintQuo{\xintPow{2}{1000}}{\xintFac{100}}}
% \immediate\closeout\outfile
```

the tex run creates a file `myfile-out.tex` containing the decimal representation of the integer quotient `2^{1000}/100!`. Such macros can also be used inside a `\csname...\endcsname`, and of course in an `\edef`.

Furthermore the package macros give their final results in two expansion steps. They expand 'fully' (the first token of) their arguments so that they can be arbitrarily chained. Hence

```
\xintLen{\xintQuo{\xintPow{2}{1000}}{\xintFac{100}}}
```

expands in two steps and tells us that `[2^{1000}/100!]` has 144 digits. This is not so many, let us print them here: `114813249641507505482278393872551066259805517784186172883663478065826541894704737970419535798876630484358265060061503749531707793118627774829601`.

For the sake of typesetting this documentation and not have big numbers extend into the margin and go beyond the page physical limits, I use these commands (not provided by the package):

```
\def\allowsplits #1{\ifx #1\relax \else #1\hskip 0pt plus 1pt \relax
                     \expandafter\allowsplits\fi}%
\def\printnumber #1{\expandafter\expandafter\expandafter
                    \allowsplits #1\relax }%
% Expands twice before printing.
```

The `\printnumber` macro is not part of the package and would need additional thinking for more general use.[11] It may be used as `\printnumber {\xintQuo{\xintPow {2}{1000}}{\xintFac{100}}}`, or as `\printnumber\mynumber` if the macro `\mynumber` was previously defined via an `\edef`, as for example:

```
\edef\mynumber {\xintQuo {\xintPow {2}{1000}}{\xintFac{100}}}
```

or as `\expandafter\printnumber\expandafter{\mynumber}`, if the macro `\mynumber` is defined by a `\newcommand` or a `\def` (see below item 3 for the underlying expansion issue; adding four `\expandafter`'s to `\printnumber` would allow to use it directly as `\printnumber\mynumber` with a `\mynumber` itself defined via a `\def` or `\newcommand`).

Just to show off, let's print 300 digits (after the decimal point) of the decimal expansion of `0.7^{-25}`:[12]

```
\np {\xintTrunc {300}{\xinttheexpr .7^-25\relax}}\dots
```

7,456.739,985,837,358,837,609,119,727,341,853,488,853,339,101,579,533,584,812,792,108,394,305,337,246,328,231,852,818,407,506,767,353,741,490,769,900,570,763,145,015,081,436,139,227,188,742,972,826,645,967,904,896,381,378,616,815,228,254,509,149,848,168,782,309,405,985,245,

[11] as explained in a previous footnote, the `numprint` package may also be used, in text mode only (as the thousand separator seemingly ends up typeset in a `\hbox` when in math mode).

[12] the `\np` typesetting macro is from the `numprint` package.

368,923,678,816,256,779,083,136,938,645,362,240,130,036,489,416,562,
067,450,212,897,407,646,036,464,074,648,484,309,937,461,948,589...

This computation uses the macro \xintTrunc from package **xintfrac** wich extends to fractions the basic arithmetic operations defined for integers by **xint**. It also uses \xinttheexpr from package **xintexpr**, which allows to use standard notations. Note that the fraction .7^-25 is first evaluated exactly; for some more complex inputs, such as .7123045678952^-243, the exact evaluation before truncation would be expensive, and (assuming one needs twenty digits) one would rather use floating mode:

```
\xintDigits:=20; \np{\xintthefloatexpr .7123045678952^-243\relax}
```

$$\texttt{.7123045678952\^{}-243} \approx 6.342,022,117,488,416,127,3 \times 10^{35}$$

Important points, to be noted, related to the expansion of arguments:

1. the macros expand 'fully' their arguments, this means that they expand the first token seen (for each argument), then expand , etc..., until something un-expandable such as a digit or a brace is hit against.[13] This example

   Changed → in 1.06

   ```
   \def\x{98765}\def\y{43210}\xintAdd {\x}{\x\y}
   ```

   is *not* a legal construct, as the \y will remain untouched by expansion and not get converted into the digits which are expected by the sub-routines of \xintAdd. It is a \numexpr which will expand it and an arithmetic overflow will arise as 9876543210 exceeds the TEX bounds.

   New with → 1.07

   The 1.07 novelty \xinttheexpr has brought a solution: here one would write \xinttheexpr \x+\x\y\relax, or \xintAdd\x{\xinttheexpr\x\y\relax}.

2. Unfortunately, after \def\x {12}, one can not use just -\x as input to one of the package macros: the rules above explain that the expansion will act only on the minus sign, hence do nothing. The only way is to use the \xintOpp macro, which replaces a number with its opposite.

   New with → 1.07

   Again, this is otherwise inside an \xinttheexpr-ession or \xintthefloatexpr-ession. There, the minus sign may prefix macros which will expand to numbers (or parentheses etc...)

3. With the definition

   ```
   \def\AplusBC #1#2#3{\xintAdd {#1}{\xintMul {#2}{#3}}}
   ```

   one obtains an expandable macro producing the expected result, not in two, but rather in three steps: a first expansion is consumed by the macro expanding to its definition. The new expansion policy starting with the package release 1.06 allows to use this inside other package 'primitives' or also similar macros: \xintAdd {\AplusBC {1}{2}{3}}{4} does work and returns 11/1[0].[14]

   If, for some reason, it is important to create a macro expanding in two steps to its final value, the solution is to use the *lowercase* form of \xintAdd:

   ```
   \def\AplusBC #1#2#3{\romannumeral0\xintadd {#1}{\xintMul {#2}{#3}}}
   ```

   and then \AplusBC will share the same properties as do the other **xint** 'primitive' macros.

[13] the knowledgeable people will have recognized \romannumeral-`0

[14] this strange thing is because this document uses **xintfrac**, and we have printed the raw output of addition which is automatically a fraction.

The lowercase form is *only* for the external highest level of chained commands. All **xint** provided public macros have such a lowercase form. To more fully imitate the **xint** standard habits, the example above should thus be treated via the creation of two macros:

```
\def\aplusbc #1#2#3{\xintadd {#1}{\xintMul {#2}{#3}}}
\def\AplusBC {\romannumeral0\aplusbc}
```

Or, for people using the LaTeX vocabulary:

```
\newcommand*{\aplusbc}[3]{\xintadd {#1}{\xintMul {#2}{#3}}}
\newcommand*{\AplusBC}{\romannumeral0\aplusbc}
```

This then allows further definitions of macros expanding in two steps only, such as:

```
\def\aplusbcsquared #1#2#3{\aplusbc {#1}{#2}{\xintSqr{#3}}}
\def\AplusBCSquared {\romannumeral0\aplusbcsquared}
\newcommand*\myalgebra [6]{\xintmul {\AplusBC {#1}{#2}{#3}}{\AplusBC
{#4}{#5}{#6}}}
\newcommand*\MyAlgebra {\romannumeral0\myalgebra}
```

The `\romannumeral0` things above look like an invitation to hacker's territory; if it is not important that the macro expands in two steps only, there is no reason to follow these guidelines. Just chain arbitrarily the package macros, and the new ones will be completely expandable and usable one within the other.

New with 1.07 → Release `1.07` has the `\xintNewExpr` command which automatizes the creation of such expandable macros:

```
\xintNewExpr\AplusBC[3]{_1+_2*_3}
```

creates the `\AplusBC` macro doing the above and expanding in two expansion steps.

3 Inputs and outputs

The core bundle constituents are **xint**, **xintfrac**, **xintexpr**, each one loading its predecessor. The base constituent **xint** only deals with integers, of arbitrary sizes, and apart from its macro `\xintNum`, the input format is rather strict. Then **xintfrac** extends the scope to fractions: numerators and denominators are separated by a forward slash and may contain each an optional fractional part after the decimal mark (which has to be a dot) and

New with 1.07 → a scientific part (with a lower case `e`).

The numeric arguments to the bundle macros may be of various types, extending in generality:

1. 'short' integers, *i.e.* less than (or equal to) in absolute value 2,147,483,647. I will refer to this as the 'TeX' or '`\numexpr`' limit. This is the case for arguments which serve to count or index something. It is also the case for the exponent in the power function and for the argument to the factorial function. The bounds have been (arbitrarily) lowered to 999,999,999 and 999,999 respectively for the latter cases.[15] When the argument exceeds the TeX bound (either positively or negatively), an error will originate from a `\numexpr` expression and it may sometimes be followed by a more specific error 'message' from a package macro.

[15] the float power function limits the exponent to the TeX bound, not 999999999, and it has a variant with no imposed limit on the exponent; but the result of the computation must in all cases be representable with a power of ten exponent obeying the TeX bound.

2. 'long' integers, which are the bread and butter of the package commands. They are signed integers with an illimited number of digits. Theoretically though, most of the macros require that the number of digits itself be less than the TEX-`\numexpr` bound.[16] Some macros, such as addition when **xintfrac** has not been loaded, do not measure first the length of their arguments and could theoretically be used with 'gigantic' integers with a larger number of digits. However memory constraints from the TEX implementation probably exclude such inputs. Concretely though, multiplying out two 1000 digits numbers is already a longish operation.

3. 'fractions': they become available after having loaded the **xintfrac** package. Their format on input will be described next, a fraction has a numerator, a forward slash and then a denominator. It is now possible to use scientific notation, with a lowercase `e` on input (an uppercase `E` is accepted inside the `\xintexpr`-essions). The decimal mark must be a dot and not a comma. No separator for thousands should be used on inputs, and except within `\xintexpr`-essions, spaces should be avoided.

New with 1.07 →

> With only package **xint** loaded TEX's count registers must be prefixed by `\the` or `\number` inside the arguments to the package macros, except in places (argument of the factorial, exponent of the power function, ...) where the documentation of the macro says otherwise.
>
> Not previously documented → With the macros of **xintfrac** (including those of **xint** extended to fractions) a count register is *accepted* on input, with no need to be prefixed by `\the` or `\number`.
>
> Inside `\xinttheexpr...\relax`, count registers must again be prefixed by `\the` or `\number` (if they are not arguments to macros of **xintfrac**).

New with 1.06 → The package macros first operate a 'full' expansion of their arguments, as explained above: only the first token is repeatedly expanded until no more is possible.

New with 1.06 → On the other hand, this expansion is a complete one for those arguments which are constrained to obey the TEX bounds on numbers, as they are systematically inserted inside a `\numexpr...\relax` expression.

The allowed input formats for 'long numbers' and 'fractions' are:

1. the strict format is when **xintfrac** is not loaded. The number should be a string of digits, optionally preceded by a unique minus sign. The first digit can be zero only if the number is zero. A plus sign is not accepted. There is a macro `\xintNum` which normalizes to this form an input having arbitrarily many minus and plus signs, followed by a string of zeros, then digits:
   ```
   \xintNum {+-+-+----++-++----00000000009876543210}=-9876543210
   ```
   Note that `-0` is not legal input and will confuse **xint** (but not `\xintNum` which even accepts an empty input).

2. the extended format is with **xintfrac** is loaded: the macros are extended from operating on integers to operating on fractions, which are input as (or expand to) `A/B` (or just an integer `A`), where `A` and `B` will be automatically given to the sign and zeros normalizing macro `\xintNum`. Each of `A` and `B` may be decimal numbers: with a

[16] and to be very precise, less than the TEX bound minus eight, due to the way the length is evaluated.

decimal point and digits following it. Here is an example:

```
\xintAdd {+--0367.8920280/-++278.289287}{-109.2882/+270.12898}
```

Incidentally this evaluates to

```
=-129792033529284840/7517400124223726[-1]
=-6489601676464242/3758700062111863 (irreducible)
=-1.72655481129771093694248704898677881556360055242806...
```

where the second line was produced with `\xintIrr` and the next with `\xintTrunc {50}` to get fifty digits of the decimal expansion following the decimal mark. Scientific notation is accepted on input both for the numerators and denominators of fractions, and is produced on output by `\xintFloat`:

New with 1.07 →

```
\xintAdd{10.1e1}{101.010e3}=101111/1[0]
\xintRaw{1.234e5/6.789e3}=1234/6789[2]
\xintFloat[24]{1/66049}=1.514027464458205271843 63e-5
```

Of course, even when **xintfrac** is loaded, some macros can not treat fractions on input. Starting with release 1.05 most of them have also been extended to accept the relaxed format on input as long as the fraction actually represents an integer. For example it used to be the case with the earlier releases that `\xintQuo {100/2}{12/3}` would not work (the macro `\xintQuo` computes a euclidean quotient). It now does, because its arguments are in truth integers.

A number can start directly with a decimal point:

```
\xintPow{-.3/.7}{11}=-177147/1977326743[0]
\xinttheexpr (-.3/.7)^11\relax=-177147/1977326743[0]
```

It is also licit to use `\A/\B` as input if each of `\A` and `\B` expands (in the sense previously described) to a "decimal number" as examplified above by the numerators and denominators (thus, possibly with a 'scientific' exponent part, with a lowercase 'e'). Or one may have just one macro `\C` which expands to such a "fraction with optional decimal points", or mixed things such as `\A 245/7.77`, where the numerator will be the concatenation of the expansion of `\A` and `245`. But, as explained already `123\A` is a no-go, *except inside an* `\xintexpr`*-ession*!

Finally, after the decimal point there may be `eN` where `N` is a positive or negative number (obeying the TEX bounds on integers). This 'e' part (which must be in lowercase, except inside `\xintexpr`-essions) may appear both at the numerator and at the denominator.

New with 1.07 →

```
\xintRaw {+--+1253.2782e++--3/---0087.123e---5}=-12532782/87123[7]
```

New documentation section (1.08b) →

Use of count registers: when an argument to a macro is said in the documentation to have to obey the TEX bound, this means that it is fed to a `\numexpr...\relax`, hence it is subjected to a complete expansion which must delivers an integer, and count registers and even algebraic expressions with them like `\mycountA+\mycountB*17-\mycountC/12+\mycountD` are admissible arguments (the slash stands here for the integer (rounded) division done by `\numexpr`). This applies in particular to the number of digits to truncate or round with, to the indices of a series partial sum, ...

Not previously documented →

With **xintfrac**.sty loaded and for arguments of macros accepting fractions on inputs, use of count registers and even direct algebra with them is possible: a count register `\mycountA` or `\count 255` is admissible as numerator or also as denominator, with no need to be prefixed by `\the` or `\number`. It is even possible to have algebraic expressions, with the limitation (how to overcome it in complete generality will be explained later) that

each of the numerator and denominator should be expressed with at most *eight* tokens, and the forward slash symbol must be protected by braces to be used inside the `\numexpr` and not be interpreted as the fraction slash. Note that `\mycountA` is one token but `\count 255` is four tokens. Example: `\mycountA+\mycountB{/}17/1+\mycountA*\mycountB`, or `\count 0+\count 2{/}17/1+\count 0*\count 2`, but in the latter case the numerator has the maximal allowed number of tokens (the braced slash counts for only one).

```
\cnta 10 \cntb 35 \xintRaw {\cnta+\cntb{/}17/1+\cnta*\cntb}->12/351[0]
```

This possibility of using directly count registers and even algebraic expression is only for arguments to macros of **xintfrac**: inside `\xintexpr...\relax` one can not use directly a count register, it must be prefixed by `\the` or `\number`. And with only **xint**.sty is loaded, the *only* macro allowing the above is `\xintNum`:

```
\cnta 10 \cntb 100 \xintNum {\cnta+\cntb+\cnta*\cntb}->1110
```

Note that `\cnta+\cntb+2*\cnta*\cntb` would be too long (it has nine tokens). Using braces works:

```
\cnta 10 \cntb 100 \xintNum {\cnta+\cntb+{2*\cnta*\cntb}}->2110
```

The braces should be used for some sub-part of the expression, not for the entire thing; alternatively, one can always use `\numexpr {arbitrarily long expression}\relax` as input:

```
\cnta 100 \cntb 10 \cntc 1
\xintRaw {\numexpr {\cnta*\cnta+\cntb*\cntb+\cntc*\cntc+
                    2*\cnta*\cntb+2*\cnta*\cntc+2*\cntb*\cntc}\relax/%
          \numexpr {\cnta*\cnta+\cntb*\cntb+\cntc*\cntc}\relax }
                              12321/10101[0]
```

> Macros expecting fractions may be fed with arbitrarily long `\numexpr`-expressions by the trick of using `\numexpr {long_expression}\relax` as numerator and/or denominator of the argument to the macro.
>
> Macros expecting an integer obeying the TEX bound must to the contrary receive directly `long_expression` as argument (or `\numexpr long_expression\relax`, but this is redundant as it will be done by the macro itself.)

This is a trick as the braces would not be accepted as regular `\numexpr`-syntax: and indeed, they are removed at some point in the processing.

Outputs: loading **xintfrac** not only relaxes the format of the inputs; it also modifies the format of the outputs: except when a fraction is filtered on output by `\xintIrr` (and `\xintJrr`) or `\xintRawWithZeros`, or by the truncation or rounding macros, it will always be in the `A/B[n]` form (which stands for `(A/B)×10^n`). The `A` and `B` may end in zeros (*i.e*, `n` does not represent all powers of ten), and will generally have a common factor. The denominator `B` is always strictly positive.

A macro `\xintFrac` is provided for the typesetting (math-mode only) of such a 'raw' output. Of course, the `\xintFrac` itself is not accepted as input to the package macros.

Direct user input of things such as `16000/289072[17]` or `3[-4]` is authorized. It is even possible to use `\A/\B[17]` if `\A` expands to `16000` and `\B` to `289072`, or `\A` if `\A` expands to `3[-4]`. However, NEITHER the numerator NOR the denominator may then have a decimal

Important! →

point. And, for this format, ONLY the numerator may carry a UNIQUE minus sign (and no superfluous leading zeros; and NO plus sign). This format with a power of ten represented by a number within square brackets is the output format used by (almost all) **xintfrac** macros dealing with fractions. It is allowed for user input but the parsing is minimal and it is very important to follow the above rules. This reduced flexibility, compared to the format without the square brackets, allows chaining package macros without too much speed impact, as they always output computation results in the `A/B[n]` form.

> All computations done by **xintfrac** on fractions are exact. Inputs containing decimal points or scientific parts do not make the package switch to a 'floating-point' mode. The inputs, however long, are always converted into exact internal representations.
>
> Floating point evaluations are done with special macros containing 'Float' in their names, or inside `\xintthefloatexpr`-essions.

Generally speaking, there should be no spaces among the digits in the inputs (in arguments to the package macros). Although most would be harmless in most macros, there are some cases where spaces could break havoc. So the best is to avoid them entirely.

This is entirely otherwise inside an `\xintexpr`-ession, where spaces are expected to, as a general rule (with possible exceptions related to the allowed use of braces, see the documentation) be completely harmless, and even recommended for making the source more legible.

Syntax such as `\xintMul\A\B` is accepted and equivalent[17] to `\xintMul {\A}{\B}`. Or course `\xintAdd\xintMul\A\B\C` does not work, the product operation must be put within braces: `\xintAdd{\xintMul\A\B}\C`. It would be nice to have a functional form `\add(x,\mul(y,z))` but this is not provided by the package. Arguments must be either within braces or a single control sequence.

Note that - and + may serve only as unary operators, on *explicit* numbers. They can not serve to prefix macros evaluating to such numbers, *except inside an* `\xintexpr`*-ession.*

4 More on fractions

With package **xintfrac** loaded, the routines `\xintAdd`, `\xintSub`, `\xintMul`, `\xintPow`, `\xintSum`, `\xintPrd` are modified to allow fractions on input,[18] [19] [20] [21] and produce on output a fractional number `f=A/B[n]` where `A` and `B` are integers, with `B` positive, and `n` is a signed "small" integer (*i.e* less in absolute value than `2^{31}-9`). This represents `(A/B)`

[17] see however near the end of this later section for the important difference when used in contexts where TEX expects a number, such as following an `\ifcase` or an `\ifnum`.

[18] of course, the power function does not accept a fractional exponent. Or rather, does not expect, and errors will result if one is provided.

[19] macros `\xintiAdd`, `\xintiSub`, `\xintiMul`, `\xintiPow`, `\xintiSum`, `\xintiPrd` are the original ones dealing only with integers. They are available as synonyms, also when **xintfrac** is not loaded.

[20] also `\xintCmp`, `\xintSgn`, `\xintOpp`, `\xintAbs`, `\xintMax`, `\xintMin` are extended to fractions and have their integer-only initial synonyms.

[21] and `\xintQuo`, `\xintRem`, `\xintDivision`, `\xintGeq`, `\xintFDg`, `\xintLDg`, `\xintOdd`, `\xintMON`, `\xintMMON` all accept a fractional input as long as it reduces to an integer.

times 10^n. The fraction f may be, and generally is, reducible, and A and B may well end up with zeros (*i.e.* n does not contain all powers of 10). Conversely, this format is accepted on input (and is parsed more quickly than fractions containing decimal points; the input may be a number without denominator).[22]

The \xintiAdd, \xintiSub, \xintiMul, \xintiPow, \xintiSum, \xintiPrd, etc... are the original un-modified integer-only versions. They have less parsing overhead.

Changed in 1.07 → The macro \xintRaw prints the fraction directly from its internal representation in A/B[n] form. To convert the trailing [n] into explicit zeros either at the numerator or the denominator, use \xintRawWithZeros. In both cases the B is printed even if it has value 1.

Conversely (sort of), the macro \xintREZ puts all powers of ten into the [n] (REZ stands for remove zeros). Here also, the B is printed even if it has value 1.

The macro \xintIrr reduces the fraction to its irreducible form C/D (without a trailing

Changed in 1.08 → [0]), and it prints the D even if D=1.

The macro \xintNum from package **xint** is extended: it now does like \xintIrr, raises an error if the fraction did not reduce to an integer, and outputs the numerator. This macro should be used when one knows that necessarily the result of a computation is an integer, and one wants to get rid of its denominator /1 which would be left by \xintIrr.

The macro \xintTrunc{N}{f} prints[23] the decimal expansion of f with N digits after the decimal point.[24] Currently, it does not verify that N is non-negative and strange things could happen with a negative N. Of course a negative f is no problem, needless to say. When the original fraction is negative and its truncation has only zeros, it is printed as -0.0...0, with N zeros following the decimal point:

```
\xintTrunc {5}{\xintPow {-13}{-9}}=-0.00000
\xintTrunc {20}{\xintPow {-13}{-9}}=-0.00000000009429959537
```

The output always contains a decimal point (even for N=0) followed by N digits, except when the original fraction was zero. In that case the output is 0, with no decimal point.

```
\xintTrunc {10}{\xintSum {{1/2}{1/3}{1/5}{-31/30}}}=0
```

The macro \xintiTrunc{N}{f} is like \xintTrunc{N}{f} followed by multiplication by 10^N. Thus, it outputs an integer in a format acceptable by the integer-only macros. To get the integer part of the decimal expansion of f, use \xintiTrunc{0}{f}:

```
\xintiTrunc {0}{\xintPow {1.01}{100}}=2
\xintiTrunc {0}{\xintPow{0.123}{-10}}=1261679032
```

See also the documentations of \xintRound, \xintiRound and \xintFloat.

[22] at each stage of the computations, the sum of n and the length of A, or of the absolute value of n and the length of B, must be kept less than 2^{31}-9.

[23] 'prints' does not at all mean that this macro is designed for typesetting; I am just using the verb here in analogy to the effect of the functioning of a computing software in console mode. The package does not provide any 'printing' facility, besides its rudimentary \xintFrac and \xintFwOver math-mode only macros. To deal with really long numbers, some macros are necessary as TEX by default will print a long number on a single line extending beyond the page limits. The \printnumber command used in this documentation is just one way to address this problem, some other method should be used if it is important that digits occupy the same width always.

[24] the current release does not provide a macro to get the period of the decimal expansion.

5 \ifcase, \ifnum, ... constructs

When using things such as \ifcase \xintSgn{\A} one has to leave a space after the closing brace for TEX to stop its scanning for a number: once TEX has finished expanding \xintSgn{\A} and has so far obtained either 1, 0, or -1, a space (or something 'unexpandable') must stop it looking for more digits. Using \ifcase\xintSgn\A without the braces is very dangerous, because the blanks (including the end of line) following \A will be skipped and not serve to stop the number which \ifcase is looking for. With \def\A{1}:

```
\ifcase \xintSgn\A   0\or OK\else ERROR\fi   ---> gives ERROR
\ifcase \xintSgn{\A} 0\or OK\else ERROR\fi   ---> gives OK
```

New with 1.07 →

Release 1.07 provides the expandable \xintSgnFork which chooses one of three branches according to whether its argument expand to -1, 0 or 1. This, rather than the corresponding \ifcase, should be used when such a fork is needed as argument to one of the package macros.

6 Multiple outputs

Some macros have an output consisting of more than one number, each one is then within braces. Examples of multiple-output macros are \xintDivision which gives first the quotient and then the remainder of euclidean division, \xintBezout from the **xintgcd** package which outputs five numbers, \xintFtoCv from the **xintcfrac** package which returns the list of the convergents of a fraction, ... the next two sections explain ways to deal, expandably or not, with such outputs.

See the subsection 14.48 for a rare example of a bundle macro which may return an empty string, or a number prefixed by a chain of zeros. This is the only situation where a macro from the package **xint** may output something which could require parsing through \xintNum before further processing by the other (integer-only) package macros from **xint**.

7 Assignments

It might not be necessary to maintain at all times complete expandability. For example why not allow oneself the two definitions \edef\A {\xintQuo{100}{3}} and \edef\B {\xintRem {100}{3}}. A special syntax is provided to make these things more efficient, as the package provides \xintDivision which computes both quotient and remainder at the same time:

```
\xintAssign\xintDivision{100}{3}\to\A\B
  \xintAssign\xintDivision{\xintiPow {2}{1000}}{\xintFac{100}}\to\A\B
gives \meaning\A: macro:->1148132496415075054822783938725510662598055177841861728836634780658265418947047379704195357988766304843582650600615037495317077931186277748296 01 and \meaning\B: macro:->5493629452133983225138128786223912807341050049847605059532189961231327664902288388132878702444582075129603152041054804964625083138567652624386837205668069376.
```

Another example (which uses a macro from the **xintgcd** package):

```
\xintAssign\xintBezout{357}{323}\to\A\B\U\V\D
```

is equivalent to setting \A to 357, \B to 323, \U to -9, \V to -10, and \D to 17. And indeed (-9)×357-(-10)×323=17 is a Bezout Identity.

```
\xintAssign\xintBezout{3570902836026}{200467139463}\to\A\B\U\V\D
```

gives then \U: macro:->5812117166, \V: macro:->103530711951 and \D=3.

When one does not know in advance the number of tokens, one can use \xintAssignArray or its synonym \xintDigitsOf:

```
\xintDigitsOf\xintiPow{2}{100}\to\Out
```

This defines \Out to be macro with one parameter, \Out{0} gives the size N of the array and \Out{n}, for n from 1 to N then gives the nth element of the array, here the nth digit of 2^{100}, from the most significant to the least significant. As usual, the generated macro \Out is completely expandable (in two steps). As it wouldn't make much sense to allow indices exceeding the TEX bounds, the macros created by \xintAssignArray put their argument inside a \numexpr, so it is completely expanded and may be a count register, not necessarily prefixed by \the or \number. Consider the following code snippet:

Changed in 1.06

```
\newcount\cnta
\newcount\cntb
\begingroup
\xintDigitsOf\xintiPow{2}{100}\to\Out
\cnta = 1
\cntb = 0
\loop
\advance \cntb \xintiSqr{\Out{\cnta}}
\ifnum \cnta < \Out{0}
\advance\cnta 1
\repeat

|2^{100}| (=\xintiPow {2}{100}) has \Out{0} digits and the sum of
their squares is \the\cntb. These digits are, from the least to
the most significant: \cnta = \Out{0}
\loop \Out{\cnta}\ifnum \cnta > 1 \advance\cnta -1 , \repeat.
\endgroup
```

2^{100} (=1267650600228229401496703205376) has 31 digits and the sum of their squares is 679. These digits are, from the least to the most significant: 6, 7, 3, 5, 0, 2, 3, 0, 7, 6, 9, 4, 1, 0, 4, 9, 2, 2, 8, 2, 2, 0, 0, 6, 0, 5, 6, 7, 6, 2, 1.

We used a group in order to release the memory taken by the \Out array: indeed internally, besides \Out itself, additional macros are defined which are \Out0, \Out00, \Out1, \Out2, ..., \OutN, where N is the size of the array (which is the value returned by \Out{0}; the digits are parts of the names not arguments).

The command \xintRelaxArray\Out sets all these macros to \relax, but it was simpler to put everything withing a group.

Needless to say \xintAssign, \xintAssignArray and \xintDigitsOf do not do any check on whether the macros they define are already defined.

In the example above, we deliberately broke all rules of complete expandability, but had we wanted to compute the sum of the digits, not the sum of the squares, we could just have written:

```
\xintiSum{\xintiPow{2}{100}}=115
```

Indeed, \xintiSum is usually used as in

```
\xintiSum{{123}{-345}{\xintFac{7}}{\xintiOpp{\xintRem{3347}{591}}}}=4426
```

but in the example above each digit of `2^{100}` is treated as would have been a summand enclosed within braces, due to the rules of TEX for parsing macro arguments.

Note that `{-\xintRem{3347}{591}}` is not a valid input, because the expansion will apply only to the minus sign and leave unaffected the `\xintRem`. So we used `\xintiOpp` which replaces a number with its opposite.

As a last example with `\xintAssignArray` here is one line extracted from the source code of the **xintgcd** macro `\xintTypesetEuclideAlgorithm`:

```
\xintAssignArray\xintEuclideAlgorithm {#1}{#2}\to\U
```

This is done inside a group. After this command `\U{1}` contains the number `N` of steps of the algorithm (not to be confused with `\U{0}=2N+4` which is the number of elements in the `\U` array), and the GCD is to be found in `\U{3}`, a convenient location between `\U{2}` and `\U{4}` which are (absolute values of the expansion of) the initial inputs. Then follow `N` quotients and remainders from the first to the last step of the algorithm. The `\xintTypesetEuclideAlgorithm` macro organizes this data for typesetting: this is just an example of one way to do it.

8 Utilities for expandable manipulations

Extended in 1.06 → The package now has more utilities to deal expandably with 'lists of things', which were treated un-expandably in the previous section with `\xintAssign` and `\xintAssignArray`: `\xintRev`, `\xintReverseOrder`, `\xintLen` and `\xintLength` since the first release, `\xintApply` and `\xintListWithSep` since `1.04`, `\xintRevWithBraces`, `\xintCSVtoList`, `\xintNthElt` with `1.06`, and `\xintApplyUnbraced`, new with `1.06b`.

As an example the following code uses only expandable operations:

```
|2^{100}| (=\xintiPow {2}{100}) has \xintLen{\xintiPow {2}{100}}} digits
and the sum of their squares is
\xintiSum{\xintApply {\xintiSqr}{\xintiPow {2}{100}}}.
These digits are, from the least to the most significant:
\xintListWithSep {, }{\xintRev{\xintiPow {2}{100}}}. The thirteenth most
significant digit is \xintNthElt{13}{\xintiPow {2}{100}}. The seventh
least significant one is \xintNthElt{7}{\xintRev{\xintiPow {2}{100}}}.
```

`2^{100}` (=1267650600228229401496703205376) has 31 digits and the sum of their squares is 679. These digits are, from the least to the most significant: 6, 7, 3, 5, 0, 2, 3, 0, 7, 6, 9, 4, 1, 0, 4, 9, 2, 2, 8, 2, 2, 0, 0, 6, 0, 5, 6, 7, 6, 2, 1. The thirteenth most significant digit is 8. The seventh least significant one is 3.

Of course, it would be nicer to do `\edef\z{\xintiPow {2}{100}}`, and then use `\z` in place of `\xintiPow {2}{100}` everywhere as this would spare the CPU some repetitions.

9 Exceptions (error messages)

In situations such as division by zero, the package will insert in the TEX processing an undefined control sequence (we copy this method from the `bigintcalc` package). This will trigger the writing to the log of a message signaling an undefined control sequence. The name of the control sequence is the message. The error is raised *before* the end of the expansion so as to not disturb further processing of the token stream, after completion of

the operation. Generally the problematic operation will output a zero. Possible such error message control sequences:

```
\xintError:ArrayIndexIsNegative
\xintError:ArrayIndexBeyondLimit
\xintError:FactorialOfNegativeNumber
\xintError:FactorialOfTooBigNumber
\xintError:DivisionByZero
\xintError:NaN
\xintError:FractionRoundedToZero
\xintError:NotAnInteger
\xintError:ExponentTooBig
\xintError:TooBigDecimalShift
\xintError:TooBigDecimalSplit
\xintError:RootOfNegative
\xintError:NoBezoutForZeros
\xintError:ignored
\xintError:removed
\xintError:use_xintthe!
\xintError:inserted
```

10 Common input errors when using the package macros

Here is a list of common input errors. Some will cause compilation errors, others are more annoying as they may pass through unsignaled.

- using - to prefix some macro: `-\xintiSqr{35}/271`.[25]
- using one pair of braces too many `\xintIrr{{\xintiPow {3}{13}}/243}` (the computation goes through with no error signaled, but the result is completely wrong).
- using `[]` and decimal points at the same time `1.5/3.5[2]`, or with a sign in the denominator `3/-5[7]`. The scientific notation has no such restriction, the two inputs `1.5/-3.5e-2` and `-1.5e2/3.5` are equivalent: `\xintRaw{1.5/-3.5e-2}=-15/35[2]`, `\xintRaw{-1.5e2/3.5}=-15/35[2]`.
- specifying numerators and denominators with macros producing fractions when **xintfrac** is loaded: `\edef\x{\xintMul {3}{5}/\xintMul{7}{9}}`. This expands to `15/1[0]/63/1[0]` which is invalid on input. Using this `\x` in a fraction macro will most certainly cause a compilation error, with its usual arcane and undecipherable accompanying message. The fix here would be to use `\xintiMul`. The simpler alternative with package **xintexpr**: `\xinttheexpr 3*5/(7*9)\relax`.
- generally speaking, using in a context expecting an integer (possibly restricted to the TEX bound) a macro or expression which returns a fraction: `\xinttheexpr 4/2\relax` outputs `4/2[0]`, not 2. Use `\xintNum {\xinttheexpr 4/2\relax}`.

[25] to the contrary, this *is* allowed inside an `\xintexpr`-ession.

11 Package namespace

Inner macros of **xint**, **xintfrac**, **xintexpr**, **xintbinhex**, **xintgcd**, **xintseries**, and **xintcfrac** all begin either with `\XINT_` or with `\xint_`.[26] The package public commands all start with `\xint`. The major forms have their initials capitalized, and lowercase forms, prefixed with `\romannumeral0`, allow definitions of further macros expanding in only two steps to their final outputs. Some other control sequences are used only as delimiters, and left undefined, they may have been defined elsewhere, their meaning doesn't matter and is not touched.

12 Loading and usage

```
Usage with LaTeX: \usepackage{xint}
                  \usepackage{xintfrac}   % (loads xint)
                  \usepackage{xintexpr}   % (loads xintfrac)

                  \usepackage{xintbinhex} % (loads xint)
                  \usepackage{xintgcd}    % (loads xint)
                  \usepackage{xintseries} % (loads xintfrac)
                  \usepackage{xintcfrac}  % (loads xintfrac)

Usage with TeX:   \input xint.sty\relax
                  \input xintfrac.sty\relax   % (loads xint)
                  \input xintexpr.sty\relax   % (loads xintfrac)

                  \input xintbinhex.sty\relax % (loads xint)
                  \input xintgcd.sty\relax    % (loads xint)
                  \input xintseries.sty\relax % (loads xintfrac)
                  \input xintcfrac.sty\relax  % (loads xintfrac)
```

We have added, directly copied from packages by Heiko Oberdiek, a mecanism of reload and ε-TeX detection, especially for Plain TeX. As ε-TeX is required, the executable `tex` can not be used, `etex` or `pdftex` (version `1.40` or later) or ..., must be invoked.

Furthermore, **xintfrac**, **xintbinhex**, and **xintgcd** check for the previous loading of **xint**, and will try to load it if this was not already done. Similarly **xintseries**, **xintcfrac** and **xintexpr** do the necessary loading of **xintfrac**. Each package will refuse to be loaded twice.

Also inspired from the Heiko Oberdiek packages we have included a complete catcode protection mecanism. The packages may be loaded in any catcode configuration satisfying these requirements: the percent is of category code comment character, the backslash is of category code escape character, digits have category code other and letters have category code letter. Nothing else is assumed, and the previous configuration is restored after the loading of each one of the packages.

This is for the loading of the packages.

[26] starting with release `1.06b` the style files use for macro names a more modern underscore _ rather than the @ sign. Probability of a name clash with LaTeX2e packages is now even closer to nil, and with LaTeX3 packages it is also close to nil as our control sequences are all lacking the argument specifier part of LaTeX3 function names. A few macros starting with `\XINT` do not have the underscore.

For the actual use of the macros, note that when feeding them with negative numbers the minus sign must have category code other, as is standard. Similarly the slash used for inputting fractions must be of category other, as usual. And the square brackets also must be of category code other, if used on input. The 'e' of the scientific notation must be of category code letter. All of that is relaxed when inside an `\xintexpr`-ession (but arguments to macros which have been inserted in the expression must obey the rules, as it is the macro and not the parser which will get the tokens). In an `\xintexpr`-ession, the scientific 'e' may be 'E'.

The components of the **xint** bundle presuppose that the usual `\space` and `\empty` macros are pre-defined, which is the case in Plain TEX as well as in LATEX.

Lastly, the macros `\xintRelaxArray` (of **xint**) and `\xintTypesetEuclideAlgorithm` and `\xintTypesetBezoutAlgorithm` (of **xintgcd**) use `\loop`, both Plain and LATEX incarnations are compatible. `\xintTypesetBezoutAlgorithm` also uses the `\endgraf` macro.

13 Installation

```
Run tex or latex on xint.dtx.

This will extract the style files xint.sty, xintfrac.sty, xintexpr.sty,
xintbinhex.sty, xintgcd.sty, xintseries.sty, xintcfrac.sty (and xint.ins).

Files with the same names and in the same repertory will be overwritten.
The tex (not latex) run will stop with the complaint that it does not
understand \NeedsTeXFormat, but the style files will already have been
extracted by that time.

Alternatively, run tex or latex on xint.ins if available.

To get xint.pdf run pdflatex thrice on xint.dtx

           xint.sty |
       xintfrac.sty |
       xintexpr.sty |
     xintbinhex.sty | --> TDS:tex/generic/xint/
        xintgcd.sty |
     xintseries.sty |
      xintcfrac.sty |
           xint.dtx   --> TDS:source/generic/xint/
           xint.pdf   --> TDS:doc/generic/xint/

It may be necessary to then refresh the TeX installation filename
database.
```

14 Commands of the xint package

`{N}` (or also `{M}`) stands for a (long) number within braces with one optional minus sign and no leading zeros, or for a control sequence possibly within braces and expanding to

such a number (without the braces!), or for material within braces which expands to such a number after repeated expansions of the first token.

The letter x stands for something which will be inserted in-between a \numexpr and a \relax. It will thus be completely expanded and must give an integer obeying the TEX bounds. Thus, it may be for example a count register, or itself a \numexpr expression, or just a number written explicitely with digits or something like 4*\count 255 + 17, etc...

A count register or \numexpr expression, used as an argument to a macro dealing with long integers, must be prefixed by \the or \number.

Some of these macros are extended by xintfrac to accept fractions on input, and, generally, to output a fraction. This will be mentioned and the original macro \xintAbc remains then available under the name \xintiAbc.

> For the macros extended by the loading of xintfrac.sty, it is not necessary anymore to prefix a count register with \the. See the previous 'Use of count registers' section.

Some macros such as \xintQuo or \xintNum (which are among those made to accept fractions on input when xintfrac.sty is loaded) check that the fraction is an integer in disguise. They still produce on output integers without any forward slash mark nor trailing [n]. Again the original is still available with an additional 'i' in the name, in case it is important to skip the parsing, but here the output format is the same. See the xintfrac documentation for more information.

IMPORTANT! The integer-only macros are a bit more efficient, even for simple things such as determining the sign of a (long) number, as there is always some overhead due to the parsing the fraction format on input. This overhead, when package xintfrac has been loaded and has modified the xint routines, usually will not matter much, but there are contexts where obtaining an integer without a forward slash nor trailing [n] is mandatory: for example after an \ifnum or inside a \numexpr (for 'short' integers) or when used as argument to one of the package macros which are stricly integer-only on input such as \xintiSqrt, or \xintDouble or \xintDecSplit. A fraction which in disguise is an integer can be stripped of the slash and trailing [n] using \xintNum.

Contents

14.1 \xintRev

`\xintRev{N}` will revert the order of the digits of the number, keeping the optional sign. Leading zeros resulting from the operation are not removed (see the `\xintNum` macro for this). As described early, this macro and all other macros dealing with numbers first expand 'fully' their arguments.

```
\xintRev{-123000}=-000321
\xintNum{\xintRev{-123000}}=-321
```

14.2 \xintReverseOrder

`\xintReverseOrder{`⟨*list*⟩`}` does not do any expansion of its argument and just reverses the order of the tokens in the ⟨*list*⟩.[27] Brace pairs encountered are removed once and the enclosed material does not get reverted. Spaces are gobbled.

```
\xintReverseOrder{\xintDigitsOf\xintiPow {2}{100}\to\Stuff}
gives: \Stuff\to1002\xintiPow\xintDigitsOf
```

14.3 \xintRevWithBraces

New in release 1.06.

`\xintRevWithBraces{`⟨*list*⟩`}` first does the expansion of its argument (which thus may be macro), then it reverses the order of the tokens, or braced material, it encounters, adding a pair of braces to each (thus, maintaining brace pairs already existing). Spaces (in-between external brace pairs) are gobbled. This macro is mainly thought out for use on a ⟨*list*⟩ of such braced material; with such a list as argument the expansion will only hit against the first opening brace, hence do nothing, and the braced stuff may thus be macros one does not want to expand.

```
\edef\x{\xintRevWithBraces{12345}}
\meaning\x:macro:->{5}{4}{3}{2}{1}
  \edef\y{\xintRevWithBraces\x}
\meaning\y:macro:->{1}{2}{3}{4}{5}
```

The examples above could be defined with `\edef`'s because the braced material did not

[27] the argument is not a token list variable, just a ⟨*list*⟩ of tokens.

contain macros. Alternatively:

```
\expandafter\def\expandafter\w\expandafter
{\romannumeral0\xintrevwithbraces{{\A}{\B}{\C}{\D}{\E}}}
\meaning\w:macro:->{\E }{\D }{\C }{\B }{\A }
```

The macro `\xintReverseWithBracesNoExpand` does the same job without the initial expansion of its argument.

14.4 \xintLen

`\xintLen{N}` returns the length of the number, not counting the sign.

```
\xintLen{-12345678901234567890123456789}=29
```

Extended by **xintfrac** to fractions: the length of `A/B[n]` is the length of `A` plus the length of `B` plus the absolute value of `n` and minus one (an integer input as `N` is internally `N/1[0]` so the minus one means that the extended `\xintLen` behaves the same as the original for integers). The whole thing should sum up to less than circa `2^{31}`.

14.5 \xintLength

`\xintLength{`⟨*list*⟩`}` does not do any expansion of its argument and just counts how many tokens there are (possibly none). Things enclosed in braces count as one.

```
\xintLength {\xintiPow {2}{100}}=3
≠ \xintLen {\xintiPow {2}{100}}=31
```

14.6 \xintCSVtoList

New with release `1.06`.

`\xintCSVtoList{a,b,c...,z}` returns `{a}{b}{c}...{z}`. The argument may be a macro. It is first expanded: this means that if the argument is `a,b,..`, then `a`, if a macro, will be expanded which may or may not be a good thing (starting the replacement text of the macro with `\space` stops the expansion at the first level and gobbles the space; prefixing a macro with `\space` stops preemptively the expansion and gobbles the space). Chains of contiguous spaces are collapsed by the TEX scanning into single spaces.

```
\xintCSVtoList {1,2,a , b ,c d,x,y }->{1}{2}{a }{ b }{c d}{x}{y }
\def\y{a,b,c,d,e}\xintCSVtoList\y->{a}{b}{c}{d}{e}
```

The macro `\xintCSVtoListNoExpand` does the same job without the initial expansion.

14.7 \xintNthElt

New in release `1.06` and modified in `1.06a`.

`\xintNthElt{x}{`⟨*list*⟩`}` gets (expandably) the `x`th element of the ⟨*list*⟩, which may be a macro: it is first expanded (fully for the first tokens). The seeked element is returned with one pair of braces removed (if initially present).

```
\xintNthElt {37}{\xintFac {100}}=9
```

is the thirty-seventh digit of `100!`.

```
\xintNthElt {10}{\xintFtoCv {566827/208524}}=1457/536[0]
```

is the tenth convergent of `566827/208524` (uses **xintcfrac** package).

If `x=0` or `x<0`, the macro returns the length of the expanded list: this is not equivalent to `\xintLength` due to the initial full expansion of the first token, and differs from `\xintLen`

which is to be used on numbers or fractions only. The situation with x larger than the length of the list is kept silent, the macro then returns nothing; this will perhaps be modified in future versions.

```
\xintNthElt {7}{\xintCSVtoList {1,2,3,4,5,6,7,8,9}}=7
\xintNthElt {0}{\xintCSVtoList {1,2,3,4,5,6,7,8,9}}=9
```

The macro \xintNthEltNoExpand does the same job without first expanding its second argument.

14.8 \xintListWithSep

New with release 1.04.

\xintListWithSep{sep}{⟨*list*⟩} just inserts the given separator sep in-between all elements of the given list: this separator may be a macro but will not be expanded. The second argument also may be itself a macro: it is expanded as usual, *i.e.* fully for what comes first. Applying \xintListWithSep removes one level of top braces to each list constituent. An empty input gives an empty output, a singleton gives a singleton, the separator is used starting with at least two elements. Using an empty separator has the net effect of removing one-level of brace pairs from each ot the top-level braced material constituting the ⟨*list*⟩.

```
\xintListWithSep{:}{\xintFac {20}}=2:4:3:2:9:0:2:0:0:8:1:7:6:6:4:0:0:0:0
```

The macro \xintListWithSepNoExpand does the same job without the initial expansion.

14.9 \xintApply

New with release 1.04.

\xintApply{\macro}{⟨*list*⟩} applies the one parameter command \macro to each item in the ⟨*list*⟩ (no separator) given as second argument. Each item is given in turn as parameter to \macro which is expanded (as usual, *i.e.* fully for what comes first), and the result is braced. On output, a new list with these braced results. The ⟨*list*⟩ may itself be some macro expanding (in the previously described way) to the list of tokens to which the command \macro will be applied. For example, if the ⟨*list*⟩ expands to some positive number, then each digit will be replaced by the result of applying \macro on it.

```
\def\macro #1{\the\numexpr 9-#1\relax}
\xintApply\macro{\xintFac {20}}=7567097991823359999
```

The macro \xintApplyNoExpand does the same job without the first initial expansion which gave the ⟨*list*⟩ of braced tokens to which \macro is applied.

14.10 \xintApplyUnbraced

New in release 1.06b.

\xintApplyUnbraced{\macro}{⟨*list*⟩} is like \xintApply except that the various outputs are not again braced. The net effect is the same as doing

```
\xintListWithSep {}{\xintApply {\macro}{⟨list⟩}}
```

This command is useful for non-expandable things like doing macro definitions, for which braces are an inconvenience. (sorry for the silly example:)

```
\def\macro #1{\expandafter\def\csname myself#1\endcsname {#1}}
\xintApplyUnbraced\macro{{elta}{eltb}{eltc}}
\meaning\myselfelta:  macro:->elta
```

The macro \xintApplyUnbracedNoExpand does the same job without the first initial expansion which gave the ⟨*list*⟩ of braced tokens to which \macro is applied.

14.11 \xintAssign

\xintAssign⟨*braced things*⟩\to⟨*as many cs as they are things*⟩ defines (without checking if something gets overwritten) the control sequences on the right of \to to be the complete expansions of the successive things on the left of \to enclosed within braces.

Important: a 'full' expansion (as previously described) is applied first to the material in front of \xintAssign.

As a special exception, if after this initial expansion a brace does not immediately follows \xintAssign, it is assumed that there is only one control sequence to define and it is then defined to be the complete expansion of the entire material between \xintAssign and \to.

```
\xintAssign\xintDivision{1000000000000}{133333333}\to\Q\R
   \meaning\Q: macro:->7500, \meaning\R: macro:->2500
\xintAssign\xintiPow {7}{13}\to\SevenToThePowerThirteen
          \SevenToThePowerThirteen=96889010407
```

Of course this macro and its cousins completely break usage in pure expansion contexts, as assignments are made via the \edef primitive.

14.12 \xintAssignArray

Changed in release 1.06 to let the defined macro pass its argument through a \numexpr...\relax.

\xintAssignArray⟨*braced things*⟩\to\myArray first expands fully the first token then defines \myArray to be a macro with one parameter, such that \myArray{x} expands in two steps (which provoke the full expansion of the 'short' number {x}, given to a \numexpr) to give the x-th braced thing, itself completely expanded. \myArray{0} returns the number M of elements of the array so that the successive elements are \myArray{1}, ..., \myArray{M}.

```
\xintAssignArray\xintBezout {1000}{113}\to\Bez
```

will set \Bez{0} to 5, \Bez{1} to 1000, \Bez{2} to 113, \Bez{3} to -20, \Bez{4} to -177, and \Bez{5} to 1: $(-20)\times 1000-(-177)\times 113=1$.

14.13 \xintRelaxArray

\xintRelaxArray\myArray sets to \relax all macros which were defined by the previous \xintAssignArray with \myArray as array name.

14.14 \xintDigitsOf

This is a synonym for \xintAssignArray, to be used to define an array giving all the digits of a given number.

```
\xintDigitsOf\xintiPow {7}{500}\to\digits
```

7^500 has \digits{0}=423 digits, and the 123rd among them (starting from the most significant) is \digits{123}=3.

14.15 \xintNum

\xintNum{N} removes chains of plus or minus signs, followed by zeros.

```
\xintNum{+---++----+--00000000367941789479}=-367941789479
```

Extended by xintfrac to accept also a fraction on input, as long as it reduces to an integer after division of the numerator by the denominator.

```
\xintNum{123.48/-0.03}=-4116
```

14.16 \xintSgn

\xintSgn{N} returns 1 if the number is positive, 0 if it is zero and -1 if it is negative. Extended by xintfrac to fractions.

14.17 \xintSgnFork

New with release 1.07.

\xintSgnFork{-1|0|1}{⟨A⟩}{⟨B⟩}{⟨C⟩} expandably chooses to execute either the ⟨A⟩, ⟨B⟩ or ⟨C⟩ code, depending on its first argument. This first argument should be anything expanding to either -1, 0 or 1 (a count register should be prefixed by \the and a \numexpr...\relax also should be prefixed by \the). This utility is provided to help construct expandable macros choosing depending on a condition which one of the package macros to use, or which values to confer to their arguments.

```
\def\myfunction #1%
% expands to |x+1| if x < -1, x-1 if x > 1, else 1 - x^2
% rounded to two decimal places
   {\xintRound {2}{\xintSgnFork
       {\xintSgnFork{\xintGeq{#1}{1}}{}{0}{\xintSgn{#1}}}
       {\xintSub{-1}{#1}}{\xintSub{1}{\xintSqr{#1}}}{\xintSub{#1}{1}}}}%
\xintListWithSep{,\,}{\xintApply\myfunction
                 {{-5/2}{-2}{-3/2}{-1}{-1/2}{0}{1/2}{1}{3/2}{2}{5/2}}}
```

1.50, 1.00, 0.50, 0, 0.75, 1.00, 0.75, 0, 0.50, 1.00, 1.50

Using an xintexpr-ession, one may simplify the coding:

```
\def\myfunction #1% expands to |x+1| if x < -1, x-1 if x > 1, else 1 - x^2
   {\xintRound {2}{\xinttheexpr\xintSgnFork
       {\xintSgnFork{\xintGeq{#1}{1}}{}{0}{\xintSgn{#1}}}
       { -#1 - 1 }{ 1 - (#1)^2 }{ #1 - 1 } \relax }}%
```

1.50, 1.00, 0.50, 0, 0.75, 1.00, 0.75, 0, 0.50, 1.00, 1.50

Notice the use of parentheses, with #1=-1, 1-#1^2 would give 1--1^2 which evaluates to 2. Or with #1=3/2, 1-#1^2 gives 1-3/2^2 which evaluates inside an xintexpr-ession to 1-3/4=1/4 not 1-9/4=-5/4.

14.18 \xintOpp

\xintOpp{N} returns the opposite -N of the number N. Extended by xintfrac to fractions.

14.19 \xintAbs

\xintAbs{N} returns the absolute value of the number. Extended by xintfrac to fractions.

14.20 \xintAdd

\xintAdd{N}{M} returns the sum of the two numbers. Extended by xintfrac to fractions.

14.21 \xintSub

\xintSub{N}{M} returns the difference N-M. Extended by xintfrac to fractions.

14.22 \xintCmp

\xintCmp{N}{M} returns 1 if N>M, 0 if N=M, and -1 if N<M. Extended by xintfrac to fractions.

14.23 \xintGeq

\xintGeq{N}{M} returns 1 if the *absolute value* of the first number is at least equal to the absolute value of the second number. If |N|<|M| it returns 0. Extended by xintfrac to fractions (starting with relaease 1.07). Please note that the macro compares *absolute values*.

14.24 \xintMax

\xintMax{N}{M} returns the largest of the two in the sense of the order structure on the relative integers (*i.e.* the right-most number if they are put on a line with positive numbers on the right): \xintiMax {-5}{-6}=-5. Extended by xintfrac to fractions.

14.25 \xintMin

\xintMin{N}{M} returns the smallest of the two in the sense of the order structure on the relative integers (*i.e.* the left-most number if they are put on a line with positive numbers on the right): \xintiMin {-5}{-6}=-6. Extended by xintfrac to fractions.

14.26 \xintSum

\xintSum{⟨*braced things*⟩} after expanding its argument expects to find a sequence of tokens (or braced material). Each is expanded (with the usual meaning), and the sum of all these numbers is returned.

```
\xintiSum{{123}{-98763450}{\xintFac{7}}{\xintiMul{3347}{591}}}=-96780210
                        \xintiSum{1234567890}=45
```

An empty sum is no error and returns zero: \xintiSum {}=0. A sum with only one term returns that number: \xintiSum {{-1234}}=-1234. Attention that \xintiSum {-1234} is not legal input and will make the TEX run fail. On the other hand \xintiSum {1234}=10. Extended by xintfrac to fractions.

14.27 \xintSumExpr

\xintSumExpr⟨*braced things*⟩\relax is to what \xintSum expands. The argument is then expanded (with the usual meaning) and should give a list of braced quantities or macros,

each one will be expanded in turn.

```
\xintiSumExpr {123}{-98763450}{\xintFac{7}}{\xintiMul{3347}{591}}\relax=-96780210
```

Note: I am not so happy with the name which seems to suggest that the + sign should be used instead of braces. Perhaps this will change in the future.

Extended by xintfrac to fractions.

14.28 \xintMul

Modified in release 1.03.

\xintMul{N}{M} returns the product of the two numbers. Starting with release 1.03 of xint, the macro checks the lengths of the two numbers and then activates its algorithm with the best (or at least, hoped-so) choice of which one to put first. This makes the macro a bit slower for numbers up to 50 digits, but may give substantial speed gain when one of the number has 100 digits or more. Extended by xintfrac to fractions.

14.29 \xintSqr

\xintSqr{N} returns the square. Extended by xintfrac to fractions.

14.30 \xintPrd

\xintPrd{⟨*braced things*⟩} after expanding its argument expects to find a sequence of tokens (or braced material). Each is expanded (with the usual meaning), and the product of all these numbers is returned.

```
 \xintiPrd{{-9876}{\xintFac{7}}{\xintiMul{3347}{591}}}=-98458861798080
                \xintiPrd{123456789123456789}=131681894400
```

An empty product is no error and returns 1: \xintiPrd {}=1. A product reduced to a single term returns this number: \xintiPrd {{-1234}}=-1234. Attention that \xintiPrd {-1234} is not legal input and will make the TEX compilation fail. On the other hand \xintiPrd {1234}=24.

$$2^{200}3^{100}7^{100}$$

```
=\xintiPrd {{\xintiPow {2}{200}}{\xintiPow {3}{100}}{\xintiPow {7}{100}}}
=267872793166157757576627951700754840232474026637401534897445961481 5
42641296549949000044400724076572713000016531207640654562118014357199
40159033435392440282124389668222489278629880843827161333 76
```

Extended by xintfrac to fractions.

With xintexpr, the above would be coded simply as

```
\xintNum {\xinttheexpr 2^200*3^100*7^100\relax }
```

(\xintNum to print an integer, not a fraction).

14.31 \xintPrdExpr

Name change in 1.06a! I apologize, but I suddenly decided that \xintProductExpr was a bad choice; so I just replaced it by the current name.

\xintPrdExpr{⟨*argument*⟩}\relax is to what \xintPrd expands ; its argument is expanded (with the usual meaning) and should give a list of braced numbers or macros. Each will be expanded when it is its turn.

```
\xintiPrdExpr 123456789123456789\relax=131681894400
```

Note: I am not so happy with the name which seems to suggest that the * sign should be used instead of braces. Perhaps this will change in the future.

Extended by xintfrac to fractions.

14.32 \xintPow

\xintPow{N}{x} returns N^x. When x is zero, this is 1. If N is zero and x<0, if |N|>1 and x<0 negative, or if |N|>1 and x>999999999, then an error is raised. 2^999999999 has 301,029,996 digits; each exact multiplication of two one thousand digits numbers already takes a few seconds, so needless to say this bound is completely irrealistic. Already 2^9999 has 3,010 digits,[28] so I should perhaps lower the bound to 99999.

Extended by xintfrac to fractions (\xintPow) and also to floats (\xintFloatPow). Of course, negative exponents do not then cause errors anymore. The float version is able to deal with things such as 2^999999999 without any problem. For example \xintFloatPow[4]{2}{9999}=9.975e3009 and \xintFloatPow[4]{2}{999999999}=2.306e301029995.

> The macros described next are all integer-only on input. With xintfrac loaded their argument is filtered through \xintNum and may thus be a fraction, as long as it is an integer in disguise.

14.33 \xintFac

\xintFac{x} returns the factorial. It is an error if the argument is negative or at least 10^6. It is not recommended to launch the computation of things such as 100000!, if you need your computer for other tasks. Note that the argument is of the x type, it must obey the TEX bounds, but on the other hand may involve count registers and even arithmetic operations as it will be completely expanded inside a \numexpr.

Modified in 1.08b →

With xintfrac loaded, the macro also accepts a fraction as argument, as long as this fraction turns out to be an integer: \xintFac {66/3}=112400072777607680000.

14.34 \xintDivision

\xintDivision{N}{M} returns {quotient Q}{remainder R}. This is euclidean division: N = QM + R, 0 ≤ R < |M|. So the remainder is always non-negative and the formula N = QM + R always holds independently of the signs of N or M. Division by zero is of course an error (even if N vanishes) and returns {0}{0}.

This macro is integer only (with xintfrac loaded it accepts fractions on input, but they must be integers in disguise) and not to be confused with the xintfrac macro \xintDiv which divides one fraction by another.

[28] on my laptop \xintiPow{2}{9999} obtains all 3010 digits in about ten or eleven seconds. In contrast, the float versions for 8, 16, 24, or even more significant figures, do their jobs in circa one hundredth of a second (1.08b). This is done without log/exp which are not (yet?) implemented in xintfrac. The LaTeX3 l3fp does this with log/exp and is ten times faster (16 figures only).

14.35 \xintQuo

\xintQuo{N}{M} returns the quotient from the euclidean division. When both N and M are positive one has \xintQuo{N}{M}=\xintiTrunc {0}{N/M} (using package xintfrac). With xintfrac loaded it accepts fractions on input, but they must be integers in disguise.

14.36 \xintRem

\xintRem{N}{M} returns the remainder from the euclidean division. With xintfrac loaded it accepts fractions on input, but they must be integers in disguise.

14.37 \xintFDg

\xintFDg{N} returns the first digit (most significant) of the decimal expansion.

14.38 \xintLDg

\xintLDg{N} returns the least significant digit. When the number is positive, this is the same as the remainder in the euclidean division by ten.

14.39 \xintMON, \xintMMON

New in version 1.03.

\xintMON{N} returns (-1)^N and \xintMMON{N} returns (-1)^{N-1}.

```
\xintMON {-280914019374101929}=-1, \xintMMON {-280914019374101929}=1
```

14.40 \xintOdd

\xintOdd{N} is 1 if the number is odd and 0 otherwise.

> The macros described next are strictly for integer-only arguments. If xintfrac is loaded, use \xintNum if necessary.

14.41 \xintiSqrt, \xintiSquareRoot

New with 1.08.

\xintiSqrt{N} returns the largest integer whose square is at most equal to N.

```
\xintiSqrt {200000000000000000000000000000000000}=1414213562373095048
\xintiSqrt {300000000000000000000000000000000000}=1732050807568877293
                  \xintiSqrt {\xintDSH {-120}{2}}=
   1414213562373095048801688724209698078569671875376948073176679
```

\xintiSquareRoot{N} returns {M}{d} with d>0, M^2-d=N and M smallest (hence =1+\xintiSqrt{N}).

```
    \xintAssign\xintiSquareRoot {17000000000000000000000000}\to\A\B
                  \xintiSub{\xintiSqr\A}\B=\A^2-\B
      17000000000000000000000000=4123105625618^2-2799177881924
```

A rational approximation to $\sqrt{\texttt{N}}$ is $\texttt{M} - \frac{\texttt{d}}{\texttt{2M}}$ (this is a majorant and the error is at most `1/2M`; if `N` is a perfect square `k^2` then `M=k+1` and this gives `k+1/(2k+2)`, not `k`).

Package **xintfrac** has `\xintFloatSqrt` for square roots of floating point numbers.

14.42 \xintInc, \xintDec

New with `1.08`.

`\xintInc{N}` is `N+1` and `\xintDec{N}` is `N-1`. These macros remain integer-only, even with **xintfrac** loaded.

14.43 \xintDouble, \xintHalf

New with `1.08`.

`\xintDouble{N}` returns `2N` and `\xintHalf{N}` is `N/2` rounded towards zero. These macros remain integer-only, even with **xintfrac** loaded.

14.44 \xintDSL

`\xintDSL{N}` is decimal shift left, *i.e.* multiplication by ten.

14.45 \xintDSR

`\xintDSR{N}` is decimal shift right, *i.e.* it removes the last digit (keeping the sign), equivalently it is the closest integer to `N/10` when starting at zero.

14.46 \xintDSH

`\xintDSH{x}{N}` is parametrized decimal shift. When `x` is negative, it is like iterating `\xintDSL |x|` times (*i.e.* multiplication by `10^{-x}`). When `x` positive, it is like iterating `\DSR x` times (and is more efficient of course), and for a non-negative `N` this is thus the same as the quotient from the euclidean division by `10^x`.

14.47 \xintDSHr, \xintDSx

New in release `1.01`.

`\xintDSHr{x}{N}` expects `x` to be zero or positive and it returns then a value `R` which is correlated to the value `Q` returned by `\xintDSH{x}{N}` in the following manner:

- if `N` is positive or zero, `Q` and `R` are the quotient and remainder in the euclidean division by `10^x` (obtained in a more efficient manner than using `\xintDivision`),
- if `N` is negative let `Q1` and `R1` be the quotient and remainder in the euclidean division by `10^x` of the absolute value of `N`. If `Q1` does not vanish, then `Q=-Q1` and `R=R1`. If `Q1` vanishes, then `Q=0` and `R=-R1`.
- for `x=0`, `Q=N` and `R=0`.

So one has `N = 10^x Q + R` if `Q` turns out to be zero or positive, and `N = 10^x Q - R` if `Q` turns out to be negative, which is exactly the case when `N` is at most `-10^x`.

`\xintDSx{x}{N}` for `x` negative is exactly as `\xintDSH{x}{N}`, *i.e.* multiplication by `10^{-x}`. For `x` zero or positive it returns the two numbers `{Q}{R}` described above, each one within braces. So `Q` is `\xintDSH{x}{N}`, and `R` is `\xintDSHr{x}{N}`, but computed simultaneously.

```
\xintAssign\xintDSx {-1}{-123456789}\to\M
\meaning\M: macro:->-1234567890.
\xintAssign\xintDSx {-20}{123456789}\to\M
\meaning\M: macro:->12345676890000000000000000000.
\xintAssign\xintDSx {0}{-123004321}\to\Q\R
\meaning\Q: macro:->-123004321, \meaning\R: macro:->0.
\xintDSH {0}{-123004321}=-123004321, \xintDSHr {0}{-123004321}=0
\xintAssign\xintDSx {6}{-123004321}\to\Q\R
\meaning\Q: macro:->-123, \meaning\R: macro:->4321.
\xintDSH {6}{-123004321}=-123, \xintDSHr {6}{-123004321}=4321
\xintAssign\xintDSx {8}{-123004321}\to\Q\R
\meaning\Q: macro:->-1, \meaning\R: macro:->23004321.
\xintDSH {8}{-123004321}=-1, \xintDSHr {8}{-123004321}=23004321
\xintAssign\xintDSx {9}{-123004321}\to\Q\R
\meaning\Q: macro:->0, \meaning\R: macro:->-123004321.
\xintDSH {9}{-123004321}=0, \xintDSHr {9}{-123004321}=-123004321
```

14.48 \xintDecSplit

This has been modified in release `1.01`.

`\xintDecSplit{x}{N}` cuts the number into two pieces (each one within a pair of enclosing braces). First the sign if present is *removed*. Then, for `x` positive or null, the second piece contains the `x` least significant digits (*empty* if `x=0`) and the first piece the remaining digits (*empty* when `x` equals or exceeds the length of `N`). Leading zeros in the second piece are not removed. When `x` is negative the first piece contains the `|x|` most significant digits and the second piece the remaining digits (*empty* if `|x|` equals or exceeds the length of `N`). Leading zeros in this second piece are not removed. So the absolute value of the original number is always the concatenation of the first and second piece.

This macro's behavior for `N` non-negative is final and will not change. I am still hesitant about what to do with the sign of a negative `N`.

```
             \xintAssign\xintDecSplit {0}{-123004321}\to\L\R
\meaning\L: macro:->123004321, \meaning\R: macro:->.
             \xintAssign\xintDecSplit {5}{-123004321}\to\L\R
\meaning\L: macro:->1230, \meaning\R: macro:->04321.
             \xintAssign\xintDecSplit {9}{-123004321}\to\L\R
\meaning\L: macro:->, \meaning\R: macro:->123004321.
            \xintAssign\xintDecSplit {10}{-123004321}\to\L\R
\meaning\L: macro:->, \meaning\R: macro:->123004321.
           \xintAssign\xintDecSplit {-5}{-12300004321}\to\L\R
\meaning\L: macro:->12300, \meaning\R: macro:->004321.
```

```
          \xintAssign\xintDecSplit {-11}{-12300004321}\to\L\R
\meaning\L: macro:->12300004321, \meaning\R: macro:->.
          \xintAssign\xintDecSplit {-15}{-12300004321}\to\L\R
\meaning\L: macro:->12300004321, \meaning\R: macro:->.
```

14.49 \xintDecSplitL

`\xintDecSplitL{x}{N}` returns the first piece after the action of `\xintDecSplit`.

14.50 \xintDecSplitR

`\xintDecSplitR{x}{N}` returns the second piece after the action of `\xintDecSplit`.

15 Commands of the xintfrac package

This package was first included in release `1.03` of the **xint** bundle. The general rule of the bundle that each macro first expands (what comes first, fully) each one of its arguments applies.

`f` stands for an integer or a fraction (see section 3 for the accepted input formats) or something which expands to an integer or fraction. It is possible to use in the numerator or the denominator of `f` count registers and even expressions with infix arithmetic operators, under some rules which are explained in the previous Use of count registers section.

Not previously documented →

As in the xint.sty documentation, `x` stands for something which will internally be embedded in a `\numexpr`. It may thus be a count register or something like `4*\count 255 + 17`, etc..., but must expand to an integer obeying the TEX bound.

The fraction format on output is the scientific notation for the 'float' macros, and the `A/B[n]` format for all other fraction macros, with the exception of `\xintTrunc`, `\xintRound` (which produce decimal numbers) and `\xintIrr`, `\xintJrr`, `\xintRawWithZeros` (which return an `A/B` with no trailing `[n]`, even if `B` turns out to be `1`). Use `\xintNum` for fractions a priori known to simplify to integers: `\xintNum {\xintAdd {2}{3}}` gives `5` whereas `\xintAdd {2}{3}` returns `5/1[0]`. Some macros (among them `\xintiTrunc`, `\xintiRound`, and `\xintFac`) already produce integers on output.

Contents

15.1 \xintLen

The original macro is extended to accept a fraction on input.

```
\xintLen {201710/298219}=11, \xintLen {1234/1}=4, \xintLen {1234}=4
```

15.2 \xintRaw

New with release 1.04.

MODIFIED IN 1.07.

This macro 'prints' the fraction f as it is received by the package after its parsing and expansion, in a printable form A/B[n] equivalent to the internal representation: the denominator B is always strictly positive and is printed even if it has value 1.

```
\xintRaw{\the\numexpr 571*987\relax.123e-10/\the\numexpr -201+59\relax e-7}=
                                -563577123/142[-6]
```

15.3 \xintRawWithZeros

New name in 1.07 (former name \xintRaw).

This macro 'prints' the fraction f (after its parsing and expansion) in A/B form, with A as returned by \xintNumerator{f} and B as returned by \xintDenominator{f}.

```
\xintRawWithZeros{\the\numexpr 571*987\relax.123e-10/\the\numexpr -201+59\relax e-7}=
                                -563577123/142000000
```

15.4 \xintNumerator

This returns the numerator corresponding to the internal representation of a fraction, with positive powers of ten converted into zeros of this numerator:

```
\xintNumerator {178000/25600000[17]}=178000000000000000000
        \xintNumerator {312.289001/20198.27}=312289001
            \xintNumerator {178000e-3/256e5}=178000
           \xintNumerator {178.000/25600000}=178000
```

As shown by the examples, no simplification of the input is done. For a result uniquely associated to the value of the fraction first apply \xintIrr.

15.5 \xintDenominator

This returns the denominator corresponding to the internal representation of the fraction:[29]

```
\xintDenominator {178000/25600000[17]}=25600000
\xintDenominator {312.289001/20198.27}=20198270000
\xintDenominator {178000e-3/256e5}=25600000000
\xintDenominator {178.000/25600000}=25600000000
```

As shown by the examples, no simplification of the input is done. The denominator looks wrong in the last example, but the numerator was tacitly multiplied by 1000 through the removal of the decimal point. For a result uniquely associated to the value of the fraction first apply \xintIrr.

15.6 \xintFrac

This is a LaTeX only command, to be used in math mode only. It will print a fraction, internally represented as something equivalent to A/B[n] as \frac {A}{B}10^n. The power of ten is omitted when n=0, the denominator is omitted when it has value one, the number being separated from the power of ten by a \cdot. $\xintFrac {178.000/25600000}$ gives $\frac{178000}{25600000}10^{-3}$, $\xintFrac {178.000/1}$ gives $178000\cdot 10^{-3}$, $\xintFrac {3.5/5.7}$ gives $\frac{35}{57}$, and $\xintFrac {\xintNum {\xintFac{10}/\xintiSqr{\xintFac {5}}}}$ gives 252. As shown by the examples, simplification of the input (apart from removing the decimal points and moving the minus sign to the numerator) is not done automatically and must be the result of macros such as \xintIrr, \xintREZ, or \xintNum (for fractions being in fact integers.)

15.7 \xintSignedFrac

New with release 1.04.

This is as \xintFrac except that a negative fraction has the sign put in front, not in the numerator.

```
\[\xintFrac {-355/113}=\xintSignedFrac {-355/113}\]
```

$$\frac{-355}{113} = -\frac{355}{113}$$

15.8 \xintFwOver

This does the same as \xintFrac except that the \over primitive is used for the fraction (in case the denominator is not one; and a pair of braces contains the A\over B part). $\xintFwOver {178.000/25600000}$ gives $\frac{178000}{25600000}10^{-3}$, $\xintFwOver {178.000/1}$ gives $178000\cdot 10^{-3}$, $\xintFwOver {3.5/5.7}$ gives $\frac{35}{57}$, and $\xintFwOver {\xintNum {\xintFac{10}/\xintiSqr{\xintFac {5}}}}$ gives 252.

15.9 \xintSignedFwOver

New with release 1.04.

[29] recall that the [] construct excludes presence of a decimal point.

This is as \xintFwOver except that a negative fraction has the sign put in front, not in the numerator.

```
\[\xintFwOver {-355/113}=\xintSignedFwOver {-355/113}\]
```

$$\frac{-355}{113} = -\frac{355}{113}$$

15.10 \xintREZ

This command normalizes a fraction by removing the powers of ten from its numerator and denominator: `\xintREZ {178000/25600000[17]}=178/256[15]`, `\xintREZ {1780000000000e30/2560000000000e15}=178/256[15]`. As shown by the example, it does not otherwise simplify the fraction.

15.11 \xintE

New with 1.07.

`\xintE {f}{x}` multiplies the fraction `f` by `10^x`. The *second* argument `x` must obey the TEX bounds. It may be a count register: `\count 255 123456789 \xintE {10}{\count 255}->10/1[123456789]`. Be careful that for obvious reasons such gigantic numbers should not be given to \xintNum, or added to something with a widely different order of magnitude, as the package always works to get the *exact* result. There is *no problem* using them for *float* operations:

```
\xintFloatAdd {1e1234567890}{1}=1.000000000000000e1234567890
```

15.12 \xintIrr

MODIFIED IN 1.08.

This puts the fraction into its unique irreducible form:

```
\xintIrr {178.256/256.178}=6856/9853
```

$= \frac{6856}{9853}$

Note that the current implementation does not cleverly first factor powers of 2 and 5, so input such as `\xintIrr {2/3[100]}` will make xintfrac do the Euclidean division of `2·10^{100}` by 3, which is a bit stupid.

Starting with release 1.08, `\xintIrr` does not remove the trailing `/1` when the output is an integer. This makes things easier for post-treatment by user defined macros. So the output format is now *always* `A/B` with `B>0`. Use \xintNum rather than `\xintIrr` if it is known that the output is an integer and the trailing `/1` is a nuisance.

15.13 \xintJrr

MODIFIED IN 1.08.

This also puts the fraction into its unique irreducible form:

```
\xintJrr {178.256/256.178}=6856/9853
```

This is faster than `\xintIrr` for fractions having some big common factor in the numerator and the denominator.

```
\xintJrr {\xintiPow{\xintFac {15}}{3}/\xintiPrdExpr
{\xintFac{10}}{\xintFac{30}}{\xintFac{5}}\relax }=1001/51705840
```

But to notice the difference one would need computations with much bigger numbers than in this example. Starting with release 1.08, \xintJrr does not remove the trailing /1 when the output is an integer.

15.14 \xintTrunc

\xintTrunc{x}{f} returns the start of the decimal expansion of the fraction f, with x digits after the decimal point. The argument x should be non-negative. When x=0, the integer part of f results, with an ending decimal point. Only when f evaluates to zero does \xintTrunc not print a decimal point. When f is not zero, the sign is maintained in the output, also when the digits are all zero.

```
\xintTrunc {16}{-803.2028/20905.298}=-0.0384210165289200
\xintTrunc {20}{-803.2028/20905.298}=-0.03842101652892008523
\xintTrunc {10}{\xintPow {-11}{-11}}=-0.0000000000
\xintTrunc {12}{\xintPow {-11}{-11}}=-0.000000000003
\xintTrunc {12}{\xintAdd {-1/3}{3/9}}=0
```

The digits printed are exact up to and including the last one. The identity \xintTrunc {x}{-f}=-\xintTrunc {x}{f} holds.[30]

15.15 \xintiTrunc

\xintiTrunc{x}{f} returns the integer equal to 10^x times what \xintTrunc{x}{f} would return.

```
\xintiTrunc {16}{-803.2028/20905.298}=-384210165289200
\xintiTrunc {10}{\xintPow {-11}{-11}}=0
\xintiTrunc {12}{\xintPow {-11}{-11}}=-3
```

Differences between \xintTrunc{0}{f} and \xintiTrunc{0}{f}: the former cannot be used inside integer-only macros, and the latter removes the decimal point, and never returns -0 (and of course removes all superfluous leading zeros.)

15.16 \xintRound

New with release 1.04.

\xintRound{x}{f} returns the start of the decimal expansion of the fraction f, rounded to x digits precision after the decimal point. The argument x should be non-negative. Only when f evaluates exactly to zero does \xintRound return 0 without decimal point. When f is not zero, its sign is given in the output, also when the digits printed are all zero.

```
\xintRound {16}{-803.2028/20905.298}=-0.0384210165289201
\xintRound {20}{-803.2028/20905.298}=-0.03842101652892008523
\xintRound {10}{\xintPow {-11}{-11}}=-0.0000000000
\xintRound {12}{\xintPow {-11}{-11}}=-0.000000000004
\xintRound {12}{\xintAdd {-1/3}{3/9}}=0
```

The identity \xintRound {x}{-f}=-\xintRound {x}{f} holds. And regarding $(-11)^{-11}$ here is some more of its expansion:

```
-0.00000000000350493899481392497604003313162598556370...
```

[30] Recall that -\macro is not valid as argument to any package macro, one must use \xintOpp{\macro} or \xintiOpp{\macro}, except inside \xinttheexpr...\relax.

15.17 \xintiRound

New with release 1.04.

\xintiRound{x}{f} returns the integer equal to 10^x times what \xintRound{x}{f} would return.

```
\xintiRound {16}{-803.2028/20905.298}=-384210165289201
\xintiRound {10}{\xintPow {-11}{-11}}=0
```

Differences between \xintRound{0}{f} and \xintiRound{0}{f}: the former cannot be used inside integer-only macros, and the latter removes the decimal point, and never returns -0 (and of course removes all superfluous leading zeros.)

15.18 \xintDigits, \xinttheDigits

New with release 1.07.

The syntax \xintDigits := D; (where spaces do not matter) assigns the value of D to the number of digits to be used by floating point operations. The default is 16. The maximal value is 32767. The macro \xinttheDigits serves to print the current value.

15.19 \xintFloat

New with release 1.07.

The macro \xintFloat [P]{f} has an optional argument P which replaces the current value of \xintDigits. The (rounded truncation of the) fraction f is then printed in scientific form, with P digits, a lowercase e and an exponent N. The first digit is from 1 to 9, it is preceded by an optional minus sign and is followed by a dot and P-1 digits, the trailing zeros are not trimmed. In the exceptional case where the rounding went to the next power of ten, the output is 10.0...0eN (with a sign, perhaps). The sole exception is for a zero value, which then gets output as 0.e0 (in an \xintCmp test it is the only possible output of \xintFloat or one of the 'Float' macros which will test positive for equality with zero).

```
 \xintFloat[32]{1234567/7654321}=1.6129020457856418616360615134902e-1
\xintFloat[32]{1/\xintFac{100}}=1.0715102881254669231835467595192e-158
```

The argument to \xintFloat may be an \xinttheexpr-ession, like the other macros; only its final evaluation is submitted to \xintFloat: the inner evaluations of chained arguments are not at all done in 'floating' mode. For this one must use \xintthefloatexpr.

15.20 \xintAdd

The original macro is extended to accept fractions on input. Its output will now always be in the form A/B[n]. The original is available as \xintiAdd.

15.21 \xintFloatAdd

New with release 1.07.

\xintFloatAdd [P]{f}{g} first replaces f and g with their float approximations, with 2 safety digits. It then adds exactly and outputs in float format with precision P (which is optional) or \xintDigits if P was absent, the result of this computation.

15.22 \xintSub

The original macro is extended to accept fractions on input. Its output will now always be in the form A/B[n]. The original is available as \xintiSub.

15.23 \xintFloatSub

New with release 1.07.

\xintFloatSub [P]{f}{g} first replaces f and g with their float approximations, with 2 safety digits. It then subtracts exactly and outputs in float format with precision P (which is optional), or \xintDigits if P was absent, the result of this computation.

15.24 \xintMul

The original macro is extended to accept fractions on input. Its output will now always be in the form A/B[n]. The original is available as \xintiMul.

15.25 \xintFloatMul

New with release 1.07.

\xintFloatMul [P]{f}{g} first replaces f and g with their float approximations, with 2 safety digits. It then multiplies exactly and outputs in float format with precision P (which is optional), or \xintDigits if P was absent, the result of this computation.

15.26 \xintSqr

The original macro is extended to accept a fraction on input. Its output will now always be in the form A/B[n]. The original is available as \xintiSqr.

15.27 \xintDiv

\xintDiv{f}{g} computes the fraction f/g. As with all other computation macros, no simplification is done on the output, which is in the form A/B[n].

15.28 \xintFloatDiv

New with release 1.07.

\xintFloatDiv [P]{f}{g} first replaces f and g with their float approximations, with 2 safety digits. It then divides exactly and outputs in float format with precision P (which is optional), or \xintDigits if P was absent, the result of this computation.

15.29 \xintFac

Modified in 1.08b (to allow fractions on input).

The original is extended to allow a fraction on input but this fraction f must simplify to a integer n (non negative and at most 999999, but already 100000! is prohibitively time-costly). On output n! (no trailing /1[0]). The original macro (which has less overhead) is still available as \xintiFac.

15.30 \xintPow

\xintPow{f}{g}: the original macro is extended to accept fractions on input. The output will now always be in the form A/B[n] (even when the exponent vanishes: \xintPow {2/3}{0}=1/1[0]). The original is available as \xintiPow.

Changed in 1.08b →

The exponent is allowed to be input as a fraction but it must simplify to an integer: \xintPow {2/3}{10/2}=32/243[0]. This integer will be checked to not exceed 999999999; future releases will presumably lower this limit as even much much smaller values already create gigantic numerators and denominators which can not be computed exactly in a reasonable time. Indeed 2^999999999 has 301029996 digits.

15.31 \xintFloatPow

New with 1.07.

\xintFloatPow [P]{f}{x} uses either the optional argument P or the value of \xintDigits. It computes a floating approximation to f^x.

The exponent x will be fed to a \numexpr, hence count registers are accepted on input for this x. And the absolute value |x| must obey the TEX bound. For larger exponents use the slightly slower routine \xintFloatPower which allows the exponent to be a fraction simplifying to an integer and does not limit its size. This slightly slower routine is the one to which ^ is mapped inside \xintthefloatexpr...\relax.

The macro \xintFloatPow chooses dynamically an appropriate number of digits for the intermediate computations, large enough to achieve the desired accuracy (hopefully).

```
\xintFloatPow [8]{3.1415}{1234567890}=1.6122066e613749456
```

15.32 \xintFloatPower

New with 1.07.

\xintFloatPower{f}{g} computes a floating point value f^g where the exponent g is not constrained to be at most the TEX bound 2147483647. It may even be a fraction A/B but must simplify to an integer.

```
\xintFloatPower [8]{1.000000000001}{1e12}=2.7182818e0
\xintFloatPower [8]{3.1415}{3e9}=1.4317729e1491411192
```

Note that 3e9>2^31. But the number following e in the output must at any rate obey the TEX 2147483647 bound.

Inside an \xintfloatexpr-ession, \xintFloatPower is the function to which ^ is mapped. The exponent may then be something like (144/3/(1.3-.5)-37) which is, in disguise, an integer.

The intermediate multiplications are done with a higher precision than \xintDigits or the optional P argument, in order for the final result to hopefully have the desired accuracy.

15.33 \xintFloatSqrt

New with 1.08.

\xintFloatSqrt[P]{f} computes a floating point approximation of $\sqrt{f}$, either using the optional precision P or the value of \xintDigits. The computation is done for a precision of at least 17 figures (and the output is rounded if the asked-for precision was smaller).

```
\xintFloatSqrt [50]{12.3456789e12}
```

```
≈ 3.513641828644462161665823116758077037159142718124 3e6
   \xintDigits:=50;\xintFloatSqrt {\xintFloatSqrt {2}}
≈ 1.189207115002721066717499970560475915292972092463 8e0
```

15.34 \xintSum, \xintSumExpr

The original commands are extended to accept fractions on input and produce fractions on output. Their outputs will now always be in the form `A/B[n]`. The originals are available as `\xintiSum` and `\xintiSumExpr`.

15.35 \xintPrd, \xintPrdExpr

The originals are extended to accept fractions on input and produce fractions on output. Their outputs will now always be in the form `A/B[n]`. The originals are available as `\xintiPrd` and `\xintiPrdExpr`.

15.36 \xintCmp

Rewritten in `1.08a`.

The macro is extended to fractions. Of course its output is still either `-1`, `0`, or `1` with no forward slash nor trailing `[n]`. The original, which skips the overhead of the fraction format parsing, is available as `\xintiCmp`.

For choosing branches according to the result of comparing `f` and `g`, the following syntax is recommended: `\xintSgnFork{\xintCmp{f}{g}}{code for f<g}{code for f=g}{code for f>g}`.

Note that since release `1.08a` using this macro on inputs with large powers of tens does not take a quasi-infinite time, contrarily to the earlier, somewhat dumb version (the earlier version indirectly led to the creation of giant chains of zeros in certain circumstances, causing a serious efficiency impact).

15.37 \xintGeq

Rewritten in `1.08a`.

The macro is extended to fractions. The original, which skips the overhead of the fraction format parsing, is available as `\xintiGeq`. Beware that the comparison is on the *absolute values* of the fractions. Can be used as: `\xintSgnFork{\xintGeq{f}{g}}{}{code for |f|<|g|}{code for |f|⩾|g|}`

Same improvements in `1.08a` as for `\xintCmp`.

15.38 \xintMax

Rewritten in `1.08a`.

The macro is extended to fractions. But now `\xintMax {2}{3}` returns `3/1[0]`. The original is available as `\xintiMax`.

15.39 \xintMin

Rewritten in `1.08a`.

The macro is extended to fractions. The original is available as `\xintiMin`.

15.40 \xintAbs

The macro is extended to fractions. The original is available as \xintiAbs. Note that \xintAbs {-2}=2/1[0] whereas \xintiAbs {-2}=2.

15.41 \xintSgn

The macro is extended to fractions. Of course its output is still either -1, 0, or 1 with no forward slash nor trailing [n]. The original, which skips the overhead of the fraction format parsing, is available as \xintiSgn.

15.42 \xintOpp

The macro is extended to fractions. The original is available as \xintiOpp. Note that \xintOpp {3} now outputs -3/1[0].

15.43 \xintDivision, \xintQuo, \xintRem, \xintFDg, \xintLDg, \xintMON, \xintMMON, \xintOdd

These macros are extended to accept a fraction on input if this fraction in fact reduces to an integer (if not an \xintError:NotAnInteger will be raised). As usual, the 'i' variants all exist, they accept on input only integers in the strict format and have less overhead. There is no difference in the output, the difference is only in the accepted format for the inputs.

15.44 \xintNum

The macro is extended to accept a fraction on input. But this fraction should reduce to an integer. If not an error will be raised. The original is available as \xintiNum. It is imprudent to apply \xintNum to numbers with a large power of ten given either in scientific notation or with the [n] notation, as the macro will add the necessary zeros to get an explicit integer.

```
\xintNum {1e80}
```

```
100000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000
```

16 Expandable expressions with the xintexpr package

The xintexpr package was first released with version 1.07 of the xint bundle. Loading this package automatically loads xintfrac, hence also xint.

Contents

16.1 The \xintexpr expressions

An **xintexpr**ession is a construct \xintexpr⟨*expandable_expression*⟩\relax where the expandable expression is read and expanded from left to right, and whose constituents should be (they are uncovered by iterated left to right expansion of the contents during the scanning):

- integers or decimal numbers, such as 123.345, or numbers in scientific notation 6.02e23 or 6.02E23 (or anything expanding to these things; a decimal number may start directly with a decimal point),
- fractions A/B, or a.b/c.d or a.beN/c.deM, if they are to be treated as one entity should then be parenthesized, *e.g.* disambiguating A/B^2 from (A/B)^2,
- fractions A/B[n] as produced on output by the macros of the **xintfrac** package; they *must* be enclosed in one pair of braces, for example {13/35[3]} or {\x\y\z} with \x expanding to 13/, \y expanding to 35[and \z expanding to 3], (*note that using parentheses does not suffice, braces are required: the parser can not digest directly square brackets. Material within braces* must *after complete expansion give either an integer* A *or a fraction in* A/B *or* A/B[n] *form; it is only in the latter case that braces are mandatory. They should* not *be used for material expanding to a fraction in scientific notation, or something else than an integer or fraction, etc... of course braces also appear in the completely other rôle of feeding macros with their parameters.*),
- the standard binary operators, +, -, *, /, and ^ (the ** notation for exponentiation is not recognized and will give an error),
- opening and closing parentheses, with arbitrary level of nesting,
- + and - as prefix operators,
- ! as postfix factorial operator (applied to a non-negative integer),
- and sub-expressions \xintexpr⟨*stuff*⟩\relax (they do not need to be put within parentheses).

Such an expression, like a \numexpr expression, is not directly printable, nor can it be directly used as argument to the other package macros. For this one uses one of the two equivalent forms:

- \xinttheexpr⟨*expandable_expression*⟩\relax, or
- \xintthe\xintexpr⟨*expandable_expression*⟩\relax.

Both forms are equivalent and produce, always, a fraction in the standard A/B[n] format (even when the result is an integer; as usual no automatic simplification is done, and adding fractions multiplies all the denominators).

```
\xinttheexpr 1+1/2!+1/3!+1/4!+1/5!\relax=59328/34560[0]
```

One will usually post-process with \xintIrr, \xintTrunc or \xintRound, or \xintFloat, or \xintNum (when the output is known to be an integer) to get the result in the desired

form. One may imagine some future version where the output format will be given as optional argument to \xintexpr.

```
\xintIrr{\xinttheexpr 1+1/2!+1/3!+1/4!+1/5!\relax}=103/60
 \xinttheexpr 1.99^-2 - 2.01^-2 \relax=800/1599920001[4]
\xintRound{10}{\xinttheexpr 1.99^-2 - 2.01^-2 \relax}=0.0050002500
```

Again:

- xintexpressions evaluate through expansion to arbitrarily big fractions (in a non-directly printable form),
- the standard operations of addition, subtraction, multiplication, division, power, are written in infix form,
- recognized numbers on input are either integers, decimal numbers, or numbers written in scientific notation, (or anything expanding to the previous things),
- fractions on input which contain the [n] part, or macros expanding to some A/B[n] with the trailing [n] must be enclosed in (precisely one) pair of braces to be parsable by the expression scanner,[31]
- the expression may contain arbitrarily many levels of nested parenthesized sub-expressions,
- sub-contents evaluating to fractions should be either
  1. parenthesized,[32]
  2. a sub-expression \xintexpr...\relax,
  3. or braced (use of infix operators inside the braced material will have to be understood by the enclosed macros, which may be external to the package, or explicitely enclosed in a sub \xinttheexpr...\relax).
- an expression can not be given as argument to the other package macros, nor printed, for this one must use \xinttheexpr...\relax or \xintthe\xintexpr...\relax,
- the output of these latter expressions is always in the A/B[n] form, and may serve as input to the other package macros accepting fractions,
- \xinttheexpr...\relax as a sub-constituent of an \xintexpr...\relax must be within some braces, else it should be written directly as \xintexpr...\relax,
- as usual no simplification is done on the output and is the responsability of post-processing,

[31] the reason why the braced material should not be a number in scientific notation is that the 'e' will become of catcode other and not be understood then by the package macros; this is different from an 'e' directly seen by the parser, for which the catcode does not matter. Of course if the brace pair is for feeding an argument to a macro, then all of the above is irrelevant.

[32] recall that the parser does not produce explicit fractions A/B[n], hence the bracing rule does not apply to the result of the evaluation of the contents within parentheses; except of course if it was produced by some other means giving an explicit A/B[n], but then braces should have been used, not parentheses.

- very long output will need special macros to break across lines, like the \printnumber macro used in this documentation,
- everything is expanded along the way, the expression may contain macros, but of course use of +, *, ... within their arguments is only possible if these macros know how to deal with them,
- finally each xintexpression is completely expandable and obtains its result in two expansion steps.

16.2 \numexpr expressions, count and dimension registers

They can not be used directly but must be prefixed by \the or \number for the count registers and by \number for the dimension registers. The dimension is then converted to its value in scalable points sp, which are 1/65536th of a point.

One may thus compute exactly and expandably with dimensions even exceeding temporarily the TEX limits and then convert back approximately to points by division by 65536 and rounding to 4,5 or 6 decimal digits after the decimal point.

16.3 Catcodes and spaces

Spaces inside an \xinttheexpr...\relax should mostly be innocuous[33] (if the expression contains macros, then it is the macro which is responsible for grabbing its arguments, so spaces within the arguments are presumably to be avoided, as a general rule.).

\xintexpr and \xintthexpr are very agnostic regarding catcodes: digits, binary operators, minus and plus signs as prefixes, parentheses, decimal point, may be indifferently of catcode letter or other or subscript or superscript, ..., it does not matter. Of course +, -, *, /, ^ or ! should not be active as everything is expanded along the way. If one of them (especially ! which is made active by Babel for certain languages) is active, it should be prefixed with \string. In the case of the factorial, the macro \xintFac may be used rather than the postfix !, preferably within braces as this will avoid the subsequent slow scan digit by digit of its expansion (other macros from the xintfrac package generally *must* be used within a brace pair, as they expand to fractions A/B[n] with the trailing [n]; the \xintFac produces an integer with no [n] and braces are only optional, but preferable, as the scanner will get the job done faster.)

Sub-material within braces is treated technically in a different manner, and depending on the macros used therein may be more sensitive to the catcode of the five operations (the minus sign as prefix in particular). Digits, slash, square brackets, sign, produced on output by an \xinttheexpr are all of catcode 12. For the output of \xintthefloatexpr digits, decimal dot, signs are of catcode 12, and the 'e' is of catcode 11.

Note that if some macro is inserted in the expression it will expand and grab its arguments before the parser may get a chance to see them, so the situation with catcodes and spaces is not as flexible within the macro arguments.

[33] release 1.08b fixes a bug in this context.

16.4 Expandability

As is the case with all other package macros \xintexpr expands in two steps to its final (non-printable) result; and similarly for \xinttheexpr. The 'lowercase' form are a bit unusual as these macros are already in lowercase... : \xinteval for \xintexpr and \xinttheeval for \xinttheexpr.

Similarly, there are \xintfloateval and \xintthefloateval.

As explained above the expressions should contain only expandable material, except that braces are allowed when they enclose either a fraction (or decimal number) or something arbitrarily complicated but expanding (in a manner compatible to an expansion only context) to such a fraction or decimal number.

16.5 Memory considerations

The parser creates an undefined control sequence for each intermediate computation (this does not of course refer to the intermediate steps needed in the evaluations of the \xintAdd, \xintMul, etc... macros corresponding to the infix operators, but only to each conversion of such an infix operator into a computation). So, a moderately sized expression might create 10, or 20 such control sequences. On my TEX installation, the memory available for such things is of circa 200,000 multi-letter control words. So this means that a document containing hundreds, perhaps even thousands of expressions will compile with no problem. But, if the package is used for computing plots[34], this may cause a problem.

There is a solution.[35]

A document can possibly do tens of thousands of evaluations only if some formulas are being used repeatedly, for example inside loops, with counters being incremented, or with data being fetched from a file. So it is the same formula used again and again with varying numbers inside.

With the \xintNewExpr command, it is possible to convert once and for all an expression containing parameters into an expandable macro with parameters. Only this initial definition of this macro actually activates the \xintexpr parser and will (very moderately) impact the hash-table: once this unique parsing is done, a macro with parameters is produced which is built-up recursively from the \xintAdd, \xintMul, etc... macros, exactly as it was necessary to do before the availability of the xintexpr package.

16.6 The \xintNewExpr command

This allows to define a completely expandable macro with parameters, expanding in two steps to its final evaluation, and corresponding to the given xintexpression where the parameters are input using the underscore as macro-parameter: _1, ..., _9.[36]

[34] this is not very probable as so far xint does not include a mathematical library with floating point calculations, but provides only the basic operations of algebra.

[35] which convinced me that I could stick with the parser implementation despite its potential impact on the hash-table.

[36] using the character # as in standard macros would have been more complicated to implement, the question mark ? is sometimes made active for reasons of punctuation, the dollar sign was perfect but my text editor does some automatic font coloring and size change when visualizing a .tex file and encountering such a $, there was also the tab character & which could have been used. Perhaps a future release could leave the choice of the character to the user.

The command is used as:

\xintNewExpr{\myformula}[n]{⟨*stuff*⟩}

- ⟨*stuff*⟩ will be inserted inside \xinttheexpr . . . \relax,
- n is an integer between zero and nine, inclusive, and tells how many parameters will \myformula have (it is mandatory even if the macro to be defined will have no parameters),
- placeholders _1, _2, ..., _n are used inside ⟨*stuff*⟩ to play the rôle of the macro parameters.

The macro \myformula is defined without checking if it already exists, LaTeX users might prefer to do first \newcommand*\myformula {} to get a reasonable error message in case \myformula already exists.

It will be a completely expandable macro entirely built-up using \xintAdd, \xintSub, \xintMul, \xintDiv, \xintPow, \xintOpp and \xintFac and corresponding to the formula as written with the infix operators.

The formula may of course contain besides the infix operators and macro parameters some arbitrary decimal numbers, fractions (within braces) and also macros. If these macros do not involve the parameters, nothing special needs to be done, they will be expanded once during the construction of the formula. But if the parameters are to be used within the macros themselves, this has to be coded in a specific manner, which is to be explained after first examining a few simpler examples:

```
\xintNewExpr\myformA[4]{ _1 + _2 * _3^_4 }
\xintNewExpr\myformB[3]{ (_1 + 1.75)^_2 + _3*2.7 }
\xintNewExpr\myformC[3]{ _1*_1+_2*_2+_3*_3-(_1*_2+_2*_3+_3*_1) }
\xintNewExpr\myformD[2]{ (1+1.5*_1)^_2 - (1+1.5*_2)^_1 }
\xintNewExpr\myformE[2]{ -----((((((_1*10-5*_2)))))) }
\xintNewExpr\myformF[4]{ -_1^-_2*-_3-_4 }
\xintNewExpr\myformG[4]{ -_1*-_2^-_3-_4 }
\xintNewExpr\DET[9]{ _1*_5*_9+_2*_6*_7+_3*_4*_8-_1*_6*_8-_2*_4*_9-_3*_5*_7 }
```

```
  \meaning\myformA:macro:#1#2#3#4->\romannumeral0\xintraw{\xintAdd{#1}{
\xintMul{#2}{\xintPow{#3}{#4}}}}
  \meaning\myformB:macro:#1#2#3->\romannumeral0\xintraw{\xintAdd{\xintP
ow{\xintAdd{#1}{1.75}}{#2}}{\xintMul{#3}{2.7}}}
  \meaning\myformC:macro:#1#2#3->\romannumeral0\xintraw{\xintSub{\xintA
dd{\xintAdd{\xintMul{#1}{#1}}{\xintMul{#2}{#2}}}{\xintMul{#3}{#3}}}{\xi
ntAdd{\xintAdd{\xintMul{#1}{#2}}{\xintMul{#2}{#3}}}{\xintMul{#3}{#1}}}}
  \meaning\myformD:macro:#1#2->\romannumeral0\xintraw{\xintSub{\xintPow
{\xintAdd{1}{\xintMul{1.5}{#1}}}{#2}}{\xintPow{\xintAdd{1}{\xintMul{1.5
}{#2}}}{#1}}}
  \meaning\myformE:macro:#1#2->\romannumeral0\xintraw{\xintOpp{\xintOpp
{\xintOpp{\xintOpp{\xintOpp{\xintSub{\xintMul{#1}{10}}{\xintMul{5}{#2}}
}}}}}}
  \meaning\myformF:macro:#1#2#3#4->\romannumeral0\xintraw{\xintSub{\xin
tOpp{\xintMul{\xintPow{#1}{\xintOpp{#2}}}{\xintOpp{#3}}}}{#4}}
  \meaning\myformG:macro:#1#2#3#4->\romannumeral0\xintraw{\xintSub{\xin
tOpp{\xintMul{#1}{\xintOpp{\xintPow{#2}{\xintOpp{#3}}}}}}{#4}}
```

```
  \meaning\DET:macro:#1#2#3#4#5#6#7#8#9->\romannumeral0\xintraw{\xintSu
b{\xintSub{\xintSub{\xintAdd{\xintAdd{\xintMul{\xintMul{#1}{#5}}{#9}}{\
xintMul{\xintMul{#2}{#6}}{#7}}}{\xintMul{\xintMul{#3}{#4}}{#8}}}{\xintM
ul{\xintMul{#1}{#6}}{#8}}}{\xintMul{\xintMul{#2}{#4}}{#9}}}{\xintMul{\x
intMul{#3}{#5}}{#7}}}
            \xintNum{\DET {1}{1}{1}{10}{-10}{5}{11}{-9}{6}}=0
           \xintNum{\DET {1}{2}{3}{10}{0}{-10}{21}{2}{-17}}=0
```

Remark: \meaning has been used within the argument to a \printnumber command, to avoid going into the right margin, but this zaps all spaces originally in the output from \meaning. Here is as an illustration the raw output of \meaning on the last example:

```
  macro:#1#2#3#4#5#6#7#8#9->\romannumeral 0\xintraw {\xintSub {\xintSub {\xintSub
{\xintAdd {\xintAdd {\xintMul {\xintMul {#1}{#5}}{#9}}{\xintMul {\xintMul
{#2}{#6}}{#7}}}{\xintMul {\xintMul {#3}{#4}}{#8}}}{\xintMul {\xintMul {#1}{#6}}{#8}}}{\xin
Mul {\xintMul {#2}{#4}}{#9}}}{\xintMul {\xintMul {#3}{#5}}{#7}}}
```

This is why \printnumber was used, to have breaks across lines.

For macros to be inserted within such a created **xint**-formula command, there are two cases:

1. the macro does not involve the numbered parameters in its arguments: it may then be left as is, and will be evaluated once during the construction of the formula,
2. it does involve some of the parameters withing its arguments: then the whole thing (macro + argument) should be braced (this is not necessary if it is already included into a braced group) and the macro should be coded with : replacing \.

Here are some examples; they are rather silly but this is to illustrate the general principles.

```
\xintNewExpr\myformH[2]{ {:xintMax{_1}{_2}} }
\xintNewExpr\myformI[2]{ {:xintRound{_1}{_2}} - {:xintTrunc{_1}{_2}} }
\xintNewExpr\myformJ[3]{ {:xintSgnFork{:xintSgn{_1}}
                          {\xinttheexpr _2 + _3\relax }
                          {\xinttheexpr _2 - _3\relax }
                          {\xinttheexpr _2 * _3\relax }} }
\meaning\myformH:macro:#1#2->\romannumeral0\xintraw{\xintMax{#1}{#2}}
\meaning\myformI:macro:#1#2->\romannumeral0\xintraw{\xintSub{\xintRound
{#1}{#2}}{\xintTrunc{#1}{#2}}}
\meaning\myformJ:macro:#1#2#3->\romannumeral0\xintraw{\xintSgnFork{\xin
tSgn{#1}}{\romannumeral0\xintraw{\xintAdd{#2}{#3}}}{\romannumeral0\xint
raw{\xintSub{#2}{#3}}}{\romannumeral0\xintraw{\xintMul{#2}{#3}}}}
```

One more example:

```
\xintNewExpr\myfunction[1]
   { {:xintSgnFork {:xintSgnFork {:xintGeq{_1}{1}} {}{0}{:xintSgn{_1}}}
     {\xinttheexpr -_1 - 1  \relax }
     {\xinttheexpr 1 - _1^2 \relax }
     {\xinttheexpr _1 - 1   \relax }} }
```

The principles were explained earlier:

1. parameters are denoted _1, _2, ... , _9,

2. anything which can not be immediately expanded, because the parameters appear within, must be enclosed, together with its arguments, in a brace pair (no need to add one if it already exists),

3. and the macros must be written with a `:` as control character, rather than a `\`. This rule applies only to the macros involved in the previous item.

4. Finally, if the infix operators `+`, `-`, `*`, `/`, `^` are to be used inside macro arguments, this should be done within an `\xinttheexpr...\relax`; but this rule applies in general also independently of the `\xintNewExpr` context.

The produced macro `\myfunction` turns out to have meaning in this last case:

```
macro:#1->\romannumeral0\xintraw{\xintSgnFork{\xintSgnFork{\xintGe
q{#1}{1}}{}{0}{\xintSgn{#1}}}{\romannumeral0\xintraw{\xintSub{\xint0
pp{#1}}{1}}}{\romannumeral0\xintraw{\xintSub{1}{\xintPow{#1}{2}}}}{\
romannumeral0\xintraw{\xintSub{#1}{1}}}}
```

The reason why these created macros are made to start with `\romannumeral0\xintraw` is in order for them to expand in only two steps. Of course in the last example their occurences in the three sub-branches is redundant, but we had to use `\xinttheexpr` in each of the three sub-branch, else the formal parsing done by `\xintNewExpr` would not have had a chance to discover the binary infix operators and convert them to their macro form.

Things like a closing parenthesis only arising from the expansion of a macro when the parser goes from left to right will be hard to make understandable to `\xintNewExpr`, if the macro is to contain some of the parameters within its arguments.

```
\def\formula #1#2#3{\xinttheexpr #2\xintSgnFork{\xintSgn{#1}}+-*#3\relax }
```

is a perfectly valid macro definition, which will work to produce `#2+#3`, `#2-#3`, or `#2*#3` depending on the sign of `#1`. But if we tried the following:

```
\xintNewExpr\formula[3]{_2{:xintSgnFork{:xintSgn{_1}}+-*}_3}
```

we would discover that it would not compile, despite seemingly following the enunciated rules. I recall:

5. braced material, if not an argument to a macro, should correspond to the evaluation of a fraction, and in particular it can not be used to produce an infix operator or an opening or closing parenthesis, etc...

This rule was mentioned in the description of **xintexpr**-ession, and it has to be obeyed in the syntax of the expression argument to `\xintNewExpr`. We could try then:

```
\xintNewExpr\formula[3]{{_2:xintSgnFork{:xintSgn{_1}}+-*_3}}
```

This time, `\xintNewExpr` works but the produced `\formula` has meaning

```
macro:#1#2#3->\romannumeral0\xintraw{#2\xintSgnFork{\xintSgn{#1}}+-*
#3}
```

Clearly this macro will not work.

We may try

```
\xintNewExpr\formula[3]{{:xinttheexpr
                          _2:xintSgnFork{:xintSgn{_1}}+-*_3:relax}}
```

but this gives

`macro:#1#2#3->\romannumeral0\xintraw{\xinttheexpr#2\xintSgnFork{\xintSgn{#1}}+-*#3\relax}` and there was no point whatsoever in it all, as what we want is to avoid the use of `\xintexpr`... so we end up having to do:

```
\xintNewExpr\formula[3]{{:xintSgnFork{:xintSgn{_1}}
                         {\xinttheexpr _2+_3\relax}
                         {\xinttheexpr _2-_3\relax}
                         {\xinttheexpr _2*_3\relax}}}
```

which is like what was done with `\myformJ`.

All of the previous examples may not be very convincing, because it is easier for the user to define directly a macro with parameters not using `\xinttheexpr` and achieving the wished-for computation, but `\xintNewExpr` would prove very useful on more complicated cases with a high level of nesting of macros.

16.7 \xintfloatexpr, \xintthefloatexpr

`\xintfloatexpr...\relax` is exactly like `\xintexpr...\relax` but with the four binary operations and the power function mapped to `\xintFloatAdd`, `\xintFloatSub`, `\xintFloatMul`, `\xintFloatDiv` and `\xintFloatPower`. The precision is from the current setting of `\xintDigits` (it can not be given as an optional parameter).

Currently, the factorial function hasn't yet a float version; so inside `\xintthefloatexpr ... \relax`, `n!` will be computed exactly. Perhaps this will be improved in a future release.

Note that `1.000000001` and `(1+1e-9)` will not be equivalent for `D=\xinttheDigits` set to nine or less. Indeed the addition implicit in `1+1e-9` (and executed when the closing parenthesis is found) will provoke the rounding to 1. Whereas `1.000000001`, when found as operand of one of the four elementary operations is kept with `D+2` digits, and even more for the power function.

```
        \xintDigits:= 9; \xintthefloatexpr (1+1e-9)-1\relax=0.e0
 \xintDigits:= 9; \xintthefloatexpr 1.000000001-1\relax=1.00000000e-9
  For the fun of it: \xintDigits:=20;
    \xintthefloatexpr (1+1e-7)^1e7\relax=2.7182816925449662712e0
 \xintDigits:=36;
   \xintthefloatexpr ((1/13+1/121)*(1/179-1/173))/(1/19-1/18)\relax
             5.64487459334466559166166079096852897e-3
\xintFloat{\xinttheexpr ((1/13+1/121)*(1/179-1/173))/(1/19-1/18)\relax}
             5.64487459334466559166166079096852912e-3
```

The latter result is the rounding of the exact result. The previous one has rounding errors coming from the various roundings done for each sub-expression. It was a bit funny to discover that `maple`, configured with `Digits:=36;` and with decimal dots everywhere to let it input the numbers as floats, gives exactly the same result with the same rounding errors as does `\xintthefloatexpr`!

Note that using `\xintthefloatexpr` only pays off compared to using `\xinttheexpr` and then `\xintFloat` if the computations turn out to involve hundreds of digits. For elementary calculations with hand written numbers (not using the scientific notation with exponents differing greatly) it will generally be more efficient to use `\xinttheexpr`. The situation is quickly otherwise if one starts using the Power function. Then, `\xintthefloat`

is often useful; and sometimes indispensable to achieve the (approximate) computation in reasonable time.

We can try some crazy things:[37]

```
\xintDigits:=12;\xintthefloatexpr 1.0000000000000001^1e15\relax
                                  2.71828182846e0
```

Note that contrarily to some professional computing sofware which are our concurrents on this market, the `1.000000000000001` wasn't rounded to `1` despite the setting of `\xintDigits`; it would have been if we had input it as `(1+1e-15)`.

16.8 \xintNewFloatExpr

This is exactly like `\xintNewExpr` except that the created formulas are set-up to use `\xintthefloatexpr`. The precision used for numbers fetched as parameters will be the one locally given by `\xintDigits` at the time of use of the created formulas, not `\xintNewFloatExpr`. However, the numbers hard-wired in the original expression will have been evaluated with the then current setting for `\xintDigits`.

16.9 Technicalities and experimental status

As already mentioned `\xintNewExpr\myformula[n]` does not check the prior existence of a macro `\myformula`. And the number of parameters `n` given as mandatory argument withing square brackets should of course be at least equal to the actual maximal index following an underscore in the expression.

Obviously I should mention that `\xintNewExpr` itself can not be used in an expansion-only context, as it creates a macro.

The format of the output of `\xintexpr`⟨*stuff*⟩`\relax` is a `!` (with catcode 11) followed by `\XINT_expr_illegaluse` which prints an error message in the document and in the log file if it is executed, and next a token `\.A/B[n]` (which is a single control sequence: these are the famous things which may impact the hash-table). Using `\xinttheexpr` means zapping the first two things, and opening up the third token to access its name and get the result `A/B[n]` of the evaluation of the expression.

I decided to put all intermediate results (from each evaluation of an infix operators, or of a parenthesized subpart of the expression, or from application of the minus as prefix, or of the exclamation sign as postfix, or any encountered braced material) inside `\csname...\endcsname`, as this can be done expandably and encapsulates an arbitrarily long fraction in a single token (left with undefined meaning), thus providing tremendous relief to the programmer in his/her expansion control.

> This implementation and user interface are currently to be considered *experimental*, they have not been yet extensively tested. Indeed the additions brought to the **xint** bundle with release `1.07` are rather extant and I just haven't had time to thoroughly validate them all.

[37] this evaluation takes a about a fifth of a second already on my laptop. Recall the constraints of expandability.

Some 'error messages' will be issued by the scanner in case of problems, but errors may also be issued from low-level TEX processing, and are most of the time unrecoverable. An attempt has been made to handle gracefully missing or extraneous parentheses.

16.10 Acknowledgements

I was greatly helped in my preparatory thinking, prior to producing such an expandable parser, by the commented source of the l3fp package, specifically the `l3fp-parse.dtx` file. Also the source of the `calc` package was instructive, despite the fact that here for `\xintexpr` the principles are necessarily different due to the aim of achieving expandability.

I apologize for not including comments currently in my own code, the reason being that this a time-consuming task which should wait until the code has a rather certain more-or-less final form.

17 Commands of the xintbinhex package

This package was first included in the `1.08` release of **xint**. It provides expandable conversions of arbitrarily long numbers to and from binary and hexadecimal.

The argument is first fully expanded. It then may start with an optional minus sign (unique, of category code other), followed with optional leading zeros (arbitrarily many, category code other) and then "digits" (hexadecimal letters may be of category code letter or other, and must be uppercased). The optional (unique) minus sign (plus sign is not allowed) is kept in the output. Leading zeros are allowed, and stripped. The hexadecimal letters on output are of category code letter, and uppercased.

Contents

17.1 \xintDecToHex

Converts from decimal to hexadecimal.

```
\xintDecToHex{2718281828459045235360287471352662497757247093699959574
966967627724076630353547594571382178525166427427466391932003}
->11A9397C66949A97051F7D0A817914E3E0B17C41B11C48BAEF2B5760BB38D272F4
6DCE46C6032936BF37DAC918814C63
```

17.2 \xintDecToBin

Converts from decimal to binary.

```
\xintDecToBin{2718281828459045235360287471352662497757247093699959574
966967627724076630353547594571382178525166427427466391932003}
```

```
->1000110101001001110010111110001100110100101001001101010010111000001010001111101111101000010101000000101111001000101001110001111100000101100010111110001000001101100010001110001001000101110101110111100101011101110111100001011101100111000110100100111001011110100011011001110001000110001100000001100101001001101101011111100110111110110101100100100011000100000010100110001100011
```

17.3 \xintHexToDec

Converts from hexadecimal to decimal.

```
  \xintHexToDec{11A9397C66949A97051F7D0A817914E3E0B17C41B11C48BAEF2B5760BB38D272F46DCE46C6032936BF37DAC918814C63}
->27182818284590452353602874713526624977572470936999595749669676277240766303535475945713821785251664274274663919320003
```

17.4 \xintBinToDec

Converts from binary to decimal.

```
  \xintBinToDec{1000110101001001110010111110001100110100101001001101010010111000001010001111101111101000010101000000101111001000101001110001111100000101100010111110001000001101100010001110001001000101110101110111100101011101110111100001011101100111000110100100111001011110100011011001110001000110001100000001100101001001101101011111100110111110110101100100100011000100000010100110001100011}
->27182818284590452353602874713526624977572470936999595749669676277240766303535475945713821785251664274274663919320003
```

17.5 \xintBinToHex

Converts from binary to hexadecimal.

```
  \xintBinToHex{1000110101001001110010111110001100110100101001001101010010111000001010001111101111101000010101000000101111001000101001110001111100000101100010111110001000001101100010001110001001000101110101110111100101011101110111100001011101100111000110100100111001011110100011011001110001000110001100000001100101001001101101011111100110111110110101100100100011000100000010100110001100011}
->11A9397C66949A97051F7D0A817914E3E0B17C41B11C48BAEF2B5760BB38D272F46DCE46C6032936BF37DAC918814C63
```

17.6 \xintHexToBin

Converts from hexadecimal to binary.

```
  \xintHexToBin{11A9397C66949A97051F7D0A817914E3E0B17C41B11C48BAEF2B5760BB38D272F46DCE46C6032936BF37DAC918814C63}
->1000110101001001110010111110001100110100101001001101010010111000001010001111101111101000010101000000101111001000101001110001111100000101100010111110001000001101100010001110001001000101110101110111100101
```

```
01101010111011000001011101100111000110100100111001011110100011011011
10011100100011011000110000000110010100100110110101111110011011111011
01011001001000110001000000101001100011001100011
```

17.7 \xintCHexToBin

Also converts from hexadecimal to binary. Faster on inputs with at least one hundred hexadecimal digits.

```
  \xintCHexToBin{11A9397C66949A97051F7D0A817914E3E0B17C41B11C48BAEF2B57
60BB38D272F46DCE46C6032936BF37DAC918814C63}
->10001101010010011100101111100011001101001010010011010100101110000
01010001111101111101000010101000000101111001000101001110001111100000 1
01100010111110001000001101100010001110001001000101110101110111100101
01101010111011000001011101100111000110100100111001011110100011011011
10011100100011011000110000000110010100100110110101111110011011111011
01011001001000110001000000101001100011001100011
```

18 Commands of the xintgcd package

This package was included in the original release 1.0 of the xint bundle. The numbers on input have only one optional minus sign and no leading zeros, as is the rule with the macros of package xint. In case of need, macro \xintNum can be used to normalize the inputs.

Contents

18.1 \xintGCD

\xintGCD{N}{M} computes the greatest common divisor. It is positive, except when both N and M vanish, in which case the macro returns zero.

```
\xintGCD{10000}{1113}=1
\xintGCD{123456789012345}{9876543210321}=3
```

18.2 \xintBezout

\xintBezout{N}{M} returns five numbers A, B, U, V, D within braces. A is the first (expanded, as usual) input number, B the second, D is the GCD, and UA - VB = D.

```
\xintAssign {{\xintBezout {10000}{1113}}}\to\X
\meaning\X: macro:->{10000}{1113}{-131}{-1177}{1}.
\xintAssign {\xintBezout {10000}{1113}}\to\A\B\U\V\D
\A: 10000, \B: 1113, \U: -131, \V: -1177, \D: 1.
\xintAssign {\xintBezout {123456789012345}{9876543210321}}\to\A\B\U\V\D
```

\A: 123456789012345, \B: 9876543210321, \U: 256654313730, \V: 3208178892607, \D: 3.

18.3 \xintEuclideAlgorithm

\xintEuclideAlgorithm{N}{M} applies the Euclide algorithm and keeps a copy of all quotients and remainders.

```
    \xintAssign {{\xintEuclideAlgorithm {10000}{1113}}}\to\X
  \meaning\X: macro:->{5}{10000}{1}{1113}{8}{1096}{1}{17}{64}{8}{2}
{1}{8}{0}.
```

The first token is the number of steps, the second is N, the third is the GCD, the fourth is M then the first quotient and remainder, the second quotient and remainder, ... until the final quotient and last (zero) remainder.

18.4 \xintBezoutAlgorithm

\xintBezoutAlgorithm{N}{M} applies the Euclide algorithm and keeps a copy of all quotients and remainders. Furthermore it computes the entries of the successive products of the 2 by 2 matrices $\begin{pmatrix} q & 1 \\ 1 & 0 \end{pmatrix}$ formed from the quotients arising in the algorithm.

```
    \xintAssign {{\xintEuclideAlgorithm {10000}{1113}}}\to\X
  \meaning\X: macro:->{5}{10000}{0}{1}{1}{1113}{1}{0}{8}{1096}{8}{1}
{1}{17}{9}{1}{64}{8}{584}{65}{2}{1}{1177}{131}{8}{0}{10000}{1113}.
```

The first token is the number of steps, the second is N, then 0, 1, the GCD, M, 1, 0, the first quotient, the first remainder, the top left entry of the first matrix, the bottom left entry, and then these four things at each step until the end.

18.5 \xintTypesetEuclideAlgorithm

This macro is just an example of how to organize the data returned by \xintEuclideAlgorithm. Copy the source code to a new macro and modify it to what is needed.

```
    \xintTypesetEuclideAlgorithm {123456789012345}{9876543210321}
```

$$
\begin{aligned}
123456789012345 &= 12 \times 9876543210321 + 4938270488493\\
9876543210321 &= 2 \times 4938270488493 + 2233335\\
4938270488493 &= 2211164 \times 2233335 + 536553\\
2233335 &= 4 \times 536553 + 87123\\
536553 &= 6 \times 87123 + 13815\\
87123 &= 6 \times 13815 + 4233\\
13815 &= 3 \times 4233 + 1116\\
4233 &= 3 \times 1116 + 885\\
1116 &= 1 \times 885 + 231\\
885 &= 3 \times 231 + 192\\
231 &= 1 \times 192 + 39\\
192 &= 4 \times 39 + 36\\
39 &= 1 \times 36 + 3\\
36 &= 12 \times 3 + 0
\end{aligned}
$$

18.6 \xintTypesetBezoutAlgorithm

This macro is just an example of how to organize the data returned by \xintBezoutAlgorithm. Copy the source code to a new macro and modify it to what is needed.

```
\xintTypesetBezoutAlgorithm {10000}{1113}
```

$$
\begin{aligned}
10000 &= 8\times 1113 + 1096\\
8 &= 8\times 1 + 0\\
1 &= 8\times 0 + 1\\
1113 &= 1\times 1096 + 17\\
9 &= 1\times 8 + 1\\
1 &= 1\times 1 + 0\\
1096 &= 64\times 17 + 8\\
584 &= 64\times 9 + 8\\
65 &= 64\times 1 + 1\\
17 &= 2\times 8 + 1\\
1177 &= 2\times 584 + 9\\
131 &= 2\times 65 + 1\\
8 &= 8\times 1 + 0\\
10000 &= 8\times 1177 + 584\\
1113 &= 8\times 131 + 65\\
131\times 10000 &- 1177\times 1113 = -1
\end{aligned}
$$

19 Commands of the xintseries package

Some arguments to the package commands are macros which are expanded only later, when given their parameters. The arguments serving as indices are systematically given to a \numexpr expressions (new with 1.06!) , hence fully expanded, they may be count registers, etc...

This package was first released with version 1.03 of the xint bundle.

Contents

19.1 \xintSeries

\xintSeries{A}{B}{\coeff} computes $\sum_{n=A}^{n=B}$ \coeff{n}. The initial and final indices must obey the \numexpr constraint of expanding to numbers at most 2^31-1. The \coeff macro must be a one-parameter fully expandable command, taking on input an explicit number n and producing some fraction \coeff{n}; it is expanded at the time it is needed.

```
\def\coeff #1{\xintiMON{#1}/#1.5} % (-1)^n/(n+1/2)
\edef\w {\xintSeries {0}{50}{\coeff}} % we want to re-use it
```

```
\edef\z {\xintJrr {\w}[0]} % the [0] for a microsecond gain.
% \xintJrr preferred to \xintIrr: a big common factor is suspected.
% But numbers much bigger would be needed to show the greater efficiency.
\[ \sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} = \xintFrac\z \]
```

$$\sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac{1}{2}} = \frac{1739093382873709404321127921016266022787 14}{1100274671593900030252799172260397290505 75}$$

For info, before action by `\xintJrr` the inner representation of the result has a denominator of `\xintLen {\xintDenominator\w}`=117 digits. This troubled me as `101!!` has only 81 digits: `\xintLen {\xintQuo {\xintFac {101}}{\xintiMul {\xintiPow {2}{50}}{\xintFac{50}}}}`=81. The explanation lies in the too clever to be efficient `#1.5` trick. It leads to a silly extra `5^{51}` (which has 36 digits) in the denominator. See the explanations in the next section.

Note: as soon as the coefficients look like factorials, it is more efficient to use the `\xintRationalSeries` macro whose evaluation will avoid a denominator build-up; indeed the raw operations of addition and subtraction of fractions blindly multiply out denominators. So the raw evaluation of $\sum_{n=0}^{N} 1/n!$ with `\xintSeries` will have a denominator equal to $\prod_{n=0}^{N} n!$. Needless to say this makes it more difficult to compute the exact value of this sum with `N=50`, for example, whereas with `\xintRationalSeries` the denominator does not get bigger than 50!.

For info: by the way $\prod_{n=0}^{50} n!$ is easily computed by **xint** and is a number with 1394 digits. And $\prod_{n=0}^{100} n!$ is also computable by **xint** (24 seconds on my laptop for the brute force iterated multiplication of all factorials, a specialized routine would do it faster) and has 6941 digits (this means more than two pages if printed...). Whereas 100! only has 158 digits.

```
\def\coeffleibnitz #1{\the\numexpr\ifodd #1 1\else-1\fi\relax/#1[0]}
\cnta 1
\loop  % in this loop we recompute from scratch each partial sum!
% we can afford that, as \xintSeries is fast enough.
\noindent\hbox to 2em{\hfil\texttt{\the\cnta.} }%
         \xintTrunc {12}
                    {\xintSeries {1}{\cnta}{\coeffleibnitz}}\dots
\endgraf
\ifnum\cnta < 30 \advance\cnta 1 \repeat
```

1. 1.000000000000...
2. 0.500000000000...
3. 0.833333333333...
4. 0.583333333333...
5. 0.783333333333...
6. 0.616666666666...
7. 0.759523809523...
8. 0.634523809523...
9. 0.745634920634...
10. 0.645634920634...
11. 0.736544011544...
12. 0.653210678210...
13. 0.730133755133...
14. 0.658705183705...
15. 0.725371850371...
16. 0.662871850371...
17. 0.721695379783...
18. 0.666139824228...
19. 0.718771403175...
20. 0.668771403175...
21. 0.716390450794...
22. 0.670935905339...
23. 0.714414166209...
24. 0.672747499542...
25. 0.712747499542...
26. 0.674285961081...
27. 0.711322998118...
28. 0.675608712404...
29. 0.710091471024...
30. 0.676758137691...

19.2 \xintiSeries

`\xintiSeries{A}{B}{\coeff}` computes $\sum_{n=A}^{n=B}$ `\coeff{n}` where now `\coeff{n}` *must* expand to a (possibly long) integer, as is acceptable on input by the integer-only `\xintiAdd`.

```
\def\coeff #1{\xintiTrunc {40}{\xintMON{#1}/#1.5}}%
% better:
\def\coeff #1{\xintiTrunc {40}
   {\the\numexpr 2*\xintiMON{#1}\relax/\the\numexpr 2*#1+1\relax [0]}}%
% better still:
\def\coeff #1{\xintiTrunc {40}
 {\the\numexpr\ifodd #1 -2\else2\fi\relax/\the\numexpr 2*#1+1\relax [0]}}%
% (-1)^n/(n+1/2) times 10^40, truncated to an integer.
\[ \sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} \approx
        \xintTrunc {40}{\xintiSeries {0}{50}{\coeff}[-40]}\dots\]
```

The `#1.5` trick to define the `\coeff` macro was neat, but `1/3.5`, for example, turns internally into `10/35` whereas it would be more efficient to have `2/7`. The second way of coding the wanted coefficient avoids a superfluous factor of five and leads to a faster evaluation. The third way is faster, after all there is no need to use `\xintMON` (or rather `\xintiMON` which has less parsing overhead) on integers obeying the TEX bound. The denominator having no sign, we have added the `[0]` as this speeds up (infinitesimally) the parsing.

$$\sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} \approx 1.58059930649352504123678950695672641448 10$$

We should have cut out at least the last two digits: truncating errors originating with the first coefficients of the sum will never go away, and each truncation introduces an uncertainty in the last digit, so as we have 40 terms, we should trash the last two digits, or at least round at 38 digits. It is interesting to compare with the computation where rounding rather than truncation is used, and with the decimal expansion of the exactly computed partial sum of the series:

```
\def\coeff #1{\xintiRound {40} % rounding at 40
  {\the\numexpr\ifodd #1 -2\else2\fi\relax/\the\numexpr 2*#1+1\relax [0]}}%
% (-1)^n/(n+1/2) times 10^40, rounded to an integer.
\[ \sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} \approx
        \xintTrunc {40}{\xintiSeries {0}{50}{\coeff}[-40]}\]
\def\exactcoeff #1%
  {\the\numexpr\ifodd #1 -2\else2\fi\relax/\the\numexpr 2*#1+1\relax [0]}%
\[ \sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12}
   = \xintTrunc {50}{\xintSeries {0}{50}{\exactcoeff}}\dots\]
```

$$\sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} \approx 1.58059930649352504123678950695672641448 04$$

$$\sum_{n=0}^{n=50} \frac{(-1)^n}{n+\frac12} = 1.58059930649352504123678950695672641448068680288367\dots$$

This shows indeed that our sum of truncated terms estimated wrongly the 39th and 40th digits of the exact result[38] and that the sum of rounded terms fared a bit better.

[38] as the series is alternating, we can roughly expect an error of $\sqrt{40}$ and the last two digits are off by 4 units, which is not contradictory to our expectations.

19.3 \xintRationalSeries

New with release 1.04.

`\xintRationalSeries{A}{B}{f}{\ratio}` evaluates $\sum_{n=A}^{n=B} F(n)$, where `F(n)` is specified indirectly via the data of `f=F(A)` and the one-parameter macro `\ratio` which must be such that `\macro{n}` expands to `F(n)/F(n-1)`. The name indicates that `\xintRationalSeries` was designed to be useful in the cases where `F(n)/F(n-1)` is a rational function of `n` but it may be anything expanding to a fraction. The macro `\ratio` must be an expandable-only compatible command and expand to its value after iterated full expansion of its first token. `A` and `B` are fed to a `\numexpr` hence may be count registers or arithmetic expressions built with such; they must obey the TEX bound. The initial term `f` may be a macro `\f`, it will be expanded to its value representing `F(A)`.

```
\def\ratio #1{2/#1[0]}% 2/n, to compute exp(2)
\cnta 0 % previously declared count
\loop \edef\z {\xintRationalSeries {0}{\cnta}{1}{\ratio }}%
\noindent$\sum_{n=0}^{\the\cnta} \frac{2^n}{n!}=
          \xintTrunc{12}\z\dots=
          \xintFrac\z=\xintFrac{\xintIrr\z}$\vtop to 5pt{}\endgraf
\ifnum\cnta<20 \advance\cnta 1 \repeat
```

$\sum_{n=0}^{0} \frac{2^n}{n!} = 1.000000000000\cdots = 1 = 1$
$\sum_{n=0}^{1} \frac{2^n}{n!} = 3.000000000000\cdots = 3 = 3$
$\sum_{n=0}^{2} \frac{2^n}{n!} = 5.000000000000\cdots = \frac{10}{2} = 5$
$\sum_{n=0}^{3} \frac{2^n}{n!} = 6.333333333333\cdots = \frac{38}{6} = \frac{19}{3}$
$\sum_{n=0}^{4} \frac{2^n}{n!} = 7.000000000000\cdots = \frac{168}{24} = 7$
$\sum_{n=0}^{5} \frac{2^n}{n!} = 7.266666666666\cdots = \frac{872}{120} = \frac{109}{15}$
$\sum_{n=0}^{6} \frac{2^n}{n!} = 7.355555555555\cdots = \frac{5296}{720} = \frac{331}{45}$
$\sum_{n=0}^{7} \frac{2^n}{n!} = 7.380952380952\cdots = \frac{37200}{5040} = \frac{155}{21}$
$\sum_{n=0}^{8} \frac{2^n}{n!} = 7.387301587301\cdots = \frac{297856}{40320} = \frac{2327}{315}$
$\sum_{n=0}^{9} \frac{2^n}{n!} = 7.388712522045\cdots = \frac{2681216}{362880} = \frac{20947}{2835}$
$\sum_{n=0}^{10} \frac{2^n}{n!} = 7.388994708994\cdots = \frac{26813184}{3628800} = \frac{34913}{4725}$
$\sum_{n=0}^{11} \frac{2^n}{n!} = 7.389046015712\cdots = \frac{294947072}{39916800} = \frac{164591}{22275}$
$\sum_{n=0}^{12} \frac{2^n}{n!} = 7.389054566832\cdots = \frac{3539368960}{479001600} = \frac{691283}{93555}$
$\sum_{n=0}^{13} \frac{2^n}{n!} = 7.389055882389\cdots = \frac{46011804672}{6227020800} = \frac{14977801}{2027025}$
$\sum_{n=0}^{14} \frac{2^n}{n!} = 7.389056070325\cdots = \frac{644165281792}{87178291200} = \frac{314533829}{42567525}$
$\sum_{n=0}^{15} \frac{2^n}{n!} = 7.389056095384\cdots = \frac{9662479259648}{1307674368000} = \frac{4718007451}{638512875}$
$\sum_{n=0}^{16} \frac{2^n}{n!} = 7.389056098516\cdots = \frac{154599668219904}{20922789888000} = \frac{1572669151}{212837625}$
$\sum_{n=0}^{17} \frac{2^n}{n!} = 7.389056098884\cdots = \frac{2628194359869440}{355687428096000} = \frac{16041225341}{2170943775}$
$\sum_{n=0}^{18} \frac{2^n}{n!} = 7.389056098925\cdots = \frac{47307498477912064}{6402373705728000} = \frac{103122162907}{13956067125}$
$\sum_{n=0}^{19} \frac{2^n}{n!} = 7.389056098930\cdots = \frac{898842471080853504}{121645100408832000} = \frac{4571749222213}{618718975875}$
$\sum_{n=0}^{20} \frac{2^n}{n!} = 7.389056098930\cdots = \frac{17976849421618118656}{2432902008176640000} = \frac{68576238333199}{9280784638125}$

Such computations would become quickly completely inaccessible via the `\xintSeries` macros, as the factorials in the denominators would get all multiplied together: the raw addition and subtraction on fractions just blindly multiplies denominators! Whereas `\xintRationalSeries` evaluate the partial sums via a less silly iterative scheme.

```
\def\ratio #1{-1/#1[0]}% -1/n, comes from the series of exp(-1)
\cnta 0 % previously declared count
\loop
\edef\z {\xintRationalSeries {0}{\cnta}{1}{\ratio }}%
\noindent$\sum_{n=0}^{\the\cnta} \frac{(-1)^n}{n!}=
          \xintTrunc{20}\z\dots=\xintFrac{\z}=\xintFrac{\xintIrr\z}$
        \vtop to 5pt{}\endgraf
\ifnum\cnta<20 \advance\cnta 1 \repeat
```

$\sum_{n=0}^{0} \frac{(-1)^n}{n!} = 1.00000000000000000000\cdots = 1 = 1$
$\sum_{n=0}^{1} \frac{(-1)^n}{n!} = 0\cdots = 0 = 0$
$\sum_{n=0}^{2} \frac{(-1)^n}{n!} = 0.50000000000000000000\cdots = \frac{1}{2} = \frac{1}{2}$
$\sum_{n=0}^{3} \frac{(-1)^n}{n!} = 0.33333333333333333333\cdots = \frac{2}{6} = \frac{1}{3}$
$\sum_{n=0}^{4} \frac{(-1)^n}{n!} = 0.37500000000000000000\cdots = \frac{9}{24} = \frac{3}{8}$
$\sum_{n=0}^{5} \frac{(-1)^n}{n!} = 0.36666666666666666666\cdots = \frac{44}{120} = \frac{11}{30}$
$\sum_{n=0}^{6} \frac{(-1)^n}{n!} = 0.36805555555555555555\cdots = \frac{265}{720} = \frac{53}{144}$
$\sum_{n=0}^{7} \frac{(-1)^n}{n!} = 0.36785714285714285714\cdots = \frac{1854}{5040} = \frac{103}{280}$
$\sum_{n=0}^{8} \frac{(-1)^n}{n!} = 0.36788194444444444444\cdots = \frac{14833}{40320} = \frac{2119}{5760}$
$\sum_{n=0}^{9} \frac{(-1)^n}{n!} = 0.36787918871252204585\cdots = \frac{133496}{362880} = \frac{16687}{45360}$
$\sum_{n=0}^{10} \frac{(-1)^n}{n!} = 0.36787946428571428571\cdots = \frac{1334961}{3628800} = \frac{16481}{44800}$
$\sum_{n=0}^{11} \frac{(-1)^n}{n!} = 0.36787943923360590027\cdots = \frac{14684570}{39916800} = \frac{1468457}{3991680}$
$\sum_{n=0}^{12} \frac{(-1)^n}{n!} = 0.36787944132128159905\cdots = \frac{176214841}{479001600} = \frac{16019531}{43545600}$
$\sum_{n=0}^{13} \frac{(-1)^n}{n!} = 0.36787944116069116069\cdots = \frac{2290792932}{6227020800} = \frac{63633137}{172972800}$
$\sum_{n=0}^{14} \frac{(-1)^n}{n!} = 0.36787944117216190628\cdots = \frac{32071101049}{87178291200} = \frac{2467007773}{6706022400}$
$\sum_{n=0}^{15} \frac{(-1)^n}{n!} = 0.36787944117139718991\cdots = \frac{481066515734}{1307674368000} = \frac{34361893981}{93405312000}$
$\sum_{n=0}^{16} \frac{(-1)^n}{n!} = 0.36787944117144498468\cdots = \frac{7697064251745}{20922789888000} = \frac{15549624751}{42268262400}$
$\sum_{n=0}^{17} \frac{(-1)^n}{n!} = 0.36787944117144217323\cdots = \frac{130850092279664}{355687428096000} = \frac{8178130767479}{22230464256000}$
$\sum_{n=0}^{18} \frac{(-1)^n}{n!} = 0.36787944117144232942\cdots = \frac{2355301661033953}{6402373705728000} = \frac{138547156531409}{376610217984000}$
$\sum_{n=0}^{19} \frac{(-1)^n}{n!} = 0.36787944117144232120\cdots = \frac{44750731559645106}{121645100408832000} = \frac{92079694567171}{250298560512000}$
$\sum_{n=0}^{20} \frac{(-1)^n}{n!} = 0.36787944117144232161\cdots = \frac{895014631192902121}{2432902008176640000} = \frac{4282366656425369}{11640679464960000}$

We can incorporate an indeterminate if we define `\ratio` to be a macro with two parameters: `\def\ratioexp #1#2{\xintDiv{#1}{#2}}% x/n: x=#1, n=#2`. Then, if `\x` expands to some fraction `x`, the command

```
\xintRationalSeries {0}{b}{1}{\ratioexp{\x}}
```

will compute $\sum_{n=0}^{n=b} x^n/n!$:

```
\cnta 0
\def\ratioexp #1#2{\xintDiv{#1}{#2}}% #1/#2
\loop
\noindent
$\sum_{n=0}^{\the\cnta} (.57)^n/n! = \xintTrunc {50}
     {\xintRationalSeries {0}{\cnta}{1}{\ratioexp{.57}}}\dots$
     \vtop to 5pt {}\endgraf
\ifnum\cnta<50 \advance\cnta 10 \repeat
```

$\sum_{n=0}^{0}(.57)^n/n! = 1.000000000000000000000000000000000000000000000000000\ldots$
$\sum_{n=0}^{10}(.57)^n/n! = 1.768267051379470024806680580357142857142857142857142\ldots$
$\sum_{n=0}^{20}(.57)^n/n! = 1.768267051433735151620893242711870822728330055290820\ldots$
$\sum_{n=0}^{30}(.57)^n/n! = 1.768267051433735151620893392823821449154848849794300\ldots$
$\sum_{n=0}^{40}(.57)^n/n! = 1.768267051433735151620893392823821449154852198677760\ldots$
$\sum_{n=0}^{50}(.57)^n/n! = 1.768267051433735151620893392823821449154852198677760\ldots$

Observe that in this last example the `x` was directly inserted; if it had been a more complicated explicit fraction it would have been worthwile to use `\ratioexp\x` with `\x` defined to expand to its value. In the further situation where this fraction `x` is not explicit but itself defined via a complicated, and time-costly, formula, it should be noted that `\xintRationalSeries` will do again the evaluation of `\x` for each term of the partial sum. The easiest is thus when `x` can be defined as an `\edef`. If however, you are in an expandable-only context and cannot store in a macro like `\x` the value to be used, a variant of `\xintRationalSeries` is needed which will first evaluate this `\x` and then use this result without recomputing it. This is `\xintRationalSeriesX`, documented next.

Here is a slightly more complicated evaluation:

```
\cnta 1
\loop \edef\z {\xintRationalSeries
                    {\cnta}
                    {2*\cnta-1}
                    {\xintiPow {\the\cnta}{\cnta}/\xintFac{\cnta}}
                    {\ratioexp{\the\cnta}}}%
\edef\w {\xintRationalSeries {0}{2*\cnta-1}{1}{\ratioexp{\the\cnta}}}%
\noindent
$\sum_{n=\the\cnta}^{\the\numexpr 2*\cnta-1\relax} \frac{\the\cnta^n}{n!}/%
          \sum_{n=0}^{\the\numexpr 2*\cnta-1\relax} \frac{\the\cnta^n}{n!} =
          \xintTrunc{8}{\xintDiv\z\w}\dots$ \vtop to 5pt{}\endgraf
\ifnum\cnta<20 \advance\cnta 1 \repeat
```

$\sum_{n=1}^{1}\frac{1^n}{n!}/\sum_{n=0}^{1}\frac{1^n}{n!} = 0.50000000\ldots$
$\sum_{n=2}^{3}\frac{2^n}{n!}/\sum_{n=0}^{3}\frac{2^n}{n!} = 0.52631578\ldots$
$\sum_{n=3}^{5}\frac{3^n}{n!}/\sum_{n=0}^{5}\frac{3^n}{n!} = 0.53804347\ldots$
$\sum_{n=4}^{7}\frac{4^n}{n!}/\sum_{n=0}^{7}\frac{4^n}{n!} = 0.54317053\ldots$
$\sum_{n=5}^{9}\frac{5^n}{n!}/\sum_{n=0}^{9}\frac{5^n}{n!} = 0.54502576\ldots$
$\sum_{n=6}^{11}\frac{6^n}{n!}/\sum_{n=0}^{11}\frac{6^n}{n!} = 0.54518217\ldots$
$\sum_{n=7}^{13}\frac{7^n}{n!}/\sum_{n=0}^{13}\frac{7^n}{n!} = 0.54445274\ldots$
$\sum_{n=8}^{15}\frac{8^n}{n!}/\sum_{n=0}^{15}\frac{8^n}{n!} = 0.54327992\ldots$
$\sum_{n=9}^{17}\frac{9^n}{n!}/\sum_{n=0}^{17}\frac{9^n}{n!} = 0.54191055\ldots$
$\sum_{n=10}^{19}\frac{10^n}{n!}/\sum_{n=0}^{19}\frac{10^n}{n!} = 0.54048295\ldots$
$\sum_{n=11}^{21}\frac{11^n}{n!}/\sum_{n=0}^{21}\frac{11^n}{n!} = 0.53907332\ldots$
$\sum_{n=12}^{23}\frac{12^n}{n!}/\sum_{n=0}^{23}\frac{12^n}{n!} = 0.53772178\ldots$
$\sum_{n=13}^{25}\frac{13^n}{n!}/\sum_{n=0}^{25}\frac{13^n}{n!} = 0.53644744\ldots$
$\sum_{n=14}^{27}\frac{14^n}{n!}/\sum_{n=0}^{27}\frac{14^n}{n!} = 0.53525726\ldots$
$\sum_{n=15}^{29}\frac{15^n}{n!}/\sum_{n=0}^{29}\frac{15^n}{n!} = 0.53415135\ldots$
$\sum_{n=16}^{31}\frac{16^n}{n!}/\sum_{n=0}^{31}\frac{16^n}{n!} = 0.53312615\ldots$
$\sum_{n=17}^{33}\frac{17^n}{n!}/\sum_{n=0}^{33}\frac{17^n}{n!} = 0.53217628\ldots$
$\sum_{n=18}^{35}\frac{18^n}{n!}/\sum_{n=0}^{35}\frac{18^n}{n!} = 0.53129566\ldots$
$\sum_{n=19}^{37}\frac{19^n}{n!}/\sum_{n=0}^{37}\frac{19^n}{n!} = 0.53047810\ldots$
$\sum_{n=20}^{39}\frac{20^n}{n!}/\sum_{n=0}^{39}\frac{20^n}{n!} = 0.52971771\ldots$

19.4 \xintRationalSeriesX

New with release 1.04.

`\xintRationalSeriesX{A}{B}{\first}{\ratio}{\g}` is a parametrized version of `\xintRationalSeries` where `\first` is turned into a one parameter macro with `\first{\g}` giving `F(A,\g)` and `\ratio` is a two parameters macro such that `\ratio{n}{\g}` gives

`F(n,\g)/F(n-1,\g)`. The parameter `\g` is evaluated only once at the beginning of the computation, and can thus itself be the yet unevaluated result of a previous computation.

Let `\ratio` be such a two-parameters macro; note the subtle differences between

`\xintRationalSeries {A}{B}{\first}{\ratio{\g}}`

and `\xintRationalSeriesX {A}{B}{\first}{\ratio}{\g}`.

First the location of braces differ... then, in the former case `\first` is a *no-parameter* macro expanding to a fractional number, and in the latter, it is a *one-parameter* macro which will use `\g`. Furthermore the `X` variant will expand `\g` at the very beginning whereas the former non-`X` former variant will evaluate it each time it needs it (which is bad if this evaluation is time-costly, but good if `\g` is a big explicit fraction encapsulated in a macro).

The example will use the macro `\xintPowerSeries` which computes efficiently exact partial sums of power series, and is discussed in the next section.

```
\def\firstterm #1{1[0]}% first term of the exponential series
% although it is the constant 1, here it must be defined as a
% one-parameter macro. Next comes the ratio function for exp:
\def\ratioexp  #1#2{\xintDiv {#1}{#2}}% x/n
% These are the (-1)^{n-1}/n of the log(1+h) series:
\def\coefflog #1{\the\numexpr\ifodd #1 1\else-1\fi\relax/#1[0]}%
% Let L(h) be the first 10 terms of the log(1+h) series and
% let E(t) be the first 10 terms of the exp(t) series.
% The following computes E(L(a/10)) for a=1,...,12.
\cnta 0
\loop
\noindent\xintTrunc {18}{%
     \xintRationalSeriesX {0}{9}{\firstterm}{\ratioexp}
         {\xintPowerSeries{1}{10}{\coefflog}{\the\cnta[-1]}}}\dots
\endgraf
\ifnum\cnta < 12 \advance \cnta 1 \repeat
```

1.099999999999083906...	1.499954310225476533...	1.870485649686617459...
1.199999998111624029...	1.599659266069210466...	1.907197560339468199...
1.299999835744121464...	1.698137473697423757...	1.845117565491393752...
1.399996091955359088...	1.791898112718884531...	1.593831932293536053...

These completely exact operations rapidly create numbers with many digits. Let us print in full the raw fractions created by the operation illustrated above:

`E(L(1[-1]))`=
435534952734304993753128478305695755446525998418916420656308534427154141471013807206588202981046013155342233701289165089056830056936564478988779520000000000/39594086612242519324387557078266845776303882240000000000000000000[-90]
(length of numerator: 155)

`E(L(12[-2]))`=
443453770054417465442109252347264824711893599160411729603882584198084153226108070707505890096280305971037133280203464123715588771418838065898295901413463294640275999939742200930346362653264354170486398431674455531227136795459841404436480000000000/39594086612242519324387557078266845776303882240000000000000000000[-180]
(length of numerator: 245)

`E(L(123[-3]))`=
444641592651941777154254148848854866198954971552616390074295913531792113850864779762350800814416981762774148663052493217 5

66759754097977420731516373336789722730765496139079185229545102248282
39119962102923779381174012211091973543316113275716895586401771088185
05853950798598438316179662071953915678034718321474363029365556301004
8000000000/39594086612242519324387557078266845776303882240000000000000000000[-270] (length of numerator: 335)

We see that the denominators here remain the same, as our input only had various powers of ten as denominators, and **xintfrac** efficiently assemble (some only, as we can see) powers of ten. Notice that 1 more digit in an input denominator seems to mean 90 more in the raw output. We can check that with some other test cases:

E(L(1/7))=518138516117322604916074833164833344883840590133006168125
12534667430913353255394804713669158571590044976892591448945234186435
1924224000000000/45337120162108979178809662782137765289223265381758152546654836095087089601022689942796465342115407786358809263904208715776000000000000000000[0] (length of numerator: 141; length of denominator: 141)

E(L(1/71))=164799489177219556498025955806107098256158101756209369864657152282149780083067798039175325186850716609293467854603842163754716919123274624394132188208895310089982001627351524910000588238596565380887916286153347403881434316800000000/16251060738309150710228315926583043448560635097998286551792304600401711584442548604911127392639471285026166742651015948354491747514663603304596379819982611548681495538153647264137927630891689041426777132144944742400000000000000000000[0] (length of numerator: 232; length of denominator: 232)

E(L(1/712))=209623173880163120675481637897216200283968902248203238943136902264182865559717266406341976325767001357109452980607391271438079195073959301528254006087908156888129567520269011715459969154688799089625738271433856535377918700884980798641197021855117078629780316835353043067415753497212012899985019017494798220551782400000000/2093291722337673799732719862311619975662927884547744846526034295741465968177583093786412050480958301357075221213896546903011983961080605724903426024563430558292203346913309844190901402018394162270065876670575550330002721292096217682473000829618103432600036119035084894266166648343032219206471638591733760000000000000000000[0] (length of numerator: 322; length of denominator: 322)

For info the last fraction put into irreducible form still has 288 digits in its denominator.[39] Thus decimal numbers such as `0.123` (equivalently `123[-3]`) give less computing intensive tasks than fractions such as `1/712`: in the case of decimal numbers the (raw) denominators originate in the coefficients of the series themselves, powers of ten of the input within brackets being treated separately. And even then the numerators will grow with the size of the input in a sort of linear way, the coefficient being given by the order of series: here 10 from the log and 9 from the exp, so 90. One more digit in the input means 90 more digits in the numerator of the output: obviously we can not go on composing such partial sums of series and hope that **xint** will joyfully do all at the speed of light! Briefly said, imagine that the rules of the game make the programmer like a security guard at an airport scanning machine: a never-ending flux of passengers keep on arriving and all you can do

[39] putting this fraction in irreducible form takes more time than is typical of the other computations in this document; so exceptionally I have hard-coded the 288 in the document source.

is re-shuffle the first nine of them, organize marriages among some, execute some, move children farther back among the first nine only. If a passenger comes along with many hand luggages, this will slow down the process even if you move him to ninth position, because sooner or later you will have to digest him, and the children will be big too. There is no way to move some guy out of the file and to a discrete interrogatory room for separate treatment or to give him/her some badge saying "I left my stuff in storage box 357".

Hence, truncating the output (or better, rounding) is the only way to go if one needs a general calculus of special functions. This is why the package **xintseries** provides, besides `\xintSeries`, `\xintRationalSeries`, or `\xintPowerSeries` which compute *exact* sums, also has `\xintFxPtPowerSeries` for fixed-point computations.

Update: release `1.08a` of **xintseries** now includes a tentative naive `\xintFloatPowerSeries`.

19.5 \xintPowerSeries

`\xintPowerSeries{A}{B}{\coeff}{f}` evaluates the sum $\sum_{n=A}^{n=B} \coeff\{n\} \cdot f^n$. The initial and final indices are given to a `\numexpr` expression. The `\coeff` macro (which, as argument to `\xintPowerSeries` is expanded only at the time `\coeff{n}` is needed) should be defined as a one-parameter expandable command, its input will be an explicit number.

The `f` can be either a fraction directly input or a macro `\f` expanding to such a fraction. It is actually more efficient to encapsulate an explicit fraction `f` in such a macro, if it has big numerators and denominators ('big' means hundreds of digits) as it will then take less space in the processing until being (repeatedly) used.

This macro computes the *exact* result (one can use it also for polynomial evaluation). Starting with release `1.04` a Horner scheme for polynomial evaluation is used, which has the advantage to avoid a denominator build-up which was plaguing the `1.03` version. [40]

> Note: as soon as the coefficients look like factorials, it is more efficient to use the `\xintRationalSeries` macro whose evaluation, also based on a similar Horner scheme, will avoid a denominator build-up originating in the coefficients themselves.

```
\def\geom #1{1[0]} % the geometric series
\def\f {5/17[0]}
\[ \sum_{n=0}^{n=20} \Bigl(\frac 5{17}\Bigr)^n
 =\xintFrac{\xintIrr{\xintPowerSeries {0}{20}{\geom}{\f}}}
 =\xintFrac{\xinttheexpr (17^21-5^21)/12/17^20\relax}\]
```

$$\sum_{n=0}^{n=20}\Big(\frac{5}{17}\Big)^n = \frac{57576611593776579768853 41}{40642314066475725224016 01} = \frac{69091933912531895722624092}{48770776879770870268819212}$$

```
\def\coefflog #1{1/#1[0]}% 1/n
\def\f {1/2[0]}%
\[ \log 2 \approx \sum_{n=1}^{20} \frac1{n\cdot 2^n}
    = \xintFrac {\xintIrr {\xintPowerSeries {1}{20}{\coefflog}{\f}}}\]
```

[40] with powers `f^k`, from `k=0` to `N`, a denominator `d` of `f` became `d^{1+2+...+N}`, which is bad. With the `1.04` method, the part of the denominator originating from `f` does not accumulate to more than `d^N`.

```
\[ \log 2 \approx \sum_{n=1}^{50} \frac1{n\cdot 2^n}
    = \xintFrac {\xintIrr {\xintPowerSeries {1}{50}{\coefflog}{\f}}}\]
```

$$\log 2 \approx \sum_{n=1}^{20} \frac{1}{n\cdot 2^n} = \frac{42299423848079}{61025172848640}$$

$$\log 2 \approx \sum_{n=1}^{50} \frac{1}{n\cdot 2^n} = \frac{6046346975175226566357988455973921 9}{872303479657928392239462081783398 40}$$

```
\cnta 1 % previously declared count
\loop   % in this loop we recompute from scratch each partial sum!
% we can afford that, as \xintPowerSeries is fast enough.
\noindent\hbox to 2em{\hfil\texttt{\the\cnta.} }%
         \xintTrunc {12}
             {\xintPowerSeries {1}{\cnta}{\coefflog}{\f}}\dots
\endgraf
\ifnum \cnta < 30 \advance\cnta 1 \repeat
```

1. 0.500000000000...	11. 0.693109245355...	21. 0.693147159757...
2. 0.625000000000...	12. 0.693129590407...	22. 0.693147170594...
3. 0.666666666666...	13. 0.693138980431...	23. 0.693147175777...
4. 0.682291666666...	14. 0.693143340085...	24. 0.693147178261...
5. 0.688541666666...	15. 0.693145374590...	25. 0.693147179453...
6. 0.691145833333...	16. 0.693146328265...	26. 0.693147180026...
7. 0.692261904761...	17. 0.693146777052...	27. 0.693147180302...
8. 0.692750186011...	18. 0.693146988980...	28. 0.693147180435...
9. 0.692967199900...	19. 0.693147089367...	29. 0.693147180499...
10. 0.693064856150...	20. 0.693147137051...	30. 0.693147180530...

```
%\def\coeffarctg #1{1/\the\numexpr\xintMON{#1}*(2*#1+1)\relax }%
\def\coeffarctg  #1{1/\the\numexpr\ifodd #1 -2*#1-1\else2*#1+1\fi\relax }%
% the above gives (-1)^n/(2n+1). The sign being in the denominator,
%             **** no [0] should be added ****,
% else nothing is guaranteed to work (even if it could by sheer luck)
% NOTE in passing this aspect of \numexpr:
%         ****  \numexpr -(1)\relax does not work!!! ****
\def\f {1/25[0]}% 1/5^2
\[\mathrm{Arctg}(\frac15)\approx
            \frac15\sum_{n=0}^{15} \frac{(-1)^n}{(2n+1)25^n}
= \xintFrac{\xintIrr {\xintDiv
            {\xintPowerSeries {0}{15}{\coeffarctg}{\f}}{5}}}\]
```

$$\mathrm{Arctg}(\frac{1}{5}) \approx \frac{1}{5}\sum_{n=0}^{15} \frac{(-1)^n}{(2n+1)25^n} = \frac{165918726519122955895391793269168}{840539304153062403202056884765625}$$

19.6 \xintPowerSeriesX

New with release 1.04.

This is the same as \xintPowerSeries apart from the fact that the last parameter f is expanded once and for all before being then used repeatedly. If the f parameter is to be an explicit big fraction with many (dozens) digits, rather than using it directly it is slightly better to have some macro \g defined to expand to the explicit fraction and then use \xintPowerSeries with \g; but if f has not yet been evaluated and will be the output of a complicated expansion of some \f, and if, due to an expanding only context, doing \edef\g{\f} is no option, then \xintPowerSeriesX should be used with \f as last parameter.

```
\def\ratioexp #1#2{\xintDiv {#1}{#2}}% x/n
% These are the (-1)^{n-1}/n of the log(1+h) series:
\def\coefflog #1{\the\numexpr\ifodd #1 1\else-1\fi\relax/#1[0]}%
% Let L(h) be the first 10 terms of the log(1+h) series and
% let E(t) be the first 10 terms of the exp(t) series.
% The following computes L(E(a/10)-1) for a=1,..., 12.
\cnta 1
\loop
\noindent\xintTrunc {18}{%
   \xintPowerSeriesX {1}{10}{\coefflog}
  {\xintSub
      {\xintRationalSeries {0}{9}{1[0]}{\ratioexp{\the\cnta[-1]}}}
      {1}}}\dots
\endgraf
\ifnum\cnta < 12 \advance \cnta 1 \repeat
```

0.099999999998556159...	0.499511320760604148...	-1.597091692317639401...
0.199999995263443554...	0.593980619762352217...	-12.648937932093322763...
0.299999338075041781...	0.645144282733914916...	-66.259639046914679687...
0.399974460740121112...	0.398118280111436442...	-304.768437445462801227...

19.7 \xintFxPtPowerSeries

\xintFxPtPowerSeries{A}{B}{\coeff}{f}{D} computes $\sum_{n=A}^{n=B}$ \coeff{n} $\cdot$ f^n with each term of the series truncated to D digits after the decimal point. As usual, A and B are completely expanded through their inclusion in a \numexpr expression. Regarding D it will be similarly be expanded each time it is used inside an \xintTrunc. The one-parameter macro \coeff is similarly expanded at the time it is used inside the computations. Idem for f. If f itself is some complicated macro it is thus better to use the variant \xintFxPtPowerSeriesX which expands it first and then uses the result of that expansion.

The current (1.04) implementation is: the first power f^A is computed exactly, then *truncated*. Then each successive power is obtained from the previous one by multiplication by the exact value of f, and truncated. And \coeff{n}·f^n is obtained from that by multiplying by \coeff{n} (untruncated) and then truncating. Finally the sum is computed exactly. Apart from that \xintFxPtPowerSeries (where FxPt means 'fixed-point') is like \xintPowerSeries.

There should be a variant for things of the type $\sum c_n \frac{f^n}{n!}$ to avoid having to compute the factorial from scratch at each coefficient, the same way \xintFxPtPowerSeries does not compute f^n from scratch at each n. Perhaps in the next package release.

$$e^{-\frac{1}{2}} \approx$$

1.00000000000000000000	0.60653056795634920635	0.60653065971263344622
0.50000000000000000000	0.60653066483754960317	0.60653065971263342289
0.62500000000000000000	0.60653065945526069224	0.60653065971263342361
0.60416666666666666667	0.60653065972437513778	0.60653065971263342359
0.60677083333333333333	0.60653065971214266299	0.60653065971263342359
0.60651041666666666667	0.60653065971265234943	0.60653065971263342359
0.60653211805555555555	0.60653065971263274611	

```
\def\coeffexp #1{1/\xintFac {#1}[0]}% 1/n!
\def\f {-1/2[0]}% [0] for faster input parsing
\cnta 0 % previously declared \count register
\noindent\loop
$\xintFxPtPowerSeries {0}{\cnta}{\coeffexp}{\f}{20}$\\
\ifnum\cnta<19 \advance\cnta 1 \repeat\par
% One should **not** trust the final digits, as the potential truncation
% errors of up to 10^{-20} per term accumulate and never disappear! (the
% effect is attenuated by the alternating signs in the series). We  can
% confirm that the last two digits (of our evaluation of the nineteenth
% partial sum) are wrong via the evaluation with more digits:

\xintFxPtPowerSeries {0}{19}{\coeffexp}{\f}{25}= 0.6065306597126334236037992
```

It is no difficulty for xintfrac to compute exactly, with the help of `\xintPowerSeries`, the nineteenth partial sum, and to then give (the start of) its exact decimal expansion:

$$\texttt{\xintPowerSeries \{0\}\{19\}\{\coeffexp\}\{\f\}} = \frac{3868274616003639731775 7}{6377706640314571161600 0} = 0.60653065971263342360379915 2126\ldots$$

Thus, one should always estimate a priori how many ending digits are not reliable: if there are `N` terms and `N` has `k` digits, then digits up to but excluding the last `k` may usually be trusted. If we are optimistic and the series is alternating we may even replace `N` with $\sqrt{\texttt{N}}$ to get the number `k` of digits possibly of dubious significance.

19.8 \xintFxPtPowerSeriesX

New with release `1.04`.

`\xintFxPtPowerSeriesX{A}{B}{\coeff}{\f}{D}` computes, exactly as `\xintFxPtPowerSeries`, the sum of `\coeff{n}·\f^n` from `n=A` to `n=B` with each term of the series being *truncated* to `D` digits after the decimal point. The sole difference is that `\f` is first expanded and it is the result of this which is used in the computations.

Let us illustrate this on the numerical exploration of the identity

```
log(1+x) = -log(1/(1+x))
```

Let `L(h)=log(1+h)`, and `D(h)=L(h)+L(-h/(1+h))`. Theoretically thus, `D(h)=0` but we shall evaluate `L(h)` and `-h/(1+h)` keeping only 10 terms of their respective series. We will assume `|h|<0.5`. With only ten terms kept in the power series we do not have quite 3 digits precision as `2^10=1024`. So it wouldn't make sense to evaluate things more precisely than, say circa 5 digits after the decimal points.

```
\cnta 0
```

```
\def\coefflog #1{\the\numexpr\ifodd#1 1\else-1\fi\relax/#1[0]}% (-1)^{n-
1}/n
\def\coeffalt #1{\the\numexpr\ifodd#1 -1\else1\fi\relax [0]}%   (-1)^n
\loop
\noindent \hbox to 2.5cm {\hss\texttt{D(\the\cnta/100): }}%
\xintAdd {\xintFxPtPowerSeriesX {1}{10}{\coefflog}{\the\cnta [-2]}{5}}
         {\xintFxPtPowerSeriesX {1}{10}{\coefflog}
             {\xintFxPtPowerSeriesX {1}{10}{\coeffalt}{\the\cnta [-2]}{5}}
          {5}}\endgraf
\ifnum\cnta < 49 \advance\cnta 7 \repeat
```

```
   D(0/100): 0/1[0]                  D(28/100): 4/1[-5]
   D(7/100): 2/1[-5]                 D(35/100): 4/1[-5]
  D(14/100): 2/1[-5]                 D(42/100): 9/1[-5]
  D(21/100): 3/1[-5]                 D(49/100): 42/1[-5]
```

Let's say we evaluate functions on `[-1/2,+1/2]` with values more or less also in `[-1/2,+1/2]` and we want to keep 4 digits of precision. So, roughly we need at least 14 terms in series like the geometric or log series. Let's make this 15. Then it doesn't make sense to compute intermediate summands with more than 6 digits precision. So we compute with 6 digits precision but return only 4 digits (rounded) after the decimal point. This result with 4 post-decimal points precision is then used as input to the next evaluation.

```
\loop
\noindent \hbox to 2.5cm {\hss\texttt{D(\the\cnta/100): }}%
\xintRound{4}
 {\xintAdd {\xintFxPtPowerSeriesX {1}{15}{\coefflog}{\the\cnta [-2]}{6}}
           {\xintFxPtPowerSeriesX {1}{15}{\coefflog}
                  {\xintRound {4}{\xintFxPtPowerSeriesX {1}{15}{\coeffalt}
                                 {\the\cnta [-2]}{6}}}
            {6}}%
 }\endgraf
\ifnum\cnta < 49 \advance\cnta 7 \repeat
```

```
   D(0/100): 0                       D(28/100): -0.0001
   D(7/100): 0.0000                  D(35/100): -0.0001
  D(14/100): 0.0000                  D(42/100): -0.0000
  D(21/100): -0.0001                 D(49/100): -0.0001
```

Not bad... I have cheated a bit: the 'four-digits precise' numeric evaluations were left unrounded in the final addition. However the inner rounding to four digits worked fine and made the next step faster than it would have been with longer inputs. The morale is that one should not use the raw results of `\xintFxPtPowerSeriesX` with the `D` digits with which it was computed, as the last are to be considered garbage. Rather, one should keep from the output only some smaller number of digits. This will make further computations faster and not less precise. I guess there should be some command to do this final truncating, or better, rounding, at a given number `D'<D` of digits. Maybe for the next release.

19.9 \xintFloatPowerSeries

New with 1.08a.

`\xintFloatPowerSeries[P]{A}{B}{\coeff}{f}` computes $\sum_{n=A}^{n=B}$`\coeff{n}` $\cdot$ `f`^{n} with a floating point precision given by the optional parameter `P` or by the current setting of `\xintDigits`.

In the current, preliminary, version, no attempt has been made to try to guarantee to the final result the precision P. Rather, P is used for all intermediate floating point evaluations. So rounding errors will make some of the last printed digits invalid. The operations done are first the evaluation of f^A using \xintFloatPow, then each successive power is obtained from this first one by multiplication by f using \xintFloatMul, then again with \xintFloatMul this is multiplied with \coeff{n}, and the sum is done adding one term at a time with \xintFloatAdd. To sum up, this is just the naive transformation of \xintFxPtPowerSeries from fixed point to floating point.

```
\def\coefflog #1{\the\numexpr\ifodd#1 1\else-1\fi\relax/#1[0]}%
\xintFloatPowerSeries [8]{1}{30}{\coefflog}{-1/2[0]}
```

-6.9314718e-1

19.10 \xintFloatPowerSeriesX

New with 1.08a.

\xintFloatPowerSeriesX[P]{A}{B}{\coeff}{f} is like \xintFloatPowerSeries with the difference that f is expanded once and for all at the start of the computation, thus allowing efficient chaining of such series evaluations.

```
\def\coeffexp #1{1/\xintFac {#1}[0]}% 1/n! (exact, not float)
\def\coefflog #1{\the\numexpr\ifodd#1 1\else-1\fi\relax/#1[0]}%
\xintFloatPowerSeriesX [8]{0}{30}{\coeffexp}
    {\xintFloatPowerSeries [8]{1}{30}{\coefflog}{-1/2[0]}}
```

5.0000001e-1

19.11 Computing $\log 2$ and π

In this final section, the use of \xintFxPtPowerSeries (and \xintPowerSeries) will be illustrated on the (expandable... why make things simple when it is so easy to make them difficult!) computations of the first digits of the decimal expansion of the familiar constants $\log 2$ and π.

Let us start with $\log 2$. We will get it from this formula (which is left as an exercise):

$$\log(2) = -2\log(1-13/256) - 5\log(1-1/9)$$

The number of terms to be kept in the log series, for a desired precision of 10^{-D} was roughly estimated without much theoretical analysis. Computing exactly the partial sums with \xintPowerSeries and then printing the truncated values, from D=0 up to D=100 showed that it worked in terms of quality of the approximation. Because of possible strings of zeros or nines in the exact decimal expansion (in the present case of $\log 2$, strings of zeros around the fourtieth and the sixtieth decimals), this does not mean though that all digits printed were always exact. In the end one always end up having to compute at some higher level of desired precision to validate the earlier result.

Then we tried with \xintFxPtPowerSeries: this is worthwile only for D's at least 50, as the exact evaluations are faster (with these short-length f's) for a lower number of digits. And as expected the degradation in the quality of approximation was in this range of the order of two or three digits. This meant roughly that the 3+1=4 ending digits were wrong. Again, we ended up having to compute with five more digits and compare with the earlier value to validate it. We use truncation rather than rounding because our goal is not to obtain the correct rounded decimal expansion but the correct exact truncated one.

```
\def\coefflog #1{1/#1[0]}% 1/n
\def\xa {13/256[0]}%  we will compute log(1-13/256)
\def\xb {1/9[0]}%     we will compute log(1-1/9)
\def\LogTwo #1%
%  get log(2)=-2log(1-13/256)- 5log(1-1/9)
{% we want to use \printnumber, hence need something expanding in two steps
 % only, so we use here the \romannumeral0 method
  \romannumeral0\expandafter\LogTwoDoIt \expandafter
    % Nb Terms for 1/9:
  {\the\numexpr #1*150/143\expandafter}\expandafter
    % Nb Terms for 13/256:
  {\the\numexpr #1*100/129\expandafter}\expandafter
    % We print #1 digits, but we know the ending ones are garbage
  {\the\numexpr #1\relax}% allows #1 to be a count register
}%
\def\LogTwoDoIt #1#2#3%
%  #1=nb of terms for 1/9, #2=nb of terms for 13/256,
{% #3=nb of digits for computations, also used for printing
 \xinttrunc {#3} % lowercase form to stop the \romannumeral0 expansion!
 {\xintAdd
  {\xintMul {2}{\xintFxPtPowerSeries {1}{#2}{\coefflog}{\xa}{#3}}}
  {\xintMul {5}{\xintFxPtPowerSeries {1}{#1}{\coefflog}{\xb}{#3}}}%
 }%
}%
\noindent $\log 2 \approx \LogTwo {60}\dots$\endgraf
\noindent\phantom{$\log 2$}${}\approx{}$\printnumber{\LogTwo {65}}\dots\endgraf
\noindent\phantom{$\log 2$}${}\approx{}$\printnumber{\LogTwo {70}}\dots\endgraf
```

$\log 2 \approx 0.693147180559945309417232121458176568075500134360255254120484\ldots$

$\approx 0.693147180559945309417232121458176568075500134360255254120680$
00711...

$\approx 0.693147180559945309417232121458176568075500134360255254120680$
0094933723...

Here is the code doing an exact evaluation of the partial sums. We have added a +1 to the number of digits for estimating the number of terms to keep from the log series: we experimented that this gets exactly the first D digits, for all values from D=0 to D=100, except in one case (D=40) where the last digit is wrong. For values of D higher than 100 it is more efficient to use the code using \xintFxPtPowerSeries.

```
\def\LogTwo #1% get log(2)=-2log(1-13/256)- 5log(1-1/9)
{%
    \romannumeral0\expandafter\LogTwoDoIt \expandafter
    {\the\numexpr (#1+1)*150/143\expandafter}\expandafter
    {\the\numexpr (#1+1)*100/129\expandafter}\expandafter
    {\the\numexpr #1\relax}%
}%
\def\LogTwoDoIt #1#2#3%
{%   #3=nb of digits for truncating an EXACT partial sum
  \xinttrunc {#3}
    {\xintAdd
      {\xintMul {2}{\xintPowerSeries {1}{#2}{\coefflog}{\xa}}}
      {\xintMul {5}{\xintPowerSeries {1}{#1}{\coefflog}{\xb}}}%
    }%
```

```
}%
```

Let us turn now to Pi, computed with the Machin formula. Again the numbers of terms to keep in the two `arctg` series were roughly estimated, and some experimentations showed that removing the last three digits was enough (at least for `D=0-100` range). And the algorithm does print the correct digits when used with `D=1000` (to be convinced of that one needs to run it for `D=1000` and again, say for `D=1010`.) A theoretical analysis could help confirm that this algorithm always gets better than `10^{-D}` precision, but again, strings of zeros or nines encountered in the decimal expansion may falsify the ending digits, nines may be zeros (and the last non-nine one should be increased) and zeros may be nine (and the last non-zero one should be decreased).

```
% pi = 16 Arctg(1/5) - 4 Arctg(1/239) (John Machin's formula)
\def\coeffarctg #1{\the\numexpr\ifodd#1 -1\else1\fi\relax/%
                                        \the\numexpr 2*#1+1\relax [0]}%
% the above computes (-1)^n/(2n+1).
% Alternatives:
% \def\coeffarctg #1{1/\the\numexpr\xintiMON{#1}*(2*#1+1)\relax }%
% The [0] can *not* be used above, as the denominator is signed.
% \def\coeffarctg #1{\xintiMON{#1}/\the\numexpr 2*#1+1\relax [0]}%
\def\xa {1/25[0]}%      1/5^2, the [0] for faster parsing
\def\xb {1/57121[0]}% 1/239^2, the [0] for faster parsing
\def\Machin #1{% \Machin {\mycount} is allowed
    \romannumeral0\expandafter\MachinA \expandafter
     % number of terms for arctg(1/5):
    {\the\numexpr (#1+3)*5/7\expandafter}\expandafter
     % number of terms for arctg(1/239):
    {\the\numexpr (#1+3)*10/45\expandafter}\expandafter
     % do the computations with 3 additional digits:
    {\the\numexpr #1+3\expandafter}\expandafter
     % allow #1 to be a count register:
    {\the\numexpr #1\relax }}%
\def\MachinA #1#2#3#4%
% #4: digits to keep after decimal point for final printing
% #3=#4+3: digits for evaluation of the necessary number of terms
% to be kept in the arctangent series, also used to truncate each
% individual summand.
{\xinttrunc {#4} % must be lowercase to stop \romannumeral0!
 {\xintSub
  {\xintMul {16/5}{\xintFxPtPowerSeries {0}{#1}{\coeffarctg}{\xa}{#3}}}
  {\xintMul {4/239}{\xintFxPtPowerSeries {0}{#2}{\coeffarctg}{\xb}{#3}}}%
 }}%
\[ \pi = \Machin {60}\dots \]
```

$$\pi = 3.14159265358979323846264338327950288419716939937510582097494 4\ldots$$

Here is a variant `\MachinBis`, which evaluates the partial sums *exactly* using `\xintPowerSeries`, before their final truncation. No need for a "+3" then.

```
\def\MachinBis #1{% #1 may be a count register,
```

```
% the final result will be truncated to #1 digits post decimal point
    \romannumeral0\expandafter\MachinBisA \expandafter
     % number of terms for arctg(1/5):
    {\the\numexpr #1*5/7\expandafter}\expandafter
     % number of terms for arctg(1/239):
    {\the\numexpr #1*10/45\expandafter}\expandafter
      % allow #1 to be a count register:
    {\the\numexpr #1\relax }}%
\def\MachinBisA #1#2#3%
{\xinttrunc {#3} %
 {\xintSub
   {\xintMul {16/5}{\xintPowerSeries {0}{#1}{\coeffarctg}{\xa}}}
   {\xintMul{4/239}{\xintPowerSeries {0}{#2}{\coeffarctg}{\xb}}}%
}}%
```

Let us use this variant for a loop showing the build-up of digits:

```
\cnta 0 % previously declared \count register
\loop
\MachinBis{\cnta} \endgraf  % Plain's \loop does not accept \par
\ifnum\cnta < 30 \advance\cnta 1 \repeat
```

```
                                    3.141592653589793
                3.                  3.1415926535897932
                3.1                 3.14159265358979323
                3.14                3.141592653589793238
                3.141               3.1415926535897932384
                3.1415              3.14159265358979323846
                3.14159             3.141592653589793238462
                3.141592            3.1415926535897932384626
                3.1415926           3.14159265358979323846264
                3.14159265          3.141592653589793238462643
                3.141592653         3.1415926535897932384626433
                3.1415926535        3.14159265358979323846264338
                3.14159265358       3.141592653589793238462643383
                3.141592653589      3.1415926535897932384626433832
                3.1415926535897     3.14159265358979323846264338327
                3.14159265358979    3.141592653589793238462643383279
```

You want more digits and have some time? Copy the `\Machin` code to a Plain TEX or LATEX document loading **xintseries**, and compile:

```
\newwrite\outfile
\immediate\openout\outfile \jobname-out\relax
\immediate\write\outfile {\Machin {1000}}
\immediate\closeout\outfile
```

This will create a file with the correct first 1000 digits of π after the decimal point. On my laptop (a 2012 model) this took about 42 seconds last time I tried (and for 200 digits it is less than 1 second). As mentioned in the introduction, the file pi.tex by D. ROEGEL shows that orders of magnitude faster computations are possible within TEX, but recall our constraints of complete expandability and be merciful, please.

Why truncating rather than rounding? One of our main competitors on the market of scientific computing, a canadian product (not encumbered with expandability constraints, and having barely ever heard of TEX ;-), prints numbers rounded in the last digit. Why didn't we follow suit in the macros `\xintFxPtPowerSeries` and `\xintFxPtPowerSeriesX`? To round at `D` digits, and excluding a rewrite or cloning of the division algorithm which anyhow would add to it some overhead in its final steps, **xintfrac** needs to truncate at `D+1`, then round. And rounding loses information! So, with more time spent, we obtain a worst result than the one truncated at `D+1` (one could imagine that additions and so on, done with only `D` digits, cost less; true, but this is a negligeable effect per summand compared to the additional cost for this term of having been truncated at `D+1` then rounded). Rounding is the way to go when setting up algorithms to evaluate functions destined to be composed one after the other: exact algebraic operations with many summands and an `f` variable which is a fraction are costly and create an even bigger fraction; replacing `f` with a reasonable rounding, and rounding the result, is necessary to allow arbitrary chaining.

But, for the computation of a single constant, we are really interested in the exact decimal expansion, so we truncate and compute more terms until the earlier result gets validated. Finally if we do want the rounding we can always do it on a value computed with `D+1` truncation.

20 Commands of the xintcfrac package

This package was first included in release `1.04` of the **xint** bundle.

Contents

20.1 Package overview

A *simple* continued fraction has coefficients `[c0,c1,...,cN]` (usually called partial quotients, but I really dislike this entrenched terminology), where `c0` is a positive or negative integer and the others are positive integers. As we will see it is possible with **xintcfrac** to specify the coefficient function `c:n->cn`. Note that the index then starts at zero as indi-

cated. With the amsmath macro \cfrac one can display such a continued fraction as

$$c_0 + \cfrac{1}{c_1 + \cfrac{1}{c_2 + \cfrac{1}{c_3 + \cfrac{1}{\ddots}}}}$$

Here is a concrete example:

$$\frac{208341}{66317} = 3 + \cfrac{1}{7 + \cfrac{1}{15 + \cfrac{1}{1 + \cfrac{1}{292 + \cfrac{1}{2}}}}}$$

But the difference with amsmath's \cfrac is that this was input as

```
\[ \xintFrac {208341/66317}=\xintCFrac {208341/66317} \]
```

The command \xintCFrac produces in two expansion steps the whole thing with the many chained \cfrac's and all necessary braces, ready to be printed, in math mode. This is LaTeX only and with the amsmath package (we shall mention another method for Plain TeX users of amstex).

A *generalized* continued fraction has the same structure but the numerators are not restricted to be ones, and numbers used in the continued fraction may be arbitrary, also fractions, irrationals, indeterminates. The *centered* continued fraction associated to a rational number is an example:

```
\[ \xintFrac {915286/188421}=\xintGCFrac {\xintFtoCC {915286/188421}} \]
```

$$\frac{915286}{188421} = 5 - \cfrac{1}{7 + \cfrac{1}{39 - \cfrac{1}{53 - \cfrac{1}{13}}}} = 4 + \cfrac{1}{1 + \cfrac{1}{6 + \cfrac{1}{38 + \cfrac{1}{1 + \cfrac{1}{51 + \cfrac{1}{1 + \cfrac{1}{12}}}}}}}$$

The command \xintGCFrac, contrarily to \xintCFrac, does not compute anything, it just typesets. Here, it is the command \xintFtoCC which did the computation of the centered continued fraction of f. Its output has the 'inline format' described in the next paragraph. In the display, we also used \xintCFrac (code not shown), for comparison of the two types of continued fractions.

A generalized continued fraction may be input 'inline' as:

```
a0+b0/a1+b1/a2+b2/...../a(n-1)+b(n-1)/an
```

Fractions among the coefficients are allowed but they must be enclosed within braces. Signed integers may be left without braces (but the + signs are mandatory). Or, they may be macros expanding (in two steps) to some number or fractional number.

```
\xintGCFrac {1+-1/57+\xintPow {-3}{7}/\xintQuo {132}{25}}
```

$$\frac{1907}{1902} = 1 - \cfrac{1}{57 - \cfrac{2187}{5}}$$

The left hand side was obtained with the following code:

```
\xintFrac{\xintGCtoF {1+-1/57+\xintPow {-3}{7}/\xintQuo {132}{25}}}
```

It uses the macro \xintGCtoF to convert a generalized fraction from the 'inline format' to the fraction it evaluates to.

A simple continued fraction is a special case of a generalized continued fraction and may be input as such to macros expecting the 'inline format', for example `-7+1/6+1/19+1/1+1/33`. There is a simpler comma separated format:

```
\xintFrac{\xintCstoF{-7,6,19,1,33}}=\xintCFrac{\xintCstoF{-7,6,19,1,33}}
```

$$\frac{-28077}{4108} = -7 + \cfrac{1}{6 + \cfrac{1}{19 + \cfrac{1}{1 + \cfrac{1}{33}}}}$$

This comma separated format may also be used with fractions among the coefficients: of course in that case, computing with \xintFtoCs from the resulting `f` its real coefficients will give a new comma separated list with only integers. This list has no spaces: the spaces in the display below arise from the math mode processing.

```
\xintFrac{1084483/398959}=[\xintFtoCs{1084483/398959}]
```

$$\frac{1084483}{398959} = [2, 1, 2, 1, 1, 4, 1, 1, 6, 1, 1, 8, 1, 1, 10, 2]$$

If one prefers other separators, one can use \xintFtoCx whose first argument will be the separator to be used.

```
\xintFrac{2721/1001}=\xintFtoCx {+1/(}{2721/1001})\cdots)
```

$$\frac{2721}{1001} = 2 + 1/(1 + 1/(2 + 1/(1 + 1/(1 + 1/(4 + 1/(1 + 1/(1 + 1/(6 + 1/(2)\cdots)$$

People using Plain TEX and `amstex` can achieve the same effect as \xintCFrac with:

```
$$\xintFwOver{2721/1001}=\xintFtoCx {+\cfrac1\\ }{2721/1001}\endcfrac$$
```

Using \xintFtoCx with first argument an empty pair of braces `{}` will return the list of the coefficients of the continued fraction of `f`, without separator, and each one enclosed in a pair of group braces. This can then be manipulated by the non-expandable macro \xintAssignArray or the expandable ones \xintApply and \xintListWithSep.

As a shortcut to using \xintFtoCx with separator `1+/`, there is \xintFtoGC:

```
2721/1001=\xintFtoGC {2721/1001}
```

2721/1001=2+1/1+1/2+1/1+1/1+1/4+1/1+1/1+1/6+1/2

Let us compare in that case with the output of \xintFtoCC:

```
2721/1001=\xintFtoCC {2721/1001}
2721/1001=3+-1/4+-1/2+1/5+-1/2+1/7+-1/2
```

The '\printnumber' macro which we use to print long numbers can also be useful on long continued fractions.

```
\printnumber{\xintFtoCC {350370189063507202043510 49/%
    244241737886197404558180}}
```

143+1/2+1/5+-1/4+-1/4+-1/4+-1/3+1/2+1/2+1/6+-1/22+1/2+1/10+-1/5+-1/11+-1/3+1/4+-1/2+1/2+1/4+-1/2+1/23+1/3+1/8+-1/6+-1/9. If we apply \xintGCtoF to this generalized continued fraction, we discover that the original fraction was reducible:

```
\xintGCtoF {143+1/2+...+-1/9}=2897319801297630107/20197107104701740[0]
```

When a generalized continued fraction is built with integers, and numerators are only 1's or -1's, the produced fraction is irreducible. And if we compute it again with the last sub-fraction omitted we get another irreducible fraction related to the bigger one by a Bezout identity. Doing this here we get:

```
\xintGCtoF {143+1/2+...+-1/6}=328124887710626729/2287346221788023[0]
```

and indeed:

$$\begin{vmatrix} 2897319801297630107 & 328124887710626729 \\ 20197107104701740 & 2287346221788023 \end{vmatrix} = 1$$

More generally the various fractions obtained from the truncation of a continued fraction to its initial terms are called the convergents. The commands of **xintcfrac** such as \xintFtoCv, \xintFtoCCv, and others which compute such convergents, return them as a list of braced items, with no separator. This list can then be treated either with \xintAssignArray, or \xintListWithSep, or any other way (but then, some TEX programming knowledge will be necessary). Here is an example:

```
$$\xintFrac{915286/188421}\to \xintListWithSep {,}%
{\xintApply{\xintFrac}{\xintFtoCv{915286/188421}}}$$
```

$$\frac{915286}{188421} \to 4, 5, \frac{34}{7}, \frac{1297}{267}, \frac{1331}{274}, \frac{69178}{14241}, \frac{70509}{14515}, \frac{915286}{188421}$$

```
$$\xintFrac{915286/188421}\to \xintListWithSep {,}%
{\xintApply{\xintFrac}{\xintFtoCCv{915286/188421}}}$$
```

$$\frac{915286}{188421} \to 5, \frac{34}{7}, \frac{1331}{274}, \frac{70509}{14515}, \frac{915286}{188421}$$

We thus see that the 'centered convergents' obtained with \xintFtoCCv are among the fuller list of convergents as returned by \xintFtoCv.

Here is a more complicated use of \xintApply and \xintListWithSep. We first define a macro which will be applied to each convergent:

```
\newcommand{\mymacro}[1]{$\xintFrac{#1}=[\xintFtoCs{#1}]$\vtop to 6pt{}}
```

Next, we use the following code:

```
$\xintFrac{49171/18089}\to{}$
\xintListWithSep {, }{\xintApply{\mymacro}{\xintFtoCv{49171/18089}}}
```

It produces:

$\frac{49171}{18089} \to 2 = [2]$, $3 = [3]$, $\frac{8}{3} = [2,1,2]$, $\frac{11}{4} = [2,1,3]$, $\frac{19}{7} = [2,1,2,2]$, $\frac{87}{32} = [2,1,2,1,1,4]$, $\frac{106}{39} = [2,1,2,1,1,5]$, $\frac{193}{71} = [2,1,2,1,1,4,2]$, $\frac{1264}{465} = [2,1,2,1,1,4,1,1,6]$, $\frac{1457}{536} = [2,1,2,1,1,4,1,1,7]$, $\frac{2721}{1001} = [2,1,2,1,1,4,1,1,6,2]$, $\frac{23225}{8544} = [2,1,2,1,1,4,1,1,6,1,1,8]$, $\frac{49171}{18089} = [2,1,2,1,1,4,1,1,6,1,1,8,2]$.

The macro \xintCntoF allows to specify the coefficients as functions of the index. The values to which expand the coefficient function do not have to be integers.

```
\def\cn #1{\xintiPow {2}{#1}}% 2^n
\[\xintFrac{\xintCntoF {6}{\cn}}=\xintCFrac [l]{\xintCntoF {6}{\cn}}\]
```

$$\frac{3541373}{2449193} = 1 + \cfrac{1}{2 + \cfrac{1}{4 + \cfrac{1}{8 + \cfrac{1}{16 + \cfrac{1}{32 + \frac{1}{64}}}}}}$$

Notice the use of the optional argument [l] to \xintCFrac. Other possibilities are [r] and (default) [c].

```
\def\cn #1{\xintPow {2}{-#1}}% 1/2^n
\[\xintFrac{\xintCntoF {6}{\cn}} = \xintGCFrac [r]{\xintCntoGC {6}{\cn}}
                    = [\xintFtoCs {\xintCntoF {6}{\cn}}]\]
```

$$\frac{3159019}{2465449} = 1 + \cfrac{1}{\frac{1}{2} + \cfrac{1}{\frac{1}{4} + \cfrac{1}{\frac{1}{8} + \cfrac{1}{\frac{1}{16} + \cfrac{1}{\frac{1}{32} + \frac{1}{\frac{1}{64}}}}}}}} = [1,3,1,1,4,14,1,1,1,1,79,2,1,1,2]$$

We used \xintCntoGC as we wanted to display also the continued fraction and not only the fraction returned by \xintCntoF.

There are also \xintGCntoF and \xintGCntoGC which allow the same for generalized fractions. The following initial portion of a generalized continued fraction for π:

$$\frac{92736}{29520} = \cfrac{4}{1 + \cfrac{1}{3 + \cfrac{4}{5 + \cfrac{9}{7 + \cfrac{16}{9 + \frac{25}{11}}}}}} = 3.1414634146\ldots$$

was obtained with this code:

```
\def\an #1{\the\numexpr 2*#1+1\relax }%
\def\bn #1{\the\numexpr (#1+1)*(#1+1)\relax }%
\[ \xintFrac{\xintDiv {4}{\xintGCntoF {5}{\an}{\bn}}} =
        \cfrac{4}{\xintGCFrac{\xintGCntoGC {5}{\an}{\bn}}} =
\xintTrunc {10}{\xintDiv {4}{\xintGCntoF {5}{\an}{\bn}}}\dots\]
```

We see that the quality of approximation is not fantastic compared to the simple continued fraction of π with about as many terms:

```
\[ \xintFrac{\xintCstoF{3,7,15,1,292,1,1}}=
   \xintGCFrac{3+1/7+1/15+1/1+1/292+1/1+1/1}=
   \xintTrunc{10}{\xintCstoF{3,7,15,1,292,1,1}}\dots\]
```

$$\frac{208341}{66317} = 3 + \cfrac{1}{7 + \cfrac{1}{15 + \cfrac{1}{1 + \cfrac{1}{292 + \cfrac{1}{1 + \cfrac{1}{1}}}}}} = 3.1415926534\ldots$$

To conclude this overview of most of the package functionalities, let us explore the convergents of Euler's number e.

```
\def\cn #1{\the\numexpr\ifcase \numexpr #1+3-3*((#1+2)/3)\relax
                           1\or1\or2*(#1/3)\fi\relax }
% produces the pattern 1,1,2,1,1,4,1,1,6,1,1,8,... which are the
% coefficients of the simple continued fraction of e-1.
\cnta 0
\def\mymacro #1{\advance\cnta by 1
                \noindent
                \hbox to 3em {\hfil\small\texttt{\the\cnta.} }%
                $\xintTrunc {30}{\xintAdd {1[0]}{#1}}\dots=
                 \xintFrac{\xintAdd {1[0]}{#1}}$}%
\xintListWithSep{\vtop to 6pt{}\vbox to 12pt{}\par}
    {\xintApply\mymacro{\xintiCstoCv{\xintCntoCs {35}{\cn}}}}
```

The volume of computation is kept minimal by the following steps:

- a comma separated list of the first 36 coefficients is produced by \xintCntoCs,
- this is then given to \xintiCstoCv which produces the list of the convergents (there is also \xintCstoCv, but our coefficients being integers we used the infinitesimally faster \xintiCstoCv),
- then the whole list was converted into a sequence of one-line paragraphs, each convergent becomes the argument to a macro printing it together with its decimal expansion with 30 digits after the decimal point.
- A count register \cnta was used to give a line count serving as a visual aid: we could also have done that in an expandable way, but well, let's relax from time to time...

1. $2.000000000000000000000000000000\cdots = 2$
2. $3.000000000000000000000000000000\cdots = 3$
3. $2.666666666666666666666666666666\cdots = \frac{8}{3}$
4. $2.750000000000000000000000000000\cdots = \frac{11}{4}$
5. $2.714285714285714285714285714285\cdots = \frac{19}{7}$
6. $2.718750000000000000000000000000\cdots = \frac{87}{32}$
7. $2.717948717948717948717948717948\cdots = \frac{106}{39}$
8. $2.718309859154929577464788732394\cdots = \frac{193}{71}$
9. $2.718279569892473118279569892473\cdots = \frac{1264}{465}$
10. $2.718283582089552238805970149253\cdots = \frac{1457}{536}$
11. $2.718281718281718281718281718281\cdots = \frac{2721}{1001}$
12. $2.718281835205992509363295880149\cdots = \frac{23225}{8544}$
13. $2.718281822943949711891042430591\cdots = \frac{25946}{9545}$
14. $2.718281828735695726684725523798\cdots = \frac{49171}{18089}$
15. $2.718281828445401318035025074172\cdots = \frac{517656}{190435}$
16. $2.718281828470583721777828930962\cdots = \frac{566827}{208524}$
17. $2.718281828458563411277850606202\cdots = \frac{1084483}{398959}$
18. $2.718281828459065114074529546648\cdots = \frac{13580623}{4996032}$
19. $2.718281828459028013207065591026\cdots = \frac{14665106}{5394991}$
20. $2.718281828459045851404621084949\cdots = \frac{28245729}{10391023}$
21. $2.718281828459045213521983758221\cdots = \frac{410105312}{150869313}$
22. $2.718281828459045254624795027092\cdots = \frac{438351041}{161260336}$
23. $2.718281828459045234757560631479\cdots = \frac{848456353}{312129649}$
24. $2.718281828459045235379013372772\cdots = \frac{14013652689}{5155334720}$
25. $2.718281828459045235343535532787\cdots = \frac{14862109042}{5467464369}$
26. $2.718281828459045235360753230188\cdots = \frac{28875761731}{10622799089}$
27. $2.718281828459045235360274593941\cdots = \frac{534625820200}{196677847971}$
28. $2.718281828459045235360299120911\cdots = \frac{563501581931}{207300647060}$
29. $2.718281828459045235360287179900\cdots = \frac{1098127402131}{403978495031}$
30. $2.718281828459045235360287478611\cdots = \frac{22526049624551}{8286870547680}$
31. $2.718281828459045235360287464726\cdots = \frac{23624177026682}{8690849042711}$
32. $2.718281828459045235360287471503\cdots = \frac{46150226651233}{16977719590391}$
33. $2.718281828459045235360287471349\cdots = \frac{1038929163353808}{382200680031313}$

34. $2.71828182845904523536028747135\cdots = \frac{1085079390005041}{399178399621704}$

35. $2.71828182845904523536028747135\cdots = \frac{2124008553358849}{781379079653017}$

36. $2.71828182845904523536028747135\cdots = \frac{52061284670617417}{19152276311294112}$

The actual computation of the list of all 36 convergents accounts for only 8% of the total time (total time equal to about 5 hundredths of a second in my testing, on my laptop): another 80% is occupied with the computation of the truncated decimal expansions (and the addition of 1 to everything as the formula gives the continued fraction of $e-1$). One can with no problem compute much bigger convergents. Let's get the 200th convergent. It turns out to have the same first 268 digits after the decimal point as $e-1$. Higher convergents get more and more digits in proportion to their index: the 500th convergent already gets 799 digits correct! To allow speedy compilation of the source of this document when the need arises, I limit here to the 200th convergent (getting the 500th took about 1.2s on my laptop last time I tried, and the 200th convergent is obtained ten times faster).

```
\edef\z {\xintCntoF {199}{\cn}}%
\begingroup\parindent 0pt \leftskip 2.5cm
\indent\llap {Numerator = }{\printnumber{\xintNumerator\z}\par
\indent\llap {Denominator = }\printnumber{\xintDenominator\z}\par
\indent\llap {Expansion = }\printnumber{\xintTrunc{268}\z}\dots
\par\endgroup
```

Numerator = 5689640388718962675975238923158078752938890176679174460572320245471922969611182301752438601749953108177313670124170860974963432938290633112381766973761930625636081635675336546882372931443815620561546324665972858186546133769206314891601955061457059255337661142645217223

Denominator = 3311238176697376193062563608163567533654688237293144381562056154632466597285818654613376920631489160195506145705925533766114264521722333

Expansion = 1.7182818284590452353602874713526624977572470936999595749666967627724076630353547594571382178525166427427466391932003059921817413596629043572900334295260595630738132328627943490763233829880753195251019011573834187930702154089149934884167509244761460668082264800168477411833

One can also use a centered continued fraction: we get more digits but there are also more computations as the numerators may be either 1 or -1.

20.2 \xintCFrac

`\xintCFrac{f}` is a math-mode only, LaTeX with `amsmath` only, macro which first computes then displays with the help of `\cfrac` the simple continued fraction corresponding to the given fraction (or macro expanding in two steps to one such). It admits an optional argument which may be `[l]`, `[r]` or (the default) `[c]` to specify the location of the one's in the numerators of the sub-fractions. Each coefficient is typeset using the `\xintFrac` macro from the **xintfrac** package.

20.3 \xintGCFrac

`\xintGCFrac{a+b/c+d/e+f/g+h/...}` uses similarly `\cfrac` to typeset a generalized continued fraction in inline format. It admits the same optional argument as `\xintCFrac`.

```
\[\xintGCFrac {1+\xintPow{1.5}{3}/{1/7}+{-3/5}/\xintFac {6}}\]
```

$$1+\cfrac{3375\cdot 10^{-3}}{\frac{1}{7}-\cfrac{\frac{3}{5}}{720}}$$

As can be seen this is typesetting macro, although it does proceed to the evaluation of the coefficients themselves. See `\xintGCtoF` if you are impatient to see this fraction computed. Numerators and denominators are made arguments to the `\xintFrac` macro.

20.4 \xintGCtoGCx

New with release `1.05`.

`\xintGCtoGCx{sepa}{sepb}{a+b/c+d/e+f/...+x/y}` returns the list of the coefficients of the generalized continued fraction of `f`, each one within a pair of braces, and separated with the help of `sepa` and `sepb`. Thus

`\xintGCtoGCx :;{1+2/3+4/5+6/7}` gives 1:2;3:4;5:6;7

Plain TEX+`amstex` users may be interested in:

```
$$\xintGCtoGCx {+\cfrac}{\\}{a+b/...}\endcfrac$$
$$\xintGCtoGCx {+\cfrac\xintFwOver}{\\\xintFwOver}{a+b/...}\endcfrac$$
```

20.5 \xintFtoCs

`\xintFtoCs{f}` returns the comma separated list of the coefficients of the simple continued fraction of `f`.

```
\[ \xintSignedFrac{-5262046/89233} = [\xintFtoCs{-5262046/89233}]\]
```

$$-\frac{5262046}{89233}=[-59,33,27,100]$$

20.6 \xintFtoCx

`\xintFtoCx{sep}{f}` returns the list of the coefficients of the simple continued fraction of `f`, withing group braces and separated with the help of `sep`.

```
$$\xintFtoCx {+\cfrac1\\ }{f}\endcfrac$$
```

will display the continued fraction in `\cfrac` format, with Plain TEX and `amstex`.

20.7 \xintFtoGC

`\xintFtoGC{f}` does the same as `\xintFtoCx{+1/}{f}`. Its output may thus be used in the package macros expecting such an 'inline format'. This continued fraction is a *simple* one, not a *generalized* one, but as it is produced in the format used for user input of generalized continued fractions, the macro was called `\xintFtoGC` rather than `\xintFtoC` for example.

```
566827/208524=\xintFtoGC {566827/208524}
```

566827/208524=2+1/1+1/2+1/1+1/1+1/4+1/1+1/1+1/6+1/1+1/1+1/8+1/1+1/1+1/11

20.8 \xintFtoCC

\xintFtoCC{f} returns the 'centered' continued fraction of f, in 'inline format'.

```
566827/208524=\xintFtoCC {566827/208524}
```

566827/208524=3+-1/4+-1/2+1/5+-1/2+1/7+-1/2+1/9+-1/2+1/11

```
\[\xintFrac{566827/208524} = \xintGCFrac{\xintFtoCC{566827/208524}}\]
```

$$\frac{566827}{208524} = 3 - \cfrac{1}{4 - \cfrac{1}{2 + \cfrac{1}{5 - \cfrac{1}{2 + \cfrac{1}{7 - \cfrac{1}{2 + \cfrac{1}{9 - \cfrac{1}{2 + \cfrac{1}{11}}}}}}}}}$$

20.9 \xintFtoCv

\xintFtoCv{f} returns the list of the (braced) convergents of f, with no separator. To be treated with \xintAssignArray or \xintListWithSep.

```
\[\xintListWithSep{\to}{\xintApply\xintFrac{\xintFtoCv{5211/3748}}}\]
```

$$1 \to \frac{3}{2} \to \frac{4}{3} \to \frac{7}{5} \to \frac{25}{18} \to \frac{32}{23} \to \frac{57}{41} \to \frac{317}{228} \to \frac{374}{269} \to \frac{691}{497} \to \frac{5211}{3748}$$

20.10 \xintFtoCCv

\xintFtoCCv{f} returns the list of the (braced) centered convergents of f, with no separator. To be treated with \xintAssignArray or \xintListWithSep.

```
\[\xintListWithSep{\to}{\xintApply\xintFrac{\xintFtoCCv{5211/3748}}}\]
```

$$1 \to \frac{4}{3} \to \frac{7}{5} \to \frac{32}{23} \to \frac{57}{41} \to \frac{374}{269} \to \frac{691}{497} \to \frac{5211}{3748}$$

20.11 \xintCstoF

\xintCstoF{a,b,c,d,...,z} computes the fraction corresponding to the coefficients, which may be fractions or even macros expanding to such fractions (in two steps). The final fraction may then be highly reducible.

```
\[\xintGCFrac {-1+1/3+1/-5+1/7+1/-9+1/11+1/-13}
=\xintSignedFrac{\xintCstoF {-1,3,-5,7,-9,11,-13}}
```

```
=\xintSignedFrac{\xintGCtoF {-1+1/3+1/-5+1/7+1/-9+1/11+1/-13}}\]
```

$$-1+\cfrac{1}{3+\cfrac{1}{-5+\cfrac{1}{7+\cfrac{1}{-9+\cfrac{1}{11+\cfrac{1}{-13}}}}}}=-\frac{75887}{118187}=-\frac{75887}{118187}$$

```
\xintGCFrac{{1/2}+1/{1/3}+1/{1/4}+1/{1/5}}=
   \xintFrac{\xintCstoF {1/2,1/3,1/4,1/5}}
```

$$\frac{1}{2}+\cfrac{1}{\frac{1}{3}+\cfrac{1}{\frac{1}{4}+\frac{1}{\frac{1}{5}}}}=\frac{159}{66}$$

A generalized continued fraction may produce a reducible fraction (`\xintCstoF` tries its best not to accumulate in a silly way superfluous factors but will not do simplifications which would be obvious to a human, like simplification by 3 in the result above).

20.12 \xintCstoCv

`\xintCstoCv{a,b,c,d,...,z}` returns the list of the corresponding convergents. It is allowed to use fractions as coefficients (the computed convergents have then no reason to be the real convergents of the final fraction). When the coefficients are integers, the convergents are irreducible fractions, but otherwise it is of course not necessarily the case.

```
\xintListWithSep:{\xintCstoCv{1,2,3,4,5,6}}
1/1[0]:3/2[0]:10/7[0]:43/30[0]:225/157[0]:1393/972[0]
\xintListWithSep:{\xintCstoCv{1,1/2,1/3,1/4,1/5,1/6}}
1/1[0]:3/1[0]:9/7[0]:45/19[0]:225/159[0]:1575/729[0]
```

I know that these `[0]` are a bit annoying[41] but this is the way **xintfrac** likes to reception fractions: this format is best for further processing by the bundle macros. For 'inline' printing, one may apply `\xintRaw` and for display in math mode `\xintFrac`.

```
\[\xintListWithSep{\to}{\xintApply\xintFrac{\xintCstoCv
{\xintPow {-.3}{-5},7.3/4.57,\xintCstoF{3/4,9,-1/3}}}}\]
```

$$\frac{-100000}{243}\to\frac{-72888949}{177390}\to\frac{-2700356878}{6567804}$$

20.13 \xintCstoGC

`\xintCstoGC{a,b,..,z}` transforms a comma separated list (or something expanding to such a list) into an 'inline format' continued fraction `{a}+1/{b}+1/...+1/{z}`. The coefficients are just copied and put within braces, without expansion. The output can then be

[41] and the awful truth is that it is added forcefully by `\xintCstoCv` at the last step...

used in \xintGCFrac for example.

```
\[\xintGCFrac {\xintCstoGC {-1,1/2,-1/3,1/4,-1/5}}
=\xintSignedFrac {\xintCstoF {-1,1/2,-1/3,1/4,-1/5}}\]
```

$$-1+\cfrac{1}{\frac{1}{2}+\cfrac{1}{\frac{-1}{3}+\cfrac{1}{\frac{1}{4}+\frac{1}{\frac{-1}{5}}}}}=-\frac{145}{83}$$

20.14 \xintGCtoF

\xintGCtoF{a+b/c+d/e+f/g+.....+v/w+x/y} computes the fraction defined by the inline generalized continued fraction. Coefficients may be fractions but must then be put within braces. They can be macros. The plus signs are mandatory.

```
\[\xintGCFrac {1+\xintPow{1.5}{3}/{1/7}+{-3/5}/\xintFac {6}} =
\xintFrac{\xintGCtoF {1+\xintPow{1.5}{3}/{1/7}+{-3/5}/\xintFac {6}}} =
\xintFrac{\xintIrr{\xintGCtoF
                  {1+\xintPow{1.5}{3}/{1/7}+{-3/5}/\xintFac {6}}}}\]
```

$$1+\cfrac{3375\cdot 10^{-3}}{\frac{1}{7}-\frac{\frac{3}{5}}{720}}=\frac{88629000}{3579000}=\frac{29543}{1193}$$

```
\[ \xintGCFrac{{1/2}+{2/3}/{4/5}+{1/2}/{1/5}+{3/2}/{5/3}} =
   \xintFrac{\xintGCtoF {{1/2}+{2/3}/{4/5}+{1/2}/{1/5}+{3/2}/{5/3}}} \]
```

$$\frac{1}{2}+\cfrac{\frac{2}{3}}{\frac{4}{5}+\cfrac{\frac{1}{2}}{\frac{1}{5}+\frac{\frac{3}{2}}{\frac{5}{3}}}}=\frac{4270}{4140}$$

The macro tries its best not to accumulate superfluous factor in the denominators, but doesn't reduce the fraction to irreducible form before returning it and does not do simplifications which would be obvious to a human.

20.15 \xintGCtoCv

\xintGCtoCv{a+b/c+d/e+f/g+.....+v/w+x/y} returns the list of the corresponding convergents. The coefficients may be fractions, but must then be inside braces. Or they may be macros, too.

The convergents will in the general case be reducible. To put them into irreducible form, one needs one more step, for example it can be done with \xintApply\xintIrr.

```
\[\xintListWithSep{,}{\xintApply\xintFrac
                  {\xintGCtoCv{3+{-2}/{7/2}+{3/4}/12+{-56}/3}}}\]
\[\xintListWithSep{,}{\xintApply\xintFrac{\xintApply\xintIrr
                  {\xintGCtoCv{3+{-2}/{7/2}+{3/4}/12+{-56}/3}}}}\]
```

$$3,\frac{17}{7},\frac{834}{342},\frac{1306}{542}$$

$$3, \frac{17}{7}, \frac{139}{57}, \frac{653}{271}$$

20.16 \xintCntoF

`\xintCntoF{N}{\macro}` computes the fraction `f` having coefficients `c(j)=\macro{j}` for `j=0,1,...,N`. The `N` parameter is given to a `\numexpr`. The values of the coefficients, as returned by `\macro` do not have to be positive, nor integers, and it is thus not necessarily the case that the original `c(j)` are the true coefficients of the final `f`.

```
\def\macro #1{\the\numexpr 1+#1*#1\relax}\xintCntoF {5}{\macro}
72625/49902[0]
```

20.17 \xintGCntoF

`\xintGCntoF{N}{\macroA}{\macroB}` returns the fraction `f` corresponding to the inline generalized continued fraction `a0+b0/a1+b1/a2+....+b(N-1)/aN`, with `a(j)=\macroA{j}` and `b(j)=\macroB{j}`. The `N` parameter is given to a `\numexpr`.

$$1+\cfrac{1}{2-\cfrac{1}{3+\cfrac{1}{1-\cfrac{1}{2+\cfrac{1}{3-\cfrac{1}{1}}}}}} = \frac{39}{25}$$

There is also `\xintGCntoGC` to get the 'inline format' continued fraction. The previous display was obtained with:

```
\def\coeffA #1{\the\numexpr #1+4-3*((#1+2)/3)\relax }%
        \def\coeffB #1{\xintMON{#1}}% (-1)^n
  \[\xintGCFrac{\xintGCntoGC {6}{\coeffA}{\coeffB}}
   = \xintFrac{\xintGCntoF {6}{\coeffA}{\coeffB}}\]
```

20.18 \xintCntoCs

`\xintCntoCs{N}{\macro}` produces the comma separated list of the corresponding coefficients, from `n=0` to `n=N`. The `N` is given to a `\numexpr`.

```
\def\macro #1{\the\numexpr 1+#1*#1\relax}
 \xintCntoCs {5}{\macro}->1,2,5,10,17,26
\[\xintFrac{\xintCntoF {5}{\macro}}=\xintCFrac{\xintCntoF {5}{\macro}}\]
```

$$\frac{72625}{49902} = 1+\cfrac{1}{2+\cfrac{1}{5+\cfrac{1}{10+\cfrac{1}{17+\cfrac{1}{26}}}}}$$

20.19 \xintCntoGC

`\xintCntoGC{N}{\macro}` evaluates the `c(j)=\macro{j}` from `j=0` to `j=N` and returns a continued fraction written in inline format: `{c(0)}+1/{c(1)}+1/...+1/{c(N)}`. The parameter `N` is given to a `\numexpr`. The coefficients, after expansion, are, as shown, being enclosed in an added pair of braces, they may thus be fractions.

```
\def\macro #1{\the\numexpr\ifodd#1 -1-#1\else1+#1\fi\relax/%
              \the\numexpr 1+#1*#1\relax}
\edef\x{\xintCntoGC {5}{\macro}}\meaning\x
macro:->{1/1}+1/{-2/2}+1/{3/5}+1/{-4/10}+1/{5/17}+1/{-6/26}
\[\xintGCFrac{\xintCntoGC {5}{\macro}}\]
```

$$1+\cfrac{1}{\frac{-2}{2}+\cfrac{1}{\frac{3}{5}+\cfrac{1}{\frac{-4}{10}+\cfrac{1}{\frac{5}{17}+\frac{1}{\frac{-6}{26}}}}}}$$

20.20 \xintGCntoGC

`\xintGCntoGC{N}{\macroA}{\macroB}` evaluates the coefficients and then returns the corresponding `{a0}+{b0}/{a1}+{b1}/{a2}+...+{b(N-1)}/{aN}` inline generalized fraction. `N` is givent to a `\numexpr`. As shown, the coefficients are enclosed into added pairs of braces, and may thus be fractions.

```
\def\an #1{\the\numexpr #1*#1*#1+1\relax}%
\def\bn #1{\the\numexpr \xintiMON{#1}*(#1+1)\relax}%
$\xintGCntoGC {5}{\an}{\bn}}=\xintGCFrac {\xintGCntoGC {5}{\an}{\bn}}
        = \displaystyle\xintFrac {\xintGCntoF  {5}{\an}{\bn}}$\par
```

$$1 + 1/2 + -2/9 + 3/28 + -4/65 + 5/126 = 1+\cfrac{1}{2-\cfrac{2}{9+\cfrac{3}{28-\cfrac{4}{65+\frac{5}{126}}}}} = \frac{5797655}{3712466}$$

20.21 \xintiCstoF, \xintiGCtoF, \xintiCstoCv, \xintiGCtoCv

The same as the corresponding macros without the 'i', but for integer-only input. Infinitesimally faster; to notice the higher efficiency one would need to use them with an input having (at least) hundreds of coefficients.

20.22 \xintGCtoGC

`\xintGCtoGC{a+b/c+d/e+f/g+.....+v/w+x/y}` expands (with the usual meaning) each one of the coefficients and returns an inline continued fraction of the same type, each

expanded coefficient being enclosed withing braces.

```
\edef\x {\xintGCtoGC
  {1+\xintPow{1.5}{3}/{1/7}+{-3/5}/\xintFac {6}+\xintCstoF {2,-7,-5}/16}}
\meaning\x
```

```
macro:->{1}+{3375/1[-3]}/{1/7}+{-3/5}/{720}+{67/36[0]}/{16}
```

To be honest I have, it seems, forgotten why I wrote this macro in the first place.

21 Package xint implementation

The commenting of the macros is currently (2013/06/16) very sparse.

Contents

21.1 Catcodes, ε-TEX and reload detection

The method for package identification and reload detection is copied verbatim from the packages by Heiko Oberdiek.

The method for catcodes was also inspired by these packages, we proceed slightly differently. `1.05` adds a `\relax` near the end of `\XINT_restorecatcodes_endinput`. Plain TeX users following the doc instruction to do `\input xint.sty\relax` were anyhow protected from any side effect. I did not realize earlier that the `\endinput` would not stop TEX's scan for a number which was initiated by the last `\the\catcode`.

Starting with version `1.06` of the package, also ` must be sanitized, because we replace everywhere in the code the twice-expansion done with `\expandafter` by the systematic use of `\romannumeral-`0`.

Starting with version 1.06b I decide that I suffer from an indigestion of @ signs, so I replace them all with underscores _, à la LaTeX3.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode95=11   % _  (starting with 1.06b, used inside cs names)
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter\let\expandafter\x\csname ver@xint.sty\endcsname
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \expandafter
  \ifx\csname numexpr\endcsname\relax
     \y{xint}{\numexpr not available, aborting input}%
     \aftergroup\endinput
  \else
    \ifx\x\relax % plain-TeX, first loading
    \else
      \def\empty {}%
      \ifx\x\empty % LaTeX, first loading,
      % variable is initialized, but \ProvidesPackage not yet seen
      \else
        \y{xint}{I was already loaded, aborting input}%
        \aftergroup\endinput
      \fi
    \fi
  \fi
  \def\ChangeCatcodesIfInputNotAborted
  {%
      \endgroup
      \edef\XINT_restorecatcodes_endinput
      {%
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
```

```
47        \catcode43=\the\catcode43   % +
48        \catcode62=\the\catcode62   % >
49        \catcode60=\the\catcode60   % <
50        \catcode58=\the\catcode58   % :
51        \catcode46=\the\catcode46   % .
52        \catcode45=\the\catcode45   % -
53        \catcode44=\the\catcode44   % ,
54        \catcode35=\the\catcode35   % #
55        \catcode95=\the\catcode95   % _
56        \catcode125=\the\catcode125 % }
57        \catcode123=\the\catcode123 % {
58        \endlinechar=\the\endlinechar
59        \catcode13=\the\catcode13   % ^^M
60        \catcode32=\the\catcode32   %
61        \catcode61=\the\catcode61\relax   % =
62        \noexpand\endinput
63      }%
64      \def\XINT_setcatcodes
65      {%
66        \catcode61=12   % =
67        \catcode32=10   % space
68        \catcode13=5    % ^^M
69        \endlinechar=13 %
70        \catcode123=1   % {
71        \catcode125=2   % }
72        \catcode95=11   % _ (replaces @ everywhere, starting with 1.06b)
73        \catcode35=6    % #
74        \catcode44=12   % ,
75        \catcode45=12   % -
76        \catcode46=12   % .
77        \catcode58=11   % : (made letter for error cs)
78        \catcode60=12   % <
79        \catcode62=12   % >
80        \catcode43=12   % +
81        \catcode42=12   % *
82        \catcode40=12   % (
83        \catcode41=12   % )
84        \catcode47=12   % /
85        \catcode96=12   % `
86        \catcode94=11   % ^
87      }%
88      \XINT_setcatcodes
89  }%
90 \ChangeCatcodesIfInputNotAborted
```

21.2 Package identification

Copied verbatim from Heiko Oberdiek's packages.

```
\begingroup
  \catcode64=11 % @
  \catcode91=12 % [
  \catcode93=12 % ]
  \catcode58=12 % : (does not really matter, was letter)
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xint.sty\endcsname
\ProvidesPackage{xint}%
  [2013/06/14 v1.08b Expandable operations on long numbers (jfB)]%
```

21.3 Token management, constants

```
\def\xint_gobble_     {}%
\def\xint_gobble_i    #1{}%
\def\xint_gobble_ii   #1#2{}%
\def\xint_gobble_iii  #1#2#3{}%
\def\xint_gobble_iv   #1#2#3#4{}%
\def\xint_gobble_v    #1#2#3#4#5{}%
\def\xint_gobble_vi   #1#2#3#4#5#6{}%
\def\xint_gobble_vii  #1#2#3#4#5#6#7{}%
\def\xint_gobble_viii #1#2#3#4#5#6#7#8{}%
\def\xint_firstoftwo  #1#2{#1}%
\def\xint_secondoftwo #1#2{#2}%
\def\xint_firstoftwo_andstop  #1#2{ #1}%
\def\xint_secondoftwo_andstop #1#2{ #2}%
\def\xint_exchangetwo_keepbraces_andstop #1#2{ {#2}{#1}}%
\def\xint_firstofthree  #1#2#3{#1}%
\def\xint_secondofthree #1#2#3{#2}%
\def\xint_thirdofthree  #1#2#3{#3}%
\def\xint_minus_andstop { -}%
\def\xint_gob_til_R     #1\R {}%
\def\xint_gob_til_W     #1\W {}%
\def\xint_gob_til_Z     #1\Z {}%
\def\xint_gob_til_zero  #10{}%
```

```
\def\xint_gob_til_one   #11{}%
\def\xint_gob_til_G     #1G{}%
\def\xint_gob_til_zeros_iii #1000{}%
\def\xint_gob_til_zeros_iv  #10000{}%
\def\xint_gob_til_relax      #1\relax {}%
\def\xint_gob_til_xint_undef #1\xint_undef {}%
\def\xint_gob_til_xint_relax #1\xint_relax {}%
\def\xint_UDzerofork      #10\dummy  #2#3\krof {#2}%
\def\xint_UDsignfork      #1-\dummy  #2#3\krof {#2}%
\def\xint_UDwfork         #1\W\dummy #2#3\krof {#2}%
\def\xint_UDzerosfork     #100\dummy #2#3\krof {#2}%
\def\xint_UDonezerofork   #110\dummy #2#3\krof {#2}%
\def\xint_UDzerominusfork #10-\dummy #2#3\krof {#2}%
\def\xint_UDsignsfork     #1--\dummy #2#3\krof {#2}%
\def\xint_afterfi #1#2\fi {\fi #1}%
\let\xint_relax\relax
\def\xint_braced_xint_relax {\xint_relax }%
\chardef\xint_c_     0
\chardef\xint_c_i    1
\chardef\xint_c_ii   2
\chardef\xint_c_iii  3
\chardef\xint_c_iv   4
\chardef\xint_c_v    5
\chardef\xint_c_viii 8
\chardef\xint_c_ix   9
\chardef\xint_c_x   10
\newcount\xint_c_x^viii  \xint_c_x^viii 100000000
```

21.4 \xintRev, \xintReverseOrder

```
\xintRev: fait l'expansion avec \romannumeral-`0, vérifie le signe.
\xintReverseOrder: ne fait PAS l'expansion, ne regarde PAS le signe.
```

```
\def\xintRev {\romannumeral0\xintrev }%
\def\xintrev #1%
{%
    \expandafter\XINT_rev_fork
    \romannumeral-`0#1\xint_relax % empty #1 ok
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
    \xint_relax
}%
\def\XINT_rev_fork #1%
{%
    \xint_UDsignfork
      #1\dummy {\expandafter\xint_minus_andstop
                \romannumeral0\XINT_rord_main {}}%
       -\dummy {\XINT_rord_main {}#1}%
    \krof
}%
```

```
\def\XINT_Rev         {\romannumeral0\XINT_rev }%
\def\xintReverseOrder {\romannumeral0\XINT_rev }%
\def\XINT_rev #1%
{%
    \XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
\def\XINT_rord_main #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_xint_undef #9\XINT_rord_cleanup\xint_undef
    \XINT_rord_main {#9#8#7#6#5#4#3#2#1}%
}%
\def\XINT_rord_cleanup\xint_undef\XINT_rord_main #1#2\xint_relax
{%
    \expandafter\space\xint_gob_til_xint_relax #1%
}%
```

21.5 \xintRevWithBraces

New with 1.06. Makes the expansion of its argument and then reverses the resulting tokens or braced tokens, adding a pair of braces to each (thus, maintaining it when it was already there.)
hmm, at some point when I was cleaning up the code towards 1.07, I have accidentally removed the {} which must be after\XINT_revwbr_loop. Corrected for 1.07a.
Damn'it all the 'noexpand' things in 1.07a were buggy, this was caused by a frivolous midnight de-commenting-out. Fixed for 1.08.

```
\def\xintRevWithBraces         {\romannumeral0\xintrevwithbraces }%
\def\xintRevWithBracesNoExpand {\romannumeral0\xintrevwithbracesnoexpand }%
\def\xintrevwithbraces #1%
{%
    \expandafter\XINT_revwbr_loop\expandafter{\expandafter}%
    \romannumeral-`0#1\xint_relax\xint_relax\xint_relax\xint_relax
                      \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\def\xintrevwithbracesnoexpand #1%
{%
    \XINT_revwbr_loop {}%
    #1\xint_relax\xint_relax\xint_relax\xint_relax
      \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\def\XINT_revwbr_loop #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_xint_relax #9\XINT_revwbr_finish_a\xint_relax
    \XINT_revwbr_loop {{#9}{#8}{#7}{#6}{#5}{#4}{#3}{#2}#1}%
}%
```

```
\def\XINT_revwbr_finish_a\xint_relax\XINT_revwbr_loop #1#2\Z
{%
    \XINT_revwbr_finish_b #2\R\R\R\R\R\R\R\Z #1%
}%
\def\XINT_revwbr_finish_b #1#2#3#4#5#6#7#8\Z
{%
    \xint_gob_til_R
            #1\XINT_revwbr_finish_c 8%
            #2\XINT_revwbr_finish_c 7%
            #3\XINT_revwbr_finish_c 6%
            #4\XINT_revwbr_finish_c 5%
            #5\XINT_revwbr_finish_c 4%
            #6\XINT_revwbr_finish_c 3%
            #7\XINT_revwbr_finish_c 2%
            \R\XINT_revwbr_finish_c 1\Z
}%
\def\XINT_revwbr_finish_c #1#2\Z
{%
    \expandafter\expandafter\expandafter
        \space
    \csname xint_gobble_\romannumeral #1\endcsname
}%
```

21.6 \xintLen, \xintLength

```
\xintLen -> fait l'expansion, ne compte PAS le signe.
\xintLength -> ne fait PAS l'expansion, compte le signe.
1.06: improved code is roughly 20% faster than the one from earlier versions.
```

```
\def\xintiLen {\romannumeral0\xintilen }%
\def\xintilen #1%
{%
    \expandafter\XINT_length_fork
    \romannumeral-`0#1\xint_relax\xint_relax\xint_relax\xint_relax
                      \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\let\xintLen\xintiLen \let\xintlen\xintilen
\def\XINT_Len #1%
{%
    \romannumeral0\XINT_length_fork
    #1\xint_relax\xint_relax\xint_relax\xint_relax
      \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\def\XINT_length_fork #1%
{%
    \expandafter\XINT_length_loop
    \xint_UDsignfork
      #1\dummy {{0}}%
       -\dummy {{0}#1}%
```

```
    \krof
}%
\def\XINT_Length {\romannumeral0\XINT_length }%
\def\XINT_length #1%
{%
    \XINT_length_loop
    {0}#1\xint_relax\xint_relax\xint_relax\xint_relax
         \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\let\xintLength\XINT_Length
\def\XINT_length_loop #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_xint_relax #9\XINT_length_finish_a\xint_relax
    \expandafter\XINT_length_loop\expandafter {\the\numexpr #1+8\relax}%
}%
\def\XINT_length_finish_a\xint_relax
    \expandafter\XINT_length_loop\expandafter #1#2\Z
{%
    \XINT_length_finish_b #2\W\W\W\W\W\W\W\Z {#1}%
}%
\def\XINT_length_finish_b #1#2#3#4#5#6#7#8\Z
{%
    \xint_gob_til_W
            #1\XINT_length_finish_c 8%
            #2\XINT_length_finish_c 7%
            #3\XINT_length_finish_c 6%
            #4\XINT_length_finish_c 5%
            #5\XINT_length_finish_c 4%
            #6\XINT_length_finish_c 3%
            #7\XINT_length_finish_c 2%
            \W\XINT_length_finish_c 1\Z
}%
\def\XINT_length_finish_c #1#2\Z #3%
   {\expandafter\space\the\numexpr #3-#1\relax}%
```

21.7 \xintCSVtoList

`\xintCSVtoList {a,b,..,z}` returns {a}{b}...{z}. The comma separated list may be a macro which is first expanded. Each chain of spaces from the initial input will be collapsed as usual by the TeX initial scanning First included in release 1.06.

```
\def\xintCSVtoList {\romannumeral0\xintcsvtolist }%
\def\xintCSVtoListNoExpand {\romannumeral0\xintcsvtolistnoexpand }%
\def\xintcsvtolist #1%
{%
    \expandafter\XINT_csvtol_loop_a\expandafter
    {\expandafter}\romannumeral-`0#1%
        ,\xint_undef,\xint_undef,\xint_undef,\xint_undef
```

```
        ,\xint_undef,\xint_undef,\xint_undef,\xint_undef,\Z
}%
\def\xintcsvtolistnoexpand #1%
{%
    \XINT_csvtol_loop_a
    {}#1,\xint_undef,\xint_undef,\xint_undef,\xint_undef
        ,\xint_undef,\xint_undef,\xint_undef,\xint_undef,\Z
}%
\def\XINT_csvtol_loop_a #1#2,#3,#4,#5,#6,#7,#8,#9,%
{%
    \xint_gob_til_xint_undef #9\XINT_csvtol_finish_a\xint_undef
    \XINT_csvtol_loop_b {#1}{{#2}{#3}{#4}{#5}{#6}{#7}{#8}{#9}}%
}%
\def\XINT_csvtol_loop_b #1#2{\XINT_csvtol_loop_a {#1#2}}%
\def\XINT_csvtol_finish_a\xint_undef\XINT_csvtol_loop_b #1#2#3\Z
{%
    \XINT_csvtol_finish_b #3\R,\R,\R,\R,\R,\R,\Z #2{#1}%
}%
\def\XINT_csvtol_finish_b #1,#2,#3,#4,#5,#6,#7,#8\Z
{%
    \xint_gob_til_R
            #1\XINT_csvtol_finish_c 8%
            #2\XINT_csvtol_finish_c 7%
            #3\XINT_csvtol_finish_c 6%
            #4\XINT_csvtol_finish_c 5%
            #5\XINT_csvtol_finish_c 4%
            #6\XINT_csvtol_finish_c 3%
            #7\XINT_csvtol_finish_c 2%
            \R\XINT_csvtol_finish_c 1\Z
}%
\def\XINT_csvtol_finish_c #1#2\Z
{%
    \csname XINT_csvtol_finish_d\romannumeral #1\endcsname
}%
\def\XINT_csvtol_finish_dviii #1#2#3#4#5#6#7#8#9{ #9}%
\def\XINT_csvtol_finish_dvii  #1#2#3#4#5#6#7#8#9{ #9{#1}}%
\def\XINT_csvtol_finish_dvi   #1#2#3#4#5#6#7#8#9{ #9{#1}{#2}}%
\def\XINT_csvtol_finish_dv    #1#2#3#4#5#6#7#8#9{ #9{#1}{#2}{#3}}%
\def\XINT_csvtol_finish_div   #1#2#3#4#5#6#7#8#9{ #9{#1}{#2}{#3}{#4}}%
\def\XINT_csvtol_finish_diii  #1#2#3#4#5#6#7#8#9{ #9{#1}{#2}{#3}{#4}{#5}}%
\def\XINT_csvtol_finish_dii   #1#2#3#4#5#6#7#8#9{ #9{#1}{#2}{#3}{#4}{#5}{#6}}%
\def\XINT_csvtol_finish_di    #1#2#3#4#5#6#7#8#9%
                                          { #9{#1}{#2}{#3}{#4}{#5}{#6}{#7}}%
```

21.8 \xintListWithSep

```
\xintListWithSep {sep}{{a}{b}...{z}} returns a sep b sep .... sep z
Included in release 1.04. The 'sep' can be \par's: the macro xintlistwithsep
etc... are all declared long. 'sep' does not have to be a single token. The list
```

```
may be a macro it is first expanded. 1.06 modifies the 'feature' of returning
sep if the list is empty: the output is now empty in that case. (sep was not
used for a one element list, but strangely it was for a zero-element list).
```

```
\def\xintListWithSep {\romannumeral0\xintlistwithsep }%
\def\xintListWithSepNoExpand {\romannumeral0\xintlistwithsepnoexpand }%
\long\def\xintlistwithsep #1#2%
    {\expandafter\XINT_lws\expandafter {\romannumeral-`0#2}{#1}}%
\long\def\XINT_lws #1#2{\XINT_lws_start {#2}#1\Z }%
\long\def\xintlistwithsepnoexpand #1#2{\XINT_lws_start {#1}#2\Z }%
\long\def\XINT_lws_start #1#2%
{%
    \xint_gob_til_Z #2\XINT_lws_dont\Z
    \XINT_lws_loop_a {#2}{#1}%
}%
\long\def\XINT_lws_dont\Z\XINT_lws_loop_a #1#2{ }%
\long\def\XINT_lws_loop_a #1#2#3%
{%
    \xint_gob_til_Z #3\XINT_lws_end\Z
    \XINT_lws_loop_b {#1}{#2#3}{#2}%
}%
\long\def\XINT_lws_loop_b #1#2{\XINT_lws_loop_a {#1#2}}%
\long\def\XINT_lws_end\Z\XINT_lws_loop_b #1#2#3{ #1}%
```

21.9 \xintNthElt

```
\xintNthElt {i}{{a}{b}...{z}} (or 'tokens' abcd...z) returns the i th element
(one pair of braces removed). The list is first expanded. First included in re-
lease 1.06. With 1.06a, a value of i = 0 (or negative) makes the macro return
the length. This is different from \xintLen which is for numbers (checks sign)
and different from \xintLength which does not first expand its argument.
```

```
\def\xintNthElt         {\romannumeral0\xintnthelt }%
\def\xintNthEltNoExpand {\romannumeral0\xintntheltnoexpand }%
\def\xintnthelt #1#2%
{%
    \expandafter\XINT_nthelt\expandafter {\romannumeral-`0#2}%
                                         {\numexpr #1\relax }%
}%
\def\xintntheltnoexpand #1#2%
{%
    \XINT_nthelt {#2}{\numexpr #1\relax}%
}%
\def\XINT_nthelt #1#2%
{%
    \ifnum #2>\xint_c_
          \xint_afterfi {\XINT_nthelt_loop_a {#2}}%
    \else
          \xint_afterfi {\XINT_length_loop {0}}%
```

```
    \fi #1\xint_relax\xint_relax\xint_relax\xint_relax
          \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\def\XINT_nthelt_loop_a #1%
{%
    \ifnum #1>\xint_c_viii
        \expandafter\XINT_nthelt_loop_b
    \else
        \expandafter\XINT_nthelt_getit
    \fi
    {#1}%
}%
\def\XINT_nthelt_loop_b #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_xint_relax #9\XINT_nthelt_silentend\xint_relax
    \expandafter\XINT_nthelt_loop_a\expandafter{\the\numexpr #1-8\relax}%
}%
\def\XINT_nthelt_silentend #1\Z { }%
\def\XINT_nthelt_getit #1%
{%
    \expandafter\expandafter\expandafter\XINT_nthelt_finish
    \csname xint_gobble_\romannumeral\numexpr#1-1\endcsname
}%
\def\XINT_nthelt_finish #1#2\Z
{%
    \xint_UDwfork
      #1\dummy { }%
      \W\dummy { #1}%
    \krof
}%
```

21.10 \xintApply

```
\xintApply {\macro}{{a}{b}...{z}} returns {\macro{a}}...{\macro{b}} where each
instance of \macro is expanded. The list is first expanded. Introduced with re-
lease 1.04
```

```
\def\xintApply         {\romannumeral0\xintapply }%
\def\xintApplyNoExpand {\romannumeral0\xintapplynoexpand }%
\def\xintapply #1#2%
{%
    \expandafter\XINT_apply\expandafter {\romannumeral-`0#2}%
    {#1}%
}%
\def\XINT_apply #1#2{\XINT_apply_loop_a {}{#2}#1\Z }%
\def\xintapplynoexpand #1#2{\XINT_apply_loop_a {}{#1}#2\Z }%
\def\XINT_apply_loop_a #1#2#3%
{%
    \xint_gob_til_Z #3\XINT_apply_end\Z
```

```
    \expandafter
    \XINT_apply_loop_b
    \expandafter {\romannumeral-`0#2{#3}}{#1}{#2}%
}%
\def\XINT_apply_loop_b #1#2{\XINT_apply_loop_a {#2{#1}}}%
\def\XINT_apply_end\Z\expandafter\XINT_apply_loop_b\expandafter #1#2#3{ #2}%
```

21.11 \xintApplyUnbraced

```
\xintApplyUnbraced {\macro}{{a}{b}...{z}} returns \macro{a}...\macro{b} where
each instance of \macro is expanded using \romannumeral-`0. No braces are added:
this allows for example a non-expandable \def in \macro, without having to do
\gdef. The list is first expanded. Introduced with release 1.06b
```

```
\def\xintApplyUnbraced {\romannumeral0\xintapplyunbraced }%
\def\xintApplyUnbracedNoExpand {\romannumeral0\xintapplyunbracednoexpand }%
\def\xintapplyunbraced #1#2%
{%
    \expandafter\XINT_applyunbr\expandafter {\romannumeral-`0#2}%
    {#1}%
}%
\def\XINT_applyunbr #1#2{\XINT_applyunbr_loop_a {}{#2}#1\Z }%
\def\xintapplyunbracednoexpand #1#2%
   {\XINT_applyunbr_loop_a {}{#1}#2\Z }%
\def\XINT_applyunbr_loop_a #1#2#3%
{%
    \xint_gob_til_Z #3\XINT_applyunbr_end\Z
    \expandafter\XINT_applyunbr_loop_b
    \expandafter {\romannumeral-`0#2{#3}}{#1}{#2}%
}%
\def\XINT_applyunbr_loop_b #1#2{\XINT_applyunbr_loop_a {#2#1}}%
\def\XINT_applyunbr_end\Z
    \expandafter\XINT_applyunbr_loop_b\expandafter #1#2#3{ #2}%
```

21.12 \xintAssign, \xintAssignArray, \xintDigitsOf

```
\xintAssign {a}{b}..{z}\to\A\B...\Z,
\xintAssignArray {a}{b}..{z}\to\U
  version 1.01 corrects an oversight in 1.0 related to the value of \escapechar
at the time of using \xintAssignArray or \xintRelaxArray These macros are an
exception in the xint bundle, they do not care at all about compatibility with
expansion-only contexts.
  In version 1.05a I suddenly see some incongruous \expandafter's in (what is
called now) \XINT_assignarray_end_c, which I remove.
  Release 1.06 modifies the macros created by \xintAssignArray to feed their
argument to a \numexpr.
  Release 1.06a detects an incredible typo in 1.01, (bad copy-paste from \xin-
tRelaxArray) which caused \xintAssignArray to use #1 rather than the #2 as in
```

```
the correct earlier 1.0 version!!! This went through undetected because \xint_arrayname,
although weird, was still usable: the probability to overwrite something was
almost zero. The bug got finally revealed doing \xintAssignArray {}{}{}\to\Stuff.
  With release 1.06b an empty argument (or expanding to empty) to \xintAssig-
nArray is ok.

\def\xintAssign #1\to
{%
    \expandafter\XINT_assign_a\romannumeral-`0#1{}\to
}%
\def\XINT_assign_a #1% attention to the # at the beginning of next line
#{%
    \def\xint_temp {#1}%
    \ifx\empty\xint_temp
        \expandafter\XINT_assign_b
    \else
        \expandafter\XINT_assign_B
    \fi
}%
\def\XINT_assign_b #1#2\to #3%
{%
    \edef #3{#1}\def\xint_temp {#2}%
    \ifx\empty\xint_temp
      \else
      \xint_afterfi{\XINT_assign_a #2\to }%
    \fi
}%
\def\XINT_assign_B #1\to #2%
{%
    \edef #2{\xint_temp}%
}%
\def\xintRelaxArray #1%
{%
    \edef\XINT_restoreescapechar {\escapechar\the\escapechar\relax}%
    \escapechar -1
    \edef\xint_arrayname {\string #1}%
    \XINT_restoreescapechar
    \expandafter\let\expandafter\xint_temp
                \csname\xint_arrayname 0\endcsname
    \count 255 0
    \loop
      \global\expandafter\let
             \csname\xint_arrayname\the\count255\endcsname\relax
      \ifnum \count 255 < \xint_temp
      \advance\count 255 1
    \repeat
    \global\expandafter\let\csname\xint_arrayname 00\endcsname\relax
    \global\let #1\relax
}%
```

```
\def\xintAssignArray #1\to #2% 1.06b: #1 may now be empty
{%
    \edef\XINT_restoreescapechar {\escapechar\the\escapechar\relax }%
    \escapechar -1
    \edef\xint_arrayname {\string #2}%
    \XINT_restoreescapechar
    \count 255 0
    \expandafter\XINT_assignarray_loop \romannumeral-`0#1\xint_relax
    \csname\xint_arrayname 00\endcsname
    \csname\xint_arrayname 0\endcsname
    {\xint_arrayname}%
    #2%
}%
\def\XINT_assignarray_loop #1%
{%
    \def\xint_temp {#1}%
    \ifx\xint_braced_xint_relax\xint_temp
       \expandafter\edef\csname\xint_arrayname 0\endcsname{\the\count 255 }%
       \expandafter\expandafter\expandafter\XINT_assignarray_end_a
    \else
       \advance\count 255 1
       \expandafter\edef
          \csname\xint_arrayname\the\count 255\endcsname{\xint_temp }%
       \expandafter\XINT_assignarray_loop
    \fi
}%
\def\XINT_assignarray_end_a #1%
{%
    \expandafter\XINT_assignarray_end_b\expandafter #1%
}%
\def\XINT_assignarray_end_b #1#2#3%
{%
    \expandafter\XINT_assignarray_end_c
    \expandafter #1\expandafter #2\expandafter {#3}%
}%
\def\XINT_assignarray_end_c #1#2#3#4%
{%
    \def #4##1%
    {%
        \romannumeral0\expandafter #1\expandafter{\the\numexpr ##1}%
    }%
    \def #1##1%
    {%
        \ifnum ##1< 0
            \xint_afterfi {\xintError:ArrayIndexIsNegative\space 0}%
        \else
            \xint_afterfi {%
              \ifnum ##1>#2
                  \xint_afterfi {\xintError:ArrayIndexBeyondLimit\space 0}%
```

```
                \else
                    \xint_afterfi
                    {\expandafter\expandafter\expandafter
                     \space\csname #3##1\endcsname}%
                \fi}%
        \fi
    }%
}%
\let\xintDigitsOf\xintAssignArray
```

21.13 \XINT_RQ

cette macro renverse et ajoute le nombre minimal de zéros à la fin pour que la longueur soit alors multiple de 4
\romannumeral0\XINT_RQ {}<le truc à renverser>\R\R\R\R\R\R\R\R\Z
Attention, ceci n'est utilisé que pour des chaînes de chiffres, et donc le comportement avec des {..} ou autres espaces n'a fait l'objet d'aucune attention

```
\def\XINT_RQ #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_R #9\XINT_RQ_end_a\R\XINT_RQ {#9#8#7#6#5#4#3#2#1}%
}%
\def\XINT_RQ_end_a\R\XINT_RQ #1#2\Z
{%
    \XINT_RQ_end_b #1\Z
}%
\def\XINT_RQ_end_b #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_R
            #8\XINT_RQ_end_viii
            #7\XINT_RQ_end_vii
            #6\XINT_RQ_end_vi
            #5\XINT_RQ_end_v
            #4\XINT_RQ_end_iv
            #3\XINT_RQ_end_iii
            #2\XINT_RQ_end_ii
            \R\XINT_RQ_end_i
            \Z #2#3#4#5#6#7#8%
}%
\def\XINT_RQ_end_viii #1\Z #2#3#4#5#6#7#8#9\Z { #9}%
\def\XINT_RQ_end_vii  #1\Z #2#3#4#5#6#7#8#9\Z { #8#9000}%
\def\XINT_RQ_end_vi   #1\Z #2#3#4#5#6#7#8#9\Z { #7#8#900}%
\def\XINT_RQ_end_v    #1\Z #2#3#4#5#6#7#8#9\Z { #6#7#8#90}%
\def\XINT_RQ_end_iv   #1\Z #2#3#4#5#6#7#8#9\Z { #5#6#7#8#9}%
\def\XINT_RQ_end_iii  #1\Z #2#3#4#5#6#7#8#9\Z { #4#5#6#7#8#9000}%
\def\XINT_RQ_end_ii   #1\Z #2#3#4#5#6#7#8#9\Z { #3#4#5#6#7#8#900}%
\def\XINT_RQ_end_i      \Z #1#2#3#4#5#6#7#8\Z { #1#2#3#4#5#6#7#80}%
\def\XINT_SQ #1#2#3#4#5#6#7#8%
{%
```

```
    \xint_gob_til_R #8\XINT_SQ_end_a\R\XINT_SQ {#8#7#6#5#4#3#2#1}%
}%
\def\XINT_SQ_end_a\R\XINT_SQ #1#2\Z
{%
    \XINT_SQ_end_b #1\Z
}%
\def\XINT_SQ_end_b #1#2#3#4#5#6#7%
{%
    \xint_gob_til_R
            #7\XINT_SQ_end_vii
            #6\XINT_SQ_end_vi
            #5\XINT_SQ_end_v
            #4\XINT_SQ_end_iv
            #3\XINT_SQ_end_iii
            #2\XINT_SQ_end_ii
            \R\XINT_SQ_end_i
            \Z #2#3#4#5#6#7%
}%
\def\XINT_SQ_end_vii  #1\Z #2#3#4#5#6#7#8\Z { #8}%
\def\XINT_SQ_end_vi   #1\Z #2#3#4#5#6#7#8\Z { #7#8000000}%
\def\XINT_SQ_end_v    #1\Z #2#3#4#5#6#7#8\Z { #6#7#800000}%
\def\XINT_SQ_end_iv   #1\Z #2#3#4#5#6#7#8\Z { #5#6#7#80000}%
\def\XINT_SQ_end_iii  #1\Z #2#3#4#5#6#7#8\Z { #4#5#6#7#8000}%
\def\XINT_SQ_end_ii   #1\Z #2#3#4#5#6#7#8\Z { #3#4#5#6#7#800}%
\def\XINT_SQ_end_i      \Z #1#2#3#4#5#6#7\Z { #1#2#3#4#5#6#70}%
\def\XINT_OQ #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_R #9\XINT_OQ_end_a\R\XINT_OQ {#9#8#7#6#5#4#3#2#1}%
}%
\def\XINT_OQ_end_a\R\XINT_OQ #1#2\Z
{%
    \XINT_OQ_end_b #1\Z
}%
\def\XINT_OQ_end_b #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_R
            #8\XINT_OQ_end_viii
            #7\XINT_OQ_end_vii
            #6\XINT_OQ_end_vi
            #5\XINT_OQ_end_v
            #4\XINT_OQ_end_iv
            #3\XINT_OQ_end_iii
            #2\XINT_OQ_end_ii
            \R\XINT_OQ_end_i
            \Z #2#3#4#5#6#7#8%
}%
\def\XINT_OQ_end_viii #1\Z #2#3#4#5#6#7#8#9\Z { #9}%
\def\XINT_OQ_end_vii  #1\Z #2#3#4#5#6#7#8#9\Z { #8#90000000}%
\def\XINT_OQ_end_vi   #1\Z #2#3#4#5#6#7#8#9\Z { #7#8#9000000}%
```

```
\def\XINT_OQ_end_v    #1\Z #2#3#4#5#6#7#8#9\Z { #6#7#8#900000}%
\def\XINT_OQ_end_iv   #1\Z #2#3#4#5#6#7#8#9\Z { #5#6#7#8#90000}%
\def\XINT_OQ_end_iii  #1\Z #2#3#4#5#6#7#8#9\Z { #4#5#6#7#8#9000}%
\def\XINT_OQ_end_ii   #1\Z #2#3#4#5#6#7#8#9\Z { #3#4#5#6#7#8#900}%
\def\XINT_OQ_end_i      \Z #1#2#3#4#5#6#7#8\Z { #1#2#3#4#5#6#7#80}%
```

21.14 \XINT_cuz

```
\def\xint_cleanupzeros_andstop #1#2#3#4%
{%
    \expandafter\space\the\numexpr #1#2#3#4\relax
}%
\def\xint_cleanupzeros_nospace #1#2#3#4%
{%
    \the\numexpr #1#2#3#4\relax
}%
\def\XINT_rev_andcuz #1%
{%
    \expandafter\xint_cleanupzeros_andstop
    \romannumeral0\XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
```

```
routine CleanUpZeros. Utilisée en particulier par la soustraction.
INPUT: longueur **multiple de 4** (<-- ATTENTION)
OUTPUT: on a retiré tous les leading zéros, on n'est **plus* nécessairement de
longueur 4n
Délimiteur pour _main: \W\W\W\W\W\W\W\Z avec SEPT \W
```

```
\def\XINT_cuz #1%
{%
    \XINT_cuz_loop #1\W\W\W\W\W\W\W\Z%
}%
\def\XINT_cuz_loop #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_W #8\xint_cuz_end_a\W
    \xint_gob_til_Z #8\xint_cuz_end_A\Z
    \XINT_cuz_check_a {#1#2#3#4#5#6#7#8}%
}%
\def\xint_cuz_end_a #1\XINT_cuz_check_a #2%
{%
    \xint_cuz_end_b #2%
}%
\def\xint_cuz_end_b #1#2#3#4#5\Z
{%
    \expandafter\space\the\numexpr #1#2#3#4\relax
}%
```

```
\def\xint_cuz_end_A \Z\XINT_cuz_check_a #1{ 0}%
\def\XINT_cuz_check_a #1%
{%
    \expandafter\XINT_cuz_check_b\the\numexpr #1\relax
}%
\def\XINT_cuz_check_b #1%
{%
    \xint_gob_til_zero #1\xint_cuz_backtoloop 0\XINT_cuz_stop #1%
}%
\def\XINT_cuz_stop #1\W #2\Z{ #1}%
\def\xint_cuz_backtoloop 0\XINT_cuz_stop 0{\XINT_cuz_loop }%
```

21.15 \XINT_isOne

```
Added in 1.03. Attention: does not do any expansion.
```

```
\def\XINT_isOne #1{\romannumeral0\XINT_isone #1\W\Z }%
\def\XINT_isone #1#2%
{%
    \xint_gob_til_one #1\XINT_isone_b 1%
    \expandafter\space\expandafter 0\xint_gob_til_Z #2%
}%
\def\XINT_isone_b #1\xint_gob_til_Z #2%
{%
    \xint_gob_til_W #2\XINT_isone_yes \W
    \expandafter\space\expandafter 0\xint_gob_til_Z
}%
\def\XINT_isone_yes #1\Z { 1}%
```

21.16 \xintNum

```
For example \xintNum {----+-++---+----000000000000003}
1.05 defines \xintiNum, which allows redefinition of \xintNum by xintfrac.sty
Slightly modified in 1.06b (\R->\xint_relax) to avoid initial re-scan of in-
put stack (while still allowing empty #1)
```

```
\def\xintiNum {\romannumeral0\xintinum }%
\def\xintinum #1%
{%
    \expandafter\XINT_num_loop
    \romannumeral-`0#1\xint_relax\xint_relax\xint_relax\xint_relax
                       \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\let\xintNum\xintiNum \let\xintnum\xintinum
\def\XINT_num #1%
{%
    \XINT_num_loop #1\xint_relax\xint_relax\xint_relax\xint_relax
                      \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
```

```
\def\XINT_num_loop #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_xint_relax #8\XINT_num_end\xint_relax
    \XINT_num_NumEight #1#2#3#4#5#6#7#8%
}%
\def\XINT_num_end\xint_relax\XINT_num_NumEight #1\xint_relax #2\Z
{%
    \expandafter\space\the\numexpr #1+0\relax
}%
\def\XINT_num_NumEight #1#2#3#4#5#6#7#8%
{%
    \ifnum \numexpr #1#2#3#4#5#6#7#8+0= 0
      \xint_afterfi {\expandafter\XINT_num_keepsign_a
                     \the\numexpr #1#2#3#4#5#6#7#81\relax}%
    \else
      \xint_afterfi {\expandafter\XINT_num_finish
                     \the\numexpr #1#2#3#4#5#6#7#8\relax}%
    \fi
}%
\def\XINT_num_keepsign_a #1%
{%
    \xint_gob_til_one#1\XINT_num_gobacktoloop 1\XINT_num_keepsign_b
}%
\def\XINT_num_gobacktoloop 1\XINT_num_keepsign_b {\XINT_num_loop }%
\def\XINT_num_keepsign_b #1{\XINT_num_loop -}%
\def\XINT_num_finish #1\xint_relax #2\Z { #1}%
```

21.17 \xintSgn

Changed in 1.05. Earlier code was unnecessarily strange.

```
\def\xintiSgn {\romannumeral0\xintisgn }%
\def\xintisgn #1%
{%
    \expandafter\XINT_sgn \romannumeral-`0#1\Z%
}%
\let\xintSgn\xintiSgn \let\xintsgn\xintisgn
\def\XINT_Sgn #1{\romannumeral0\XINT_sgn #1\Z }%
\def\XINT_sgn #1#2\Z
{%
    \xint_UDzerominusfork
      #1-\dummy  { 0}%
      0#1\dummy  { -1}%
       0-\dummy  { 1}%
    \krof
}%
```

21.18 \xintSgnFork

Expandable three-way fork added in 1.07. It is not used in the code but is provided for use inside the arguments to the package macros. The argument #1 must expand to -1,0 or 1. A \count should be put within a \numexpr..\relax.

```
\def\xintSgnFork {\romannumeral0\xintsgnfork }%
\def\xintsgnfork #1%
{%
    \ifcase #1 \xint_afterfi{\expandafter\space\xint_secondofthree}%
            \or\xint_afterfi{\expandafter\space\xint_thirdofthree}%
          \else\xint_afterfi{\expandafter\space\xint_firstofthree}%
    \fi
}%
```

21.19 \xintOpp

```
\def\xintiOpp {\romannumeral0\xintiopp }%
\def\xintiopp #1%
{%
    \expandafter\XINT_opp \romannumeral-`0#1%
}%
\let\xintOpp\xintiOpp \let\xintopp\xintiopp
\def\XINT_Opp #1{\romannumeral0\XINT_opp #1}%
\def\XINT_opp #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  { 0}%      zero
      0#1\dummy  { }%     negative
       0-\dummy  { -#1}%  positive
    \krof
}%
```

21.20 \xintAbs

```
\def\xintiAbs {\romannumeral0\xintiabs }%
\def\xintiabs #1%
{%
    \expandafter\XINT_abs \romannumeral-`0#1%
}%
\let\xintAbs\xintiAbs \let\xintabs\xintiabs
\def\XINT_Abs #1{\romannumeral0\XINT_abs #1}%
\def\XINT_abs #1%
{%
    \xint_UDsignfork
      #1\dummy  { }%
       -\dummy  { #1}%
    \krof
}%
```

```
-----------------------------------------------------------------
-----------------------------------------------------------------
ARITHMETIC OPERATIONS: ADDITION, SUBTRACTION, SUMS, MULTIPLICATION, PRODUCTS,
FACTORIAL, POWERS, EUCLIDEAN DIVISION.
  Release 1.03 re-organizes sub-routines to facilitate future developments: the
diverse variants of addition, with diverse conditions on inputs and output are
first listed; they will be used in multiplication, or in the summation, or in
the power routines. I am aware that the commenting is close to non-existent,
sorry about that.
  ADDITION I: \XINT_add_A
  INPUT:
\romannumeral0\XINT_add_A 0{}<N1>\W\X\Y\Z <N2>\W\X\Y\Z
1. <N1> et <N2> renversés
2. de longueur 4n (avec des leading zéros éventuels)
3. l'un des deux ne doit pas se terminer par 0000
[Donc on peut avoir 0000 comme input si l'autre est >0 et ne se termine pas en
0000 bien sûr]. On peut avoir l'un des deux vides. Mais alors l'autre ne doit
être ni vide ni 0000.
  OUTPUT: la somme <N1>+<N2>, ordre normal, plus sur 4n, pas de leading zeros
La procédure est plus rapide lorsque <N1> est le plus court des deux.
Nota bene: (30 avril 2013). J'ai une version qui est deux fois plus rapide sur
des nombres d'environ 1000 chiffres chacun, et qui commence à être avantageuse
pour des nombres d'au moins 200 chiffres. Cependant il serait vraiment compliqué
d'en étendre l'utilisation aux emplois de l'addition dans les autres routines,
comme celle de multiplication ou celle de division; et son implémentation ajouterait
au minimum la mesure de la longueur des summands.
```

```
\def\XINT_add_A #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_add_az\W
    \XINT_add_AB #1{#3#4#5#6}{#2}%
}%
\def\xint_add_az\W\XINT_add_AB #1#2%
{%
    \XINT_add_AC_checkcarry #1%
}%
```

```
ici #2 est prévu pour l'addition, mais attention il devra être renversé pour
\numexpr. #3 = résultat partiel. #4 = chiffres qui restent. On vérifie si le
deuxième nombre s'arrête.
```

```
\def\XINT_add_AB #1#2#3#4\W\X\Y\Z #5#6#7#8%
{%
    \xint_gob_til_W #5\xint_add_bz\W
    \XINT_add_ABE #1#2{#8#7#6#5}{#3}#4\W\X\Y\Z
}%
\def\XINT_add_ABE #1#2#3#4#5#6%
{%
    \expandafter\XINT_add_ABEA\the\numexpr #1+10#5#4#3#2+#6\relax.%
}%
```

```
\def\XINT_add_ABEA #1#2#3.#4%
{%
    \XINT_add_A  #2{#3#4}%
}%

ici le deuxième nombre est fini #6 part à la poubelle, #2#3#4#5 est le #2 dans
\XINT_add_AB on ne vérifie pas la retenue cette fois, mais les fois suivantes

\def\xint_add_bz\W\XINT_add_ABE #1#2#3#4#5#6%
{%
    \expandafter\XINT_add_CC\the\numexpr #1+10#5#4#3#2\relax.%
}%
\def\XINT_add_CC #1#2#3.#4%
{%
    \XINT_add_AC_checkcarry  #2{#3#4}% on va examiner et \'eliminer #2
}%

retenue plus chiffres qui restent de l'un des deux nombres. #2 = résultat par-
tiel #3#4#5#6 = summand, avec plus significatif à droite

\def\XINT_add_AC_checkcarry #1%
{%
    \xint_gob_til_zero #1\xint_add_AC_nocarry 0\XINT_add_C
}%
\def\xint_add_AC_nocarry 0\XINT_add_C #1#2\W\X\Y\Z
{%
    \expandafter
    \xint_cleanupzeros_andstop
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1%
}%
\def\XINT_add_C #1#2#3#4#5%
{%
    \xint_gob_til_W #2\xint_add_cz\W
    \XINT_add_CD {#5#4#3#2}{#1}%
}%
\def\XINT_add_CD #1%
{%
    \expandafter\XINT_add_CC\the\numexpr 1+10#1\relax.%
}%
\def\xint_add_cz\W\XINT_add_CD #1#2{ 1#2}%

Addition II: \XINT_addr_A.
INPUT: \romannumeral0\XINT_addr_A 0{}<N1>\W\X\Y\Z <N2>\W\X\Y\Z
  Comme \XINT_add_A, la différence principale c'est qu'elle donne son résul-
tat aussi *sur 4n*, renversé. De plus cette variante accepte que l'un ou même
```

```
les deux inputs soient vides. Utilisé par la sommation et par la division (pour
les quotients). Et aussi par la multiplication d'ailleurs.
INPUT: comme pour \XINT_add_A
1. <N1> et <N2> renversés
2. de longueur 4n (avec des leading zéros éventuels)
3. l'un des deux ne doit pas se terminer par 0000
OUTPUT: la somme <N1>+<N2>, *aussi renversée* et *sur 4n*
\def\XINT_addr_A #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_addr_az\W
    \XINT_addr_B #1{#3#4#5#6}{#2}%
}%
\def\xint_addr_az\W\XINT_addr_B #1#2%
{%
    \XINT_addr_AC_checkcarry #1%
}%
\def\XINT_addr_B #1#2#3#4\W\X\Y\Z #5#6#7#8%
{%
    \xint_gob_til_W #5\xint_addr_bz\W
    \XINT_addr_E #1#2{#8#7#6#5}{#3}#4\W\X\Y\Z
}%
\def\XINT_addr_E #1#2#3#4#5#6%
{%
    \expandafter\XINT_addr_ABEA\the\numexpr #1+10#5#4#3#2+#6\relax
}%
\def\XINT_addr_ABEA #1#2#3#4#5#6#7%
{%
    \XINT_addr_A  #2{#7#6#5#4#3}%
}%
\def\xint_addr_bz\W\XINT_addr_E #1#2#3#4#5#6%
{%
    \expandafter\XINT_addr_CC\the\numexpr #1+10#5#4#3#2\relax
}%
\def\XINT_addr_CC #1#2#3#4#5#6#7%
{%
    \XINT_addr_AC_checkcarry  #2{#7#6#5#4#3}%
}%
\def\XINT_addr_AC_checkcarry #1%
{%
    \xint_gob_til_zero #1\xint_addr_AC_nocarry 0\XINT_addr_C
}%
\def\xint_addr_AC_nocarry 0\XINT_addr_C #1#2\W\X\Y\Z { #1#2}%
\def\XINT_addr_C #1#2#3#4#5%
{%
    \xint_gob_til_W #2\xint_addr_cz\W
    \XINT_addr_D {#5#4#3#2}{#1}%
}%
\def\XINT_addr_D #1%
{%
```

```
    \expandafter\XINT_addr_CC\the\numexpr 1+10#1\relax
}%
\def\xint_addr_cz\W\XINT_addr_D #1#2{ #21000}%

 ADDITION III, \XINT_addm_A
 INPUT:\romannumeral0\XINT_addm_A 0{}<N1>\W\X\Y\Z <N2>\W\X\Y\Z
 1. <N1> et <N2> renversés
 2. <N1> de longueur 4n ; <N2> non
 3. <N2> est *garanti au moins aussi long* que <N1>
 OUTPUT: la somme <N1>+<N2>, ordre normal, pas sur 4n, leading zeros retirés.
 Utilisé par la multiplication.

\def\XINT_addm_A #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_addm_az\W
    \XINT_addm_AB #1{#3#4#5#6}{#2}%
}%
\def\xint_addm_az\W\XINT_addm_AB #1#2%
{%
    \XINT_addm_AC_checkcarry #1%
}%
\def\XINT_addm_AB #1#2#3#4\W\X\Y\Z #5#6#7#8%
{%
    \XINT_addm_ABE #1#2{#8#7#6#5}{#3}#4\W\X\Y\Z
}%
\def\XINT_addm_ABE #1#2#3#4#5#6%
{%
    \expandafter\XINT_addm_ABEA\the\numexpr #1+10#5#4#3#2+#6\relax.%
}%
\def\XINT_addm_ABEA #1#2#3.#4%
{%
    \XINT_addm_A  #2{#3#4}%
}%
\def\XINT_addm_AC_checkcarry #1%
{%
    \xint_gob_til_zero #1\xint_addm_AC_nocarry 0\XINT_addm_C
}%
\def\xint_addm_AC_nocarry 0\XINT_addm_C #1#2\W\X\Y\Z
{%
    \expandafter
    \xint_cleanupzeros_andstop
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1%
}%
\def\XINT_addm_C #1#2#3#4#5%
```

```
{%
    \xint_gob_til_W
    #5\xint_addm_cw
    #4\xint_addm_cx
    #3\xint_addm_cy
    #2\xint_addm_cz
    \W\XINT_addm_CD {#5#4#3#2}{#1}%
}%
\def\XINT_addm_CD #1%
{%
    \expandafter\XINT_addm_CC\the\numexpr 1+10#1\relax.%
}%
\def\XINT_addm_CC #1#2#3.#4%
{%
    \XINT_addm_AC_checkcarry  #2{#3#4}%
}%
\def\xint_addm_cw
    #1\xint_addm_cx
    #2\xint_addm_cy
    #3\xint_addm_cz
    \W\XINT_addm_CD
{%
    \expandafter\XINT_addm_CDw\the\numexpr 1+#1#2#3\relax.%
}%
\def\XINT_addm_CDw #1.#2#3\X\Y\Z
{%
    \XINT_addm_end #1#3%
}%
\def\xint_addm_cx
    #1\xint_addm_cy
    #2\xint_addm_cz
    \W\XINT_addm_CD
{%
    \expandafter\XINT_addm_CDx\the\numexpr 1+#1#2\relax.%
}%
\def\XINT_addm_CDx #1.#2#3\Y\Z
{%
    \XINT_addm_end #1#3%
}%
\def\xint_addm_cy
    #1\xint_addm_cz
    \W\XINT_addm_CD
{%
    \expandafter\XINT_addm_CDy\the\numexpr 1+#1\relax.%
}%
\def\XINT_addm_CDy  #1.#2#3\Z
{%
    \XINT_addm_end #1#3%
}%
```

```
\def\xint_addm_cz\W\XINT_addm_CD #1#2#3{\XINT_addm_end #1#3}%
\def\XINT_addm_end #1#2#3#4#5%
    {\expandafter\space\the\numexpr #1#2#3#4#5\relax}%
```

```
ADDITION IV, variante \XINT_addp_A
INPUT: \romannumeral0\XINT_addp_A 0{}<N1>\W\X\Y\Z <N2>\W\X\Y\Z
1. <N1> et <N2> renversés
2. <N1> de longueur 4n ; <N2> non
3. <N2> est *garanti au moins aussi long* que <N1>
OUTPUT: la somme <N1>+<N2>, dans l'ordre renversé, sur 4n, et en faisant at-
tention de ne pas terminer en 0000. Utilisé par la multiplication servant pour
le calcul des puissances.
```

```
\def\XINT_addp_A #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_addp_az\W
    \XINT_addp_AB #1{#3#4#5#6}{#2}%
}%
\def\xint_addp_az\W\XINT_addp_AB #1#2%
{%
    \XINT_addp_AC_checkcarry #1%
}%
\def\XINT_addp_AC_checkcarry #1%
{%
    \xint_gob_til_zero #1\xint_addp_AC_nocarry 0\XINT_addp_C
}%
\def\xint_addp_AC_nocarry 0\XINT_addp_C
{%
    \XINT_addp_F
}%
\def\XINT_addp_AB #1#2#3#4\W\X\Y\Z #5#6#7#8%
{%
    \XINT_addp_ABE #1#2{#8#7#6#5}{#3}#4\W\X\Y\Z
}%
\def\XINT_addp_ABE #1#2#3#4#5#6%
{%
    \expandafter\XINT_addp_ABEA\the\numexpr #1+10#5#4#3#2+#6\relax
}%
\def\XINT_addp_ABEA #1#2#3#4#5#6#7%
{%
   \XINT_addp_A  #2{#7#6#5#4#3}%<-- attention on met donc \`a droite
}%
\def\XINT_addp_C #1#2#3#4#5%
{%
    \xint_gob_til_W
    #5\xint_addp_cw
    #4\xint_addp_cx
    #3\xint_addp_cy
    #2\xint_addp_cz
    \W\XINT_addp_CD   {#5#4#3#2}{#1}%
```

```
}%
\def\XINT_addp_CD #1%
{%
    \expandafter\XINT_addp_CC\the\numexpr 1+10#1\relax
}%
\def\XINT_addp_CC #1#2#3#4#5#6#7%
{%
    \XINT_addp_AC_checkcarry  #2{#7#6#5#4#3}%
}%
\def\xint_addp_cw
    #1\xint_addp_cx
    #2\xint_addp_cy
    #3\xint_addp_cz
    \W\XINT_addp_CD
{%
    \expandafter\XINT_addp_CDw\the\numexpr \xint_c_i+10#1#2#3\relax
}%
\def\XINT_addp_CDw #1#2#3#4#5#6%
{%
    \xint_gob_til_zeros_iv #2#3#4#5\XINT_addp_endDw_zeros
                           0000\XINT_addp_endDw #2#3#4#5%
}%
\def\XINT_addp_endDw_zeros 0000\XINT_addp_endDw 0000#1\X\Y\Z{ #1}%
\def\XINT_addp_endDw #1#2#3#4#5\X\Y\Z{ #5#4#3#2#1}%
\def\xint_addp_cx
    #1\xint_addp_cy
    #2\xint_addp_cz
    \W\XINT_addp_CD
{%
    \expandafter\XINT_addp_CDx\the\numexpr \xint_c_i+100#1#2\relax
}%
\def\XINT_addp_CDx #1#2#3#4#5#6%
{%
    \xint_gob_til_zeros_iv #2#3#4#5\XINT_addp_endDx_zeros
                           0000\XINT_addp_endDx #2#3#4#5%
}%
\def\XINT_addp_endDx_zeros 0000\XINT_addp_endDx 0000#1\Y\Z{ #1}%
\def\XINT_addp_endDx #1#2#3#4#5\Y\Z{ #5#4#3#2#1}%
\def\xint_addp_cy #1\xint_addp_cz\W\XINT_addp_CD
{%
    \expandafter\XINT_addp_CDy\the\numexpr \xint_c_i+1000#1\relax
}%
\def\XINT_addp_CDy #1#2#3#4#5#6%
{%
    \xint_gob_til_zeros_iv #2#3#4#5\XINT_addp_endDy_zeros
                           0000\XINT_addp_endDy #2#3#4#5%
}%
\def\XINT_addp_endDy_zeros 0000\XINT_addp_endDy 0000#1\Z{ #1}%
\def\XINT_addp_endDy #1#2#3#4#5\Z{ #5#4#3#2#1}%
```

```
\def\xint_addp_cz\W\XINT_addp_CD #1#2{ #21000}%
\def\XINT_addp_F #1#2#3#4#5%
{%
    \xint_gob_til_W
    #5\xint_addp_Gw
    #4\xint_addp_Gx
    #3\xint_addp_Gy
    #2\xint_addp_Gz
    \W\XINT_addp_G   {#2#3#4#5}{#1}%
}%
\def\XINT_addp_G #1#2%
{%
    \XINT_addp_F {#2#1}%
}%
\def\xint_addp_Gw
    #1\xint_addp_Gx
    #2\xint_addp_Gy
    #3\xint_addp_Gz
    \W\XINT_addp_G #4%
{%
    \xint_gob_til_zeros_iv  #3#2#10\XINT_addp_endGw_zeros
                            0000\XINT_addp_endGw #3#2#10%
}%
\def\XINT_addp_endGw_zeros 0000\XINT_addp_endGw 0000#1\X\Y\Z{ #1}%
\def\XINT_addp_endGw #1#2#3#4#5\X\Y\Z{ #5#1#2#3#4}%
\def\xint_addp_Gx
    #1\xint_addp_Gy
    #2\xint_addp_Gz
    \W\XINT_addp_G #3%
{%
    \xint_gob_til_zeros_iv  #2#100\XINT_addp_endGx_zeros
                           0000\XINT_addp_endGx #2#100%
}%
\def\XINT_addp_endGx_zeros 0000\XINT_addp_endGx 0000#1\Y\Z{ #1}%
\def\XINT_addp_endGx #1#2#3#4#5\Y\Z{ #5#1#2#3#4}%
\def\xint_addp_Gy
    #1\xint_addp_Gz
    \W\XINT_addp_G #2%
{%
    \xint_gob_til_zeros_iv   #1000\XINT_addp_endGy_zeros
                           0000\XINT_addp_endGy #1000%
}%
\def\XINT_addp_endGy_zeros 0000\XINT_addp_endGy 0000#1\Z{ #1}%
\def\XINT_addp_endGy #1#2#3#4#5\Z{ #5#1#2#3#4}%
\def\xint_addp_Gz\W\XINT_addp_G #1#2{ #2}%
```

21.21 \xintAdd

```
\def\xintiAdd {\romannumeral0\xintiadd }%
\def\xintiadd #1%
```

```
{%
    \expandafter\xint_add\expandafter{\romannumeral-`0#1}%
}%
\let\xintAdd\xintiAdd \let\xintadd\xintiadd
\def\xint_add #1#2%
{%
    \expandafter\XINT_add_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Add #1#2{\romannumeral0\XINT_add_fork #2\Z #1\Z }%
\def\XINT_add #1#2{\XINT_add_fork #2\Z #1\Z }%
```

ADDITION Ici #1#2 vient du *deuxième* argument de \xintAdd et #3#4 donc du *premier* [algo plus efficace lorsque le premier est plus long que le second]

```
\def\XINT_add_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_add_secondiszero
      #3\dummy \XINT_add_firstiszero
       0\dummy
        {\xint_UDsignsfork
          #1#3\dummy \XINT_add_minusminus          % #1 = #3 = -
           #1-\dummy \XINT_add_minusplus           % #1 = -
           #3-\dummy \XINT_add_plusminus           % #3 = -
            --\dummy \XINT_add_plusplus
         \krof }%
    \krof
    {#2}{#4}#1#3%
}%
\def\XINT_add_secondiszero #1#2#3#4{ #4#2}%
\def\XINT_add_firstiszero #1#2#3#4{ #3#1}%
```

#1 vient du *deuxième* et #2 vient du *premier*

```
\def\XINT_add_minusminus #1#2#3#4%
{%
    \expandafter\xint_minus_andstop%
    \romannumeral0\XINT_add_pre {#2}{#1}%
}%
\def\XINT_add_minusplus #1#2#3#4%
{%
    \XINT_sub_pre {#4#2}{#1}%
}%
\def\XINT_add_plusminus #1#2#3#4%
{%
    \XINT_sub_pre {#3#1}{#2}%
}%
\def\XINT_add_plusplus #1#2#3#4%
{%
    \XINT_add_pre {#4#2}{#3#1}%
}%
```

```
\def\XINT_add_pre #1%
{%
  \expandafter\XINT_add_pre_b\expandafter
  {\romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\Z }%
}%
\def\XINT_add_pre_b #1#2%
{%
    \expandafter\XINT_add_A
        \expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\Z
        \W\X\Y\Z #1\W\X\Y\Z
}%
```

21.22 \xintSub

```
\def\xintiSub {\romannumeral0\xintisub }%
\def\xintisub #1%
{%
    \expandafter\xint_sub\expandafter{\romannumeral-`0#1}%
}%
\let\xintSub\xintiSub \let\xintsub\xintisub
\def\xint_sub #1#2%
{%
    \expandafter\XINT_sub_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Sub #1#2{\romannumeral0\XINT_sub_fork #2\Z #1\Z }%
\def\XINT_sub #1#2{\XINT_sub_fork #2\Z #1\Z }%
```

```
 SOUSTRACTION #3#4-#1#2: #3#4 vient du *premier* #1#2 vient du *second*
```

```
\def\XINT_sub_fork #1#2\Z #3#4\Z
{%
    \xint_UDsignsfork
          #1#3\dummy \XINT_sub_minusminus
           #1-\dummy \XINT_sub_minusplus   % attention, #3=0 possible
           #3-\dummy \XINT_sub_plusminus   % attention, #1=0 possible
            --\dummy {\xint_UDzerofork
                      #1\dummy \XINT_sub_secondiszero
                      #3\dummy \XINT_sub_firstiszero
                       0\dummy \XINT_sub_plusplus
                      \krof }%
    \krof
    {#2}{#4}#1#3%
}%
\def\XINT_sub_secondiszero #1#2#3#4{ #4#2}%
\def\XINT_sub_firstiszero  #1#2#3#4{ -#3#1}%
\def\XINT_sub_plusplus #1#2#3#4%
{%
    \XINT_sub_pre {#4#2}{#3#1}%
}%
\def\XINT_sub_minusminus #1#2#3#4%
```

```
{%
    \XINT_sub_pre {#1}{#2}%
}%
\def\XINT_sub_minusplus #1#2#3#4%
{%
    \xint_gob_til_zero #4\xint_sub_mp0\XINT_add_pre {#4#2}{#1}%
}%
\def\xint_sub_mp0\XINT_add_pre #1#2{ #2}%
\def\XINT_sub_plusminus #1#2#3#4%
{%
    \xint_gob_til_zero #3\xint_sub_pm0\expandafter\xint_minus_andstop%
    \romannumeral0\XINT_add_pre {#2}{#3#1}%
}%
\def\xint_sub_pm #1\XINT_add_pre #2#3{ -#2}%
\def\XINT_sub_pre #1%
{%
  \expandafter\XINT_sub_pre_b\expandafter
  {\romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\R\Z }%
}%
\def\XINT_sub_pre_b #1#2%
{%
    \expandafter\XINT_sub_A
        \expandafter1\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\R\Z
        \W\X\Y\Z #1 \W\X\Y\Z
}%
```

```
 \romannumeral0\XINT_sub_A 1{}<N1>\W\X\Y\Z<N2>\W\X\Y\Z
 N1 et N2 sont présentés à l'envers ET ON A RAJOUTÉ DES ZÉROS POUR QUE LEURS LONGUEURS
 À CHACUN SOIENT MULTIPLES DE 4, MAIS AUCUN NE SE TERMINE EN 0000.
 output: N2 - N1
 Elle donne le résultat dans le **bon ordre**, avec le bon signe, et sans zéros
 superflus.
```

```
\def\XINT_sub_A #1#2#3\W\X\Y\Z #4#5#6#7%
{%
    \xint_gob_til_W
    #4\xint_sub_az
    \W\XINT_sub_B #1{#4#5#6#7}{#2}#3\W\X\Y\Z
}%
\def\XINT_sub_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W
    #4\xint_sub_bz
    \W\XINT_sub_onestep #1#2{#7#6#5#4}{#3}%
}%
```

```
 d'abord la branche principale #6 = 4 chiffres de N1, plus significatif en *pre-
 mier*, #2#3#4#5 chiffres de N2, plus significatif en *dernier* On veut N2 - N1.
```

```
\def\XINT_sub_onestep #1#2#3#4#5#6%
```

```
{%
    \expandafter\XINT_sub_backtoA\the\numexpr 11#5#4#3#2-#6+#1-\xint_c_i\relax.%
}%
```

ON PRODUIT LE RÉSULTAT DANS LE BON ORDRE

```
\def\XINT_sub_backtoA #1#2#3.#4%
{%
    \XINT_sub_A #2{#3#4}%
}%
\def\xint_sub_bz
    \W\XINT_sub_onestep #1#2#3#4#5#6#7%
{%
    \xint_UDzerofork
      #1\dummy  \XINT_sub_C   % une retenue
       0\dummy  \XINT_sub_D   % pas de retenue
    \krof
    {#7}#2#3#4#5%
}%
\def\XINT_sub_D #1#2\W\X\Y\Z
{%
    \expandafter
    \xint_cleanupzeros_andstop
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1%
}%
\def\XINT_sub_C #1#2#3#4#5%
{%
    \xint_gob_til_W
    #2\xint_sub_cz
    \W\XINT_sub_AC_onestep {#5#4#3#2}{#1}%
}%
\def\XINT_sub_AC_onestep #1%
{%
    \expandafter\XINT_sub_backtoC\the\numexpr 11#1-\xint_c_i\relax.%
}%
\def\XINT_sub_backtoC #1#2#3.#4%
{%
    \XINT_sub_AC_checkcarry #2{#3#4}% la retenue va \^etre examin\'ee
}%
\def\XINT_sub_AC_checkcarry #1%
{%
    \xint_gob_til_one #1\xint_sub_AC_nocarry 1\XINT_sub_C
}%
\def\xint_sub_AC_nocarry 1\XINT_sub_C #1#2\W\X\Y\Z
```

```
{%
    \expandafter
    \XINT_cuz_loop
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1\W\W\W\W\W\W\W\Z
}%
\def\xint_sub_cz\W\XINT_sub_AC_onestep #1%
{%
    \XINT_cuz
}%
\def\xint_sub_az\W\XINT_sub_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W
    #4\xint_sub_ez
    \W\XINT_sub_Eenter #1{#3}#4#5#6#7%
}%
```

le premier nombre continue, le résultat sera < 0.

```
\def\XINT_sub_Eenter #1#2%
{%
    \expandafter
    \XINT_sub_E\expandafter1\expandafter{\expandafter}%
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    \W\X\Y\Z #1%
}%
\def\XINT_sub_E #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_sub_F\W
    \XINT_sub_Eonestep #1{#6#5#4#3}{#2}%
}%
\def\XINT_sub_Eonestep #1#2%
{%
    \expandafter\XINT_sub_backtoE\the\numexpr 109999-#2+#1\relax.%
}%
\def\XINT_sub_backtoE #1#2#3.#4%
{%
    \XINT_sub_E #2{#3#4}%
}%
\def\xint_sub_F\W\XINT_sub_Eonestep #1#2#3#4%
```

```
{%
    \xint_UDonezerofork
      #4#1\dummy {\XINT_sub_Fdec 0}% soustraire  1. Et faire signe -
      #1#4\dummy {\XINT_sub_Finc 1}% additionner 1. Et faire signe -
        10\dummy  \XINT_sub_DD     % terminer. Mais avec signe -
    \krof
    {#3}%
}%
\def\XINT_sub_DD {\expandafter\xint_minus_andstop\romannumeral0\XINT_sub_D }%
\def\XINT_sub_Fdec #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_sub_Fdec_finish\W
    \XINT_sub_Fdec_onestep #1{#6#5#4#3}{#2}%
}%
\def\XINT_sub_Fdec_onestep #1#2%
{%
    \expandafter\XINT_sub_backtoFdec\the\numexpr 11#2+#1-\xint_c_i\relax.%
}%
\def\XINT_sub_backtoFdec #1#2#3.#4%
{%
    \XINT_sub_Fdec #2{#3#4}%
}%
\def\xint_sub_Fdec_finish\W\XINT_sub_Fdec_onestep #1#2%
{%
    \expandafter\xint_minus_andstop\romannumeral0\XINT_cuz
}%
\def\XINT_sub_Finc #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_sub_Finc_finish\W
    \XINT_sub_Finc_onestep #1{#6#5#4#3}{#2}%
}%
\def\XINT_sub_Finc_onestep #1#2%
{%
    \expandafter\XINT_sub_backtoFinc\the\numexpr 10#2+#1\relax.%
}%
\def\XINT_sub_backtoFinc #1#2#3.#4%
{%
    \XINT_sub_Finc #2{#3#4}%
}%
\def\xint_sub_Finc_finish\W\XINT_sub_Finc_onestep #1#2#3%
{%
    \xint_UDzerofork
     #1\dummy {\expandafter\xint_minus_andstop\xint_cleanupzeros_nospace}%
      0\dummy { -1}%
    \krof
    #3%
}%
\def\xint_sub_ez\W\XINT_sub_Eenter #1%
{%
```

```
    \xint_UDzerofork
      #1\dummy \XINT_sub_K % il y a une retenue
       0\dummy \XINT_sub_L % pas de retenue
    \krof
}%
\def\XINT_sub_L #1\W\X\Y\Z {\XINT_cuz_loop #1\W\W\W\W\W\W\W\Z }%
\def\XINT_sub_K #1%
{%
    \expandafter
    \XINT_sub_KK\expandafter1\expandafter{\expandafter}%
    \romannumeral0%
    \XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
\def\XINT_sub_KK #1#2#3#4#5#6%
{%
    \xint_gob_til_W #3\xint_sub_KK_finish\W
    \XINT_sub_KK_onestep #1{#6#5#4#3}{#2}%
}%
\def\XINT_sub_KK_onestep #1#2%
{%
    \expandafter\XINT_sub_backtoKK\the\numexpr 109999-#2+#1\relax.%
}%
\def\XINT_sub_backtoKK #1#2#3.#4%
{%
    \XINT_sub_KK #2{#3#4}%
}%
\def\xint_sub_KK_finish\W\XINT_sub_KK_onestep #1#2#3%
{%
    \expandafter\xint_minus_andstop
    \romannumeral0\XINT_cuz_loop #3\W\W\W\W\W\W\W\Z
}%
```

21.23 \xintCmp

```
\def\xintiCmp {\romannumeral0\xinticmp }%
\def\xinticmp #1%
{%
    \expandafter\xint_cmp\expandafter{\romannumeral-`0#1}%
}%
\let\xintCmp\xintiCmp \let\xintcmp\xinticmp
\def\xint_cmp #1#2%
{%
    \expandafter\XINT_cmp_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Cmp #1#2{\romannumeral0\XINT_cmp_fork #2\Z #1\Z }%
```

```
 COMPARAISON
 1 si #3#4>#1#2, 0 si #3#4=#1#2, -1 si #3#4<#1#2
 #3#4 vient du *premier*, #1#2 vient du *second*
\def\XINT_cmp_fork #1#2\Z #3#4\Z
{%
    \xint_UDsignsfork
          #1#3\dummy \XINT_cmp_minusminus
           #1-\dummy \XINT_cmp_minusplus
           #3-\dummy \XINT_cmp_plusminus
            --\dummy {\xint_UDzerosfork
                       #1#3\dummy \XINT_cmp_zerozero
                        #10\dummy \XINT_cmp_zeroplus
                        #30\dummy \XINT_cmp_pluszero
                         00\dummy \XINT_cmp_plusplus
                       \krof }%
    \krof
    {#2}{#4}#1#3%
}%
\def\XINT_cmp_minusplus #1#2#3#4{ 1}%
\def\XINT_cmp_plusminus #1#2#3#4{ -1}%
\def\XINT_cmp_zerozero  #1#2#3#4{ 0}%
\def\XINT_cmp_zeroplus  #1#2#3#4{ 1}%
\def\XINT_cmp_pluszero  #1#2#3#4{ -1}%
\def\XINT_cmp_plusplus #1#2#3#4%
{%
    \XINT_cmp_pre {#4#2}{#3#1}%
}%
\def\XINT_cmp_minusminus #1#2#3#4%
{%
    \XINT_cmp_pre {#1}{#2}%
}%
\def\XINT_cmp_pre #1%
{%
  \expandafter\XINT_cmp_pre_b\expandafter
  {\romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\R\Z }%
}%
\def\XINT_cmp_pre_b #1#2%
{%
    \expandafter\XINT_cmp_A
    \expandafter1\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\R\Z
        \W\X\Y\Z #1\W\X\Y\Z
}%

 COMPARAISON
 N1 et N2 sont présentés à l'envers ET ON A RAJOUTÉ DES ZÉROS POUR QUE LEUR LONGUEURS
 À CHACUN SOIENT MULTIPLES DE 4, MAIS AUCUN NE SE TERMINE EN 0000. routine ap-
 pelée via
 \XINT_cmp_A 1{}<N1>\W\X\Y\Z<N2>\W\X\Y\Z
```

```
 ATTENTION RENVOIE 1 SI N1 < N2, 0 si N1 = N2, -1 si N1 > N2
\def\XINT_cmp_A #1#2#3\W\X\Y\Z #4#5#6#7%
{%
    \xint_gob_til_W #4\xint_cmp_az\W
    \XINT_cmp_B #1{#4#5#6#7}{#2}#3\W\X\Y\Z
}%
\def\XINT_cmp_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W#4\xint_cmp_bz\W
    \XINT_cmp_onestep #1#2{#7#6#5#4}{#3}%
}%
\def\XINT_cmp_onestep #1#2#3#4#5#6%
{%
    \expandafter\XINT_cmp_backtoA\the\numexpr 11#5#4#3#2-#6+#1-\xint_c_i\relax.%
}%
\def\XINT_cmp_backtoA #1#2#3.#4%
{%
    \XINT_cmp_A #2{#3#4}%
}%
\def\xint_cmp_bz\W\XINT_cmp_onestep #1\Z { 1}%
\def\xint_cmp_az\W\XINT_cmp_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W #4\xint_cmp_ez\W
    \XINT_cmp_Eenter #1{#3}#4#5#6#7%
}%
\def\XINT_cmp_Eenter #1\Z { -1}%
\def\xint_cmp_ez\W\XINT_cmp_Eenter #1%
{%
    \xint_UDzerofork
      #1\dummy \XINT_cmp_K             %     il y a une retenue
       0\dummy \XINT_cmp_L             %     pas de retenue
    \krof
}%
\def\XINT_cmp_K #1\Z { -1}%
\def\XINT_cmp_L #1{\XINT_OneIfPositive_main #1}%
\def\XINT_OneIfPositive #1%
{%
    \XINT_OneIfPositive_main #1\W\X\Y\Z%
}%
\def\XINT_OneIfPositive_main #1#2#3#4%
{%
    \xint_gob_til_Z #4\xint_OneIfPositive_terminated\Z
    \XINT_OneIfPositive_onestep #1#2#3#4%
}%
\def\xint_OneIfPositive_terminated\Z\XINT_OneIfPositive_onestep\W\X\Y\Z { 0}%
\def\XINT_OneIfPositive_onestep #1#2#3#4%
{%
    \expandafter\XINT_OneIfPositive_check\the\numexpr #1#2#3#4\relax
}%
```

```
\def\XINT_OneIfPositive_check #1%
{%
    \xint_gob_til_zero #1\xint_OneIfPositive_backtomain 0%
    \XINT_OneIfPositive_finish #1%
}%
\def\XINT_OneIfPositive_finish #1\W\X\Y\Z{ 1}%
\def\xint_OneIfPositive_backtomain 0\XINT_OneIfPositive_finish 0%
                    {\XINT_OneIfPositive_main }%
```

21.24 \xintGeq

```
 PLUS GRAND OU ÉGAL attention compare les **valeurs absolues**

\def\xintiGeq {\romannumeral0\xintigeq }%
\def\xintigeq #1%
{%
    \expandafter\xint_geq\expandafter {\romannumeral-`0#1}%
}%
\let\xintGeq\xintiGeq \let\xintgeq\xintigeq
\def\xint_geq #1#2%
{%
    \expandafter\XINT_geq_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Geq #1#2{\romannumeral0\XINT_geq_fork #2\Z #1\Z }%

 PLUS GRAND OU ÉGAL ATTENTION, TESTE les VALEURS ABSOLUES

\def\XINT_geq_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_geq_secondiszero % |#1#2|=0
      #3\dummy \XINT_geq_firstiszero % |#1#2|>0
       0\dummy {\xint_UDsignsfork
                   #1#3\dummy \XINT_geq_minusminus
                    #1-\dummy \XINT_geq_minusplus
                    #3-\dummy \XINT_geq_plusminus
                     --\dummy \XINT_geq_plusplus
                \krof }%
    \krof
    {#2}{#4}#1#3%
}%
\def\XINT_geq_secondiszero     #1#2#3#4{ 1}%
\def\XINT_geq_firstiszero      #1#2#3#4{ 0}%
\def\XINT_geq_plusplus   #1#2#3#4{\XINT_geq_pre {#4#2}{#3#1}}%
\def\XINT_geq_minusminus #1#2#3#4{\XINT_geq_pre {#2}{#1}}%
\def\XINT_geq_minusplus  #1#2#3#4{\XINT_geq_pre {#4#2}{#1}}%
\def\XINT_geq_plusminus  #1#2#3#4{\XINT_geq_pre {#2}{#3#1}}%
\def\XINT_geq_pre #1%
{%
  \expandafter\XINT_geq_pre_b\expandafter
```

```
  {\romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\Z }%
}%
\def\XINT_geq_pre_b #1#2%
{%
    \expandafter\XINT_geq_A
    \expandafter1\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\Z
        \W\X\Y\Z #1 \W\X\Y\Z
}%

 PLUS GRAND OU ÉGAL
 N1 et N2 sont présentés à l'envers ET ON A RAJOUTÉ DES ZÉROS POUR QUE LEURS LONGUEURS
 À CHACUN SOIENT MULTIPLES DE 4, MAIS AUCUN NE SE TERMINE EN 0000
 routine appelée via
 \romannumeral0\XINT_geq_A 1{}<N1>\W\X\Y\Z<N2>\W\X\Y\Z
 ATTENTION RENVOIE 1 SI N1 < N2 ou N1 = N2 et 0 si N1 > N2

\def\XINT_geq_A #1#2#3\W\X\Y\Z #4#5#6#7%
{%
    \xint_gob_til_W #4\xint_geq_az\W
    \XINT_geq_B #1{#4#5#6#7}{#2}#3\W\X\Y\Z
}%
\def\XINT_geq_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W #4\xint_geq_bz\W
    \XINT_geq_onestep #1#2{#7#6#5#4}{#3}%
}%
\def\XINT_geq_onestep #1#2#3#4#5#6%
{%
    \expandafter\XINT_geq_backtoA\the\numexpr 11#5#4#3#2-#6+#1-\xint_c_i\relax.%
}%
\def\XINT_geq_backtoA #1#2#3.#4%
{%
    \XINT_geq_A #2{#3#4}%
}%
\def\xint_geq_bz\W\XINT_geq_onestep #1\W\X\Y\Z { 1}%
\def\xint_geq_az\W\XINT_geq_B #1#2#3#4#5#6#7%
{%
    \xint_gob_til_W #4\xint_geq_ez\W
    \XINT_geq_Eenter #1%
}%
\def\XINT_geq_Eenter #1\W\X\Y\Z { 0}%
\def\xint_geq_ez\W\XINT_geq_Eenter #1%
{%
    \xint_UDzerofork
      #1\dummy { 0}             %     il y a une retenue
       0\dummy { 1}             %     pas de retenue
    \krof
}%
```

21.25 \xintMax

```
The rationale is that it is more efficient than using \xintCmp. 1.03 makes the
code a tiny bit slower but easier to re-use for fractions. Note: actually since
1.08a code for fractions does not all reduce to these entry points, so perhaps
I should revert the changes made in 1.03.
```

```
\def\xintiMax {\romannumeral0\xintimax }%
\def\xintimax #1%
{%
    \expandafter\xint_max\expandafter {\romannumeral-`0#1}%
}%
\let\xintMax\xintiMax \let\xintmax\xintimax
\def\xint_max #1#2%
{%
    \expandafter\XINT_max_pre\expandafter {\romannumeral-`0#2}{#1}%
}%
\def\XINT_max_pre #1#2{\XINT_max_fork #1\Z #2\Z {#2}{#1}}%
\def\XINT_Max #1#2{\romannumeral0\XINT_max_fork #2\Z #1\Z {#1}{#2}}%
```

```
#3#4 vient du *premier*, #1#2 vient du *second*
```

```
\def\XINT_max_fork #1#2\Z #3#4\Z
{%
    \xint_UDsignsfork
          #1#3\dummy \XINT_max_minusminus  % A < 0, B < 0
           #1-\dummy \XINT_max_minusplus   % B < 0, A >= 0
           #3-\dummy \XINT_max_plusminus   % A < 0, B >= 0
            --\dummy {\xint_UDzerosfork
                      #1#3\dummy \XINT_max_zerozero % A = B = 0
                       #10\dummy \XINT_max_zeroplus % B = 0, A > 0
                       #30\dummy \XINT_max_pluszero % A = 0, B > 0
                        00\dummy \XINT_max_plusplus % A, B > 0
                      \krof }%
    \krof
    {#2}{#4}#1#3%
}%
```

```
A = #4#2, B = #3#1
```

```
\def\XINT_max_zerozero  #1#2#3#4{\xint_firstoftwo_andstop }%
\def\XINT_max_zeroplus  #1#2#3#4{\xint_firstoftwo_andstop }%
\def\XINT_max_pluszero  #1#2#3#4{\xint_secondoftwo_andstop }%
\def\XINT_max_minusplus #1#2#3#4{\xint_firstoftwo_andstop }%
\def\XINT_max_plusminus #1#2#3#4{\xint_secondoftwo_andstop }%
\def\XINT_max_plusplus  #1#2#3#4%
{%
    \ifodd\XINT_Geq {#4#2}{#3#1}
      \expandafter\xint_firstoftwo_andstop
    \else
```

```
      \expandafter\xint_secondoftwo_andstop
    \fi
}%
```

```
#3=-, #4=-, #1 = |B| = -B, #2 = |A| = -A
```

```
\def\XINT_max_minusminus #1#2#3#4%
{%
    \ifodd\XINT_Geq {#1}{#2}
      \expandafter\xint_firstoftwo_andstop
    \else
      \expandafter\xint_secondoftwo_andstop
    \fi
}%
```

21.26 \xintMin

```
\def\xintiMin {\romannumeral0\xintimin }%
\def\xintimin #1%
{%
    \expandafter\xint_min\expandafter {\romannumeral-`0#1}%
}%
\let\xintMin\xintiMin \let\xintmin\xintimin
\def\xint_min #1#2%
{%
    \expandafter\XINT_min_pre\expandafter {\romannumeral-`0#2}{#1}%
}%
\def\XINT_min_pre #1#2{\XINT_min_fork #1\Z #2\Z {#2}{#1}}%
\def\XINT_Min #1#2{\romannumeral0\XINT_min_fork #2\Z #1\Z {#1}{#2}}%
```

```
#3#4 vient du *premier*, #1#2 vient du *second*
```

```
\def\XINT_min_fork #1#2\Z #3#4\Z
{%
    \xint_UDsignsfork
          #1#3\dummy \XINT_min_minusminus  % A < 0, B < 0
           #1-\dummy \XINT_min_minusplus   % B < 0, A >= 0
           #3-\dummy \XINT_min_plusminus   % A < 0, B >= 0
            --\dummy {\xint_UDzerosfork
                      #1#3\dummy \XINT_min_zerozero % A = B = 0
                       #10\dummy \XINT_min_zeroplus % B = 0, A > 0
                       #30\dummy \XINT_min_pluszero % A = 0, B > 0
                        00\dummy \XINT_min_plusplus % A, B > 0
                      \krof }%
    \krof
    {#2}{#4}#1#3%
}%
```

```
A = #4#2, B = #3#1
```

```
\def\XINT_min_zerozero  #1#2#3#4{\xint_firstoftwo_andstop }%
```

```
\def\XINT_min_zeroplus  #1#2#3#4{\xint_secondoftwo_andstop }%
\def\XINT_min_pluszero  #1#2#3#4{\xint_firstoftwo_andstop }%
\def\XINT_min_minusplus #1#2#3#4{\xint_secondoftwo_andstop }%
\def\XINT_min_plusminus #1#2#3#4{\xint_firstoftwo_andstop }%
\def\XINT_min_plusplus  #1#2#3#4%
{%
    \ifodd\XINT_Geq {#4#2}{#3#1}
      \expandafter\xint_secondoftwo_andstop
    \else
      \expandafter\xint_firstoftwo_andstop
    \fi
}%
```

```
#3=-, #4=-, #1 = |B| = -B, #2 = |A| = -A
```

```
\def\XINT_min_minusminus #1#2#3#4%
{%
    \ifodd\XINT_Geq {#1}{#2}
      \expandafter\xint_secondoftwo_andstop
    \else
      \expandafter\xint_firstoftwo_andstop
    \fi
}%
```

21.27 \xintSum, \xintSumExpr

```
\xintSum {{a}{b}...{z}}
\xintSumExpr {a}{b}...{z}\relax
1.03 (drastically) simplifies and makes the routines more efficient (for big
computations). Also the way \xintSum and \xintSumExpr ...\relax are related.
has been modified. Now \xintSumExpr \z \relax is accepted input when \z expands
to a list of braced terms (prior only \xintSum {\z} or \xintSum \z was possi-
ble).
```

```
\def\xintiSum {\romannumeral0\xintisum }%
\def\xintisum #1{\xintisumexpr #1\relax }%
\def\xintiSumExpr {\romannumeral0\xintisumexpr }%
\def\xintisumexpr {\expandafter\XINT_sumexpr\romannumeral-`0}%
\let\xintSum\xintiSum \let\xintsum\xintisum
\let\xintSumExpr\xintiSumExpr \let\xintsumexpr\xintisumexpr
\def\XINT_sumexpr {\XINT_sum_loop {0000}{0000}}%
\def\XINT_sum_loop #1#2#3%
{%
    \expandafter\XINT_sum_checksign\romannumeral-`0#3\Z {#1}{#2}%
}%
\def\XINT_sum_checksign #1%
{%
    \xint_gob_til_relax #1\XINT_sum_finished\relax
    \xint_gob_til_zero #1\XINT_sum_skipzeroinput0%
    \xint_UDsignfork
```

```
      #1\dummy \XINT_sum_N
       -\dummy {\XINT_sum_P #1}%
    \krof
}%
\def\XINT_sum_finished #1\Z #2#3%
{%
    \XINT_sub_A 1{}#3\W\X\Y\Z #2\W\X\Y\Z
}%
\def\XINT_sum_skipzeroinput #1\krof #2\Z {\XINT_sum_loop }%
\def\XINT_sum_P #1\Z #2%
{%
    \expandafter\XINT_sum_loop\expandafter
    {\romannumeral0\expandafter
     \XINT_addr_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\Z
    \W\X\Y\Z #2\W\X\Y\Z }%
}%
\def\XINT_sum_N #1\Z #2#3%
{%
    \expandafter\XINT_sum_NN\expandafter
    {\romannumeral0\expandafter
     \XINT_addr_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\Z
    \W\X\Y\Z #3\W\X\Y\Z }{#2}%
}%
\def\XINT_sum_NN #1#2{\XINT_sum_loop {#2}{#1}}%
```

21.28 \xintMul

```
\def\xintiMul {\romannumeral0\xintimul }%
\def\xintimul #1%
{%
    \expandafter\xint_mul\expandafter {\romannumeral-`0#1}%
}%
\let\xintMul\xintiMul \let\xintmul\xintimul
\def\xint_mul #1#2%
{%
    \expandafter\XINT_mul_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Mul #1#2{\romannumeral0\XINT_mul_fork #2\Z #1\Z }%
```

```
 MULTIPLICATION
 Ici #1#2 = 2e input et #3#4 = 1er input
 Release 1.03 adds some overhead to first compute and compare the lengths of the
 two inputs. The algorithm is asymmetrical and whether the first input is the
 longest or the shortest sometimes has a strong impact. 50 digits times 1000 dig-
 its used to be 5 times faster than 1000 digits times 50 digits. With the new
 code, the user input order does not matter as it is decided by the routine what
 is best. This is important for the extension to fractions, as there is no way
```

then to generally control or guess the most frequent sizes of the inputs besides actually computing their lengths.

```
\def\XINT_mul_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_mul_zero
      #3\dummy \XINT_mul_zero
       0\dummy
        {\xint_UDsignsfork
          #1#3\dummy \XINT_mul_minusminus          % #1 = #3 = -
           #1-\dummy {\XINT_mul_minusplus #3}%          % #1 = -
           #3-\dummy {\XINT_mul_plusminus #1}%          % #3 = -
            --\dummy {\XINT_mul_plusplus #1#3}%
         \krof }%
    \krof
    {#2}{#4}%
}%
\def\XINT_mul_zero #1#2{ 0}%
\def\XINT_mul_minusminus #1#2%
{%
      \expandafter\XINT_mul_choice_a
      \expandafter{\romannumeral0\XINT_length {#2}}%
      {\romannumeral0\XINT_length {#1}}{#1}{#2}%
}%
\def\XINT_mul_minusplus #1#2#3%
{%
    \expandafter\xint_minus_andstop\romannumeral0\expandafter
    \XINT_mul_choice_a
    \expandafter{\romannumeral0\XINT_length {#1#3}}%
    {\romannumeral0\XINT_length {#2}}{#2}{#1#3}%
}%
\def\XINT_mul_plusminus #1#2#3%
{%
    \expandafter\xint_minus_andstop\romannumeral0\expandafter
    \XINT_mul_choice_a
    \expandafter{\romannumeral0\XINT_length {#3}}%
    {\romannumeral0\XINT_length {#1#2}}{#1#2}{#3}%
}%
\def\XINT_mul_plusplus #1#2#3#4%
{%
    \expandafter\XINT_mul_choice_a
    \expandafter{\romannumeral0\XINT_length {#2#4}}%
    {\romannumeral0\XINT_length {#1#3}}{#1#3}{#2#4}%
}%
\def\XINT_mul_choice_a #1#2%
{%
    \expandafter\XINT_mul_choice_b\expandafter{#2}{#1}%
}%
\def\XINT_mul_choice_b #1#2%
```

```
{%
    \ifnum #1<\xint_c_v
       \expandafter\XINT_mul_choice_littlebyfirst
    \else
    \ifnum #2<\xint_c_v
      \expandafter\expandafter\expandafter\XINT_mul_choice_littlebysecond
      \else
      \expandafter\expandafter\expandafter\XINT_mul_choice_compare
      \fi
    \fi
    {#1}{#2}%
}%
\def\XINT_mul_choice_littlebyfirst #1#2#3#4%
{%
    \expandafter\XINT_mul_M
    \expandafter{\the\numexpr #3\expandafter}%
    \romannumeral0\XINT_RQ {}#4\R\R\R\R\R\R\R\Z \Z\Z\Z\Z
}%
\def\XINT_mul_choice_littlebysecond #1#2#3#4%
{%
    \expandafter\XINT_mul_M
    \expandafter{\the\numexpr #4\expandafter}%
    \romannumeral0\XINT_RQ {}#3\R\R\R\R\R\R\R\Z \Z\Z\Z\Z
}%
\def\XINT_mul_choice_compare #1#2%
{%
    \ifnum #1>#2
        \expandafter \XINT_mul_choice_i
    \else
        \expandafter \XINT_mul_choice_ii
    \fi
    {#1}{#2}%
}%
\def\XINT_mul_choice_i #1#2%
{%
   \ifnum #1<\numexpr\ifcase \numexpr (#2-\xint_c_iii)/\xint_c_iv\relax
                      \or 330\or 168\or 109\or 80\or 66\or 52\else 0\fi\relax
       \expandafter\XINT_mul_choice_same
   \else
       \expandafter\XINT_mul_choice_permute
   \fi
}%
\def\XINT_mul_choice_ii #1#2%
{%
   \ifnum #2<\numexpr\ifcase \numexpr (#1-\xint_c_iii)/\xint_c_iv\relax
                      \or 330\or 168\or 109\or 80\or 66\or 52\else 0\fi\relax
       \expandafter\XINT_mul_choice_permute
   \else
       \expandafter\XINT_mul_choice_same
```

```
    \fi
}%
\def\XINT_mul_choice_same #1#2%
{%
    \expandafter\XINT_mul_enter
    \romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\Z
    \Z\Z\Z\Z #2\W\W\W\W
}%
\def\XINT_mul_choice_permute #1#2%
{%
    \expandafter\XINT_mul_enter
    \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\Z
    \Z\Z\Z\Z #1\W\W\W\W
}%
```

Cette portion de routine d'addition se branche directement sur _addr_ lorsque le premier nombre est épuisé, ce qui est garanti arriver avant le second nombre. Elle produit son résultat toujours sur 4n, renversé. Ses deux inputs sont garantis sur 4n.

```
\def\XINT_mul_Ar #1#2#3#4#5#6%
{%
    \xint_gob_til_Z #6\xint_mul_br\Z\XINT_mul_Br #1{#6#5#4#3}{#2}%
}%
\def\xint_mul_br\Z\XINT_mul_Br #1#2%
{%
     \XINT_addr_AC_checkcarry #1%
}%
\def\XINT_mul_Br #1#2#3#4\W\X\Y\Z #5#6#7#8%
{%
    \expandafter\XINT_mul_ABEAr
    \the\numexpr #1+10#2+#8#7#6#5\relax.{#3}#4\W\X\Y\Z
}%
\def\XINT_mul_ABEAr #1#2#3#4#5#6.#7%
{%
    \XINT_mul_Ar #2{#7#6#5#4#3}%
}%
```

<< Petite >> multiplication. mul_Mr renvoie le résultat *à l'envers*, sur *4n*
\romannumeral0\XINT_mul_Mr {<n>}<N>\Z\Z\Z\Z
Fait la multiplication de <N> par <n>, qui est < 10000. <N> est présenté *à l'envers*, sur *4n*. Lorsque <n> vaut 0, donne 0000.

```
\def\XINT_mul_Mr #1%
{%
    \expandafter\XINT_mul_Mr_checkifzeroorone\expandafter{\the\numexpr #1}%
}%
\def\XINT_mul_Mr_checkifzeroorone #1%
{%
    \ifcase #1
      \expandafter\XINT_mul_Mr_zero
```

```
    \or
      \expandafter\XINT_mul_Mr_one
    \else
      \expandafter\XINT_mul_Nr
    \fi
    {0000}{}{#1}%
}%
\def\XINT_mul_Mr_zero #1\Z\Z\Z\Z { 0000}%
\def\XINT_mul_Mr_one #1#2#3#4\Z\Z\Z\Z { #4}%
\def\XINT_mul_Nr #1#2#3#4#5#6#7%
{%
    \xint_gob_til_Z #4\xint_mul_pr\Z\XINT_mul_Pr {#1}{#3}{#7#6#5#4}{#2}{#3}%
}%
\def\XINT_mul_Pr #1#2#3%
{%
    \expandafter\XINT_mul_Lr\the\numexpr \xint_c_x^viii+#1+#2*#3\relax
}%
\def\XINT_mul_Lr 1#1#2#3#4#5#6#7#8#9%
{%
    \XINT_mul_Nr {#1#2#3#4}{#9#8#7#6#5}%
}%
\def\xint_mul_pr\Z\XINT_mul_Pr #1#2#3#4#5%
{%
    \xint_gob_til_zeros_iv #1\XINT_mul_Mr_end_nocarry 0000%
    \XINT_mul_Mr_end_carry #1{#4}%
}%
\def\XINT_mul_Mr_end_nocarry 0000\XINT_mul_Mr_end_carry 0000#1{ #1}%
\def\XINT_mul_Mr_end_carry #1#2#3#4#5{ #5#4#3#2#1}%
```

```
<< Petite >> multiplication. renvoie le résultat *à l'endroit*, avec *nettoy-
age des leading zéros*.
\romannumeral0\XINT_mul_M {<n>}<N>\Z\Z\Z\Z
Fait la multiplication de <N> par <n>, qui est < 10000. <N> est présenté *à l'envers*,
sur *4n*.
```

```
\def\XINT_mul_M #1%
{%
    \expandafter\XINT_mul_M_checkifzeroorone\expandafter{\the\numexpr #1}%
}%
\def\XINT_mul_M_checkifzeroorone #1%
{%
    \ifcase #1
      \expandafter\XINT_mul_M_zero
    \or
      \expandafter\XINT_mul_M_one
    \else
      \expandafter\XINT_mul_N
    \fi
    {0000}{}{#1}%
}%
```

```
\def\XINT_mul_M_zero #1\Z\Z\Z\Z { 0}%
\def\XINT_mul_M_one #1#2#3#4\Z\Z\Z\Z
{%
    \expandafter\xint_cleanupzeros_andstop\romannumeral0\XINT_rev{#4}%
}%
\def\XINT_mul_N #1#2#3#4#5#6#7%
{%
    \xint_gob_til_Z #4\xint_mul_p\Z\XINT_mul_P {#1}{#3}{#7#6#5#4}{#2}{#3}%
}%
\def\XINT_mul_P #1#2#3%
{%
    \expandafter\XINT_mul_L\the\numexpr \xint_c_x^viii+#1+#2*#3\relax
}%
\def\XINT_mul_L 1#1#2#3#4#5#6#7#8#9%
{%
    \XINT_mul_N {#1#2#3#4}{#5#6#7#8#9}%
}%
\def\xint_mul_p\Z\XINT_mul_P #1#2#3#4#5%
{%
    \XINT_mul_M_end #1#4%
}%
\def\XINT_mul_M_end #1#2#3#4#5#6#7#8%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7#8\relax
}%
```

Routine de multiplication principale (attention délimiteurs modifiés pour 1.08)
Le résultat partiel est toujours maintenu avec significatif à droite et il a
un nombre multiple de 4 de chiffres
\romannumeral0\XINT_mul_enter <N1>\Z\Z\Z\Z <N2>\W\W\W\W
avec <N1> *renversé*, *longueur 4n* (zéros éventuellement ajoutés au-delà du
chiffre le plus significatif) et <N2> dans l'ordre *normal*, et pas forcément
longueur 4n. pas de signes.
Pour 1.08: dans \XINT_mul_enter et les modifs de 1.03 qui filtrent les courts,
on pourrait croire que le second opérande a au moins quatre chiffres; mais le
problème c'est que ceci est appelé par \XINT_sqr. Et de plus \XINT_sqr est util-
isé dans la nouvelle routine d'extraction de racine carrée: je ne veux pas ra-
jouter l'overhead à \XINT_sqr de voir si a longueur est au moins 4. Dilemme donc.
Il ne semble pas y avoir d'autres accès directs (celui de big fac n'est pas un
problème). J'ai presque été tenté de faire du 5x4, mais si on veut maintenir
les résultats intermédiaires sur 4n, il y a des complications. Par ailleurs,
je modifie aussi un petit peu la façon de coder la suite, compte tenu du style
que j'ai développé ultérieurement. Attention terminaison modifiée pour le deux-
ième opérande.

```
\def\XINT_mul_enter #1\Z\Z\Z\Z #2#3#4#5%
{%
    \xint_gob_til_W #5\XINT_mul_exit_a\W
    \XINT_mul_start {#2#3#4#5}#1\Z\Z\Z\Z
}%
```

```
\def\XINT_mul_exit_a\W\XINT_mul_start #1%
{%
    \XINT_mul_exit_b #1%
}%
\def\XINT_mul_exit_b #1#2#3#4%
{%
    \xint_gob_til_W
      #2\XINT_mul_exit_ci
      #3\XINT_mul_exit_cii
      \W\XINT_mul_exit_ciii #1#2#3#4%
}%
\def\XINT_mul_exit_ciii #1\W #2\Z\Z\Z\Z \W\W\W
{%
    \XINT_mul_M {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mul_exit_cii\W\XINT_mul_exit_ciii #1\W\W #2\Z\Z\Z\Z \W\W
{%
    \XINT_mul_M {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mul_exit_ci\W\XINT_mul_exit_cii
                      \W\XINT_mul_exit_ciii #1\W\W\W #2\Z\Z\Z\Z \W
{%
    \XINT_mul_M {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mul_start #1#2\Z\Z\Z\Z
{%
    \expandafter\XINT_mul_main\expandafter
    {\romannumeral0\XINT_mul_Mr {#1}#2\Z\Z\Z\Z}#2\Z\Z\Z\Z
}%
\def\XINT_mul_main #1#2\Z\Z\Z\Z #3#4#5#6%
{%
    \xint_gob_til_W #6\XINT_mul_finish_a\W
    \XINT_mul_compute {#3#4#5#6}{#1}#2\Z\Z\Z\Z
}%
\def\XINT_mul_compute #1#2#3\Z\Z\Z\Z
{%
    \expandafter\XINT_mul_main\expandafter
    {\romannumeral0\expandafter
     \XINT_mul_Ar\expandafter0\expandafter{\expandafter}%
     \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z
     \W\X\Y\Z 0000#2\W\X\Y\Z }#3\Z\Z\Z\Z
}%
```

Ici, le deuxième nombre se termine. Fin du calcul. On utilise la variante \XINT_addm_A de l'addition car on sait que le deuxième terme est au moins aussi long que le premier. Lorsque le multiplicateur avait longueur 4n, la dernière addition a fourni le résultat à l'envers, il faut donc encore le renverser.

```
\def\XINT_mul_finish_a\W\XINT_mul_compute #1%
{%
```

```
    \XINT_mul_finish_b #1%
}%
\def\XINT_mul_finish_b #1#2#3#4%
{%
    \xint_gob_til_W
      #1\XINT_mul_finish_c
      #2\XINT_mul_finish_ci
      #3\XINT_mul_finish_cii
      \W\XINT_mul_finish_ciii #1#2#3#4%
}%
\def\XINT_mul_finish_ciii #1\W #2#3\Z\Z\Z\Z \W\W\W
{%
    \expandafter\XINT_addm_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z \W\X\Y\Z 000#2\W\X\Y\Z
}%
\def\XINT_mul_finish_cii
    \W\XINT_mul_finish_ciii #1\W\W #2#3\Z\Z\Z\Z \W\W
{%
    \expandafter\XINT_addm_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z \W\X\Y\Z 00#2\W\X\Y\Z
}%
\def\XINT_mul_finish_ci #1\XINT_mul_finish_ciii #2\W\W\W #3#4\Z\Z\Z\Z \W
{%
    \expandafter\XINT_addm_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#2}#4\Z\Z\Z\Z \W\X\Y\Z 0#3\W\X\Y\Z
}%
\def\XINT_mul_finish_c #1\XINT_mul_finish_ciii \W\W\W\W #2#3\Z\Z\Z\Z
{%
    \expandafter\xint_cleanupzeros_andstop\romannumeral0\XINT_rev{#2}%
}%
```

```
 Variante de la Multiplication
 \romannumeral0\XINT_mulr_enter <N1>\Z\Z\Z\Z <N2>\W\W\W\W
 Ici <N1> est à l'envers sur 4n, et <N2> est à l'endroit, pas sur 4n, comme dans
 \XINT_mul_enter, mais le résultat est lui-même fourni *à l'envers*, sur *4n*
 (en faisant attention de ne pas avoir 0000 à la fin).
 Utilisé par le calcul des puissances. J'ai modifié dans 1.08 sur le modèle de
 la nouvelle version de \XINT_mul_enter. Je pourrais économiser des macros et
 fusionner \XINT_mul_enter et \XINT_mulr_enter. Une autre fois.
```

```
\def\XINT_mulr_enter #1\Z\Z\Z\Z #2#3#4#5%
{%
    \xint_gob_til_W #5\XINT_mulr_exit_a\W
    \XINT_mulr_start {#2#3#4#5}#1\Z\Z\Z\Z
}%
\def\XINT_mulr_exit_a\W\XINT_mulr_start #1%
{%
    \XINT_mulr_exit_b #1%
}%
\def\XINT_mulr_exit_b #1#2#3#4%
```

```
{%
    \xint_gob_til_W
      #2\XINT_mulr_exit_ci
      #3\XINT_mulr_exit_cii
      \W\XINT_mulr_exit_ciii #1#2#3#4%
}%
\def\XINT_mulr_exit_ciii #1\W #2\Z\Z\Z\Z \W\W\W
{%
    \XINT_mul_Mr {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mulr_exit_cii\W\XINT_mulr_exit_ciii #1\W\W #2\Z\Z\Z\Z \W\W
{%
    \XINT_mul_Mr {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mulr_exit_ci\W\XINT_mulr_exit_cii
                      \W\XINT_mulr_exit_ciii #1\W\W\W #2\Z\Z\Z\Z \W
{%
    \XINT_mul_Mr {#1}#2\Z\Z\Z\Z
}%
\def\XINT_mulr_start #1#2\Z\Z\Z\Z
{%
    \expandafter\XINT_mulr_main\expandafter
    {\romannumeral0\XINT_mul_Mr {#1}#2\Z\Z\Z\Z}#2\Z\Z\Z\Z
}%
\def\XINT_mulr_main #1#2\Z\Z\Z\Z #3#4#5#6%
{%
    \xint_gob_til_W #6\XINT_mulr_finish_a\W
    \XINT_mulr_compute {#3#4#5#6}{#1}#2\Z\Z\Z\Z
}%
\def\XINT_mulr_compute #1#2#3\Z\Z\Z\Z
{%
    \expandafter\XINT_mulr_main\expandafter
    {\romannumeral0\expandafter
     \XINT_mul_Ar\expandafter0\expandafter{\expandafter}%
     \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z
     \W\X\Y\Z 0000#2\W\X\Y\Z }#3\Z\Z\Z\Z
}%
\def\XINT_mulr_finish_a\W\XINT_mulr_compute #1%
{%
    \XINT_mulr_finish_b #1%
}%
\def\XINT_mulr_finish_b #1#2#3#4%
{%
    \xint_gob_til_W
      #1\XINT_mulr_finish_c
      #2\XINT_mulr_finish_ci
      #3\XINT_mulr_finish_cii
      \W\XINT_mulr_finish_ciii #1#2#3#4%
}%
```

```
\def\XINT_mulr_finish_ciii #1\W #2#3\Z\Z\Z\Z \W\W\W
{%
    \expandafter\XINT_addp_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z \W\X\Y\Z 000#2\W\X\Y\Z
}%
\def\XINT_mulr_finish_cii
    \W\XINT_mulr_finish_ciii #1\W\W #2#3\Z\Z\Z\Z \W\W
{%
    \expandafter\XINT_addp_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#1}#3\Z\Z\Z\Z \W\X\Y\Z 00#2\W\X\Y\Z
}%
\def\XINT_mulr_finish_ci #1\XINT_mulr_finish_ciii #2\W\W\W #3#4\Z\Z\Z\Z \W
{%
    \expandafter\XINT_addp_A\expandafter0\expandafter{\expandafter}%
    \romannumeral0\XINT_mul_Mr {#2}#4\Z\Z\Z\Z \W\X\Y\Z 0#3\W\X\Y\Z
}%
\def\XINT_mulr_finish_c #1\XINT_mulr_finish_ciii \W\W\W\W #2#3\Z\Z\Z\Z { #2}%
```

21.29 \xintSqr

```
\def\xintiSqr {\romannumeral0\xintisqr }%
\def\xintisqr #1%
{%
    \expandafter\XINT_sqr\expandafter {\romannumeral0\xintiabs{#1}}%
}%
\let\xintSqr\xintiSqr \let\xintsqr\xintisqr
\def\XINT_sqr #1%
{%
    \expandafter\XINT_mul_enter
          \romannumeral0%
          \XINT_RQ {}#1\R\R\R\R\R\R\R\Z
          \Z\Z\Z\Z #1\W\W\W\W
}%
```

21.30 \xintPrd, \xintPrdExpr

```
\xintPrd {{a}...{z}}
\xintPrdExpr {a}...{z}\relax
Release 1.02 modified the product routine. The earlier version was faster in
situations where each new term is bigger than the product of all previous terms,
a situation which arises in the algorithm for computing powers. The 1.02 ver-
sion was changed to be more efficient on big products, where the new term is
small compared to what has been computed so far (the power algorithm now has
its own product routine).
  Finally, the 1.03 version just simplifies everything as the multiplication
now decides what is best, with the price of a little overhead. So the code has
been dramatically reduced here.
  In 1.03 I also modify the way \xintPrd and \xintPrdExpr ...\relax are related.
Now \xintPrdExpr \z \relax is accepted input when \z expands to a list of braced
terms (prior only \xintPrd {\z} or \xintPrd \z was possible).
```

In 1.06a I suddenly decide that \xintProductExpr was a silly name, and as the package is new and certainly not used, I decide I may just switch to \xintPrdExpr which I should have used from the beginning.

```
\def\xintiPrd {\romannumeral0\xintiprd }%
\def\xintiprd #1{\xintiprdexpr #1\relax }%
\let\xintPrd\xintiPrd
\let\xintprd\xintiprd
\def\xintiPrdExpr {\romannumeral0\xintiprdexpr }%
\def\xintiprdexpr {\expandafter\XINT_prdexpr\romannumeral-`0}%
\let\xintPrdExpr\xintiPrdExpr
\let\xintprdexpr\xintiprdexpr
\def\XINT_prdexpr {\XINT_prod_loop_a 1\Z }%
\def\XINT_prod_loop_a #1\Z #2%
{%
    \expandafter\XINT_prod_loop_b \romannumeral-`0#2\Z #1\Z \Z
}%
\def\XINT_prod_loop_b #1%
{%
   \xint_gob_til_relax #1\XINT_prod_finished\relax
   \XINT_prod_loop_c #1%
}%
\def\XINT_prod_loop_c
{%
    \expandafter\XINT_prod_loop_a\romannumeral0\XINT_mul_fork
}%
\def\XINT_prod_finished #1\Z #2\Z \Z { #2}%
```

21.31 \xintFac

Modified with 1.02 and again in 1.03 for greater efficiency. I am tempted, here and elsewhere, to use \ifcase\XINT_Geq {#1}{1000000000} rather than \ifnum\XINT_Length {#1}>9 but for the time being I leave things as they stand. With release 1.05, rather than using \XINT_Length I opt finally for direct use of \numexpr (which will throw a suitable number too big message), and to raise the \xintError: FactorialOfTooBigNumber for argument larger than 1000000 (rather than 1000000000).

```
\def\xintiFac {\romannumeral0\xintifac }%
\def\xintifac #1%
{%
    \expandafter\XINT_fac_fork\expandafter{\the\numexpr #1}%
}%
\let\xintFac\xintiFac \let\xintfac\xintifac
\def\XINT_fac_fork #1%
{%
    \ifcase\XINT_Sgn {#1}
       \xint_afterfi{\expandafter\space\expandafter 1\xint_gobble_i }%
    \or
       \expandafter\XINT_fac_checklength
```

```
    \else
       \xint_afterfi{\expandafter\xintError:FactorialOfNegativeNumber
                \expandafter\space\expandafter 1\xint_gobble_i }%
    \fi
    {#1}%
}%
\def\XINT_fac_checklength #1%
{%
    \ifnum #1>999999
         \xint_afterfi{\expandafter\xintError:FactorialOfTooBigNumber
                       \expandafter\space\expandafter 1\xint_gobble_i }%
    \else
         \xint_afterfi{\ifnum #1>9999
                          \expandafter\XINT_fac_big_loop
                       \else
                          \expandafter\XINT_fac_loop
                       \fi }%
    \fi
    {#1}%
}%
\def\XINT_fac_big_loop #1{\XINT_fac_big_loop_main {10000}{#1}{}}%
\def\XINT_fac_big_loop_main #1#2#3%
{%
    \ifnum #1<#2
        \expandafter
            \XINT_fac_big_loop_main
        \expandafter
           {\the\numexpr #1+1\expandafter }%
    \else
        \expandafter\XINT_fac_big_docomputation
    \fi
    {#2}{#3{#1}}%
}%
\def\XINT_fac_big_docomputation #1#2%
{%
    \expandafter \XINT_fac_bigcompute_loop \expandafter
    {\romannumeral0\XINT_fac_loop {9999}}#2\relax
}%
\def\XINT_fac_bigcompute_loop #1#2%
{%
    \xint_gob_til_relax #2\XINT_fac_bigcompute_end\relax
    \expandafter\XINT_fac_bigcompute_loop\expandafter
    {\expandafter\XINT_mul_enter
     \romannumeral0\XINT_RQ {}#2\R\R\R\R\R\R\R\R\Z
     \Z\Z\Z\Z #1\W\W\W\W }%
}%
\def\XINT_fac_bigcompute_end #1#2#3#4#5%
{%
    \XINT_fac_bigcompute_end_ #5%
```

```
}%
\def\XINT_fac_bigcompute_end_ #1\R #2\Z \W\X\Y\Z #3\W\X\Y\Z { #3}%
\def\XINT_fac_loop #1{\XINT_fac_loop_main 1{1000}{#1}}%
\def\XINT_fac_loop_main #1#2#3%
{%
    \ifnum #3>#1
    \else
        \expandafter\XINT_fac_loop_exit
    \fi
    \expandafter\XINT_fac_loop_main\expandafter
    {\the\numexpr #1+1\expandafter }\expandafter
    {\romannumeral0\XINT_mul_Mr {#1}#2\Z\Z\Z\Z }%
    {#3}%
}%
\def\XINT_fac_loop_exit #1#2#3#4#5#6#7%
{%
    \XINT_fac_loop_exit_ #6%
}%
\def\XINT_fac_loop_exit_ #1#2#3%
{%
    \XINT_mul_M
}%
```

21.32 \xintPow

1.02 modified the \XINT_posprod routine, and this meant that the original version was moved here and renamed to \XINT_pow_posprod, as it was well adapted for computing powers. Then I moved in 1.03 the special variants of multiplication (hence of addition) which were needed to earlier in this file. Modified in 1.06, the exponent is given to a \numexpr rather than twice expanded.

```
\def\xintiPow {\romannumeral0\xintipow }%
\def\xintipow #1%
{%
    \expandafter\xint_pow\romannumeral-`0#1\Z%
}%
\let\xintPow\xintiPow \let\xintpow\xintipow
\def\xint_pow #1#2\Z
{%
    \xint_UDsignfork
      #1\dummy \XINT_pow_Aneg
       -\dummy \XINT_pow_Anonneg
    \krof
       #1{#2}%
}%
\def\XINT_pow_Aneg #1#2#3%
{%
   \expandafter\XINT_pow_Aneg_\expandafter{\the\numexpr #3}{#2}%
}%
```

```
\def\XINT_pow_Aneg_ #1%
{%
   \ifodd #1
       \expandafter\XINT_pow_Aneg_Bodd
   \fi
   \XINT_pow_Anonneg_ {#1}%
}%
\def\XINT_pow_Aneg_Bodd #1%
{%
    \expandafter\XINT_opp\romannumeral0\XINT_pow_Anonneg_
}%
```

```
B = #3, faire le xpxp. Modified with 1.06: use of \numexpr.
```

```
\def\XINT_pow_Anonneg #1#2#3%
{%
   \expandafter\XINT_pow_Anonneg_\expandafter {\the\numexpr #3}{#1#2}%
}%
```

```
#1 = B, #2 = |A|
```

```
\def\XINT_pow_Anonneg_ #1#2%
{%
    \ifcase\XINT_Cmp {#2}{1}
        \expandafter\XINT_pow_AisOne
    \or
        \expandafter\XINT_pow_AatleastTwo
    \else
        \expandafter\XINT_pow_AisZero
    \fi
    {#1}{#2}%
}%
\def\XINT_pow_AisOne #1#2{ 1}%
```

```
#1 = B
```

```
\def\XINT_pow_AisZero #1#2%
{%
     \ifcase\XINT_Sgn {#1}
         \xint_afterfi { 1}%
     \or
         \xint_afterfi { 0}%
     \else
         \xint_afterfi {\xintError:DivisionByZero\space 0}%
     \fi
}%
\def\XINT_pow_AatleastTwo #1%
{%
    \ifcase\XINT_Sgn {#1}
        \expandafter\XINT_pow_BisZero
```

```
    \or
        \expandafter\XINT_pow_checkBsize
    \else
        \expandafter\XINT_pow_BisNegative
    \fi
    {#1}%
}%
\def\XINT_pow_BisNegative #1#2{\xintError:FractionRoundedToZero\space 0}%
\def\XINT_pow_BisZero #1#2{ 1}%
```

B = #1 > 0, A = #2 > 1. With 1.05, I replace \xintiLen{#1}>9 by direct use of \numexpr [to generate an error message if the exponent is too large] 1.06: \numexpr was already used above.

```
\def\XINT_pow_checkBsize #1#2%
{%
    \ifnum #1>999999999
        \expandafter\XINT_pow_BtooBig
    \else
        \expandafter\XINT_pow_loop
    \fi
    {#1}{#2}\XINT_pow_posprod
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
\def\XINT_pow_BtooBig #1\xint_relax #2\xint_relax
                          {\xintError:ExponentTooBig\space 0}%
\def\XINT_pow_loop #1#2%
{%
    \ifnum #1 = 1
        \expandafter\XINT_pow_loop_end
    \else
        \xint_afterfi{\expandafter\XINT_pow_loop_a
            \expandafter{\the\numexpr 2*(#1/2)-#1\expandafter }% b mod 2
            \expandafter{\the\numexpr #1-#1/2\expandafter }%     [b/2]
            \expandafter{\romannumeral0\xintisqr{#2}}}%
    \fi
    {{#2}}%
}%
\def\XINT_pow_loop_end {\romannumeral0\XINT_rord_main {}\relax }%
\def\XINT_pow_loop_a #1%
{%
    \ifnum #1 = 1
        \expandafter\XINT_pow_loop
    \else
        \expandafter\XINT_pow_loop_throwaway
    \fi
}%
```

```
\def\XINT_pow_loop_throwaway #1#2#3%
{%
   \XINT_pow_loop {#1}{#2}%
}%
```

Routine de produit servant pour le calcul des puissances. Chaque nouveau terme est plus grand que ce qui a déjà été calculé. Par conséquent on a intérêt à le conserver en second dans la routine de multiplication, donc le précédent calcul a intérêt à avoir été donné sur 4n, à l'envers. Il faut donc modifier la multiplication pour qu'elle fasse cela. Ce qui oblige à utiliser une version spéciale de l'addition également.

```
\def\XINT_pow_posprod #1%
{%
    \XINT_pow_pprod_checkifempty #1\Z
}%
\def\XINT_pow_pprod_checkifempty #1%
{%
    \xint_gob_til_relax #1\XINT_pow_pprod_emptyproduct\relax
    \XINT_pow_pprod_RQfirst #1%
}%
\def\XINT_pow_pprod_emptyproduct #1\Z { 1}%
\def\XINT_pow_pprod_RQfirst #1\Z
{%
    \expandafter\XINT_pow_pprod_getnext\expandafter
    {\romannumeral0\XINT_RQ {}#1\R\R\R\R\R\R\R\R\Z}%
}%
\def\XINT_pow_pprod_getnext #1#2%
{%
    \XINT_pow_pprod_checkiffinished #2\Z {#1}%
}%
\def\XINT_pow_pprod_checkiffinished #1%
{%
    \xint_gob_til_relax #1\XINT_pow_pprod_end\relax
    \XINT_pow_pprod_compute #1%
}%
\def\XINT_pow_pprod_compute #1\Z #2%
{%
    \expandafter\XINT_pow_pprod_getnext\expandafter
    {\romannumeral0\XINT_mulr_enter #2\Z\Z\Z\Z #1\W\W\W\W }%
}%
\def\XINT_pow_pprod_end\relax\XINT_pow_pprod_compute #1\Z #2%
{%
    \expandafter\xint_cleanupzeros_andstop
    \romannumeral0\XINT_rev {#2}%
}%
```

21.33 \xintDivision, \xintQuo, \xintRem

```
\def\xintiQuo {\romannumeral0\xintiquo }%
\def\xintiRem {\romannumeral0\xintirem }%
\def\xintiquo {\expandafter\xint_firstoftwo_andstop
               \romannumeral0\xintidivision }%
\def\xintirem {\expandafter\xint_secondoftwo_andstop
               \romannumeral0\xintidivision }%
\let\xintQuo\xintiQuo \let\xintquo\xintiquo
\let\xintRem\xintiRem \let\xintrem\xintirem
```

```
#1 = A, #2 = B. On calcule le quotient de A par B.
1.03 adds the detection of 1 for B.
```

```
\def\xintiDivision {\romannumeral0\xintidivision }%
\def\xintidivision #1%
{%
    \expandafter\xint_division\expandafter {\romannumeral-`0#1}%
}%
\let\xintDivision\xintiDivision \let\xintdivision\xintidivision
\def\xint_division #1#2%
{%
    \expandafter\XINT_div_fork \romannumeral-`0#2\Z #1\Z
}%
\def\XINT_Division #1#2{\romannumeral0\XINT_div_fork #2\Z #1\Z }%
```

```
#1#2 = 2e input = diviseur = B. #3#4 = 1er input = divisé = A
```

```
\def\XINT_div_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_div_BisZero
      #3\dummy \XINT_div_AisZero
       0\dummy
        {\xint_UDsignfork
           #1\dummy \XINT_div_BisNegative  % B < 0
           #3\dummy \XINT_div_AisNegative  % A < 0, B > 0
            -\dummy \XINT_div_plusplus     % B > 0, A > 0
         \krof }%
    \krof
    {#2}{#4}#1#3% #1#2=B, #3#4=A
}%
\def\XINT_div_BisZero #1#2#3#4{\xintError:DivisionByZero\space {0}{0}}%
\def\XINT_div_AisZero #1#2#3#4{ {0}{0}}%
```

```
jusqu'à présent c'est facile.
minusplus signifie B < 0, A > 0
plusminus signifie B > 0, A < 0
Ici #3#1 correspond au diviseur B et #4#2 au divisé A.
  Cases with B<0 or especially A<0 are treated sub-optimally in terms of post-
processing, things get reversed which could have been produced directly in the
wanted order, but A,B>0 is given priority for optimization.
```

```
\def\XINT_div_plusplus #1#2#3#4%
{%
    \XINT_div_prepare {#3#1}{#4#2}%
}%

 B = #3#1 < 0, A non nul positif ou négatif

\def\XINT_div_BisNegative #1#2#3#4%
{%
    \expandafter\XINT_div_BisNegative_post
    \romannumeral0\XINT_div_fork #1\Z #4#2\Z
}%
\def\XINT_div_BisNegative_post #1%
{%
    \expandafter\space\expandafter {\romannumeral0\XINT_opp #1}%
}%

 B = #3#1 > 0, A =-#2< 0

\def\XINT_div_AisNegative #1#2#3#4%
{%
    \expandafter\XINT_div_AisNegative_post
    \romannumeral0\XINT_div_prepare {#3#1}{#2}{#3#1}%
}%
\def\XINT_div_AisNegative_post #1#2%
{%
    \ifcase\XINT_Sgn {#2}
       \expandafter \XINT_div_AisNegative_zerorem
    \or
       \expandafter \XINT_div_AisNegative_posrem
    \fi
    {#1}{#2}%
}%

 en #3 on a une copie de B (à l'endroit)

\def\XINT_div_AisNegative_zerorem #1#2#3%
{%
    \expandafter\space\expandafter {\romannumeral0\XINT_opp #1}{0}%
}%

 #1 = quotient, #2 = reste, #3 = diviseur initial (à l'endroit) remplace Reste
 par B - Reste, après avoir remplacé Q par -(Q+1) de sorte que la formule a =
 qb + r, 0<= r < |b| est valable

\def\XINT_div_AisNegative_posrem #1%
{%
    \expandafter \XINT_div_AisNegative_posrem_b \expandafter
       {\romannumeral0\xintiopp{\xintInc {#1}}}%
}%
\def\XINT_div_AisNegative_posrem_b #1#2#3%
{%
```

```
    \expandafter \xint_exchangetwo_keepbraces_andstop \expandafter
    {\romannumeral0\XINT_sub {#3}{#2}}{#1}%
}%

 par la suite A et B sont > 0. #1 = B. Pour le moment à l'endroit. Calcul du plus
 petit K = 4n >= longueur de B
 1.03 adds the interception of B=1
\def\XINT_div_prepare #1%
{%
    \expandafter \XINT_div_prepareB_aa \expandafter
        {\romannumeral0\XINT_length {#1}}{#1}% B > 0 ici
}%
\def\XINT_div_prepareB_aa #1%
{%
    \ifnum #1=1
      \expandafter\XINT_div_prepareB_ab
    \else
      \expandafter\XINT_div_prepareB_a
    \fi
    {#1}%
}%
\def\XINT_div_prepareB_ab #1#2%
{%
    \ifnum #2=1
      \expandafter\XINT_div_prepareB_BisOne
    \else
      \expandafter\XINT_div_prepareB_e
    \fi {000}{3}{4}{#2}%
}%
\def\XINT_div_prepareB_BisOne #1#2#3#4#5{ {#5}{0}}%
\def\XINT_div_prepareB_a #1%
{%
  \expandafter\XINT_div_prepareB_c\expandafter
  {\the\numexpr \xint_c_iv*((#1+\xint_c_i)/\xint_c_iv)}{#1}%
}%

 #1 = K
\def\XINT_div_prepareB_c #1#2%
{%
    \ifcase \numexpr #1-#2\relax
       \expandafter\XINT_div_prepareB_d
    \or
       \expandafter\XINT_div_prepareB_di
    \or
       \expandafter\XINT_div_prepareB_dii
    \or
       \expandafter\XINT_div_prepareB_diii
    \fi {#1}%
}%
```

```
\def\XINT_div_prepareB_d    {\XINT_div_prepareB_e {}{0}}%
\def\XINT_div_prepareB_di   {\XINT_div_prepareB_e {0}{1}}%
\def\XINT_div_prepareB_dii  {\XINT_div_prepareB_e {00}{2}}%
\def\XINT_div_prepareB_diii {\XINT_div_prepareB_e {000}{3}}%

 #1 = zéros à rajouter à B, #2=c, #3=K, #4 = B

\def\XINT_div_prepareB_e #1#2#3#4%
{%
    \XINT_div_prepareB_f #4#1\Z {#3}{#2}{#1}%
}%

 x = #1#2#3#4 = 4 premiers chiffres de B. #1 est non nul. Ensuite on renverse
 B pour calculs plus rapides par la suite.

\def\XINT_div_prepareB_f #1#2#3#4#5\Z
{%
    \expandafter \XINT_div_prepareB_g \expandafter
        {\romannumeral0\XINT_rev {#1#2#3#4#5}}{#1#2#3#4}%
}%

 #3= K, #4 = c, #5= {} ou {0} ou {00} ou {000}, #6 = A initial #1 = B préparé
 et renversé, #2 = x = quatre premiers chiffres On multiplie aussi A par 10^c.
 B, x, K, c, {} ou {0} ou {00} ou {000}, A initial

\def\XINT_div_prepareB_g #1#2#3#4#5#6%
{%
    \XINT_div_prepareA_a {#6#5}{#2}{#3}{#1}{#4}%
}%

 A, x, K, B, c,

\def\XINT_div_prepareA_a #1%
{%
    \expandafter \XINT_div_prepareA_b \expandafter
       {\romannumeral0\XINT_length {#1}}{#1}% A >0 ici
}%

 L0, A, x, K, B, ...

\def\XINT_div_prepareA_b #1%
{%
  \expandafter\XINT_div_prepareA_c\expandafter{\the\numexpr 4*((#1+1)/4)}{#1}%
}%

 L, L0, A, x, K, B,...

\def\XINT_div_prepareA_c #1#2%
{%
    \ifcase \numexpr #1-#2\relax
       \expandafter\XINT_div_prepareA_d
    \or
       \expandafter\XINT_div_prepareA_di
    \or
```

```
2512        \expandafter\XINT_div_prepareA_dii
2513    \or
2514        \expandafter\XINT_div_prepareA_diii
2515    \fi {#1}%
2516 }%
2517 \def\XINT_div_prepareA_d     {\XINT_div_prepareA_e {}}%
2518 \def\XINT_div_prepareA_di    {\XINT_div_prepareA_e {0}}%
2519 \def\XINT_div_prepareA_dii   {\XINT_div_prepareA_e {00}}%
2520 \def\XINT_div_prepareA_diii  {\XINT_div_prepareA_e {000}}%

 #1#3 = A préparé, #2 = longueur de ce A préparé,

2521 \def\XINT_div_prepareA_e #1#2#3%
2522 {%
2523     \XINT_div_startswitch {#1#3}{#2}%
2524 }%

 A, L, x, K, B, c

2525 \def\XINT_div_startswitch #1#2#3#4%
2526 {%
2527     \ifnum #2 > #4
2528       \expandafter\XINT_div_body_a
2529     \else
2530     \ifnum #2 = #4
2531       \expandafter\expandafter\expandafter\XINT_div_final_a
2532     \else
2533       \expandafter\expandafter\expandafter\XINT_div_finished_a
2534     \fi\fi {#1}{#4}{#3}{0000}{#2}%
2535 }%

 ---- "Finished": A, K, x, Q, L, B, c

2536 \def\XINT_div_finished_a #1#2#3%
2537 {%
2538   \expandafter\XINT_div_finished_b\expandafter {\romannumeral0\XINT_cuz {#1}}%
2539 }%

 A, Q, L, B, c no leading zeros in A at this stage

2540 \def\XINT_div_finished_b #1#2#3#4#5%
2541 {%
2542     \ifcase \XINT_Sgn {#1}
2543        \xint_afterfi {\XINT_div_finished_c {0}}%
2544     \or
2545        \xint_afterfi {\expandafter\XINT_div_finished_c\expandafter
2546                       {\romannumeral0\XINT_dsh_checksignx #5\Z {#1}}%
2547                      }%
2548     \fi
2549     {#2}%
2550 }%
2551 \def\XINT_div_finished_c #1#2%
```

```
{%
    \expandafter\space\expandafter {\romannumeral0\XINT_rev_andcuz {#2}}{#1}%
}%
```

---- "Final": A, K, x, Q, L, B, c

```
\def\XINT_div_final_a #1%
{%
    \XINT_div_final_b #1\Z
}%
\def\XINT_div_final_b #1#2#3#4#5\Z
{%
    \xint_gob_til_zeros_iv #1#2#3#4\xint_div_final_c0000%
    \XINT_div_final_c {#1#2#3#4}{#1#2#3#4#5}%
}%
\def\xint_div_final_c0000\XINT_div_final_c #1{\XINT_div_finished_a }%
```

a, A, K, x, Q, L, B ,c 1.01: code ré-écrit pour optimisations diverses. 1.04: again, code rewritten for tiny speed increase (hopefully).

```
\def\XINT_div_final_c #1#2#3#4%
{%
    \expandafter \XINT_div_final_da \expandafter
    {\the\numexpr #1-(#1/#4)*#4\expandafter }\expandafter
    {\the\numexpr #1/#4\expandafter }\expandafter
    {\romannumeral0\xint_cleanupzeros_andstop #2}%
}%
```

r, q, A sans leading zéros, Q, L, B à l'envers sur 4n, c

```
\def\XINT_div_final_da #1%
{%
    \ifnum #1>\xint_c_ix
       \expandafter\XINT_div_final_dP
    \else
       \xint_afterfi
       {\ifnum #1<\xint_c_
        \expandafter\XINT_div_final_dN
        \else
        \expandafter\XINT_div_final_db
        \fi }%
    \fi
}%
\def\XINT_div_final_dN #1%
{%
    \expandafter\XINT_div_final_dP\the\numexpr #1-\xint_c_i\relax
}%
\def\XINT_div_final_dP #1#2#3#4#5% q,A,Q,L,B (puis c)
{%
    \expandafter \XINT_div_final_f \expandafter
    {\romannumeral0\xintisub {#2}%
        {\romannumeral0\XINT_mul_M {#1}#5\Z\Z\Z\Z }}%
```

```
    {\romannumeral0\XINT_add_A 0{}#1000\W\X\Y\Z #3\W\X\Y\Z }%
}%
\def\XINT_div_final_db #1#2#3#4#5% q,A,Q,L,B (puis c)
{%
    \expandafter\XINT_div_final_dc\expandafter
    {\romannumeral0\xintisub {#2}%
        {\romannumeral0\XINT_mul_M {#1}#5\Z\Z\Z\Z }}%
    {#1}{#2}{#3}{#4}{#5}%
}%
\def\XINT_div_final_dc #1#2%
{%
    \ifnum\XINT_Sgn{#1}<\xint_c_
    \xint_afterfi
    {\expandafter\XINT_div_final_dP\the\numexpr #2-\xint_c_i\relax}%
    \else \xint_afterfi {\XINT_div_final_e {#1}#2}%
    \fi
}%
\def\XINT_div_final_e #1#2#3#4#5#6% A final, q, trash, Q, L, B
{%
    \XINT_div_final_f {#1}%
    {\romannumeral0\XINT_add_A 0{}#2000\W\X\Y\Z #4\W\X\Y\Z }%
}%
\def\XINT_div_final_f #1#2#3% R,Q \`a d\'evelopper,c
{%
    \ifcase \XINT_Sgn {#1}
       \xint_afterfi {\XINT_div_final_end {0}}%
    \or
       \xint_afterfi {\expandafter\XINT_div_final_end\expandafter
                       {\romannumeral0\XINT_dsh_checksignx #3\Z {#1}}%
                      }%
    \fi
    {#2}%
}%
\def\XINT_div_final_end #1#2%
{%
    \expandafter\space\expandafter {#2}{#1}%
}%
```

Boucle Principale (on reviendra en div_body_b pas div_body_a)
A, K, x, Q, L, B, c

```
\def\XINT_div_body_a #1%
{%
    \XINT_div_body_b #1\Z {#1}%
}%
\def\XINT_div_body_b #1#2#3#4#5#6#7#8#9\Z
{%
    \XINT_div_body_c {#1#2#3#4#5#6#7#8}%
}%
```

a, A, K, x, Q, L, B, c

```
\def\XINT_div_body_c #1#2#3%
{%
    \XINT_div_body_d {#3}{}#2\Z {#1}{#3}%
}%
\def\XINT_div_body_d #1#2#3#4#5#6%
{%
    \ifnum #1 >\xint_c_
        \expandafter\XINT_div_body_d
        \expandafter{\the\numexpr #1-\xint_c_iv\expandafter }%
    \else
        \expandafter\XINT_div_body_e
    \fi
    {#6#5#4#3#2}%
}%
\def\XINT_div_body_e #1#2\Z #3%
{%
    \XINT_div_body_f {#3}{#1}{#2}%
}%
```

a, alpha (à l'envers), alpha' (à l'endroit), K, x, Q, L, B (à l'envers), c

```
\def\XINT_div_body_f #1#2#3#4#5#6#7#8%
{%
    \expandafter\XINT_div_body_gg
    \the\numexpr (#1+(#5+\xint_c_i)/\xint_c_ii)/(#5+\xint_c_i)+99999\relax
    {#8}{#2}{#8}{#4}{#5}{#3}{#6}{#7}{#8}%
}%
```

q1 sur six chiffres (il en a 5 au max), B, alpha, B, K, x, alpha', Q, L, B, c

```
\def\XINT_div_body_gg #1#2#3#4#5#6%
{%
    \xint_UDzerofork
      #2\dummy \XINT_div_body_gk
       0\dummy {\XINT_div_body_ggk #2}%
    \krof
    {#3#4#5#6}%
}%
\def\XINT_div_body_gk #1#2#3%
{%
    \expandafter\XINT_div_body_h
    \romannumeral0\XINT_div_sub_xpxp
    {\romannumeral0\XINT_mul_Mr {#1}#2\Z\Z\Z\Z }{#3}\Z {#1}%
}%
\def\XINT_div_body_ggk #1#2#3%
{%
    \expandafter \XINT_div_body_gggk \expandafter
    {\romannumeral0\XINT_mul_Mr {#1}0000#3\Z\Z\Z\Z }%
    {\romannumeral0\XINT_mul_Mr {#2}#3\Z\Z\Z\Z }%
    {#1#2}%
}%
```

```
\def\XINT_div_body_gggk #1#2#3#4%
{%
    \expandafter\XINT_div_body_h
    \romannumeral0\XINT_div_sub_xpxp
    {\romannumeral0\expandafter\XINT_mul_Ar
     \expandafter0\expandafter{\expandafter}#2\W\X\Y\Z #1\W\X\Y\Z }%
    {#4}\Z {#3}%
}%
```

```
 alpha1 = alpha-q1 B, \Z, q1, B, K, x, alpha', Q, L, B, c
```

```
\def\XINT_div_body_h #1#2#3#4#5#6#7#8#9\Z
{%
    \ifnum #1#2#3#4>\xint_c_
        \xint_afterfi{\XINT_div_body_i {#1#2#3#4#5#6#7#8}}%
    \else
        \expandafter\XINT_div_body_k
    \fi
    {#1#2#3#4#5#6#7#8#9}%
}%
\def\XINT_div_body_k #1#2#3%
{%
    \XINT_div_body_l {#1}{#2}%
}%
```

```
 a1, alpha1 (à l'endroit), q1, B, K, x, alpha', Q, L, B, c
```

```
\def\XINT_div_body_i #1#2#3#4#5#6%
{%
    \expandafter\XINT_div_body_j
    \expandafter{\the\numexpr (#1+(#6+1)/2)/(#6+1)-1}%
       {#2}{#3}{#4}{#5}{#6}%
}%
\def\XINT_div_body_j #1#2#3#4%
{%
    \expandafter \XINT_div_body_l \expandafter
    {\romannumeral0\XINT_div_sub_xpxp
       {\romannumeral0\XINT_mul_Mr {#1}#4\Z\Z\Z\Z }{\XINT_Rev{#2}}}%
    {#3+#1}%
}%
```

```
 alpha2 (à l'endroit, ou alpha1), q1+q2 (ou q1), K, x, alpha', Q, L, B, c
```

```
\def\XINT_div_body_l #1#2#3#4#5#6#7%
{%
   \expandafter\XINT_div_body_m
   \the\numexpr \xint_c_x^viii+#2\relax {#6}{#3}{#7}{#1#5}{#4}%
}%
```

```
 chiffres de q, Q, K, L, A'=nouveau A, x, B, c
```

```
\def\XINT_div_body_m 1#1#2#3#4#5#6#7#8%
```

```
{%
    \ifnum #1#2#3#4>\xint_c_
       \xint_afterfi {\XINT_div_body_n {#8#7#6#5#4#3#2#1}}%
    \else
       \xint_afterfi {\XINT_div_body_n {#8#7#6#5}}%
    \fi
}%
```

```
q renversé, Q, K, L, A', x, B, c
```

```
\def\XINT_div_body_n #1#2%
{%
    \expandafter\XINT_div_body_o\expandafter
    {\romannumeral0\XINT_addr_A 0{}#1\W\X\Y\Z #2\W\X\Y\Z }%
}%
```

```
q+Q, K, L, A', x, B, c
```

```
\def\XINT_div_body_o #1#2#3#4%
{%
    \XINT_div_body_p {#3}{#2}{}#4\Z {#1}%
}%
```

```
L, K, {}, A'\Z, q+Q, x, B, c
```

```
\def\XINT_div_body_p #1#2#3#4#5#6#7%
{%
    \ifnum #1 > #2
        \xint_afterfi
        {\ifnum #4#5#6#7 > \xint_c_
           \expandafter\XINT_div_body_q
         \else
           \expandafter\XINT_div_body_repeatp
         \fi }%
    \else
        \expandafter\XINT_div_gotofinal_a
    \fi
    {#1}{#2}{#3}#4#5#6#7%
}%
```

```
L, K, zeros, A' avec moins de zéros\Z, q+Q, x, B, c
```

```
\def\XINT_div_body_repeatp #1#2#3#4#5#6#7%
{%
    \expandafter\XINT_div_body_p\expandafter{\the\numexpr #1-4}{#2}{0000#3}%
}%
```

```
L -> L-4, zeros->zeros+0000, répéter jusqu'à ce que soit L=K soit on ne trouve
plus 0000
nouveau L, K, zeros, nouveau A=#4, \Z, Q+q (à l'envers), x, B, c
```

```
\def\XINT_div_body_q #1#2#3#4\Z #5#6%
{%
```

```
2760     \XINT_div_body_b #4\Z {#4}{#2}{#6}{#3#5}{#1}%
2761 }%

 A, K, x, Q, L, B, c --> iterate
 Boucle Principale achevée. ATTENTION IL FAUT AJOUTER 4 ZEROS DE MOINS QUE CEUX
 QUI ONT ÉTÉ PRÉPARÉS DANS #3!!
 L, K (L=K), zeros, A\Z, Q, x, B, c
2762 \def\XINT_div_gotofinal_a #1#2#3#4\Z %
2763 {%
2764     \XINT_div_gotofinal_b #3\Z {#4}{#1}%
2765 }%
2766 \def\XINT_div_gotofinal_b 0000#1\Z #2#3#4#5%
2767 {%
2768     \XINT_div_final_a {#2}{#3}{#5}{#1#4}{#3}%
2769 }%

 La soustraction spéciale.
   Elle fait l'expansion (une fois pour le premier, deux fois pour le second)
 de ses arguments. Ceux-ci doivent être à l'envers sur 4n. De plus on sait a pri-
 ori que le second est > le premier. Et le résultat de la différence est ren-
 voyé **avec la même longueur que le second** (donc avec des leading zéros éventuels),
 et *à l'endroit*.
2770 \def\XINT_div_sub_xpxp #1%
2771 {%
2772     \expandafter \XINT_div_sub_xpxp_a  \expandafter{#1}%
2773 }%
2774 \def\XINT_div_sub_xpxp_a #1#2%
2775 {%
2776     \expandafter\expandafter\expandafter\XINT_div_sub_xpxp_b
2777      #2\W\X\Y\Z #1\W\X\Y\Z
2778 }%
2779 \def\XINT_div_sub_xpxp_b
2780 {%
2781     \XINT_div_sub_A 1{}%
2782 }%
2783 \def\XINT_div_sub_A #1#2#3#4#5#6%
2784 {%
2785     \xint_gob_til_W #3\xint_div_sub_az\W
2786     \XINT_div_sub_B #1{#3#4#5#6}{#2}%
2787 }%
2788 \def\XINT_div_sub_B #1#2#3#4\W\X\Y\Z #5#6#7#8%
2789 {%
2790     \xint_gob_til_W #5\xint_div_sub_bz\W
2791     \XINT_div_sub_onestep #1#2{#8#7#6#5}{#3}#4\W\X\Y\Z
2792 }%
2793 \def\XINT_div_sub_onestep #1#2#3#4#5#6%
2794 {%
2795     \expandafter\XINT_div_sub_backtoA
2796     \the\numexpr 11#5#4#3#2-#6+#1-\xint_c_i\relax.%
```

```
}%
\def\XINT_div_sub_backtoA #1#2#3.#4%
{%
    \XINT_div_sub_A #2{#3#4}%
}%
\def\xint_div_sub_bz\W\XINT_div_sub_onestep #1#2#3#4#5#6#7%
{%
    \xint_UDzerofork
      #1\dummy  \XINT_div_sub_C   %
       0\dummy  \XINT_div_sub_D   % pas de retenue
    \krof
    {#7}#2#3#4#5%
}%
\def\XINT_div_sub_D #1#2\W\X\Y\Z
{%
    \expandafter\space
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1%
}%
\def\XINT_div_sub_C #1#2#3#4#5%
{%
    \xint_gob_til_W #2\xint_div_sub_cz\W
    \XINT_div_sub_AC_onestep {#5#4#3#2}{#1}%
}%
\def\XINT_div_sub_AC_onestep #1%
{%
    \expandafter\XINT_div_sub_backtoC\the\numexpr 11#1-\xint_c_i\relax.%
}%
\def\XINT_div_sub_backtoC #1#2#3.#4%
{%
    \XINT_div_sub_AC_checkcarry #2{#3#4}% la retenue va \^etre examin\'ee
}%
\def\XINT_div_sub_AC_checkcarry #1%
{%
    \xint_gob_til_one #1\xint_div_sub_AC_nocarry 1\XINT_div_sub_C
}%
\def\xint_div_sub_AC_nocarry 1\XINT_div_sub_C #1#2\W\X\Y\Z
{%
    \expandafter\space
    \romannumeral0%
    \XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
```

```
      \xint_relax
    #1%
}%
\def\xint_div_sub_cz\W\XINT_div_sub_AC_onestep #1#2{ #2}%
\def\xint_div_sub_az\W\XINT_div_sub_B #1#2#3#4\Z { #3}%
```

DECIMAL OPERATIONS: FIRST DIGIT, LASTDIGIT, ODDNESS, MULTIPLICATION BY TEN, QUOTIENT BY TEN, QUOTIENT OR MULTIPLICATION BY POWER OF TEN, SPLIT OPERATION.

21.34 \xintFDg

FIRST DIGIT. Code simplified in 1.05. And prepared for redefinition by xintfrac to parse through \xintNum

```
\def\xintiFDg {\romannumeral0\xintifdg }%
\def\xintifdg #1%
{%
    \expandafter\XINT_fdg \romannumeral-`0#1\W\Z
}%
\let\xintFDg\xintiFDg \let\xintfdg\xintifdg
\def\XINT_FDg #1{\romannumeral0\XINT_fdg #1\W\Z }%
\def\XINT_fdg #1#2#3\Z
{%
    \xint_UDzerominusfork
      #1-\dummy  { 0}%   zero
      0#1\dummy  { #2}%  negative
       0-\dummy  { #1}%  positive
    \krof
}%
```

21.35 \xintLDg

LAST DIGIT. Simplified in 1.05. And prepared for extension by xintfrac to parse through \xintNum

```
\def\xintiLDg {\romannumeral0\xintildg }%
\def\xintildg #1%
{%
    \expandafter\XINT_ldg\expandafter {\romannumeral-`0#1}%
}%
\let\xintLDg\xintiLDg \let\xintldg\xintildg
\def\XINT_LDg #1{\romannumeral0\XINT_ldg {#1}}%
\def\XINT_ldg #1%
{%
    \expandafter\XINT_ldg_\romannumeral0\XINT_rev {#1}\Z
}%
\def\XINT_ldg_ #1#2\Z{ #1}%
```

21.36 \xintMON

MINUS ONE TO THE POWER N

```
\def\xintiMON {\romannumeral0\xintimon }%
\def\xintimon #1%
{%
    \ifodd\xintiLDg {#1}
        \xint_afterfi{ -1}%
    \else
        \xint_afterfi{ 1}%
    \fi
}%
\def\xintiMMON {\romannumeral0\xintimmon }%
\def\xintimmon #1%
{%
    \ifodd\xintiLDg {#1}
        \xint_afterfi{ 1}%
    \else
        \xint_afterfi{ -1}%
    \fi
}%
\let\xintMON\xintiMON \let\xintmon\xintimon
\let\xintMMON\xintiMMON \let\xintmmon\xintimmon
```

21.37 \xintOdd

ODDNESS. 1.05 defines \xintiOdd, so \xintOdd can be modified by xintfrac to parse through \xintNum.

```
\def\xintiOdd {\romannumeral0\xintiodd }%
\def\xintiodd #1%
{%
    \ifodd\xintiLDg{#1}
        \xint_afterfi{ 1}%
    \else
        \xint_afterfi{ 0}%
    \fi
}%
\def\XINT_Odd #1%
{\romannumeral0%
    \ifodd\XINT_LDg{#1}
        \xint_afterfi{ 1}%
    \else
        \xint_afterfi{ 0}%
    \fi
}%
\let\xintOdd\xintiOdd \let\xintodd\xintiodd
```

21.38 \xintDSL

```
DECIMAL SHIFT LEFT (=MULTIPLICATION PAR 10)
```

```
\def\xintDSL {\romannumeral0\xintdsl }%
\def\xintdsl #1%
{%
    \expandafter\XINT_dsl \romannumeral-`0#1\Z
}%
\def\XINT_DSL #1{\romannumeral0\XINT_dsl #1\Z }%
\def\XINT_dsl #1%
{%
    \xint_gob_til_zero #1\xint_dsl_zero 0\XINT_dsl_ #1%
}%
\def\xint_dsl_zero 0\XINT_dsl_ 0#1\Z { 0}%
\def\XINT_dsl_ #1\Z { #10}%
```

21.39 \xintDSR

```
DECIMAL SHIFT RIGHT (=DIVISION PAR 10)
```

```
\def\xintDSR {\romannumeral0\xintdsr }%
\def\xintdsr #1%
{%
    \expandafter\XINT_dsr_a\expandafter {\romannumeral-`0#1}\W\Z
}%
\def\XINT_DSR #1{\romannumeral0\XINT_dsr_a {#1}\W\Z }%
\def\XINT_dsr_a
{%
    \expandafter\XINT_dsr_b\romannumeral0\XINT_rev
}%
\def\XINT_dsr_b #1#2#3\Z
{%
    \xint_gob_til_W #2\xint_dsr_onedigit\W
    \xint_minus #2\xint_dsr_onedigit-%
    \expandafter\XINT_dsr_removew
    \romannumeral0\XINT_rev {#2#3}%
}%
\def\xint_dsr_onedigit #1\XINT_rev #2{ 0}%
\def\XINT_dsr_removew #1\W { }%
```

21.40 \xintDSH, \xintDSHr

```
DECIMAL SHIFTS \xintDSH {x}{A}
si x <= 0, fait A -> A.10^(|x|). v1.03 corrige l'oversight pour A=0.n si x >
0, et A >=0, fait A -> quo(A,10^(x))
si x > 0, et A < 0, fait A -> -quo(-A,10^(x))
(donc pour x > 0 c'est comme DSR itéré x fois)
\xintDSHr donne le 'reste' (si x<=0 donne zéro).
```

Release 1.06 now feeds x to a \numexpr first. I will revise the legacy code on another occasion.

```
\def\xintDSHr {\romannumeral0\xintdshr }%
\def\xintdshr #1%
{%
    \expandafter\XINT_dshr_checkxpositive \the\numexpr #1\relax\Z
}%
\def\XINT_dshr_checkxpositive #1%
{%
    \xint_UDzerominusfork
      0#1\dummy \XINT_dshr_xzeroorneg
      #1-\dummy \XINT_dshr_xzeroorneg
       0-\dummy \XINT_dshr_xpositive
    \krof #1%
}%
\def\XINT_dshr_xzeroorneg #1\Z #2{ 0}%
\def\XINT_dshr_xpositive #1\Z
{%
    \expandafter\xint_secondoftwo_andstop\romannumeral0\xintdsx {#1}%
}%
\def\xintDSH {\romannumeral0\xintdsh }%
\def\xintdsh #1#2%
{%
    \expandafter\xint_dsh\expandafter {\romannumeral-`0#2}{#1}%
}%
\def\xint_dsh #1#2%
{%
    \expandafter\XINT_dsh_checksignx \the\numexpr #2\relax\Z {#1}%
}%
\def\XINT_dsh_checksignx #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_dsh_xiszero
      0#1\dummy  \XINT_dsx_xisNeg_checkA     % on passe direct dans DSx
       0-\dummy  {\XINT_dsh_xisPos #1}%
    \krof
}%
\def\XINT_dsh_xiszero #1\Z #2{ #2}%
\def\XINT_dsh_xisPos #1\Z #2%
{%
    \expandafter\xint_firstoftwo_andstop
    \romannumeral0\XINT_dsx_checksignA #2\Z {#1}% via DSx
}%
```

21.41 \xintDSx

Je fais cette routine pour la version 1.01, après modification de \xintDecSplit. Dorénavant \xintDSx fera appel à \xintDecSplit et de même \xintDSH fera appel

```
à \xintDSx. J'ai donc supprimé entièrement l'ancien code de \xintDSH et re-écrit
entièrement celui de \xintDecSplit pour x positif.
  --> Attention le cas x=0 est traité dans la même catégorie que x > 0 <--
si x < 0, fait A -> A.10^(|x|)
si x >= 0, et A >=0, fait A -> {quo(A,10^(x))}{rem(A,10^(x))}
si x >= 0, et A < 0, d'abord on calcule {quo(-A,10^(x))}{rem(-A,10^(x))}
puis, si le premier n'est pas nul on lui donne le signe -
si le premier est nul on donne le signe - au second.
  On peut donc toujours reconstituer l'original A par 10^x Q \pm R où il faut
prendre le signe plus si Q est positif ou nul et le signe moins si Q est stricte-
ment négatif.
  Release 1.06 has a faster and more compactly coded \XINT_dsx_zeroloop. Also,
x is now given to a \numexpr. The earlier code should be then simplified, but
I leave as is for the time being.
  In 1.07, I decide to modify the coding of \XINT_dsx_zeroloop, to avoid im-
pacting the input stack (which prevented doing truncation or rounding or float
with more than eight times the size of input stack; 40000 = 8x5000 digits on
my installation.) I think this was the only place in the code with such non tail
recursion, as I recall being careful to avoid problems within the Factorial and
Power routines, but I would need to check. Too tired now after having finished
\xintexpr, \xintNewExpr, and \xintfloatexpr!

2988 \def\xintDSx {\romannumeral0\xintdsx }%
2989 \def\xintdsx #1#2%
2990 {%
2991     \expandafter\xint_dsx\expandafter {\romannumeral-`0#2}{#1}%
2992 }%
2993 \def\xint_dsx #1#2%
2994 {%
2995     \expandafter\XINT_dsx_checksignx \the\numexpr #2\relax\Z {#1}%
2996 }%
2997 \def\XINT_DSx #1#2{\romannumeral0\XINT_dsx_checksignx #1\Z {#2}}%
2998 \def\XINT_dsx #1#2{\XINT_dsx_checksignx #1\Z {#2}}%
2999 \def\XINT_dsx_checksignx #1%
3000 {%
3001     \xint_UDzerominusfork
3002       #1-\dummy  \XINT_dsx_xisZero
3003       0#1\dummy  \XINT_dsx_xisNeg_checkA
3004        0-\dummy  {\XINT_dsx_xisPos #1}%
3005     \krof
3006 }%
3007 \def\XINT_dsx_xisZero #1\Z #2{ {#2}{0}}% attention comme x > 0
3008 \def\XINT_dsx_xisNeg_checkA #1\Z #2%
3009 {%
3010     \XINT_dsx_xisNeg_checkA_ #2\Z {#1}%
3011 }%
3012 \def\XINT_dsx_xisNeg_checkA_ #1#2\Z #3%
3013 {%
3014     \xint_gob_til_zero #1\XINT_dsx_xisNeg_Azero 0%
```

```
    \XINT_dsx_xisNeg_checkx {#3}{#3}{}\Z {#1#2}%
}%
\def\XINT_dsx_xisNeg_Azero #1\Z #2{ 0}%
\def\XINT_dsx_xisNeg_checkx #1%
{%
    \ifnum #1>999999999
       \xint_afterfi
       {\xintError:TooBigDecimalShift
        \expandafter\space\expandafter 0\xint_gobble_iv }%
    \else
       \expandafter \XINT_dsx_zeroloop
    \fi
}%
\def\XINT_dsx_zeroloop #1#2%
{%
    \ifnum #1<9 \XINT_dsx_exita\fi
    \expandafter\XINT_dsx_zeroloop\expandafter
        {\the\numexpr #1-8}{#200000000}%
}%
\def\XINT_dsx_exita\fi\expandafter\XINT_dsx_zeroloop
{%
    \fi\expandafter\XINT_dsx_exitb
}%
\def\XINT_dsx_exitb #1#2%
{%
    \expandafter\expandafter\expandafter
    \XINT_dsx_addzeros\csname xint_gobble_\romannumeral -#1\endcsname #2%
}%
\def\XINT_dsx_addzeros #1\Z #2{ #2#1}%
\def\XINT_dsx_xisPos #1\Z #2%
{%
    \XINT_dsx_checksignA #2\Z {#1}%
}%
\def\XINT_dsx_checksignA #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_dsx_AisZero
      0#1\dummy  \XINT_dsx_AisNeg
       0-\dummy  {\XINT_dsx_AisPos #1}%
    \krof
}%
\def\XINT_dsx_AisZero #1\Z #2{ {0}{0}}%
\def\XINT_dsx_AisNeg #1\Z #2%
{%
    \expandafter\XINT_dsx_AisNeg_dosplit_andcheckfirst
    \romannumeral0\XINT_split_checksizex {#2}{#1}%
}%
\def\XINT_dsx_AisNeg_dosplit_andcheckfirst #1%
{%
```

```
3064     \XINT_dsx_AisNeg_checkiffirstempty #1\Z
3065 }%
3066 \def\XINT_dsx_AisNeg_checkiffirstempty #1%
3067 {%
3068     \xint_gob_til_Z #1\XINT_dsx_AisNeg_finish_zero\Z
3069     \XINT_dsx_AisNeg_finish_notzero #1%
3070 }%
3071 \def\XINT_dsx_AisNeg_finish_zero\Z
3072     \XINT_dsx_AisNeg_finish_notzero\Z #1%
3073 {%
3074     \expandafter\XINT_dsx_end
3075     \expandafter {\romannumeral0\XINT_num {-#1}}{0}%
3076 }%
3077 \def\XINT_dsx_AisNeg_finish_notzero #1\Z #2%
3078 {%
3079     \expandafter\XINT_dsx_end
3080     \expandafter {\romannumeral0\XINT_num {#2}}{-#1}%
3081 }%
3082 \def\XINT_dsx_AisPos #1\Z #2%
3083 {%
3084     \expandafter\XINT_dsx_AisPos_finish
3085     \romannumeral0\XINT_split_checksizex {#2}{#1}%
3086 }%
3087 \def\XINT_dsx_AisPos_finish #1#2%
3088 {%
3089     \expandafter\XINT_dsx_end
3090     \expandafter {\romannumeral0\XINT_num {#2}}%
3091                  {\romannumeral0\XINT_num {#1}}%
3092 }%
3093 \def\XINT_dsx_end #1#2%
3094 {%
3095     \expandafter\space\expandafter{#2}{#1}%
3096 }%
```

21.42 \xintDecSplit, \xintDecSplitL, \xintDecSplitR

```
DECIMAL SPLIT
  The macro \xintDecSplit {x}{A} first replaces A with |A| (*) This macro cuts
the number into two pieces L and R. The concatenation LR always reproduces |A|,
and R may be empty or have leading zeros. The position of the cut is specified
by the first argument x. If x is zero or positive the cut location is x slots
to the left of the right end of the number. If x becomes equal to or larger than
the length of the number then L becomes empty. If x is negative the location
of the cut is |x| slots to the right of the left end of the number.
  (*) warning: this may change in a future version. Only the behavior for A non-
negative is guaranteed to remain the same.
  v1.05a: \XINT_split_checksizex does not compute the length anymore, rather
the error will be from a \numexpr; but the limit of 999999999 does not make much
sense.
```

```
   v1.06: Improvements in \XINT_split_fromleft_loop, \XINT_split_fromright_loop
  and related macros. More readable coding, speed gains. Also, I now feed imme-
  diately a \numexpr with x. Some simplifications should probably be made to the
  code, which is kept as is for the time being.

3097 \def\xintDecSplitL {\romannumeral0\xintdecsplitl }%
3098 \def\xintDecSplitR {\romannumeral0\xintdecsplitr }%
3099 \def\xintdecsplitl
3100 {%
3101     \expandafter\xint_firstoftwo_andstop
3102     \romannumeral0\xintdecsplit
3103 }%
3104 \def\xintdecsplitr
3105 {%
3106     \expandafter\xint_secondoftwo_andstop
3107     \romannumeral0\xintdecsplit
3108 }%
3109 \def\xintDecSplit {\romannumeral0\xintdecsplit }%
3110 \def\xintdecsplit #1#2%
3111 {%
3112     \expandafter \xint_split \expandafter
3113     {\romannumeral0\xintiabs {#2}}{#1}%  fait expansion de A
3114 }%
3115 \def\xint_split #1#2%
3116 {%
3117     \expandafter\XINT_split_checksizex\expandafter{\the\numexpr #2}{#1}%
3118 }%
3119 \def\XINT_split_checksizex #1% 999999999 is anyhow very big, could be reduced
3120 {%
3121     \ifnum\numexpr\XINT_Abs{#1}>999999999
3122        \xint_afterfi {\xintError:TooBigDecimalSplit\XINT_split_bigx }%
3123     \else
3124        \expandafter\XINT_split_xfork
3125     \fi
3126     #1\Z
3127 }%
3128 \def\XINT_split_bigx  #1\Z #2%
3129 {%
3130     \ifcase\XINT_Sgn {#1}
3131     \or \xint_afterfi { {}{#2}}% positive big x
3132     \else
3133         \xint_afterfi { {#2}{}}% negative big x
3134     \fi
3135 }%
3136 \def\XINT_split_xfork #1%
3137 {%
3138     \xint_UDzerominusfork
3139       #1-\dummy  \XINT_split_zerosplit
3140       0#1\dummy  \XINT_split_fromleft
```

```
3141        0-\dummy  {\XINT_split_fromright #1}%
3142     \krof
3143 }%
3144 \def\XINT_split_zerosplit #1\Z #2{ {#2}{}}%
3145 \def\XINT_split_fromleft  #1\Z #2%
3146 {%
3147     \XINT_split_fromleft_loop {#1}{}#2\W\W\W\W\W\W\W\W\Z
3148 }%
3149 \def\XINT_split_fromleft_loop #1%
3150 {%
3151     \ifnum #1<8 \XINT_split_fromleft_exita\fi
3152     \expandafter\XINT_split_fromleft_loop_perhaps\expandafter
3153     {\the\numexpr #1-8\expandafter}\XINT_split_fromleft_eight
3154 }%
3155 \def\XINT_split_fromleft_eight #1#2#3#4#5#6#7#8#9{#9{#1#2#3#4#5#6#7#8#9}}%
3156 \def\XINT_split_fromleft_loop_perhaps #1#2%
3157 {%
3158     \xint_gob_til_W #2\XINT_split_fromleft_toofar\W
3159     \XINT_split_fromleft_loop {#1}%
3160 }%
3161 \def\XINT_split_fromleft_toofar\W\XINT_split_fromleft_loop #1#2#3\Z
3162 {%
3163     \XINT_split_fromleft_toofar_b #2\Z
3164 }%
3165 \def\XINT_split_fromleft_toofar_b #1\W #2\Z { {#1}{}}%
3166 \def\XINT_split_fromleft_exita\fi
3167     \expandafter\XINT_split_fromleft_loop_perhaps\expandafter #1#2%
3168    {\fi \XINT_split_fromleft_exitb #1}%
3169 \def\XINT_split_fromleft_exitb\the\numexpr #1-8\expandafter
3170 {%
3171     \csname XINT_split_fromleft_endsplit_\romannumeral #1\endcsname
3172 }%
3173 \def\XINT_split_fromleft_endsplit_ #1#2\W #3\Z { {#1}{#2}}%
3174 \def\XINT_split_fromleft_endsplit_i #1#2%
3175                 {\XINT_split_fromleft_checkiftoofar #2{#1#2}}%
3176 \def\XINT_split_fromleft_endsplit_ii #1#2#3%
3177                 {\XINT_split_fromleft_checkiftoofar #3{#1#2#3}}%
3178 \def\XINT_split_fromleft_endsplit_iii #1#2#3#4%
3179                 {\XINT_split_fromleft_checkiftoofar #4{#1#2#3#4}}%
3180 \def\XINT_split_fromleft_endsplit_iv #1#2#3#4#5%
3181                 {\XINT_split_fromleft_checkiftoofar #5{#1#2#3#4#5}}%
3182 \def\XINT_split_fromleft_endsplit_v #1#2#3#4#5#6%
3183                 {\XINT_split_fromleft_checkiftoofar #6{#1#2#3#4#5#6}}%
3184 \def\XINT_split_fromleft_endsplit_vi #1#2#3#4#5#6#7%
3185                 {\XINT_split_fromleft_checkiftoofar #7{#1#2#3#4#5#6#7}}%
3186 \def\XINT_split_fromleft_endsplit_vii #1#2#3#4#5#6#7#8%
3187                 {\XINT_split_fromleft_checkiftoofar #8{#1#2#3#4#5#6#7#8}}%
3188 \def\XINT_split_fromleft_checkiftoofar #1#2#3\W #4\Z
3189 {%
```

```
    \xint_gob_til_W #1\XINT_split_fromleft_wenttoofar\W
    \space {#2}{#3}%
}%
\def\XINT_split_fromleft_wenttoofar\W\space #1%
{%
    \XINT_split_fromleft_wenttoofar_b #1\Z
}%
\def\XINT_split_fromleft_wenttoofar_b #1\W #2\Z { {#1}}%
\def\XINT_split_fromright #1\Z #2%
{%
    \expandafter \XINT_split_fromright_a \expandafter
    {\romannumeral0\XINT_rev {#2}}{#1}{#2}%
}%
\def\XINT_split_fromright_a #1#2%
{%
    \XINT_split_fromright_loop {#2}{}#1\W\W\W\W\W\W\W\W\Z
}%
\def\XINT_split_fromright_loop #1%
{%
    \ifnum #1<8 \XINT_split_fromright_exita\fi
    \expandafter\XINT_split_fromright_loop_perhaps\expandafter
    {\the\numexpr #1-8\expandafter }\XINT_split_fromright_eight
}%
\def\XINT_split_fromright_eight #1#2#3#4#5#6#7#8#9{#9{#9#8#7#6#5#4#3#2#1}}%
\def\XINT_split_fromright_loop_perhaps #1#2%
{%
    \xint_gob_til_W #2\XINT_split_fromright_toofar\W
    \XINT_split_fromright_loop {#1}%
}%
\def\XINT_split_fromright_toofar\W\XINT_split_fromright_loop #1#2#3\Z { {}}%
\def\XINT_split_fromright_exita\fi
    \expandafter\XINT_split_fromright_loop_perhaps\expandafter #1#2%
    {\fi \XINT_split_fromright_exitb #1}%
\def\XINT_split_fromright_exitb\the\numexpr #1-8\expandafter
{%
    \csname XINT_split_fromright_endsplit_\romannumeral #1\endcsname
}%
\def\XINT_split_fromright_endsplit_ #1#2\W #3\Z #4%
{%
    \expandafter\space\expandafter {\romannumeral0\XINT_rev{#2}}{#1}%
}%
\def\XINT_split_fromright_endsplit_i   #1#2%
            {\XINT_split_fromright_checkiftoofar #2{#2#1}}%
\def\XINT_split_fromright_endsplit_ii  #1#2#3%
            {\XINT_split_fromright_checkiftoofar #3{#3#2#1}}%
\def\XINT_split_fromright_endsplit_iii #1#2#3#4%
            {\XINT_split_fromright_checkiftoofar #4{#4#3#2#1}}%
\def\XINT_split_fromright_endsplit_iv  #1#2#3#4#5%
            {\XINT_split_fromright_checkiftoofar #5{#5#4#3#2#1}}%
```

```
\def\XINT_split_fromright_endsplit_v   #1#2#3#4#5#6%
            {\XINT_split_fromright_checkiftoofar #6{#6#5#4#3#2#1}}%
\def\XINT_split_fromright_endsplit_vi  #1#2#3#4#5#6#7%
            {\XINT_split_fromright_checkiftoofar #7{#7#6#5#4#3#2#1}}%
\def\XINT_split_fromright_endsplit_vii #1#2#3#4#5#6#7#8%
            {\XINT_split_fromright_checkiftoofar #8{#8#7#6#5#4#3#2#1}}%
\def\XINT_split_fromright_checkiftoofar #1%
{%
    \xint_gob_til_W #1\XINT_split_fromright_wenttoofar\W
    \XINT_split_fromright_endsplit_
}%
\def\XINT_split_fromright_wenttoofar\W\XINT_split_fromright_endsplit_ #1\Z #2%
    { {}{#2}}%
```

21.43 \xintDouble

v1.08

```
\def\xintDouble {\romannumeral0\xintdouble }%
\def\xintdouble #1%
{%
     \expandafter\XINT_dbl\romannumeral-`0#1%
     \R\R\R\R\R\R\Z \W\W\W\W\W\W\W
}%
\def\XINT_dbl #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_dbl_zero
      0#1\dummy  \XINT_dbl_neg
       0-\dummy {\XINT_dbl_pos #1}%
    \krof
}%
\def\XINT_dbl_zero #1\Z \W\W\W\W\W\W\W { 0}%
\def\XINT_dbl_neg
   {\expandafter\xint_minus_andstop\romannumeral0\XINT_dbl_pos }%
\def\XINT_dbl_pos
{%
    \expandafter\XINT_dbl_a \expandafter{\expandafter}\expandafter 0%
    \romannumeral0\XINT_SQ {}%
}%
\def\XINT_dbl_a #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_W #9\XINT_dbl_end_a\W
    \expandafter\XINT_dbl_b
    \the\numexpr \xint_c_x^viii+#2+\xint_c_ii*#9#8#7#6#5#4#3\relax {#1}%
}%
\def\XINT_dbl_b 1#1#2#3#4#5#6#7#8#9%
{%
    \XINT_dbl_a {#2#3#4#5#6#7#8#9}{#1}%
```

```
}%
\def\XINT_dbl_end_a #1+#2+#3\relax #4%
{%
    \expandafter\XINT_dbl_end_b #2#4%
}%
\def\XINT_dbl_end_b #1#2#3#4#5#6#7#8%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7#8\relax
}%
```

21.44 \xintHalf

v1.08

```
\def\xintHalf {\romannumeral0\xinthalf }%
\def\xinthalf #1%
{%
     \expandafter\XINT_half\romannumeral-`0#1%
     \R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W
}%
\def\XINT_half #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_half_zero
      0#1\dummy  \XINT_half_neg
       0-\dummy {\XINT_half_pos #1}%
    \krof
}%
\def\XINT_half_zero #1\Z \W\W\W\W\W\W\W { 0}%
\def\XINT_half_neg {\expandafter\XINT_opp\romannumeral0\XINT_half_pos }%
\def\XINT_half_pos {\expandafter\XINT_half_a\romannumeral0\XINT_SQ {}}%
\def\XINT_half_a #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_W #8\XINT_half_dont\W
    \expandafter\XINT_half_b
    \the\numexpr \xint_c_x^viii+\xint_c_v*#7#6#5#4#3#2#1\relax #8%
}%
\def\XINT_half_dont\W\expandafter\XINT_half_b
    \the\numexpr \xint_c_x^viii+\xint_c_v*#1#2#3#4#5#6#7\relax \W\W\W\W\W\W\W
{%
    \expandafter\space
    \the\numexpr (#1#2#3#4#5#6#7+\xint_c_i)/\xint_c_ii-\xint_c_i \relax
}%
\def\XINT_half_b 1#1#2#3#4#5#6#7#8%
{%
    \XINT_half_c {#2#3#4#5#6#7}{#1}%
}%
\def\XINT_half_c #1#2#3#4#5#6#7#8#9%
{%
```

```
    \xint_gob_til_W #3\XINT_half_end_a #2\W
    \expandafter\XINT_half_d
    \the\numexpr \xint_c_x^viii+\xint_c_v*#9#8#7#6#5#4#3+#2\relax {#1}%
}%
\def\XINT_half_d 1#1#2#3#4#5#6#7#8#9%
{%
    \XINT_half_c {#2#3#4#5#6#7#8#9}{#1}%
}%
\def\XINT_half_end_a #1\W #2\relax #3%
{%
    \xint_gob_til_zero #1\XINT_half_end_b 0\space #1#3%
}%
\def\XINT_half_end_b 0\space 0#1#2#3#4#5#6#7%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7\relax
}%
```

21.45 \xintDec

v1.08

```
\def\xintDec {\romannumeral0\xintdec }%
\def\xintdec #1%
{%
     \expandafter\XINT_dec\romannumeral-`0#1%
     \R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W\W
}%
\def\XINT_dec #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_dec_zero
      0#1\dummy  \XINT_dec_neg
       0-\dummy {\XINT_dec_pos #1}%
    \krof
}%
\def\XINT_dec_zero #1\W\W\W\W\W\W\W\W { -1}%
\def\XINT_dec_neg
   {\expandafter\xint_minus_andstop\romannumeral0\XINT_inc_pos }%
\def\XINT_dec_pos
{%
    \expandafter\XINT_dec_a \expandafter{\expandafter}%
    \romannumeral0\XINT_OQ {}%
}%
\def\XINT_dec_a #1#2#3#4#5#6#7#8#9%
{%
    \expandafter\XINT_dec_b
    \the\numexpr 11#9#8#7#6#5#4#3#2-\xint_c_i\relax {#1}%
}%
\def\XINT_dec_b 1#1%
```

```
{%
    \xint_gob_til_one #1\XINT_dec_A 1\XINT_dec_c
}%
\def\XINT_dec_c #1#2#3#4#5#6#7#8#9{\XINT_dec_a {#1#2#3#4#5#6#7#8#9}}%
\def\XINT_dec_A 1\XINT_dec_c #1#2#3#4#5#6#7#8#9%
   {\XINT_dec_B {#1#2#3#4#5#6#7#8#9}}%
\def\XINT_dec_B #1#2\W\W\W\W\W\W\W\W
{%
    \expandafter\XINT_dec_cleanup
    \romannumeral0\XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    #1%
}%
\def\XINT_dec_cleanup #1#2#3#4#5#6#7#8%
{\expandafter\space\the\numexpr #1#2#3#4#5#6#7#8\relax }%
```

21.46 \xintInc

v1.08

```
\def\xintInc {\romannumeral0\xintinc }%
\def\xintinc #1%
{%
     \expandafter\XINT_inc\romannumeral-`0#1%
     \R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W\W
}%
\def\XINT_inc #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_inc_zero
      0#1\dummy  \XINT_inc_neg
       0-\dummy {\XINT_inc_pos #1}%
    \krof
}%
\def\XINT_inc_zero #1\W\W\W\W\W\W\W\W { 1}%
\def\XINT_inc_neg {\expandafter\XINT_opp\romannumeral0\XINT_dec_pos }%
\def\XINT_inc_pos
{%
    \expandafter\XINT_inc_a \expandafter{\expandafter}%
    \romannumeral0\XINT_OQ {}%
}%
\def\XINT_inc_a #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_W #9\XINT_inc_end\W
    \expandafter\XINT_inc_b
    \the\numexpr 10#9#8#7#6#5#4#3#2+\xint_c_i\relax {#1}%
```

```
}%
\def\XINT_inc_b 1#1%
{%
    \xint_gob_til_zero #1\XINT_inc_A 0\XINT_inc_c
}%
\def\XINT_inc_c #1#2#3#4#5#6#7#8#9{\XINT_inc_a {#1#2#3#4#5#6#7#8#9}}%
\def\XINT_inc_A 0\XINT_inc_c #1#2#3#4#5#6#7#8#9%
                {\XINT_dec_B {#1#2#3#4#5#6#7#8#9}}%
\def\XINT_inc_end\W #1\relax #2{ 1#2}%
```

21.47 \xintiSqrt, \xintiSquareRoot

v1.08

```
\def\XINT_dsx_addzerosnofuss #1{\XINT_dsx_zeroloop {#1}{}\Z }%
\def\xintiSqrt {\romannumeral0\xintisqrt }%
\def\xintisqrt
    {\expandafter\XINT_sqrt_post\romannumeral0\xintisquareroot }%
\def\XINT_sqrt_post #1#2{\XINT_dec_pos #1\R\R\R\R\R\R\R\R\Z
                                          \W\W\W\W\W\W\W\W }%
\def\xintiSquareRoot {\romannumeral0\xintisquareroot }%
\def\xintisquareroot #1%
    {\expandafter\XINT_sqrt_checkin\romannumeral-`0#1\Z}%
\def\XINT_sqrt_checkin #1%
{%
    \xint_UDzerominusfork
     #1-\dummy  \XINT_sqrt_iszero
     0#1\dummy  \XINT_sqrt_isneg
      0-\dummy {\XINT_sqrt #1}%
    \krof
}%
\def\XINT_sqrt_iszero #1\Z { 0}%
\def\XINT_sqrt_isneg  #1\Z {\xintError:RootOfNegative\space 0}%
\def\XINT_sqrt #1\Z
{%
    \expandafter\XINT_sqrt_start\expandafter
    {\romannumeral0\XINT_length {#1}}{#1}%
}%
\def\XINT_sqrt_start #1%
{%
    \ifnum #1<\xint_c_x
       \expandafter\XINT_sqrt_small_a
    \else
       \expandafter\XINT_sqrt_big_a
    \fi
    {#1}%
}%
\def\XINT_sqrt_small_a #1{\XINT_sqrt_a {#1}\XINT_sqrt_small_d }%
\def\XINT_sqrt_big_a   #1{\XINT_sqrt_a {#1}\XINT_sqrt_big_d   }%
```

```
\def\XINT_sqrt_a #1%
{%
   \ifodd #1
     \expandafter\XINT_sqrt_bB
   \else
     \expandafter\XINT_sqrt_bA
   \fi
   {#1}%
}%
\def\XINT_sqrt_bA #1#2#3%
{%
    \XINT_sqrt_bA_b #3\Z #2{#1}{#3}%
}%
\def\XINT_sqrt_bA_b #1#2#3\Z
{%
    \XINT_sqrt_c {#1#2}%
}%
\def\XINT_sqrt_bB #1#2#3%
{%
    \XINT_sqrt_bB_b #3\Z #2{#1}{#3}%
}%
\def\XINT_sqrt_bB_b #1#2\Z
{%
    \XINT_sqrt_c #1%
}%
\def\XINT_sqrt_c #1#2%
{%
    \expandafter #2%
    \ifcase #1
    \or 2\or 2\or 2\or 3\or 3\or 3\or 3\or 3\or %3+5
    4\or 4\or 4\or 4\or 4\or 4\or 4\or           %+7
    5\or 5\or 5\or 5\or 5\or 5\or 5\or 5\or 5\or %+9
    6\or 6\or 6\or 6\or 6\or 6\or 6\or 6\or 6\or 6\or 6\or %+11
    7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or 7\or %+13
    8\or 8\or 8\or 8\or 8\or 8\or 8\or
    8\or 8\or 8\or 8\or 8\or 8\or 8\or 8\or %+15
    9\or 9\or 9\or 9\or 9\or 9\or 9\or 9\or
    9\or 9\or 9\or 9\or 9\or 9\or 9\or 9\or 9\or %+17
    10\or 10\or 10\or 10\or 10\or 10\or 10\or 10\or 10\or
    10\or 10\or 10\or 10\or 10\or 10\or 10\or 10\or 10\or 10\or\fi %+19
}%
\def\XINT_sqrt_small_d #1\or #2\fi #3%
{%
   \fi
   \expandafter\XINT_sqrt_small_de
   \ifcase \numexpr #3/\xint_c_ii-\xint_c_i\relax
      {}%
   \or
      0%
```

```
    \or
       {00}%
    \or
       {000}%
    \or
       {0000}%
    \or
    \fi {#1}%
}%
\def\XINT_sqrt_small_de #1\or #2\fi #3%
{%
     \fi\XINT_sqrt_small_e {#3#1}%
}%
\def\XINT_sqrt_small_e #1#2%
{%
    \expandafter\XINT_sqrt_small_f\expandafter {\the\numexpr #1*#1-#2}{#1}%
}%
\def\XINT_sqrt_small_f #1#2%
{%
    \expandafter\XINT_sqrt_small_g\expandafter
    {\the\numexpr ((#1+#2)/(\xint_c_ii*#2))-\xint_c_i}{#1}{#2}%
}%
\def\XINT_sqrt_small_g #1%
{%
     \ifnum #1>\xint_c_
        \expandafter\XINT_sqrt_small_h
     \else
        \expandafter\XINT_sqrt_small_end
     \fi
     {#1}%
}%
\def\XINT_sqrt_small_h #1#2#3%
{%
     \expandafter\XINT_sqrt_small_f\expandafter
     {\the\numexpr #2-\xint_c_ii*#1*#3+#1*#1\expandafter}\expandafter
     {\the\numexpr #3-#1}%
}%
\def\XINT_sqrt_small_end #1#2#3{ {#3}{#2}}%
\def\XINT_sqrt_big_d #1\or #2\fi #3%
{%
    \fi
    \ifodd #3
      \xint_afterfi{\expandafter\XINT_sqrt_big_eB}%
    \else
      \xint_afterfi{\expandafter\XINT_sqrt_big_eA}%
    \fi
    \expandafter{\the\numexpr #3/\xint_c_ii }{#1}%
}%
\def\XINT_sqrt_big_eA  #1#2#3%
```

```
{%
    \XINT_sqrt_big_eA_a #3\Z {#2}{#1}{#3}%
}%
\def\XINT_sqrt_big_eA_a #1#2#3#4#5#6#7#8#9\Z
{%
    \XINT_sqrt_big_eA_b {#1#2#3#4#5#6#7#8}%
}%
\def\XINT_sqrt_big_eA_b #1#2%
{%
    \expandafter\XINT_sqrt_big_f
    \romannumeral0\XINT_sqrt_small_e {#2000}{#1}{#1}%
}%
\def\XINT_sqrt_big_eB #1#2#3%
{%
    \XINT_sqrt_big_eB_a #3\Z {#2}{#1}{#3}%
}%
\def\XINT_sqrt_big_eB_a #1#2#3#4#5#6#7#8#9%
{%
    \XINT_sqrt_big_eB_b {#1#2#3#4#5#6#7#8#9}%
}%
\def\XINT_sqrt_big_eB_b #1#2\Z #3%
{%
    \expandafter\XINT_sqrt_big_f
    \romannumeral0\XINT_sqrt_small_e {#30000}{#1}{#1}%
}%
\def\XINT_sqrt_big_f #1#2#3#4%
{%
   \expandafter\XINT_sqrt_big_f_a\expandafter
   {\the\numexpr #2+#3\expandafter}\expandafter
   {\romannumeral-`0\XINT_dsx_addzerosnofuss
                    {\numexpr #4-\xint_c_iv\relax}{#1}}{#4}%
}%
\def\XINT_sqrt_big_f_a #1#2#3#4%
{%
   \expandafter\XINT_sqrt_big_g\expandafter
   {\romannumeral0\xintisub
       {\XINT_dsx_addzerosnofuss
        {\numexpr \xint_c_ii*#3-\xint_c_viii\relax}{#1}}{#4}}%
   {#2}{#3}%
}%
\def\XINT_sqrt_big_g #1#2%
{%
    \expandafter\XINT_sqrt_big_j
    \romannumeral0\xintidivision{#1}
        {\romannumeral0\XINT_dbl_pos #2\R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W }{#2}%
}%
\def\XINT_sqrt_big_j #1%
{%
    \ifcase\XINT_Sgn {#1}
```

```
3606         \expandafter \XINT_sqrt_big_end
3607     \or \expandafter \XINT_sqrt_big_k
3608     \fi {#1}%
3609 }%
3610 \def\XINT_sqrt_big_k #1#2#3%
3611 {%
3612     \expandafter\XINT_sqrt_big_l\expandafter
3613     {\romannumeral0\xintisub {#3}{#1}}%
3614     {\romannumeral0\xintiadd {#2}{\xintiSqr {#1}}}%
3615 }%
3616 \def\XINT_sqrt_big_l #1#2%
3617 {%
3618    \expandafter\XINT_sqrt_big_g\expandafter
3619    {#2}{#1}%
3620 }%
3621 \def\XINT_sqrt_big_end #1#2#3#4{ {#3}{#2}}%
3622 \XINT_restorecatcodes_endinput%
```

22 Package xintbinhex implementation

The commenting is currently (2013/06/16) very sparse.

Contents

22.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the master xint package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
3623 \begingroup\catcode61\catcode48\catcode32=10\relax%
3624   \catcode13=5    % ^^M
3625   \endlinechar=13 %
3626   \catcode123=1   % {
3627   \catcode125=2   % }
3628   \catcode64=11   % @
3629   \catcode35=6    % #
3630   \catcode44=12   % ,
3631   \catcode45=12   % -
3632   \catcode46=12   % .
```

```
\catcode58=12   % :
\def\space { }%
\let\z\endgroup
\expandafter\let\expandafter\x\csname ver@xintbinhex.sty\endcsname
\expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
\expandafter
  \ifx\csname PackageInfo\endcsname\relax
    \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
  \else
    \def\y#1#2{\PackageInfo{#1}{#2}}%
  \fi
\expandafter
\ifx\csname numexpr\endcsname\relax
   \y{xintbinhex}{\numexpr not available, aborting input}%
   \aftergroup\endinput
\else
  \ifx\x\relax   % plain-TeX, first loading of xintbinhex.sty
    \ifx\w\relax % but xint.sty not yet loaded.
       \y{xintbinhex}{Package xint is required}%
       \y{xintbinhex}{Will try \string\input\space xint.sty}%
       \def\z{\endgroup\input xint.sty\relax}%
    \fi
  \else
    \def\empty {}%
    \ifx\x\empty % LaTeX, first loading,
    % variable is initialized, but \ProvidesPackage not yet seen
        \ifx\w\relax % xint.sty not yet loaded.
          \y{xintbinhex}{Package xint is required}%
          \y{xintbinhex}{Will try \string\RequirePackage{xint}}%
          \def\z{\endgroup\RequirePackage{xint}}%
        \fi
    \else
      \y{xintbinhex}{I was already loaded, aborting input}%
      \aftergroup\endinput
    \fi
  \fi
\fi
\z%
```

22.2 Confirmation of xint loading

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
```

```
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \def\empty {}%
  \expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
  \ifx\w\relax % Plain TeX, user gave a file name at the prompt
      \y{xintbinhex}{Loading of package xint failed, aborting input}%
      \aftergroup\endinput
  \fi
  \ifx\w\empty % LaTeX, user gave a file name at the prompt
      \y{xintbinhex}{Loading of package xint failed, aborting input}%
      \aftergroup\endinput
  \fi
\endgroup%
```

22.3 Catcodes

Perhaps catcodes have changed after the loading of **xint** and prior to the current loading of **xintbinhex**, so we can not employ the `\XINT_restorecatcodes_endinput` in this style file. But there is no problem using `\XINT_setcatcodes`.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_binhex_restorecatcodes_endinput
      {%
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
```

```
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
  }%
\x
```

22.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode91=12 % [
  \catcode93=12 % ]
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xintbinhex.sty\endcsname
\ProvidesPackage{xintbinhex}%
  [2013/06/14 v1.08b Expandable binary and hexadecimal conversions (jfB)]%
```

22.5 Constants, etc...

```
v1.08
```

```
\chardef\xint_c_xvi           16
\chardef\xint_c_ii^v          32
\chardef\xint_c_ii^vi         64
\chardef\xint_c_ii^vii       128
```

```
\mathchardef\xint_c_ii^viii  256
\mathchardef\xint_c_ii^xii  4096
\newcount\xint_c_ii^xv  \xint_c_ii^xv  32768
\newcount\xint_c_ii^xvi \xint_c_ii^xvi 65536
\newcount\xint_c_x^v    \xint_c_x^v    100000
\newcount\xint_c_x^ix   \xint_c_x^ix   1000000000
\def\XINT_tmp_def #1{%
  \expandafter\edef\csname XINT_sdth_#1\endcsname
  {\ifcase #1 0\or 1\or 2\or 3\or 4\or 5\or 6\or 7\or
              8\or 9\or A\or B\or C\or D\or E\or F\fi}}%
\xintApplyUnbraced\XINT_tmp_def
    {{0}{1}{2}{3}{4}{5}{6}{7}{8}{9}{10}{11}{12}{13}{14}{15}}%
\def\XINT_tmp_def #1{%
  \expandafter\edef\csname XINT_sdtb_#1\endcsname
  {\ifcase #1
   0000\or 0001\or 0010\or 0011\or 0100\or 0101\or 0110\or 0111\or
   1000\or 1001\or 1010\or 1011\or 1100\or 1101\or 1110\or 1111\fi}}%
\xintApplyUnbraced\XINT_tmp_def
    {{0}{1}{2}{3}{4}{5}{6}{7}{8}{9}{10}{11}{12}{13}{14}{15}}%
\let\XINT_tmp_def\empty
\expandafter\def\csname XINT_sbtd_0000\endcsname {0}%
\expandafter\def\csname XINT_sbtd_0001\endcsname {1}%
\expandafter\def\csname XINT_sbtd_0010\endcsname {2}%
\expandafter\def\csname XINT_sbtd_0011\endcsname {3}%
\expandafter\def\csname XINT_sbtd_0100\endcsname {4}%
\expandafter\def\csname XINT_sbtd_0101\endcsname {5}%
\expandafter\def\csname XINT_sbtd_0110\endcsname {6}%
\expandafter\def\csname XINT_sbtd_0111\endcsname {7}%
\expandafter\def\csname XINT_sbtd_1000\endcsname {8}%
\expandafter\def\csname XINT_sbtd_1001\endcsname {9}%
\expandafter\def\csname XINT_sbtd_1010\endcsname {10}%
\expandafter\def\csname XINT_sbtd_1011\endcsname {11}%
\expandafter\def\csname XINT_sbtd_1100\endcsname {12}%
\expandafter\def\csname XINT_sbtd_1101\endcsname {13}%
\expandafter\def\csname XINT_sbtd_1110\endcsname {14}%
\expandafter\def\csname XINT_sbtd_1111\endcsname {15}%
\expandafter\let\csname XINT_sbth_0000\expandafter\endcsname
                \csname XINT_sbtd_0000\endcsname
\expandafter\let\csname XINT_sbth_0001\expandafter\endcsname
                \csname XINT_sbtd_0001\endcsname
\expandafter\let\csname XINT_sbth_0010\expandafter\endcsname
                \csname XINT_sbtd_0010\endcsname
\expandafter\let\csname XINT_sbth_0011\expandafter\endcsname
                \csname XINT_sbtd_0011\endcsname
\expandafter\let\csname XINT_sbth_0100\expandafter\endcsname
                \csname XINT_sbtd_0100\endcsname
\expandafter\let\csname XINT_sbth_0101\expandafter\endcsname
                \csname XINT_sbtd_0101\endcsname
\expandafter\let\csname XINT_sbth_0110\expandafter\endcsname
```

```
                \csname XINT_sbtd_0110\endcsname
\expandafter\let\csname XINT_sbth_0111\expandafter\endcsname
                \csname XINT_sbtd_0111\endcsname
\expandafter\let\csname XINT_sbth_1000\expandafter\endcsname
                \csname XINT_sbtd_1000\endcsname
\expandafter\let\csname XINT_sbth_1001\expandafter\endcsname
                \csname XINT_sbtd_1001\endcsname
\expandafter\def\csname XINT_sbth_1010\endcsname {A}%
\expandafter\def\csname XINT_sbth_1011\endcsname {B}%
\expandafter\def\csname XINT_sbth_1100\endcsname {C}%
\expandafter\def\csname XINT_sbth_1101\endcsname {D}%
\expandafter\def\csname XINT_sbth_1110\endcsname {E}%
\expandafter\def\csname XINT_sbth_1111\endcsname {F}%
\expandafter\def\csname XINT_shtb_0\endcsname {0000}%
\expandafter\def\csname XINT_shtb_1\endcsname {0001}%
\expandafter\def\csname XINT_shtb_2\endcsname {0010}%
\expandafter\def\csname XINT_shtb_3\endcsname {0011}%
\expandafter\def\csname XINT_shtb_4\endcsname {0100}%
\expandafter\def\csname XINT_shtb_5\endcsname {0101}%
\expandafter\def\csname XINT_shtb_6\endcsname {0110}%
\expandafter\def\csname XINT_shtb_7\endcsname {0111}%
\expandafter\def\csname XINT_shtb_8\endcsname {1000}%
\expandafter\def\csname XINT_shtb_9\endcsname {1001}%
\def\XINT_shtb_A {1010}%
\def\XINT_shtb_B {1011}%
\def\XINT_shtb_C {1100}%
\def\XINT_shtb_D {1101}%
\def\XINT_shtb_E {1110}%
\def\XINT_shtb_F {1111}%
\def\XINT_shtb_G {}%
\def\XINT_smallhex #1%
{%
    \expandafter\XINT_smallhex_a\expandafter
    {\the\numexpr (#1+\xint_c_viii)/\xint_c_xvi-\xint_c_i}{#1}%
}%
\def\XINT_smallhex_a #1#2%
{%
    \csname XINT_sdth_#1\expandafter\expandafter\expandafter\endcsname
    \csname XINT_sdth_\the\numexpr #2-\xint_c_xvi*#1\endcsname
}%
\def\XINT_smallbin #1%
{%
    \expandafter\XINT_smallbin_a\expandafter
    {\the\numexpr (#1+\xint_c_viii)/\xint_c_xvi-\xint_c_i}{#1}%
}%
\def\XINT_smallbin_a #1#2%
{%
    \csname XINT_sdtb_#1\expandafter\expandafter\expandafter\endcsname
    \csname XINT_sdtb_\the\numexpr #2-\xint_c_xvi*#1\endcsname
```

```
}%
```

22.6 \xintDecToHex, \xintDecToBin

v1.08

```
\def\xintDecToHex {\romannumeral0\xintdectohex }%
\def\xintdectohex #1%
        {\expandafter\XINT_dth_checkin\romannumeral-`0#1\W\W\W\W \T}%
\def\XINT_dth_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy \XINT_dth_N
        -\dummy {\XINT_dth_P #1}%
     \krof
}%
\def\XINT_dth_N {\expandafter\xint_minus_andstop\romannumeral0\XINT_dth_P }%
\def\XINT_dth_P {\expandafter\XINT_dth_III\romannumeral-`0\XINT_dtbh_I {0.}}%
\def\xintDecToBin {\romannumeral0\xintdectobin }%
\def\xintdectobin #1%
        {\expandafter\XINT_dtb_checkin\romannumeral-`0#1\W\W\W\W \T }%
\def\XINT_dtb_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy \XINT_dtb_N
        -\dummy {\XINT_dtb_P #1}%
     \krof
}%
\def\XINT_dtb_N {\expandafter\xint_minus_andstop\romannumeral0\XINT_dtb_P }%
\def\XINT_dtb_P {\expandafter\XINT_dtb_III\romannumeral-`0\XINT_dtbh_I {0.}}%
\def\XINT_dtbh_I #1#2#3#4#5%
{%
    \xint_gob_til_W #5\XINT_dtbh_II_a\W\XINT_dtbh_I_a  {}{#2#3#4#5}#1\Z.%
}%
\def\XINT_dtbh_II_a\W\XINT_dtbh_I_a #1#2{\XINT_dtbh_II_b #2}%
\def\XINT_dtbh_II_b #1#2#3#4%
{%
    \xint_gob_til_W
      #1\XINT_dtbh_II_c
      #2\XINT_dtbh_II_ci
      #3\XINT_dtbh_II_cii
      \W\XINT_dtbh_II_ciii #1#2#3#4%
}%
\def\XINT_dtbh_II_c \W\XINT_dtbh_II_ci
                    \W\XINT_dtbh_II_cii
                    \W\XINT_dtbh_II_ciii \W\W\W\W {{}}%
\def\XINT_dtbh_II_ci #1\XINT_dtbh_II_ciii #2\W\W\W
   {\XINT_dtbh_II_d {}{#2}{0}}%
\def\XINT_dtbh_II_cii\W\XINT_dtbh_II_ciii #1#2\W\W
```

```
3906    {\XINT_dtbh_II_d {}{#1#2}{00}}%
3907 \def\XINT_dtbh_II_ciii #1#2#3\W
3908    {\XINT_dtbh_II_d {}{#1#2#3}{000}}%
3909 \def\XINT_dtbh_I_a #1#2#3.%
3910 {%
3911     \xint_gob_til_Z #3\XINT_dtbh_I_z\Z
3912     \expandafter\XINT_dtbh_I_b\the\numexpr #2+#30000.{#1}%
3913 }%
3914 \def\XINT_dtbh_I_b #1.%
3915 {%
3916     \expandafter\XINT_dtbh_I_c\the\numexpr
3917     (#1+\xint_c_ii^xv)/\xint_c_ii^xvi-\xint_c_i.#1.%
3918 }%
3919 \def\XINT_dtbh_I_c #1.#2.%
3920 {%
3921     \expandafter\XINT_dtbh_I_d\expandafter
3922     {\the\numexpr #2-\xint_c_ii^xvi*#1}{#1}%
3923 }%
3924 \def\XINT_dtbh_I_d #1#2#3{\XINT_dtbh_I_a {#3#1.}{#2}}%
3925 \def\XINT_dtbh_I_z\Z\expandafter\XINT_dtbh_I_b\the\numexpr #1+#2.%
3926 {%
3927     \ifnum #1=\xint_c_ \expandafter\XINT_dtbh_I_end_zb\fi
3928     \XINT_dtbh_I_end_za {#1}%
3929 }%
3930 \def\XINT_dtbh_I_end_za #1#2{\XINT_dtbh_I {#2#1.}}%
3931 \def\XINT_dtbh_I_end_zb\XINT_dtbh_I_end_za #1#2{\XINT_dtbh_I {#2}}%
3932 \def\XINT_dtbh_II_d #1#2#3#4.%
3933 {%
3934     \xint_gob_til_Z #4\XINT_dtbh_II_z\Z
3935     \expandafter\XINT_dtbh_II_e\the\numexpr #2+#4#3.{#1}{#3}%
3936 }%
3937 \def\XINT_dtbh_II_e #1.%
3938 {%
3939     \expandafter\XINT_dtbh_II_f\the\numexpr
3940         (#1+\xint_c_ii^xv)/\xint_c_ii^xvi-\xint_c_i.#1.%
3941 }%
3942 \def\XINT_dtbh_II_f #1.#2.%
3943 {%
3944     \expandafter\XINT_dtbh_II_g\expandafter
3945     {\the\numexpr #2-\xint_c_ii^xvi*#1}{#1}%
3946 }%
3947 \def\XINT_dtbh_II_g #1#2#3{\XINT_dtbh_II_d {#3#1.}{#2}}%
3948 \def\XINT_dtbh_II_z\Z\expandafter\XINT_dtbh_II_e\the\numexpr #1+#2.%
3949 {%
3950     \ifnum #1=\xint_c_ \expandafter\XINT_dtbh_II_end_zb\fi
3951     \XINT_dtbh_II_end_za {#1}%
3952 }%
3953 \def\XINT_dtbh_II_end_za #1#2#3{{}#2#1.\Z.}%
3954 \def\XINT_dtbh_II_end_zb\XINT_dtbh_II_end_za #1#2#3{{}#2\Z.}%
```

```
\def\XINT_dth_III #1#2.%
{%
    \xint_gob_til_Z #2\XINT_dth_end\Z
    \expandafter\XINT_dth_III\expandafter
    {\romannumeral-`0\XINT_dth_small #2.#1}%
}%
\def\XINT_dth_small #1.%
{%
    \expandafter\XINT_smallhex\expandafter
    {\the\numexpr (#1+\xint_c_ii^vii)/\xint_c_ii^viii-\xint_c_i\expandafter}%
    \romannumeral-`0\expandafter\XINT_smallhex\expandafter
    {\the\numexpr
    #1-((#1+\xint_c_ii^vii)/\xint_c_ii^viii-\xint_c_i)*\xint_c_ii^viii}%
}%
\def\XINT_dth_end\Z\expandafter\XINT_dth_III\expandafter #1#2\T
{%
    \XINT_dth_end_b #1%
}%
\def\XINT_dth_end_b #1.{\XINT_dth_end_c }%
\def\XINT_dth_end_c #1{\xint_gob_til_zero #1\XINT_dth_end_d 0\space #1}%
\def\XINT_dth_end_d 0\space 0#1%
{%
    \xint_gob_til_zero #1\XINT_dth_end_e 0\space #1%
}%
\def\XINT_dth_end_e 0\space 0#1%
{%
    \xint_gob_til_zero #1\XINT_dth_end_f 0\space #1%
}%
\def\XINT_dth_end_f 0\space 0{ }%
\def\XINT_dtb_III #1#2.%
{%
    \xint_gob_til_Z #2\XINT_dtb_end\Z
    \expandafter\XINT_dtb_III\expandafter
    {\romannumeral-`0\XINT_dtb_small #2.#1}%
}%
\def\XINT_dtb_small #1.%
{%
    \expandafter\XINT_smallbin\expandafter
    {\the\numexpr (#1+\xint_c_ii^vii)/\xint_c_ii^viii-\xint_c_i\expandafter}%
    \romannumeral-`0\expandafter\XINT_smallbin\expandafter
    {\the\numexpr
    #1-((#1+\xint_c_ii^vii)/\xint_c_ii^viii-\xint_c_i)*\xint_c_ii^viii}%
}%
\def\XINT_dtb_end\Z\expandafter\XINT_dtb_III\expandafter #1#2\T
{%
    \XINT_dtb_end_b #1%
}%
\def\XINT_dtb_end_b #1.{\XINT_dtb_end_c }%
\def\XINT_dtb_end_c #1#2#3#4#5#6#7#8%
```

```
{%
    \expandafter\XINT_dtb_end_d\the\numexpr #1#2#3#4#5#6#7#8\relax
}%
\def\XINT_dtb_end_d #1#2#3#4#5#6#7#8#9%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7#8#9\relax
}%
```

22.7 \xintHexToDec

v1.08

```
\def\xintHexToDec {\romannumeral0\xinthextodec }%
\def\xinthextodec #1%
        {\expandafter\XINT_htd_checkin\romannumeral-‘0#1\W\W\W\W \T }%
\def\XINT_htd_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy \XINT_htd_neg
        -\dummy {\XINT_htd_I {0000}#1}%
     \krof
}%
\def\XINT_htd_neg {\expandafter\xint_minus_andstop
                   \romannumeral0\XINT_htd_I {0000}}%
\def\XINT_htd_I #1#2#3#4#5%
{%
    \xint_gob_til_W #5\XINT_htd_II_a\W
    \XINT_htd_I_a  {}{"#2#3#4#5}#1\Z\Z\Z\Z
}%
\def\XINT_htd_II_a \W\XINT_htd_I_a #1#2{\XINT_htd_II_b #2}%
\def\XINT_htd_II_b "#1#2#3#4%
{%
    \xint_gob_til_W
      #1\XINT_htd_II_c
      #2\XINT_htd_II_ci
      #3\XINT_htd_II_cii
      \W\XINT_htd_II_ciii #1#2#3#4%
}%
\def\XINT_htd_II_c \W\XINT_htd_II_ci
                   \W\XINT_htd_II_cii
                   \W\XINT_htd_II_ciii \W\W\W\W #1\Z\Z\Z\Z\T
{%
    \expandafter\xint_cleanupzeros_andstop
    \romannumeral0\XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
```

```
\def\XINT_htd_II_ci #1\XINT_htd_II_ciii
                      #2\W\W\W {\XINT_htd_II_d {}{"#2}{\xint_c_xvi}}%
\def\XINT_htd_II_cii\W\XINT_htd_II_ciii
                      #1#2\W\W {\XINT_htd_II_d {}{"#1#2}{\xint_c_ii^viii}}%
\def\XINT_htd_II_ciii #1#2#3\W {\XINT_htd_II_d {}{"#1#2#3}{\xint_c_ii^xii}}%
\def\XINT_htd_I_a #1#2#3#4#5#6%
{%
    \xint_gob_til_Z #3\XINT_htd_I_end_a\Z
    \expandafter\XINT_htd_I_b\the\numexpr
    #2+\xint_c_ii^xvi*#6#5#4#3+\xint_c_x^ix\relax {#1}%
}%
\def\XINT_htd_I_b 1#1#2#3#4#5#6#7#8#9{\XINT_htd_I_c {#1#2#3#4#5}{#9#8#7#6}}%
\def\XINT_htd_I_c #1#2#3{\XINT_htd_I_a {#3#2}{#1}}%
\def\XINT_htd_I_end_a\Z\expandafter\XINT_htd_I_b\the\numexpr #1+#2\relax
{%
    \expandafter\XINT_htd_I_end_b\the\numexpr \xint_c_x^v+#1\relax
}%
\def\XINT_htd_I_end_b 1#1#2#3#4#5%
{%
    \xint_gob_til_zero #1\XINT_htd_I_end_bz0%
    \XINT_htd_I_end_c #1#2#3#4#5%
}%
\def\XINT_htd_I_end_c #1#2#3#4#5#6{\XINT_htd_I {#6#5#4#3#2#1000}}%
\def\XINT_htd_I_end_bz0\XINT_htd_I_end_c 0#1#2#3#4%
{%
    \xint_gob_til_zeros_iv #1#2#3#4\XINT_htd_I_end_bzz 0000%
    \XINT_htd_I_end_D {#4#3#2#1}%
}%
\def\XINT_htd_I_end_D  #1#2{\XINT_htd_I {#2#1}}%
\def\XINT_htd_I_end_bzz 0000\XINT_htd_I_end_D #1{\XINT_htd_I }%
\def\XINT_htd_II_d #1#2#3#4#5#6#7%
{%
    \xint_gob_til_Z #4\XINT_htd_II_end_a\Z
    \expandafter\XINT_htd_II_e\the\numexpr
    #2+#3*#7#6#5#4+\xint_c_x^viii\relax {#1}{#3}%
}%
\def\XINT_htd_II_e 1#1#2#3#4#5#6#7#8{\XINT_htd_II_f {#1#2#3#4}{#5#6#7#8}}%
\def\XINT_htd_II_f #1#2#3{\XINT_htd_II_d {#2#3}{#1}}%
\def\XINT_htd_II_end_a\Z\expandafter\XINT_htd_II_e
    \the\numexpr #1+#2\relax #3#4\T
{%
    \XINT_htd_II_end_b #1#3%
}%
\def\XINT_htd_II_end_b #1#2#3#4#5#6#7#8%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7#8\relax
}%
```

22.8 \xintBinToDec

v1.08

```
\def\xintBinToDec {\romannumeral0\xintbintodec }%
\def\xintbintodec #1{\expandafter\XINT_btd_checkin
                     \romannumeral-‘0#1\W\W\W\W\W\W\W\W \T }%
\def\XINT_btd_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy \XINT_btd_neg
        -\dummy {\XINT_btd_I {000000}#1}%
     \krof
}%
\def\XINT_btd_neg {\expandafter\xint_minus_andstop
                                \romannumeral0\XINT_btd_I {000000}}%
\def\XINT_btd_I #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_W #9\XINT_btd_II_a {#2#3#4#5#6#7#8#9}\W
    \XINT_btd_I_a {}{\csname XINT_sbtd_#2#3#4#5\endcsname*\xint_c_xvi+%
                     \csname XINT_sbtd_#6#7#8#9\endcsname}%
    #1\Z\Z\Z\Z\Z\Z
}%
\def\XINT_btd_II_a #1\W\XINT_btd_I_a #2#3{\XINT_btd_II_b #1}%
\def\XINT_btd_II_b #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_W
      #1\XINT_btd_II_c
      #2\XINT_btd_II_ci
      #3\XINT_btd_II_cii
      #4\XINT_btd_II_ciii
      #5\XINT_btd_II_civ
      #6\XINT_btd_II_cv
      #7\XINT_btd_II_cvi
      \W\XINT_btd_II_cvii #1#2#3#4#5#6#7#8%
}%
\def\XINT_btd_II_c #1\XINT_btd_II_cvii \W\W\W\W\W\W\W\W #2\Z\Z\Z\Z\Z\Z\T
{%
    \expandafter\XINT_btd_II_c_end
    \romannumeral0\XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
}%
\def\XINT_btd_II_c_end #1#2#3#4#5#6%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6\relax
}%
```

```
\def\XINT_btd_II_ci  #1\XINT_btd_II_cvii #2\W\W\W\W\W\W\W
   {\XINT_btd_II_d {}{#2}{\xint_c_ii }}%
\def\XINT_btd_II_cii #1\XINT_btd_II_cvii #2\W\W\W\W\W\W
   {\XINT_btd_II_d {}{\csname XINT_sbtd_00#2\endcsname }{\xint_c_iv }}%
\def\XINT_btd_II_ciii #1\XINT_btd_II_cvii #2\W\W\W\W\W
   {\XINT_btd_II_d {}{\csname XINT_sbtd_0#2\endcsname }{\xint_c_viii }}%
\def\XINT_btd_II_civ #1\XINT_btd_II_cvii #2\W\W\W\W
   {\XINT_btd_II_d {}{\csname XINT_sbtd_#2\endcsname}{\xint_c_xvi }}%
\def\XINT_btd_II_cv #1\XINT_btd_II_cvii #2#3#4#5#6\W\W\W
{%
    \XINT_btd_II_d {}{\csname XINT_sbtd_#2#3#4#5\endcsname*\xint_c_ii+%
                          #6}{\xint_c_ii^v }%
}%
\def\XINT_btd_II_cvi #1\XINT_btd_II_cvii #2#3#4#5#6#7\W\W
{%
    \XINT_btd_II_d {}{\csname XINT_sbtd_#2#3#4#5\endcsname*\xint_c_iv+%
                        \csname XINT_sbtd_00#6#7\endcsname}{\xint_c_ii^vi }%
}%
\def\XINT_btd_II_cvii #1#2#3#4#5#6#7\W
{%
    \XINT_btd_II_d {}{\csname XINT_sbtd_#1#2#3#4\endcsname*\xint_c_viii+%
                        \csname XINT_sbtd_0#5#6#7\endcsname}{\xint_c_ii^vii }%
}%
\def\XINT_btd_II_d #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_Z #4\XINT_btd_II_end_a\Z
    \expandafter\XINT_btd_II_e\the\numexpr
    #2+(\xint_c_x^ix+#3*#9#8#7#6#5#4)\relax {#1}{#3}%
}%
\def\XINT_btd_II_e 1#1#2#3#4#5#6#7#8#9{\XINT_btd_II_f {#1#2#3}{#4#5#6#7#8#9}}%
\def\XINT_btd_II_f #1#2#3{\XINT_btd_II_d {#2#3}{#1}}%
\def\XINT_btd_II_end_a\Z\expandafter\XINT_btd_II_e
    \the\numexpr #1+(#2\relax #3#4\T
{%
    \XINT_btd_II_end_b #1#3%
}%
\def\XINT_btd_II_end_b #1#2#3#4#5#6#7#8#9%
{%
    \expandafter\space\the\numexpr #1#2#3#4#5#6#7#8#9\relax
}%
\def\XINT_btd_I_a #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_Z #3\XINT_btd_I_end_a\Z
    \expandafter\XINT_btd_I_b\the\numexpr
    #2+\xint_c_ii^viii*#8#7#6#5#4#3+\xint_c_x^ix\relax {#1}%
}%
\def\XINT_btd_I_b 1#1#2#3#4#5#6#7#8#9{\XINT_btd_I_c {#1#2#3}{#9#8#7#6#5#4}}%
\def\XINT_btd_I_c #1#2#3{\XINT_btd_I_a {#3#2}{#1}}%
\def\XINT_btd_I_end_a\Z\expandafter\XINT_btd_I_b
```

```
    \the\numexpr #1+\xint_c_ii^viii #2\relax
{%
    \expandafter\XINT_btd_I_end_b\the\numexpr 1000+#1\relax
}%
\def\XINT_btd_I_end_b 1#1#2#3%
{%
    \xint_gob_til_zeros_iii #1#2#3\XINT_btd_I_end_bz 000%
    \XINT_btd_I_end_c #1#2#3%
}%
\def\XINT_btd_I_end_c #1#2#3#4{\XINT_btd_I {#4#3#2#1000}}%
\def\XINT_btd_I_end_bz 000\XINT_btd_I_end_c 000{\XINT_btd_I }%
```

22.9 \xintBinToHex

v1.08

```
\def\xintBinToHex {\romannumeral0\xintbintohex }%
\def\xintbintohex #1%
{%
    \expandafter\XINT_bth_checkin
                      \romannumeral0\expandafter\XINT_num_loop
                      \romannumeral-`0#1\xint_relax\xint_relax
                                         \xint_relax\xint_relax
                      \xint_relax\xint_relax\xint_relax\xint_relax\Z
    \R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W\W
}%
\def\XINT_bth_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy  \XINT_bth_N
        -\dummy {\XINT_bth_P #1}%
     \krof
}%
\def\XINT_bth_N {\expandafter\xint_minus_andstop\romannumeral0\XINT_bth_P }%
\def\XINT_bth_P {\expandafter\XINT_bth_I\expandafter{\expandafter}%
                  \romannumeral0\XINT_OQ {}}%
\def\XINT_bth_I #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_W #9\XINT_bth_end_a\W
    \expandafter\expandafter\expandafter
    \XINT_bth_I
    \expandafter\expandafter\expandafter
    {\csname XINT_sbth_#9#8#7#6\expandafter\expandafter\expandafter\endcsname
     \csname XINT_sbth_#5#4#3#2\endcsname #1}%
}%
\def\XINT_bth_end_a\W \expandafter\expandafter\expandafter
    \XINT_bth_I       \expandafter\expandafter\expandafter #1%
{%
    \XINT_bth_end_b #1%
```

```
}%
\def\XINT_bth_end_b  #1\endcsname #2\endcsname #3%
{%
    \xint_gob_til_zero #3\XINT_bth_end_z 0\space #3%
}%
\def\XINT_bth_end_z0\space 0{ }%
```

22.10 \xintHexToBin

v1.08

```
\def\xintHexToBin {\romannumeral0\xinthextobin }%
\def\xinthextobin #1%
{%
    \expandafter\XINT_htb_checkin\romannumeral-‘0#1GGGGGGGG\T
}%
\def\XINT_htb_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy  \XINT_htb_N
        -\dummy {\XINT_htb_P #1}%
     \krof
}%
\def\XINT_htb_N {\expandafter\xint_minus_andstop\romannumeral0\XINT_htb_P }%
\def\XINT_htb_P {\XINT_htb_I_a {}}%
\def\XINT_htb_I_a #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_G #9\XINT_htb_II_a G%
    \expandafter\expandafter\expandafter
    \XINT_htb_I_b
    \expandafter\expandafter\expandafter
    {\csname XINT_shtb_#2\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#3\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#4\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#5\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#6\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#7\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#8\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#9\endcsname }{#1}%
}%
\def\XINT_htb_I_b #1#2{\XINT_htb_I_a {#2#1}}%
\def\XINT_htb_II_a G\expandafter\expandafter\expandafter\XINT_htb_I_b
{%
    \expandafter\expandafter\expandafter \XINT_htb_II_b
}%
\def\XINT_htb_II_b #1#2#3\T
{%
    \XINT_num_loop #2#1%
    \xint_relax\xint_relax\xint_relax\xint_relax
```

```
    \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
```

22.11 \xintCHexToBin

v1.08

```
\def\xintCHexToBin {\romannumeral0\xintchextobin }%
\def\xintchextobin #1%
{%
    \expandafter\XINT_chtb_checkin\romannumeral-`0#1%
    \R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W\W
}%
\def\XINT_chtb_checkin #1%
{%
    \xint_UDsignfork
       #1\dummy  \XINT_chtb_N
        -\dummy {\XINT_chtb_P #1}%
     \krof
}%
\def\XINT_chtb_N {\expandafter\xint_minus_andstop\romannumeral0\XINT_chtb_P }%
\def\XINT_chtb_P {\expandafter\XINT_chtb_I\expandafter{\expandafter}%
                  \romannumeral0\XINT_OQ {}}%
\def\XINT_chtb_I #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_W #9\XINT_chtb_end_a\W
    \expandafter\expandafter\expandafter
    \XINT_chtb_I
    \expandafter\expandafter\expandafter
    {\csname XINT_shtb_#9\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#8\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#7\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#6\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#5\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#4\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#3\expandafter\expandafter\expandafter\endcsname
     \csname XINT_shtb_#2\endcsname
     #1}%
}%
\def\XINT_chtb_end_a\W\expandafter\expandafter\expandafter
    \XINT_chtb_I\expandafter\expandafter\expandafter #1%
{%
    \XINT_chtb_end_b #1%
    \xint_relax\xint_relax\xint_relax\xint_relax
    \xint_relax\xint_relax\xint_relax\xint_relax\Z
}%
\def\XINT_chtb_end_b #1\W#2\W#3\W#4\W#5\W#6\W#7\W#8\W\endcsname
{%
    \XINT_num_loop
```

```
}%
\XINT_binhex_restorecatcodes_endinput%
```

23 Package xintgcd implementation

The commenting is currently (2013/06/16) very sparse.

Contents

23.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the master xint package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \def\space { }%
  \let\z\endgroup
  \expandafter\let\expandafter\x\csname ver@xintgcd.sty\endcsname
  \expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \expandafter
  \ifx\csname numexpr\endcsname\relax
     \y{xintgcd}{\numexpr not available, aborting input}%
     \aftergroup\endinput
  \else
```

```
    \ifx\x\relax   % plain-TeX, first loading of xintgcd.sty
      \ifx\w\relax % but xint.sty not yet loaded.
         \y{xintgcd}{Package xint is required}%
         \y{xintgcd}{Will try \string\input\space xint.sty}%
         \def\z{\endgroup\input xint.sty\relax}%
      \fi
    \else
      \def\empty {}%
      \ifx\x\empty % LaTeX, first loading,
      % variable is initialized, but \ProvidesPackage not yet seen
          \ifx\w\relax % xint.sty not yet loaded.
            \y{xintgcd}{Package xint is required}%
            \y{xintgcd}{Will try \string\RequirePackage{xint}}%
            \def\z{\endgroup\RequirePackage{xint}}%
          \fi
      \else
        \y{xintgcd}{I was already loaded, aborting input}%
        \aftergroup\endinput
      \fi
    \fi
  \fi
\z%
```

23.2 Confirmation of xint loading

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \def\empty {}%
  \expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
  \ifx\w\relax % Plain TeX, user gave a file name at the prompt
     \y{xintgcd}{Loading of package xint failed, aborting input}%
     \aftergroup\endinput
  \fi
  \ifx\w\empty % LaTeX, user gave a file name at the prompt
```

```
      \y{xintgcd}{Loading of package xint failed, aborting input}%
      \aftergroup\endinput
  \fi
\endgroup%
```

23.3 Catcodes

Perhaps catcodes have changed after the loading of **xint** and prior to the current loading of **xintgcd**, so we can not employ the \XINT_restorecatcodes_endinput in this style file. But there is no problem using \XINT_setcatcodes.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_gcd_restorecatcodes_endinput
      {%
        \catcode36=\the\catcode36   % $
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
      \catcode36=3  % $
  }%
\x
```

23.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode91=12 % [
  \catcode93=12 % ]
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xintgcd.sty\endcsname
\ProvidesPackage{xintgcd}%
  [2013/06/14 v1.08b Euclide algorithm with xint package (jfB)]%
```

23.5 \xintGCD

```
\def\xintGCD {\romannumeral0\xintgcd }%
\def\xintgcd #1%
{%
    \expandafter\XINT_gcd\expandafter{\romannumeral0\xintiabs {#1}}%
}%
\def\XINT_gcd #1#2%
{%
    \expandafter\XINT_gcd_fork\romannumeral0\xintiabs {#2}\Z #1\Z
}%
```

Ici #3#4=A, #1#2=B

```
\def\XINT_gcd_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_gcd_BisZero
      #3\dummy \XINT_gcd_AisZero
       0\dummy \XINT_gcd_loop
    \krof
    {#1#2}{#3#4}%
}%
\def\XINT_gcd_AisZero #1#2{ #1}%
```

```
\def\XINT_gcd_BisZero #1#2{ #2}%
\def\XINT_gcd_CheckRem #1#2\Z
{%
    \xint_gob_til_zero #1\xint_gcd_end0\XINT_gcd_loop {#1#2}%
}%
\def\xint_gcd_end0\XINT_gcd_loop #1#2{ #2}%
```

```
#1=B, #2=A
```

```
\def\XINT_gcd_loop #1#2%
{%
    \expandafter\expandafter\expandafter
        \XINT_gcd_CheckRem
    \expandafter\xint_secondoftwo
    \romannumeral0\XINT_div_prepare {#1}{#2}\Z
    {#1}%
}%
```

23.6 \xintBezout

```
\def\xintBezout {\romannumeral0\xintbezout }%
\def\xintbezout #1%
{%
    \expandafter\xint_bezout\expandafter {\romannumeral-`0#1}%
}%
\def\xint_bezout #1#2%
{%
    \expandafter\XINT_bezout_fork \romannumeral-`0#2\Z #1\Z
}%
```

```
#3#4 = A, #1#2=B
```

```
\def\XINT_bezout_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerosfork
     #1#3\dummy \XINT_bezout_botharezero
      #10\dummy \XINT_bezout_secondiszero
      #30\dummy \XINT_bezout_firstiszero
       00\dummy
        {\xint_UDsignsfork
          #1#3\dummy \XINT_bezout_minusminus % A < 0, B < 0
           #1-\dummy \XINT_bezout_minusplus  % A > 0, B < 0
           #3-\dummy \XINT_bezout_plusminus  % A < 0, B > 0
            --\dummy \XINT_bezout_plusplus   % A > 0, B > 0
         \krof }%
    \krof
    {#2}{#4}#1#3{#3#4}{#1#2}% #1#2=B, #3#4=A
}%
\def\XINT_bezout_botharezero #1#2#3#4#5#6%
{%
    \xintError:NoBezoutForZeros
```

```
4523     \space {0}{0}{0}{0}{0}%
4524 }%

 attention première entrée doit être ici (-1)^n donc 1
 #4#2 = 0 = A, B = #3#1

4525 \def\XINT_bezout_firstiszero #1#2#3#4#5#6%
4526 {%
4527     \xint_UDsignfork
4528       #3\dummy { {0}{#3#1}{0}{1}{#1}}%
4529        -\dummy { {0}{#3#1}{0}{-1}{#1}}%
4530     \krof
4531 }%

 #4#2 = A, B = #3#1 = 0

4532 \def\XINT_bezout_secondiszero #1#2#3#4#5#6%
4533 {%
4534     \xint_UDsignfork
4535        #4\dummy{ {#4#2}{0}{-1}{0}{#2}}%
4536         -\dummy{ {#4#2}{0}{1}{0}{#2}}%
4537     \krof
4538 }%

 #4#2= A < 0, #3#1 = B < 0

4539 \def\XINT_bezout_minusminus #1#2#3#4%
4540 {%
4541     \expandafter\XINT_bezout_mm_post
4542     \romannumeral0\XINT_bezout_loop_a 1{#1}{#2}1001%
4543 }%
4544 \def\XINT_bezout_mm_post #1#2%
4545 {%
4546     \expandafter\XINT_bezout_mm_postb\expandafter
4547     {\romannumeral0\xintiopp{#2}}{\romannumeral0\xintiopp{#1}}%
4548 }%
4549 \def\XINT_bezout_mm_postb #1#2%
4550 {%
4551     \expandafter\XINT_bezout_mm_postc\expandafter {#2}{#1}%
4552 }%
4553 \def\XINT_bezout_mm_postc #1#2#3#4#5%
4554 {%
4555     \space {#4}{#5}{#1}{#2}{#3}%
4556 }%

 minusplus #4#2= A > 0, B < 0

4557 \def\XINT_bezout_minusplus #1#2#3#4%
4558 {%
4559     \expandafter\XINT_bezout_mp_post
4560     \romannumeral0\XINT_bezout_loop_a 1{#1}{#4#2}1001%
4561 }%
```

```
\def\XINT_bezout_mp_post #1#2%
{%
    \expandafter\XINT_bezout_mp_postb\expandafter
      {\romannumeral0\xintiopp {#2}}{#1}%
}%
\def\XINT_bezout_mp_postb #1#2#3#4#5%
{%
    \space {#4}{#5}{#2}{#1}{#3}%
}%
```

plusminus A < 0, B > 0

```
\def\XINT_bezout_plusminus #1#2#3#4%
{%
    \expandafter\XINT_bezout_pm_post
    \romannumeral0\XINT_bezout_loop_a 1{#3#1}{#2}1001%
}%
\def\XINT_bezout_pm_post #1%
{%
    \expandafter \XINT_bezout_pm_postb \expandafter
        {\romannumeral0\xintiopp{#1}}%
}%
\def\XINT_bezout_pm_postb #1#2#3#4#5%
{%
    \space {#4}{#5}{#1}{#2}{#3}%
}%
```

plusplus

```
\def\XINT_bezout_plusplus #1#2#3#4%
{%
    \expandafter\XINT_bezout_pp_post
    \romannumeral0\XINT_bezout_loop_a 1{#3#1}{#4#2}1001%
}%
```

la parité (-1)^N est en #1, et on la jette ici.

```
\def\XINT_bezout_pp_post #1#2#3#4#5%
{%
    \space {#4}{#5}{#1}{#2}{#3}%
}%
```

n = 0: 1BAalpha(0)beta(0)alpha(-1)beta(-1)
n général: {(-1)^n}{r(n-1)}{r(n-2)}{alpha(n-1)}{beta(n-1)}{alpha(n-2)}{beta(n-2)}
#2 = B, #3 = A

```
\def\XINT_bezout_loop_a #1#2#3%
{%
    \expandafter\XINT_bezout_loop_b
    \expandafter{\the\numexpr -#1\expandafter }%
    \romannumeral0\XINT_div_prepare {#2}{#3}{#2}%
```

```
}%
```

```
Le q(n) a ici une existence éphémère, dans le version Bezout Algorithm il fau-
dra le conserver. On voudra à la fin {{q(n)}{r(n)}{alpha(n)}{beta(n)}}. De plus
ce n'est plus (-1)^n que l'on veut mais n. (ou dans un autre ordre)
{-(-1)^n}{q(n)}{r(n)}{r(n-1)}{alpha(n-1)}{beta(n-1)}{alpha(n-2)}{beta(n-2)}
```

```
\def\XINT_bezout_loop_b #1#2#3#4#5#6#7#8%
{%
    \expandafter \XINT_bezout_loop_c \expandafter
        {\romannumeral0\xintiadd{\XINT_Mul{#5}{#2}}{#7}}%
        {\romannumeral0\xintiadd{\XINT_Mul{#6}{#2}}{#8}}%
    {#1}{#3}{#4}{#5}{#6}%
}%
```

```
{alpha(n)}{->beta(n)}{-(-1)^n}{r(n)}{r(n-1)}{alpha(n-1)}{beta(n-1)}
```

```
\def\XINT_bezout_loop_c #1#2%
{%
    \expandafter \XINT_bezout_loop_d \expandafter
        {#2}{#1}%
}%
```

```
{beta(n)}{alpha(n)}{(-1)^(n+1)}{r(n)}{r(n-1)}{alpha(n-1)}{beta(n-1)}
```

```
\def\XINT_bezout_loop_d #1#2#3#4#5%
{%
    \XINT_bezout_loop_e #4\Z {#3}{#5}{#2}{#1}%
}%
```

```
r(n)\Z {(-1)^(n+1)}{r(n-1)}{alpha(n)}{beta(n)}{alpha(n-1)}{beta(n-1)}
```

```
\def\XINT_bezout_loop_e #1#2\Z
{%
    \xint_gob_til_zero #1\xint_bezout_loop_exit0\XINT_bezout_loop_f
    {#1#2}%
}%
```

```
{r(n)}{(-1)^(n+1)}{r(n-1)}{alpha(n)}{beta(n)}{alpha(n-1)}{beta(n-1)}
```

```
\def\XINT_bezout_loop_f #1#2%
{%
    \XINT_bezout_loop_a {#2}{#1}%
}%
```

```
{(-1)^(n+1)}{r(n)}{r(n-1)}{alpha(n)}{beta(n)}{alpha(n-1)}{beta(n-1)} et itéra-
tion
```

```
\def\xint_bezout_loop_exit0\XINT_bezout_loop_f #1#2%
{%
    \ifcase #2
    \or  \expandafter\XINT_bezout_exiteven
    \else\expandafter\XINT_bezout_exitodd
    \fi
```

```
}%
\def\XINT_bezout_exiteven #1#2#3#4#5%
{%
    \space {#5}{#4}{#1}%
}%
\def\XINT_bezout_exitodd #1#2#3#4#5%
{%
    \space {-#5}{-#4}{#1}%
}%
```

23.7 \xintEuclideAlgorithm

```
Pour Euclide: {N}{A}{D=r(n)}{B}{q1}{r1}{q2}{r2}{q3}{r3}....{qN}{rN=0}
u<2n> = u<2n+3>u<2n+2> + u<2n+4> à la n ième étape
```

```
\def\xintEuclideAlgorithm {\romannumeral0\xinteuclidealgorithm }%
\def\xinteuclidealgorithm #1%
{%
    \expandafter \XINT_euc \expandafter{\romannumeral0\xintiabs {#1}}%
}%
\def\XINT_euc #1#2%
{%
    \expandafter\XINT_euc_fork \romannumeral0\xintiabs {#2}\Z #1\Z
}%
```

```
Ici #3#4=A, #1#2=B
```

```
\def\XINT_euc_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_euc_BisZero
      #3\dummy \XINT_euc_AisZero
       0\dummy \XINT_euc_a
    \krof
    {0}{#1#2}{#3#4}{{#3#4}{#1#2}}{}\Z
}%
```

```
Le {} pour protéger {{A}{B}} si on s'arrête après une étape (B divise A). On
va renvoyer:
{N}{A}{D=r(n)}{B}{q1}{r1}{q2}{r2}{q3}{r3}....{qN}{rN=0}
```

```
\def\XINT_euc_AisZero #1#2#3#4#5#6{ {1}{0}{#2}{#2}{0}{0}}%
\def\XINT_euc_BisZero #1#2#3#4#5#6{ {1}{0}{#3}{#3}{0}{0}}%
```

```
{n}{rn}{an}{{qn}{rn}}...{{A}{B}}{}\Z
a(n) = r(n-1). Pour n=0 on a juste {0}{B}{A}{{A}{B}}{}\Z
\XINT_div_prepare {u}{v} divise v par u
```

```
\def\XINT_euc_a #1#2#3%
{%
    \expandafter\XINT_euc_b
```

```
4663     \expandafter {\the\numexpr #1+1\expandafter }%
4664     \romannumeral0\XINT_div_prepare {#2}{#3}{#2}%
4665 }%

 {n+1}{q(n+1)}{r(n+1)}{rn}{{qn}{rn}}...

4666 \def\XINT_euc_b #1#2#3#4%
4667 {%
4668     \XINT_euc_c #3\Z {#1}{#3}{#4}{{#2}{#3}}%
4669 }%

 r(n+1)\Z {n+1}{r(n+1)}{r(n)}{{q(n+1)}{r(n+1)}}{{qn}{rn}}...
 Test si r(n+1) est nul.

4670 \def\XINT_euc_c #1#2\Z
4671 {%
4672     \xint_gob_til_zero #1\xint_euc_end0\XINT_euc_a
4673 }%

 {n+1}{r(n+1)}{r(n)}{{q(n+1)}{r(n+1)}}...{}\Z Ici r(n+1) = 0. On arrête on se
 prépare à inverser {n+1}{0}{r(n)}{{q(n+1)}{r(n+1)}}.....{{q1}{r1}}{{A}{B}}{}\Z
 On veut renvoyer: {N=n+1}{A}{D=r(n)}{B}{q1}{r1}{q2}{r2}{q3}{r3}....{qN}{rN=0}

4674 \def\xint_euc_end0\XINT_euc_a #1#2#3#4\Z%
4675 {%
4676     \expandafter\xint_euc_end_
4677     \romannumeral0%
4678     \XINT_rord_main {}#4{{#1}{#3}}%
4679     \xint_relax
4680       \xint_undef\xint_undef\xint_undef\xint_undef
4681       \xint_undef\xint_undef\xint_undef\xint_undef
4682     \xint_relax
4683 }%
4684 \def\xint_euc_end_ #1#2#3%
4685 {%
4686     \space {#1}{#3}{#2}%
4687 }%
```

23.8 \xintBezoutAlgorithm

```
 Pour Bezout: objectif, renvoyer
 {N}{A}{0}{1}{D=r(n)}{B}{1}{0}{q1}{r1}{alpha1=q1}{beta1=1}
 {q2}{r2}{alpha2}{beta2}....{qN}{rN=0}{alphaN=A/D}{betaN=B/D}
 alpha0=1, beta0=0, alpha(-1)=0, beta(-1)=1

4688 \def\xintBezoutAlgorithm {\romannumeral0\xintbezoutalgorithm }%
4689 \def\xintbezoutalgorithm #1%
4690 {%
4691     \expandafter \XINT_bezalg \expandafter{\romannumeral0\xintiabs {#1}}%
4692 }%
```

```
\def\XINT_bezalg #1#2%
{%
    \expandafter\XINT_bezalg_fork \romannumeral0\xintiabs {#2}\Z #1\Z
}%

 Ici #3#4=A, #1#2=B

\def\XINT_bezalg_fork #1#2\Z #3#4\Z
{%
    \xint_UDzerofork
      #1\dummy \XINT_bezalg_BisZero
      #3\dummy \XINT_bezalg_AisZero
       0\dummy \XINT_bezalg_a
    \krof
    0{#1#2}{#3#4}1001{{#3#4}{#1#2}}{}\Z
}%
\def\XINT_bezalg_AisZero #1#2#3\Z{ {1}{0}{0}{1}{#2}{#2}{1}{0}{0}{0}{0}{1}}%
\def\XINT_bezalg_BisZero #1#2#3#4\Z{ {1}{0}{0}{1}{#3}{#3}{1}{0}{0}{0}{0}{1}}%

 pour préparer l'étape n+1 il faut {n}{r(n)}{r(n-1)}{alpha(n)}{beta(n)}{alpha(n-
 1)}{beta(n-1)}{{q(n)}{r(n)}{alpha(n)}{beta(n)}}... division de #3 par #2

\def\XINT_bezalg_a #1#2#3%
{%
    \expandafter\XINT_bezalg_b
    \expandafter {\the\numexpr #1+1\expandafter }%
    \romannumeral0\XINT_div_prepare {#2}{#3}{#2}%
}%

 {n+1}{q(n+1)}{r(n+1)}{r(n)}{alpha(n)}{beta(n)}{alpha(n-1)}{beta(n-1)}...

\def\XINT_bezalg_b #1#2#3#4#5#6#7#8%
{%
    \expandafter\XINT_bezalg_c\expandafter
     {\romannumeral0\xintiadd {\xintiMul {#6}{#2}}{#8}}%
     {\romannumeral0\xintiadd {\xintiMul {#5}{#2}}{#7}}%
     {#1}{#2}{#3}{#4}{#5}{#6}%
}%

 {beta(n+1)}{alpha(n+1)}{n+1}{q(n+1)}{r(n+1)}{r(n)}{alpha(n)}{beta(n)}

\def\XINT_bezalg_c #1#2#3#4#5#6%
{%
    \expandafter\XINT_bezalg_d\expandafter {#2}{#3}{#4}{#5}{#6}{#1}%
}%

 {alpha(n+1)}{n+1}{q(n+1)}{r(n+1)}{r(n)}{beta(n+1)}

\def\XINT_bezalg_d #1#2#3#4#5#6#7#8%
{%
    \XINT_bezalg_e #4\Z {#2}{#4}{#5}{#1}{#6}{#7}{#8}{{#3}{#4}{#1}{#6}}%
}%
```

```
 r(n+1)\Z {n+1}{r(n+1)}{r(n)}{alpha(n+1)}{beta(n+1)}
 {alpha(n)}{beta(n)}{q,r,alpha,beta(n+1)}
 Test si r(n+1) est nul.

\def\XINT_bezalg_e #1#2\Z
{%
    \xint_gob_til_zero #1\xint_bezalg_end0\XINT_bezalg_a
}%

 Ici r(n+1) = 0. On arrête on se prépare à inverser.
 {n+1}{r(n+1)}{r(n)}{alpha(n+1)}{beta(n+1)}{alpha(n)}{beta(n)}
 {q,r,alpha,beta(n+1)}...{{A}{B}}{}\Z
 On veut renvoyer
 {N}{A}{0}{1}{D=r(n)}{B}{1}{0}{q1}{r1}{alpha1=q1}{beta1=1}
 {q2}{r2}{alpha2}{beta2}....{qN}{rN=0}{alphaN=A/D}{betaN=B/D}

\def\xint_bezalg_end0\XINT_bezalg_a #1#2#3#4#5#6#7#8\Z
{%
    \expandafter\xint_bezalg_end_
    \romannumeral0%
    \XINT_rord_main {}#8{{#1}{#3}}%
    \xint_relax
      \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_undef\xint_undef\xint_undef\xint_undef
    \xint_relax
}%

 {N}{D}{A}{B}{q1}{r1}{alpha1=q1}{beta1=1}{q2}{r2}{alpha2}{beta2}
 ....{qN}{rN=0}{alphaN=A/D}{betaN=B/D}
 On veut renvoyer
 {N}{A}{0}{1}{D=r(n)}{B}{1}{0}{q1}{r1}{alpha1=q1}{beta1=1}
 {q2}{r2}{alpha2}{beta2}....{qN}{rN=0}{alphaN=A/D}{betaN=B/D}

\def\xint_bezalg_end_ #1#2#3#4%
{%
    \space {#1}{#3}{0}{1}{#2}{#4}{1}{0}%
}%
```

23.9 \xintTypesetEuclideAlgorithm

```
 TYPESETTING
   Organisation:
   {N}{A}{D}{B}{q1}{r1}{q2}{r2}{q3}{r3}....{qN}{rN=0}
 \U1 = N = nombre d'étapes, \U3 = PGCD, \U2 = A, \U4=B q1 = \U5, q2 = \U7 -->
 qn = \U<2n+3>, rn = \U<2n+4> bn = rn. B = r0. A=r(-1)
   r(n-2) = q(n)r(n-1)+r(n) (n e étape)
   \U{2n} = \U{2n+3} \times \U{2n+2} + \U{2n+4}, n e étape. (avec n entre 1 et
 N)
```

```
\def\xintTypesetEuclideAlgorithm #1#2%
{% l'algo remplace #1 et #2 par |#1| et |#2|
  \par
  \begingroup
    \xintAssignArray\xintEuclideAlgorithm {#1}{#2}\to\U
    \edef\A{\U2}\edef\B{\U4}\edef\N{\U1}%
    \setbox 0 \vbox{\halign {$##$\cr \A\cr \B \cr}}%
    \noindent
    \count 255 1
    \loop
      \hbox to \wd 0 {\hfil$\U{\numexpr 2*\count 255\relax}$}%
      ${} =  \U{\numexpr 2*\count 255 + 3\relax}
      \times \U{\numexpr 2*\count 255 + 2\relax}
          +  \U{\numexpr 2*\count 255 + 4\relax}$%
    \ifnum \count 255 < \N
      \hfill\break
      \advance \count 255 1
    \repeat
  \par
  \endgroup
}%
```

23.10 \xintTypesetBezoutAlgorithm

```
Pour Bezout on a: {N}{A}{0}{1}{D=r(n)}{B}{1}{0}{q1}{r1}{alpha1=q1}{beta1=1}
{q2}{r2}{alpha2}{beta2}....{qN}{rN=0}{alphaN=A/D}{betaN=B/D} Donc 4N+8 termes:
U1 = N, U2= A, U5=D, U6=B, q1 = U9, qn = U{4n+5}, n au moins 1
rn = U{4n+6}, n au moins -1
alpha(n) = U{4n+7}, n au moins -1
beta(n) = U{4n+8}, n au moins -1
```

```
\def\xintTypesetBezoutAlgorithm #1#2%
{%
  \par
  \begingroup
    \parindent0pt
    \xintAssignArray\xintBezoutAlgorithm {#1}{#2}\to\BEZ
    \edef\A{\BEZ2}\edef\B{\BEZ6}\edef\N{\BEZ1}% A = |#1|, B = |#2|
    \setbox 0 \vbox{\halign {$##$\cr \A\cr \B \cr}}%
    \count 255 1
    \loop
      \noindent
      \hbox to \wd 0 {\hfil$\BEZ{4*\count 255 - 2}$}%
      ${} =  \BEZ{4*\count 255 + 5}
      \times \BEZ{4*\count 255 + 2}
          +  \BEZ{4*\count 255 + 6}$\hfill\break
      \hbox to \wd 0 {\hfil$\BEZ{4*\count 255 +7}$}%
      ${} = \BEZ{4*\count 255 + 5}
      \times \BEZ{4*\count 255 + 3}
```

```
          +  \BEZ{4*\count 255 - 1}$\hfill\break
      \hbox to \wd 0 {\hfil$\BEZ{4*\count 255 +8}$}%
      ${} =  \BEZ{4*\count 255 + 5}
      \times \BEZ{4*\count 255 + 4}
          +  \BEZ{4*\count 255 }$
      \endgraf
    \ifnum \count 255 < \N
    \advance \count 255 1
  \repeat
  \par
    \edef\U{\BEZ{4*\N + 4}}%
    \edef\V{\BEZ{4*\N + 3}}%
    \edef\D{\BEZ5}%
    \ifodd\N
       $\U\times\A  - \V\times \B = -\D$%
    \else
       $\U\times\A - \V\times\B = \D$%
    \fi
  \par
  \endgroup
}%
\XINT_gcd_restorecatcodes_endinput%
```

24 Package xintfrac implementation

The commenting is currently (2013/06/16) very sparse.

Contents

24.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the master **xint** package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \def\space { }%
  \let\z\endgroup
  \expandafter\let\expandafter\x\csname ver@xintfrac.sty\endcsname
  \expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \expandafter
  \ifx\csname numexpr\endcsname\relax
     \y{xintfrac}{\numexpr not available, aborting input}%
     \aftergroup\endinput
  \else
    \ifx\x\relax   % plain-TeX, first loading of xintfrac.sty
      \ifx\w\relax % but xint.sty not yet loaded.
         \y{xintfrac}{Package xint is required}%
         \y{xintfrac}{Will try \string\input\space xint.sty}%
```

```
4838         \def\z{\endgroup\input xint.sty\relax}%
4839       \fi
4840     \else
4841       \def\empty {}%
4842       \ifx\x\empty % LaTeX, first loading,
4843       % variable is initialized, but \ProvidesPackage not yet seen
4844           \ifx\w\relax % xint.sty not yet loaded.
4845             \y{xintfrac}{Package xint is required}%
4846             \y{xintfrac}{Will try \string\RequirePackage{xint}}%
4847             \def\z{\endgroup\RequirePackage{xint}}%
4848           \fi
4849       \else
4850         \y{xintfrac}{I was already loaded, aborting input}%
4851         \aftergroup\endinput
4852       \fi
4853     \fi
4854   \fi
4855 \z%
```

24.2 Confirmation of xint loading

```
4856 \begingroup\catcode61\catcode48\catcode32=10\relax%
4857   \catcode13=5    % ^^M
4858   \endlinechar=13 %
4859   \catcode123=1   % {
4860   \catcode125=2   % }
4861   \catcode64=11   % @
4862   \catcode35=6    % #
4863   \catcode44=12   % ,
4864   \catcode45=12   % -
4865   \catcode46=12   % .
4866   \catcode58=12   % :
4867   \expandafter
4868     \ifx\csname PackageInfo\endcsname\relax
4869       \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
4870     \else
4871       \def\y#1#2{\PackageInfo{#1}{#2}}%
4872     \fi
4873   \def\empty {}%
4874   \expandafter\let\expandafter\w\csname ver@xint.sty\endcsname
4875   \ifx\w\relax % Plain TeX, user gave a file name at the prompt
4876       \y{xintfrac}{Loading of package xint failed, aborting input}%
4877       \aftergroup\endinput
4878   \fi
4879   \ifx\w\empty % LaTeX, user gave a file name at the prompt
4880       \y{xintfrac}{Loading of package xint failed, aborting input}%
4881       \aftergroup\endinput
4882   \fi
4883 \endgroup%
```

24.3 Catcodes

Perhaps catcodes have changed after the loading of xint and prior to the current loading of xintfrac, so we can not employ the \XINT_restorecatcodes_endinput in this style file. But there is no problem using \XINT_setcatcodes.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_frac_restorecatcodes_endinput
      {%
        \catcode93=\the\catcode93   % ]
        \catcode91=\the\catcode91   % [
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
      \catcode91=12 % [
      \catcode93=12 % ]
  }%
\x
```

24.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xintfrac.sty\endcsname
\ProvidesPackage{xintfrac}%
  [2013/06/14 v1.08b Expandable operations on fractions (jfB)]%
\chardef\xint_c_vi     6
\chardef\xint_c_vii    7
\chardef\xint_c_xviii 18
\mathchardef\xint_c_x^iv 10000
```

24.5 \xintLen

```
\def\xintLen {\romannumeral0\xintlen }%
\def\xintlen #1%
{%
    \expandafter\XINT_flen\romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_flen #1#2#3%
{%
    \expandafter\space
    \the\numexpr -1+\XINT_Abs {#1}+\XINT_Len {#2}+\XINT_Len {#3}\relax
}%
```

24.6 \XINT_lenrord_loop

```
\def\XINT_lenrord_loop #1#2#3#4#5#6#7#8#9%
{%  faire \romannumeral-`0\XINT_lenrord_loop 0{}#1\Z\W\W\W\W\W\W\W\Z
    \xint_gob_til_W #9\XINT_lenrord_W\W
    \expandafter\XINT_lenrord_loop\expandafter
    {\the\numexpr #1+7}{#9#8#7#6#5#4#3#2}%
}%
\def\XINT_lenrord_W\W\expandafter\XINT_lenrord_loop\expandafter #1#2#3\Z
```

```
{%
    \expandafter\XINT_lenrord_X\expandafter {#1}#2\Z
}%
\def\XINT_lenrord_X #1#2\Z
{%
    \XINT_lenrord_Y #2\R\R\R\R\R\R\T {#1}%
}%
\def\XINT_lenrord_Y #1#2#3#4#5#6#7#8\T
{%
    \xint_gob_til_W
            #7\XINT_lenrord_Z \xint_c_viii
            #6\XINT_lenrord_Z \xint_c_vii
            #5\XINT_lenrord_Z \xint_c_vi
            #4\XINT_lenrord_Z \xint_c_v
            #3\XINT_lenrord_Z \xint_c_iv
            #2\XINT_lenrord_Z \xint_c_iii
            \W\XINT_lenrord_Z \xint_c_ii   \Z
}%
\def\XINT_lenrord_Z #1#2\Z #3% retourne: {longueur}renverse\Z
{%
    \expandafter{\the\numexpr #3-#1\relax}%
}%
```

24.7 \XINT_outfrac

1.06a version now outputs 0/1[0] and not 0[0] in case of zero. More generally all macros have been checked in xintfrac, xintseries, xintcfrac, to make sure the output format for fractions was always A/B[n]. (except of course \xintIrr, \xintJrr, \xintRawWithZeros)

```
\def\XINT_outfrac #1#2#3%
{%
    \ifcase\XINT_Sgn{#3}
        \expandafter \XINT_outfrac_divisionbyzero
    \or
        \expandafter \XINT_outfrac_P
    \else
        \expandafter \XINT_outfrac_N
    \fi
    {#2}{#3}[#1]%
}%
\def\XINT_outfrac_divisionbyzero #1#2{\xintError:DivisionByZero\space #1/0}%
\def\XINT_outfrac_P #1#2%
{%
    \ifcase\XINT_Sgn{#1}
        \expandafter\XINT_outfrac_Zero
    \fi
    \space #1/#2%
}%
\def\XINT_outfrac_Zero #1[#2]{ 0/1[0]}%
```

```
\def\XINT_outfrac_N #1#2%
{%
    \expandafter\XINT_outfrac_N_a\expandafter
    {\romannumeral0\XINT_opp #2}{\romannumeral0\XINT_opp #1}%
}%
\def\XINT_outfrac_N_a #1#2%
{%
    \expandafter\XINT_outfrac_P\expandafter {#2}{#1}%
}%
```

24.8 \XINT_inFrac

Extended in 1.07 to accept scientific notation on input. With lowercase e only. The \xintexpr parser does accept uppercase E also.

```
\def\XINT_inFrac {\romannumeral0\XINT_infrac }%
\def\XINT_infrac #1%
{%
    \expandafter\XINT_infrac_ \romannumeral-`0#1[\W]\Z\T
}%
\def\XINT_infrac_ #1[#2#3]#4\Z
{%
    \xint_UDwfork
      #2\dummy \XINT_infrac_A
      \W\dummy \XINT_infrac_B
    \krof
    #1[#2#3]#4%
}%
\def\XINT_infrac_A #1[\W]\T
{%
    \XINT_frac #1/\W\Z
}%
\def\XINT_infrac_B #1%
{%
    \xint_gob_til_zero #1\XINT_infrac_Zero0\XINT_infrac_BB #1%
}%
\def\XINT_infrac_BB #1[\W]\T {\XINT_infrac_BC #1/\W\Z }%
\def\XINT_infrac_BC #1/#2#3\Z
{%
    \xint_UDwfork
     #2\dummy \XINT_infrac_BCa
     \W\dummy {\expandafter\XINT_infrac_BCb \romannumeral-`0#2}%
    \krof
    #3\Z #1\Z
}%
\def\XINT_infrac_BCa \Z #1[#2]#3\Z { {#2}{#1}{1}}%
\def\XINT_infrac_BCb #1[#2]/\W\Z #3\Z { {#2}{#3}{#1}}%
\def\XINT_infrac_Zero #1\T { {0}{0}{1}}%
```

24.9 \XINT_frac

Extended in 1.07 to recognize and accept scientific notation both at the numerator and (possible) denominator. Only a lowercase e will do here, but uppercase E is possible within an \xintexpr..\relax

```
\def\XINT_frac #1/#2#3\Z
{%
    \xint_UDwfork
     #2\dummy \XINT_frac_A
     \W\dummy {\expandafter\XINT_frac_U \romannumeral-`0#2}%
    \krof
    #3e\W\Z #1e\W\Z
}%
\def\XINT_frac_U #1e#2#3\Z
{%
    \xint_UDwfork
      #2\dummy  \XINT_frac_Ua
      \W\dummy {\XINT_frac_Ub #2}%
    \krof
    #3\Z #1\Z
}%
\def\XINT_frac_Ua      \Z #1/\W\Z  {\XINT_frac_B #1.\W\Z {0}}%
\def\XINT_frac_Ub #1/\W e\W\Z #2\Z {\XINT_frac_B #2.\W\Z {#1}}%
\def\XINT_frac_B #1.#2#3\Z
{%
    \xint_UDwfork
      #2\dummy  \XINT_frac_Ba
      \W\dummy {\XINT_frac_Bb #2}%
    \krof
    #3\Z #1\Z
}%
\def\XINT_frac_Ba \Z #1\Z {\XINT_frac_T {0}{#1}}%
\def\XINT_frac_Bb #1.\W\Z #2\Z
{%
    \expandafter \XINT_frac_T \expandafter
    {\romannumeral0\XINT_length {#1}}{#2#1}%
}%
\def\XINT_frac_A e\W\Z {\XINT_frac_T {0}{1}{0}}%
\def\XINT_frac_T #1#2#3#4e#5#6\Z
{%
    \xint_UDwfork
      #5\dummy  \XINT_frac_Ta
      \W\dummy {\XINT_frac_Tb #5}%
    \krof
    #6\Z #4\Z {#1}{#2}{#3}%
}%
\def\XINT_frac_Ta \Z #1\Z      {\XINT_frac_C #1.\W\Z {0}}%
\def\XINT_frac_Tb #1e\W\Z #2\Z {\XINT_frac_C #2.\W\Z {#1}}%
```

```
\def\XINT_frac_C #1.#2#3\Z
{%
    \xint_UDwfork
      #2\dummy \XINT_frac_Ca
      \W\dummy {\XINT_frac_Cb #2}%
    \krof
    #3\Z #1\Z
}%
\def\XINT_frac_Ca \Z #1\Z {\XINT_frac_D {0}{#1}}%
\def\XINT_frac_Cb #1.\W\Z #2\Z
{%
    \expandafter\XINT_frac_D\expandafter
    {\romannumeral0\XINT_length {#1}}{#2#1}%
}%
\def\XINT_frac_D #1#2#3#4#5#6%
{%
    \expandafter \XINT_frac_E \expandafter
    {\the\numexpr -#1+#3+#4-#6\expandafter}\expandafter
    {\romannumeral0\XINT_num_loop #2%
     \xint_relax\xint_relax\xint_relax\xint_relax
     \xint_relax\xint_relax\xint_relax\xint_relax\Z }%
    {\romannumeral0\XINT_num_loop #5%
     \xint_relax\xint_relax\xint_relax\xint_relax
     \xint_relax\xint_relax\xint_relax\xint_relax\Z }%
}%
\def\XINT_frac_E #1#2#3%
{%
   \expandafter \XINT_frac_F  #3\Z {#2}{#1}%
}%
\def\XINT_frac_F #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_frac_Gdivisionbyzero
      0#1\dummy  \XINT_frac_Gneg
       0-\dummy  {\XINT_frac_Gpos #1}%
    \krof
}%
\def\XINT_frac_Gdivisionbyzero #1\Z #2#3%
{%
   \xintError:DivisionByZero\space {0}{#2}{0}%
}%
\def\XINT_frac_Gneg #1\Z #2#3%
{%
    \expandafter\XINT_frac_H \expandafter{\romannumeral0\XINT_opp #2}{#3}{#1}%
}%
\def\XINT_frac_H #1#2{ {#2}{#1}}%
\def\XINT_frac_Gpos #1\Z #2#3{ {#3}{#2}{#1}}%
```

24.10 \XINT_factortens, \XINT_cuz_cnt

```
\def\XINT_factortens #1%
{%
    \expandafter\XINT_cuz_cnt_loop\expandafter
    {\expandafter}\romannumeral0\XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    \R\R\R\R\R\R\R\Z
}%
\def\XINT_cuz_cnt #1%
{%
    \XINT_cuz_cnt_loop {}#1\R\R\R\R\R\R\R\Z
}%
\def\XINT_cuz_cnt_loop #1#2#3#4#5#6#7#8#9%
{%
    \xint_gob_til_R #9\XINT_cuz_cnt_toofara \R
    \expandafter\XINT_cuz_cnt_checka\expandafter
    {\the\numexpr #1+8\relax}{#2#3#4#5#6#7#8#9}%
}%
\def\XINT_cuz_cnt_toofara\R
    \expandafter\XINT_cuz_cnt_checka\expandafter #1#2%
{%
    \XINT_cuz_cnt_toofarb {#1}#2%
}%
\def\XINT_cuz_cnt_toofarb #1#2\Z {\XINT_cuz_cnt_toofarc #2\Z {#1}}%
\def\XINT_cuz_cnt_toofarc #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_R #2\XINT_cuz_cnt_toofard 7%
            #3\XINT_cuz_cnt_toofard 6%
            #4\XINT_cuz_cnt_toofard 5%
            #5\XINT_cuz_cnt_toofard 4%
            #6\XINT_cuz_cnt_toofard 3%
            #7\XINT_cuz_cnt_toofard 2%
            #8\XINT_cuz_cnt_toofard 1%
            \Z #1#2#3#4#5#6#7#8%
}%
\def\XINT_cuz_cnt_toofard #1#2\Z #3\R #4\Z #5%
{%
    \expandafter\XINT_cuz_cnt_toofare
    \the\numexpr #3\relax \R\R\R\R\R\R\R\Z
    {\the\numexpr #5-#1\relax}\R\Z
}%
\def\XINT_cuz_cnt_toofare #1#2#3#4#5#6#7#8%
{%
    \xint_gob_til_R #2\XINT_cuz_cnt_stopc 1%
            #3\XINT_cuz_cnt_stopc 2%
```

```
5189             #4\XINT_cuz_cnt_stopc 3%
5190             #5\XINT_cuz_cnt_stopc 4%
5191             #6\XINT_cuz_cnt_stopc 5%
5192             #7\XINT_cuz_cnt_stopc 6%
5193             #8\XINT_cuz_cnt_stopc 7%
5194             \Z #1#2#3#4#5#6#7#8%
5195 }%
5196 \def\XINT_cuz_cnt_checka #1#2%
5197 {%
5198     \expandafter\XINT_cuz_cnt_checkb\the\numexpr #2\relax \Z {#1}%
5199 }%
5200 \def\XINT_cuz_cnt_checkb #1%
5201 {%
5202     \xint_gob_til_zero #1\expandafter\XINT_cuz_cnt_loop\xint_gob_til_Z
5203     0\XINT_cuz_cnt_stopa #1%
5204 }%
5205 \def\XINT_cuz_cnt_stopa #1\Z
5206 {%
5207     \XINT_cuz_cnt_stopb #1\R\R\R\R\R\R\R\R\Z %
5208 }%
5209 \def\XINT_cuz_cnt_stopb #1#2#3#4#5#6#7#8#9%
5210 {%
5211     \xint_gob_til_R #2\XINT_cuz_cnt_stopc 1%
5212             #3\XINT_cuz_cnt_stopc 2%
5213             #4\XINT_cuz_cnt_stopc 3%
5214             #5\XINT_cuz_cnt_stopc 4%
5215             #6\XINT_cuz_cnt_stopc 5%
5216             #7\XINT_cuz_cnt_stopc 6%
5217             #8\XINT_cuz_cnt_stopc 7%
5218             #9\XINT_cuz_cnt_stopc 8%
5219             \Z #1#2#3#4#5#6#7#8#9%
5220 }%
5221 \def\XINT_cuz_cnt_stopc #1#2\Z #3\R #4\Z #5%
5222 {%
5223     \expandafter\XINT_cuz_cnt_stopd\expandafter
5224     {\the\numexpr #5-#1}#3%
5225 }%
5226 \def\XINT_cuz_cnt_stopd #1#2\R #3\Z
5227 {%
5228     \expandafter\space\expandafter
5229      {\romannumeral0\XINT_rord_main {}#2%
5230       \xint_relax
5231         \xint_undef\xint_undef\xint_undef\xint_undef
5232         \xint_undef\xint_undef\xint_undef\xint_undef
5233       \xint_relax }{#1}%
5234 }%
```

24.11 \xintRaw

1.07: this macro simply prints in a user readable form the fraction after its initial scanning. Useful when put inside braces in an \xintexpr, when the input is not yet in the A/B[n] form.

```
\def\xintRaw {\romannumeral0\xintraw }%
\def\xintraw
{%
    \expandafter\XINT_raw\romannumeral0\XINT_infrac
}%
\def\XINT_raw #1#2#3{ #2/#3[#1]}%
```

24.12 \xintRawWithZeros

This was called \xintRaw in versions earlier than 1.07

```
\def\xintRawWithZeros {\romannumeral0\xintrawwithzeros }%
\def\xintrawwithzeros
{%
    \expandafter\XINT_rawz\romannumeral0\XINT_infrac
}%
\def\XINT_rawz #1%
{%
    \ifcase\XINT_Sgn {#1}
      \expandafter\XINT_rawz_Ba
    \or
      \expandafter\XINT_rawz_A
    \else
      \expandafter\XINT_rawz_Ba
    \fi
    {#1}%
}%
\def\XINT_rawz_A  #1#2#3{\xint_dsh {#2}{-#1}/#3}%
\def\XINT_rawz_Ba #1#2#3{\expandafter\XINT_rawz_Bb
                         \expandafter{\romannumeral0\xint_dsh {#3}{#1}}{#2}}%
\def\XINT_rawz_Bb #1#2{ #2/#1}%
```

24.13 \xintNumerator

```
\def\xintNumerator {\romannumeral0\xintnumerator }%
\def\xintnumerator
{%
    \expandafter\XINT_numer\romannumeral0\XINT_infrac
}%
\def\XINT_numer #1%
{%
    \ifcase\XINT_Sgn {#1}
      \expandafter\XINT_numer_B
```

```
    \or
      \expandafter\XINT_numer_A
    \else
      \expandafter\XINT_numer_B
    \fi
    {#1}%
}%
\def\XINT_numer_A #1#2#3{\xint_dsh {#2}{-#1}}%
\def\XINT_numer_B #1#2#3{ #2}%
```

24.14 \xintDenominator

```
\def\xintDenominator {\romannumeral0\xintdenominator }%
\def\xintdenominator
{%
    \expandafter\XINT_denom\romannumeral0\XINT_infrac
}%
\def\XINT_denom #1%
{%
    \ifcase\XINT_Sgn {#1}
      \expandafter\XINT_denom_B
    \or
      \expandafter\XINT_denom_A
    \else
      \expandafter\XINT_denom_B
    \fi
    {#1}%
}%
\def\XINT_denom_A #1#2#3{ #3}%
\def\XINT_denom_B #1#2#3{\xint_dsh {#3}{#1}}%
```

24.15 \xintFrac

```
\def\xintFrac {\romannumeral0\xintfrac }%
\def\xintfrac #1%
{%
    \expandafter\XINT_fracfrac_A\romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_fracfrac_A #1{\XINT_fracfrac_B #1\Z }%
\catcode`^=7
\def\XINT_fracfrac_B #1#2\Z
{%
    \xint_gob_til_zero #1\XINT_fracfrac_C 0\XINT_fracfrac_D {10^{#1#2}}%
}%
\def\XINT_fracfrac_C #1#2#3#4#5%
{%
    \ifcase\XINT_isOne {#5}
    \or \xint_afterfi {\expandafter\xint_firstoftwo_andstop\xint_gobble_ii }%
    \fi
    \space
    \frac {#4}{#5}%
```

```
}%
\def\XINT_fracfrac_D #1#2#3%
{%
    \ifcase\XINT_isOne {#3}
    \or \XINT_fracfrac_E
    \fi
    \space
    \frac {#2}{#3}#1%
}%
\def\XINT_fracfrac_E \fi #1#2#3#4{\fi \space #3\cdot }%
```

24.16 \xintSignedFrac

```
\def\xintSignedFrac {\romannumeral0\xintsignedfrac }%
\def\xintsignedfrac #1%
{%
    \expandafter\XINT_sgnfrac_a\romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_sgnfrac_a #1#2%
{%
    \XINT_sgnfrac_b #2\Z {#1}%
}%
\def\XINT_sgnfrac_b #1%
{%
    \xint_UDsignfork
      #1\dummy \XINT_sgnfrac_N
       -\dummy {\XINT_sgnfrac_P #1}%
    \krof
}%
\def\XINT_sgnfrac_P #1\Z #2%
{%
    \XINT_fracfrac_A {#2}{#1}%
}%
\def\XINT_sgnfrac_N
{%
    \expandafter\xint_minus_andstop\romannumeral0\XINT_sgnfrac_P
}%
```

24.17 \xintFwOver

```
\def\xintFwOver {\romannumeral0\xintfwover }%
\def\xintfwover #1%
{%
    \expandafter\XINT_fwover_A\romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_fwover_A #1{\XINT_fwover_B #1\Z }%
\def\XINT_fwover_B #1#2\Z
{%
    \xint_gob_til_zero #1\XINT_fwover_C 0\XINT_fwover_D {10^{#1#2}}%
}%
\catcode`^=11
```

```
\def\XINT_fwover_C #1#2#3#4#5%
{%
    \ifcase\XINT_isOne {#5}
       \xint_afterfi { {#4\over #5}}%
    \or
       \xint_afterfi { #4}%
    \fi
}%
\def\XINT_fwover_D #1#2#3%
{%
    \ifcase\XINT_isOne {#3}
      \xint_afterfi { {#2\over #3}}%
    \or
      \xint_afterfi { #2\cdot }%
    \fi
    #1%
}%
```

24.18 \xintSignedFwOver

```
\def\xintSignedFwOver {\romannumeral0\xintsignedfwover }%
\def\xintsignedfwover #1%
{%
    \expandafter\XINT_sgnfwover_a\romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_sgnfwover_a #1#2%
{%
    \XINT_sgnfwover_b #2\Z {#1}%
}%
\def\XINT_sgnfwover_b #1%
{%
    \xint_UDsignfork
      #1\dummy \XINT_sgnfwover_N
       -\dummy {\XINT_sgnfwover_P #1}%
    \krof
}%
\def\XINT_sgnfwover_P #1\Z #2%
{%
    \XINT_fwover_A {#2}{#1}%
}%
\def\XINT_sgnfwover_N
{%
    \expandafter\xint_minus_andstop\romannumeral0\XINT_sgnfwover_P
}%
```

24.19 \xintREZ

```
\def\xintREZ {\romannumeral0\xintrez }%
\def\xintrez
{%
    \expandafter\XINT_rez_A\romannumeral0\XINT_infrac
```

```
}%
\def\XINT_rez_A #1#2%
{%
    \XINT_rez_AB #2\Z {#1}%
}%
\def\XINT_rez_AB #1%
{%
    \xint_UDzerominusfork
      #1-\dummy \XINT_rez_zero
      0#1\dummy \XINT_rez_neg
       0-\dummy {\XINT_rez_B #1}%
    \krof
}%
\def\XINT_rez_zero #1\Z #2#3{ 0/1[0]}%
\def\XINT_rez_neg {\expandafter\xint_minus_andstop\romannumeral0\XINT_rez_B }%
\def\XINT_rez_B #1\Z
{%
    \expandafter\XINT_rez_C\romannumeral0\XINT_factortens {#1}%
}%
\def\XINT_rez_C #1#2#3#4%
{%
    \expandafter\XINT_rez_D\romannumeral0\XINT_factortens {#4}{#3}{#2}{#1}%
}%
\def\XINT_rez_D #1#2#3#4#5%
{%
    \expandafter\XINT_rez_E\expandafter
    {\the\numexpr #3+#4-#2}{#1}{#5}%
}%
\def\XINT_rez_E #1#2#3{ #3/#2[#1]}%
```

24.20 \xintE

added with with 1.07, together with support for 'floats'. The fraction comes first here, contrarily to \xintTrunc and \xintRound.

```
\def\xintE {\romannumeral0\xinte }%
\def\xinte #1%
{%
    \expandafter\XINT_e \romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_e #1#2#3#4%
{%
    \expandafter\XINT_e_end\expandafter{\the\numexpr #1+#4}{#2}{#3}%
}%
\def\xintfE {\romannumeral0\xintfe }%
\def\xintfe #1%
{%
    \expandafter\XINT_fe \romannumeral0\XINT_infrac {#1}%
}%
\def\XINT_fe #1#2#3#4%
```

```
{%
    \expandafter\XINT_e_end\expandafter{\the\numexpr #1+\xintNum{#4}}{#2}{#3}%
}%
\def\XINT_e_end #1#2#3{ #2/#3[#1]}%
\let\XINTinFloatfE\xintfE
```

24.21 \xintIrr

1.04 fixes a buggy \xintIrr {0}. 1.05 modifies the initial parsing and post-processing to use \xintrawwithzeros and to more quickly deal with an input denominator equal to 1. 1.08 version does not remove a /1 denominator.

```
\def\xintIrr {\romannumeral0\xintirr }%
\def\xintirr #1%
{%
    \expandafter\XINT_irr_start\romannumeral0\xintrawwithzeros {#1}\Z
}%
\def\XINT_irr_start #1#2/#3\Z
{%
    \ifcase\XINT_isOne {#3}
      \xint_afterfi
          {\xint_UDsignfork
               #1\dummy \XINT_irr_negative
                -\dummy {\XINT_irr_nonneg #1}%
           \krof}%
    \or
      \xint_afterfi{\XINT_irr_denomisone #1}%
    \fi
    #2\Z {#3}%
}%
\def\XINT_irr_denomisone #1\Z #2{ #1/1}% changed in 1.08
\def\XINT_irr_negative   #1\Z #2{\XINT_irr_D #1\Z #2\Z \xint_minus_andstop}%
\def\XINT_irr_nonneg     #1\Z #2{\XINT_irr_D #1\Z #2\Z \space}%
\def\XINT_irr_D #1#2\Z #3#4\Z
{%
    \xint_UDzerosfork
       #3#1\dummy \XINT_irr_indeterminate
       #30\dummy  \XINT_irr_divisionbyzero
       #10\dummy  \XINT_irr_zero
        00\dummy  \XINT_irr_loop_a
    \krof
    {#3#4}{#1#2}{#3#4}{#1#2}%
}%
\def\XINT_irr_indeterminate #1#2#3#4#5{\xintError:NaN\space 0/0}%
\def\XINT_irr_divisionbyzero #1#2#3#4#5{\xintError:DivisionByZero #5#2/0}%
\def\XINT_irr_zero #1#2#3#4#5{ 0/1}% changed in 1.08
\def\XINT_irr_loop_a #1#2%
{%
    \expandafter\XINT_irr_loop_d
```

```
    \romannumeral0\XINT_div_prepare {#1}{#2}{#1}%
}%
\def\XINT_irr_loop_d #1#2%
{%
    \XINT_irr_loop_e #2\Z
}%
\def\XINT_irr_loop_e #1#2\Z
{%
    \xint_gob_til_zero #1\xint_irr_loop_exit0\XINT_irr_loop_a {#1#2}%
}%
\def\xint_irr_loop_exit0\XINT_irr_loop_a #1#2#3#4%
{%
    \expandafter\XINT_irr_loop_exitb\expandafter
    {\romannumeral0\xintiquo {#3}{#2}}%
    {\romannumeral0\xintiquo {#4}{#2}}%
}%
\def\XINT_irr_loop_exitb #1#2%
{%
   \expandafter\XINT_irr_finish\expandafter {#2}{#1}%
}%
\def\XINT_irr_finish #1#2#3{#3#1/#2}% changed in 1.08
```

24.22 \xintNum

This extension of the xint original xintNum is added in 1.05, as a synonym to \xintIrr, but raising an error when the input does not evaluate to an integer. Usable with not too much overhead on integer input as \xintIrr checks quickly for a denominator equal to 1 (which will be put there by the \XINT_infrac called by \xintrawwithzeros). This way, macros such as \xintQuo can be modified with minimal overhead to accept fractional input as long as it evaluates to an integer.

```
\def\xintNum {\romannumeral0\xintnum }%
\def\xintnum #1{\expandafter\XINT_intcheck\romannumeral0\xintirr {#1}\Z }%
\def\XINT_intcheck #1/#2\Z
{%
    \ifcase\XINT_isOne {#2}
      \xintError:NotAnInteger
    \fi\space #1%
}%
```

24.23 \xintJrr

Modified similarly as \xintIrr in release 1.05. 1.08 version does not remove a /1 denominator.

```
\def\xintJrr {\romannumeral0\xintjrr }%
\def\xintjrr #1%
```

```
{%
    \expandafter\XINT_jrr_start\romannumeral0\xintrawwithzeros {#1}\Z
}%
\def\XINT_jrr_start #1#2/#3\Z
{%
    \ifcase\XINT_isOne {#3}
      \xint_afterfi
          {\xint_UDsignfork
               #1\dummy \XINT_jrr_negative
                -\dummy {\XINT_jrr_nonneg #1}%
           \krof}%
    \or
      \xint_afterfi{\XINT_jrr_denomisone #1}%
    \fi
    #2\Z {#3}%
}%
\def\XINT_jrr_denomisone #1\Z #2{ #1/1}% changed in 1.08
\def\XINT_jrr_negative   #1\Z #2{\XINT_jrr_D #1\Z #2\Z \xint_minus_andstop }%
\def\XINT_jrr_nonneg     #1\Z #2{\XINT_jrr_D #1\Z #2\Z \space}%
\def\XINT_jrr_D #1#2\Z #3#4\Z
{%
    \xint_UDzerosfork
       #3#1\dummy \XINT_jrr_indeterminate
       #30\dummy  \XINT_jrr_divisionbyzero
       #10\dummy  \XINT_jrr_zero
        00\dummy  \XINT_jrr_loop_a
    \krof
    {#3#4}{#1#2}1001%
}%
\def\XINT_jrr_indeterminate #1#2#3#4#5#6#7{\xintError:NaN\space 0/0}%
\def\XINT_jrr_divisionbyzero #1#2#3#4#5#6#7{\xintError:DivisionByZero #7#2/0}%
\def\XINT_jrr_zero #1#2#3#4#5#6#7{ 0/1}% changed in 1.08
\def\XINT_jrr_loop_a #1#2%
{%
    \expandafter\XINT_jrr_loop_b
    \romannumeral0\XINT_div_prepare {#1}{#2}{#1}%
}%
\def\XINT_jrr_loop_b #1#2#3#4#5#6#7%
{%
    \expandafter \XINT_jrr_loop_c \expandafter
        {\romannumeral0\xintiadd{\XINT_Mul{#4}{#1}}{#6}}%
        {\romannumeral0\xintiadd{\XINT_Mul{#5}{#1}}{#7}}%
    {#2}{#3}{#4}{#5}%
}%
\def\XINT_jrr_loop_c #1#2%
{%
    \expandafter \XINT_jrr_loop_d \expandafter{#2}{#1}%
}%
\def\XINT_jrr_loop_d #1#2#3#4%
```

```
{%
    \XINT_jrr_loop_e #3\Z {#4}{#2}{#1}%
}%
\def\XINT_jrr_loop_e #1#2\Z
{%
    \xint_gob_til_zero #1\xint_jrr_loop_exit0\XINT_jrr_loop_a {#1#2}%
}%
\def\xint_jrr_loop_exit0\XINT_jrr_loop_a #1#2#3#4#5#6%
{%
    \XINT_irr_finish {#3}{#4}%
}%
```

24.24 \xintTrunc, \xintiTrunc

Modified in 1.06 to give the first argument to a \numexpr.

```
\def\xintTrunc {\romannumeral0\xinttrunc }%
\def\xintiTrunc {\romannumeral0\xintitrunc }%
\def\xinttrunc #1%
{%
    \expandafter\XINT_trunc\expandafter {\the\numexpr #1}%
}%
\def\XINT_trunc #1#2%
{%
    \expandafter\XINT_trunc_G
    \romannumeral0\expandafter\XINT_trunc_A
    \romannumeral0\XINT_infrac {#2}{#1}{#1}%
}%
\def\xintitrunc #1%
{%
    \expandafter\XINT_itrunc\expandafter {\the\numexpr #1}%
}%
\def\XINT_itrunc #1#2%
{%
    \expandafter\XINT_itrunc_G
    \romannumeral0\expandafter\XINT_trunc_A
    \romannumeral0\XINT_infrac {#2}{#1}{#1}%
}%
\def\XINT_trunc_A #1#2#3#4%
{%
    \expandafter\XINT_trunc_checkifzero
    \expandafter{\the\numexpr #1+#4}#2\Z {#3}%
}%
\def\XINT_trunc_checkifzero #1#2#3\Z
{%
    \xint_gob_til_zero #2\XINT_trunc_iszero0\XINT_trunc_B {#1}{#2#3}%
}%
\def\XINT_trunc_iszero #1#2#3#4#5{ 0\Z 0}%
\def\XINT_trunc_B #1%
```

```
{%
    \ifcase\XINT_Sgn {#1}
      \expandafter\XINT_trunc_D
    \or
      \expandafter\XINT_trunc_D
    \else
      \expandafter\XINT_trunc_C
    \fi
    {#1}%
}%
\def\XINT_trunc_C #1#2#3%
{%
    \expandafter \XINT_trunc_E
    \romannumeral0\xint_dsh {#3}{#1}\Z #2\Z
}%
\def\XINT_trunc_D #1#2%
{%
    \expandafter \XINT_trunc_DE \expandafter
    {\romannumeral0\xint_dsh {#2}{-#1}}%
}%
\def\XINT_trunc_DE #1#2{\XINT_trunc_E #2\Z #1\Z }%
\def\XINT_trunc_E #1#2\Z #3#4\Z
{%
    \xint_UDsignsfork
          #1#3\dummy \XINT_trunc_minusminus
           #1-\dummy {\XINT_trunc_minusplus #3}%
           #3-\dummy {\XINT_trunc_plusminus #1}%
            --\dummy {\XINT_trunc_plusplus  #3#1}%
    \krof
    {#4}{#2}%
}%
\def\XINT_trunc_minusminus #1#2{\xintiquo {#1}{#2}\Z \space}%
\def\XINT_trunc_minusplus #1#2#3{\xintiquo {#1#2}{#3}\Z \xint_minus_andstop}%
\def\XINT_trunc_plusminus #1#2#3{\xintiquo {#2}{#1#3}\Z \xint_minus_andstop}%
\def\XINT_trunc_plusplus  #1#2#3#4{\xintiquo {#1#3}{#2#4}\Z \space}%
\def\XINT_itrunc_G #1#2\Z #3#4%
{%
    \xint_gob_til_zero #1\XINT_trunc_zero 0\xint_firstoftwo {#3#1#2}0%
}%
\def\XINT_trunc_G #1\Z #2#3%
{%
    \xint_gob_til_zero #2\XINT_trunc_zero 0%
    \expandafter\XINT_trunc_H\expandafter
    {\the\numexpr\romannumeral0\XINT_length {#1}-#3}{#3}{#1}#2%
}%
\def\XINT_trunc_zero 0#10{ 0}%
\def\XINT_trunc_H #1#2%
{%
    \ifnum #1 > 0
```

```
5664         \xint_afterfi {\XINT_trunc_Ha {#2}}%
5665     \else
5666         \xint_afterfi {\XINT_trunc_Hb {-#1}}% -0,--1,--2, ....
5667     \fi
5668 }%
5669 \def\XINT_trunc_Ha
5670 {%
5671   \expandafter\XINT_trunc_Haa\romannumeral0\xintdecsplit
5672 }%
5673 \def\XINT_trunc_Haa #1#2#3%
5674 {%
5675     #3#1.#2%
5676 }%
5677 \def\XINT_trunc_Hb #1#2#3%
5678 {%
5679     \expandafter #3\expandafter0\expandafter.%
5680     \romannumeral0\XINT_dsx_zeroloop {#1}{}\Z {}#2% #1=-0 possible!
5681 }%
```

24.25 \xintRound, \xintiRound

Modified in 1.06 to give the first argument to a \numexpr.

```
5682 \def\xintRound {\romannumeral0\xintround }%
5683 \def\xintiRound {\romannumeral0\xintiround }%
5684 \def\xintround #1%
5685 {%
5686     \expandafter\XINT_round\expandafter {\the\numexpr #1}%
5687 }%
5688 \def\XINT_round
5689 {%
5690     \expandafter\XINT_trunc_G\romannumeral0\XINT_round_A
5691 }%
5692 \def\xintiround #1%
5693 {%
5694     \expandafter\XINT_iround\expandafter {\the\numexpr #1}%
5695 }%
5696 \def\XINT_iround
5697 {%
5698     \expandafter\XINT_itrunc_G\romannumeral0\XINT_round_A
5699 }%
5700 \def\XINT_round_A #1#2%
5701 {%
5702     \expandafter\XINT_round_B
5703     \romannumeral0\expandafter\XINT_trunc_A
5704     \romannumeral0\XINT_infrac {#2}{\the\numexpr #1+1\relax}{#1}%
5705 }%
5706 \def\XINT_round_B #1\Z
5707 {%
```

```
    \expandafter\XINT_round_C
    \romannumeral0\XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax
    \Z
}%
\def\XINT_round_C #1%
{%
    \ifnum #1<5
        \expandafter\XINT_round_Daa
    \else
        \expandafter\XINT_round_Dba
    \fi
}%
\def\XINT_round_Daa #1%
{%
    \xint_gob_til_Z #1\XINT_round_Daz\Z \XINT_round_Da #1%
}%
\def\XINT_round_Daz\Z \XINT_round_Da \Z { 0\Z }%
\def\XINT_round_Da #1\Z
{%
    \XINT_rord_main {}#1%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax  \Z
}%
\def\XINT_round_Dba #1%
{%
    \xint_gob_til_Z #1\XINT_round_Dbz\Z \XINT_round_Db #1%
}%
\def\XINT_round_Dbz\Z \XINT_round_Db \Z { 1\Z }%
\def\XINT_round_Db #1\Z
{%
    \XINT_addm_A 0{}1000\W\X\Y\Z #1000\W\X\Y\Z \Z
}%
```

24.26 \xintDigits

```
\mathchardef\XINT_digits 16
\def\xintDigits #1#2%
   {\afterassignment \xint_gobble_i \mathchardef\XINT_digits=}%
\def\xinttheDigits {\number\XINT_digits }%
```

24.27 \xintFloat

1.07. Completely re-written in 1.08a, with spectacular speed gains. The earlier version was seriously silly when dealing with inputs having a big power

```
of ten. Again some modifications in 1.08b for a better treatment of cases with
long explicit numerators or denominators.

\def\xintFloat   {\romannumeral0\xintfloat }%
\def\xintfloat #1{\XINT_float_chkopt #1\Z }%
\def\XINT_float_chkopt #1%
{%
    \ifx [#1\expandafter\XINT_float_opt
       \else\expandafter\XINT_float_noopt
    \fi  #1%
}%
\def\XINT_float_noopt #1\Z
{%
    \expandafter\XINT_float_a\expandafter\XINT_digits
    \romannumeral0\XINT_infrac {#1}\XINT_float_Q
}%
\def\XINT_float_opt [\Z #1]#2%
{%
    \expandafter\XINT_float_a\expandafter
    {\the\numexpr #1\expandafter}%
    \romannumeral0\XINT_infrac {#2}\XINT_float_Q
}%
\def\XINT_float_a #1#2#3% #1=P, #2=n, #3=A, #4=B
{%
    \XINT_float_fork #3\Z {#1}{#2}% #1 = precision, #2=n
}%
\def\XINT_float_fork #1%
{%
    \xint_UDzerominusfork
     #1-\dummy  \XINT_float_zero
     0#1\dummy  \XINT_float_J
      0-\dummy  {\XINT_float_K #1}%
    \krof
}%
\def\XINT_float_zero #1\Z #2#3#4#5{ 0.e0}%
\def\XINT_float_J {\expandafter\xint_minus_andstop\romannumeral0\XINT_float_K }%
\def\XINT_float_K #1\Z #2% #1=A, #2=P, #3=n, #4=B
{%
    \expandafter\XINT_float_L\expandafter
    {\the\numexpr\xintLength{#1}\expandafter}\expandafter
    {\the\numexpr #2+\xint_c_ii}{#1}{#2}%
}%
\def\XINT_float_L #1#2%
{%
    \ifnum #1>#2
      \expandafter\XINT_float_Ma
    \else
      \expandafter\XINT_float_Mc
    \fi {#1}{#2}%
```

```
}%
\def\XINT_float_Ma #1#2#3%
{%
    \expandafter\XINT_float_Mb\expandafter
    {\the\numexpr #1-#2\expandafter}\expandafter
    {\expandafter\xint_firstoftwo
     \romannumeral0\XINT_split_fromleft_loop {#2}{}#3\W\W\W\W\W\W\W\W\Z
     }{#2}%
}%
\def\XINT_float_Mb #1#2#3#4#5#6% #2=A', #3=P+2, #4=P, #5=n, #6=B
{%
   \expandafter\XINT_float_N\expandafter
   {\the\numexpr\xintLength{#6}\expandafter}\expandafter
   {\the\numexpr #3\expandafter}\expandafter
   {\the\numexpr #1+#5}%
   {#6}{#3}{#2}{#4}%
}% long de B, P+2, n', B, |A'|=P+2, A', P
\def\XINT_float_Mc #1#2#3#4#5#6%
{%
   \expandafter\XINT_float_N\expandafter
   {\romannumeral0\XINT_length{#6}}{#2}{#5}{#6}{#1}{#3}{#4}%
}% long de B, P+2, n, B, |A|, A, P
\def\XINT_float_N #1#2%
{%
    \ifnum #1>#2
      \expandafter\XINT_float_O
    \else
      \expandafter\XINT_float_P
    \fi {#1}{#2}%
}%
\def\XINT_float_O #1#2#3#4%
{%
    \expandafter\XINT_float_P\expandafter
    {\the\numexpr #2\expandafter}\expandafter
    {\the\numexpr #2\expandafter}\expandafter
    {\the\numexpr #3-#1+#2\expandafter}\expandafter
    {\expandafter\xint_firstoftwo
     \romannumeral0\XINT_split_fromleft_loop {#2}{}#4\W\W\W\W\W\W\W\W\Z
     }%
}% |B|,P+2,n,B,|A|,A,P
\def\XINT_float_P #1#2#3#4#5#6#7#8%
{%
    \expandafter #8\expandafter {\the\numexpr #1-#5+#2-\xint_c_i}%
    {#6}{#4}{#7}{#3}%
}% |B|-|A|+P+1,A,B,P,n
\def\XINT_float_Q #1%
{%
    \ifnum #1<\xint_c_
      \expandafter\XINT_float_Ri
```

```
5845     \else
5846       \expandafter\XINT_float_Rii
5847     \fi {#1}%
5848 }%
5849 \def\XINT_float_Ri #1#2#3%
5850 {%
5851     \expandafter\XINT_float_Sa
5852     \romannumeral0\xintiquo {#2}%
5853          {\romannumeral-`0\XINT_dsx_addzerosnofuss {-#1}{#3}}\Z {#1}%
5854 }%
5855 \def\XINT_float_Rii #1#2#3%
5856 {%
5857     \expandafter\XINT_float_Sa
5858     \romannumeral0\xintiquo
5859          {\romannumeral-`0\XINT_dsx_addzerosnofuss {#1}{#2}}{#3}\Z {#1}%
5860 }%
5861 \def\XINT_float_Sa #1%
5862 {%
5863     \if #19%
5864         \xint_afterfi {\XINT_float_Sb\XINT_float_Wb }%
5865     \else
5866         \xint_afterfi {\XINT_float_Sb\XINT_float_Wa }%
5867     \fi #1%
5868 }%
5869 \def\XINT_float_Sb #1#2\Z #3#4%
5870 {%
5871     \expandafter\XINT_float_T\expandafter
5872     {\the\numexpr #4+\xint_c_i\expandafter}%
5873     \romannumeral-`0\XINT_lenrord_loop 0{}#2\Z\W\W\W\W\W\W\W\Z #1{#3}{#4}%
5874 }%
5875 \def\XINT_float_T #1#2#3%
5876 {%
5877     \ifnum #2>#1
5878       \xint_afterfi{\XINT_float_U\XINT_float_Xb}%
5879     \else
5880       \xint_afterfi{\XINT_float_U\XINT_float_Xa #3}%
5881     \fi
5882 }%
5883 \def\XINT_float_U #1#2%
5884 {%
5885     \ifnum #2<\xint_c_v
5886       \expandafter\XINT_float_Va
5887     \else
5888       \expandafter\XINT_float_Vb
5889     \fi #1%
5890 }%
5891 \def\XINT_float_Va #1#2\Z #3%
5892 {%
5893     \expandafter#1%
```

```
    \romannumeral0\expandafter\XINT_float_Wa
    \romannumeral0\XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax \Z
}%
\def\XINT_float_Vb #1#2\Z #3%
{%
    \expandafter #1%
    \romannumeral0\expandafter #3%
    \romannumeral0\XINT_addm_A 0{}1000\W\X\Y\Z #2000\W\X\Y\Z \Z
}%
\def\XINT_float_Wa #1{ #1.}%
\def\XINT_float_Wb #1#2%
    {\if #11\xint_afterfi{ 10.}\else\xint_afterfi{ #1.#2}\fi }%
\def\XINT_float_Xa #1\Z #2#3#4%
{%
    \expandafter\XINT_float_Y\expandafter
    {\the\numexpr #3+#4-#2}{#1}%
}%
\def\XINT_float_Xb #1\Z #2#3#4%
{%
    \expandafter\XINT_float_Y\expandafter
    {\the\numexpr #3+#4+\xint_c_i-#2}{#1}%
}%
\def\XINT_float_Y #1#2{ #2e#1}%
```

24.28 \XINT_inFloat

1.07. Completely rewritten in 1.08a for immensely greater efficiency when the power of ten is big: previous version had some very serious bottlenecks arising from the creation of long strings of zeros, which made things such as 2^999999 completely impossible, but now even 2^999999999 with 24 significant digits is no problem! Again (slightly) improved in 1.08b.

```
\def\XINT_inFloat [#1]#2%
{%
    \expandafter\XINT_infloat_a\expandafter
    {\the\numexpr #1\expandafter}%
    \romannumeral0\XINT_infrac {#2}\XINT_infloat_Q
}%
\def\XINT_infloat_a #1#2#3% #1=P, #2=n, #3=A, #4=B
{%
    \XINT_infloat_fork #3\Z {#1}{#2}% #1 = precision, #2=n
}%
\def\XINT_infloat_fork #1%
{%
    \xint_UDzerominusfork
```

```
      #1-\dummy  \XINT_infloat_zero
      0#1\dummy  \XINT_infloat_J
       0-\dummy  {\XINT_float_K #1}%
    \krof
}%
\def\XINT_infloat_zero #1\Z #2#3#4#5{0[0]}%
\def\XINT_infloat_J {\expandafter-\romannumeral-`0\XINT_float_K }%
\def\XINT_infloat_Q #1%
{%
    \ifnum #1<\xint_c_
      \expandafter\XINT_infloat_Ri
    \else
      \expandafter\XINT_infloat_Rii
    \fi {#1}%
}%
\def\XINT_infloat_Ri #1#2#3%
{%
    \expandafter\XINT_infloat_S\expandafter
    {\romannumeral0\xintiquo {#2}%
         {\romannumeral-`0\XINT_dsx_addzerosnofuss {-#1}{#3}}}{#1}%
}%
\def\XINT_infloat_Rii #1#2#3%
{%
    \expandafter\XINT_infloat_S\expandafter
    {\romannumeral0\xintiquo
         {\romannumeral-`0\XINT_dsx_addzerosnofuss {#1}{#2}}{#3}}{#1}%
}%
\def\XINT_infloat_S #1#2#3%
{%
    \expandafter\XINT_infloat_T\expandafter
    {\the\numexpr #3+\xint_c_i\expandafter}%
    \romannumeral-`0\XINT_lenrord_loop 0{}#1\Z\W\W\W\W\W\W\W\Z
    {#2}%
}%
\def\XINT_infloat_T #1#2#3%
{%
    \ifnum #2>#1
      \xint_afterfi{\XINT_infloat_U\XINT_infloat_Wb}%
    \else
      \xint_afterfi{\XINT_infloat_U\XINT_infloat_Wa #3}%
    \fi
}%
\def\XINT_infloat_U #1#2%
{%
    \ifnum #2<\xint_c_v
      \expandafter\XINT_infloat_Va
    \else
      \expandafter\XINT_infloat_Vb
    \fi #1%
```

```
}%
\def\XINT_infloat_Va #1#2\Z
{%
    \expandafter#1%
    \romannumeral0\XINT_rord_main {}#2%
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax \Z
}%
\def\XINT_infloat_Vb #1#2\Z
{%
    \expandafter #1%
    \romannumeral0\XINT_addm_A 0{}1000\W\X\Y\Z #2000\W\X\Y\Z \Z
}%
\def\XINT_infloat_Wa #1\Z #2#3%
{%
    \expandafter\XINT_infloat_X\expandafter
    {\the\numexpr #3+\xint_c_i-#2}{#1}%
}%
\def\XINT_infloat_Wb #1\Z #2#3%
{%
    \expandafter\XINT_infloat_X\expandafter
    {\the\numexpr #3+\xint_c_ii-#2}{#1}%
}%
\def\XINT_infloat_X #1#2{ #2[#1]}%
```

24.29 \xintAdd

```
\def\xintAdd {\romannumeral0\xintadd }%
\def\xintadd #1%
{%
    \expandafter\xint_fadd\expandafter {\romannumeral0\XINT_infrac {#1}}%
}%
\def\xint_fadd #1#2{\expandafter\XINT_fadd_A\romannumeral0\XINT_infrac{#2}#1}%
\def\XINT_fadd_A #1#2#3#4%
{%
    \ifnum #4 > #1
       \xint_afterfi {\XINT_fadd_B {#1}}%
    \else
       \xint_afterfi {\XINT_fadd_B {#4}}%
    \fi
    {#1}{#4}{#2}{#3}%
}%
\def\XINT_fadd_B #1#2#3#4#5#6#7%
{%
    \expandafter\XINT_fadd_C\expandafter
    {\romannumeral0\xintimul {#7}{#5}}%
    {\romannumeral0\xintiadd
```

```
6029     {\romannumeral0\xintimul {\xintDSH {\the\numexpr -#3+#1\relax}{#6}}{#5}}%
6030     {\romannumeral0\xintimul {#7}{\xintDSH {\the\numexpr -#2+#1\relax}{#4}}}%
6031     }%
6032     {#1}%
6033 }%
6034 \def\XINT_fadd_C #1#2#3%
6035 {%
6036     \expandafter\XINT_fadd_D\expandafter {#2}{#3}{#1}%
6037 }%
6038 \def\XINT_fadd_D #1#2{\XINT_outfrac {#2}{#1}}%
```

24.30 \xintSub

```
6039 \def\xintSub {\romannumeral0\xintsub }%
6040 \def\xintsub #1%
6041 {%
6042     \expandafter\xint_fsub\expandafter {\romannumeral0\XINT_infrac {#1}}%
6043 }%
6044 \def\xint_fsub #1#2%
6045    {\expandafter\XINT_fsub_A\romannumeral0\XINT_infrac {#2}#1}%
6046 \def\XINT_fsub_A #1#2#3#4%
6047 {%
6048     \ifnum #4 > #1
6049        \xint_afterfi {\XINT_fsub_B {#1}}%
6050     \else
6051        \xint_afterfi {\XINT_fsub_B {#4}}%
6052     \fi
6053     {#1}{#4}{#2}{#3}%
6054 }%
6055 \def\XINT_fsub_B #1#2#3#4#5#6#7%
6056 {%
6057     \expandafter\XINT_fsub_C\expandafter
6058     {\romannumeral0\xintimul {#7}{#5}}%
6059     {\romannumeral0\xintisub
6060     {\romannumeral0\xintimul {\xintDSH {\the\numexpr -#3+#1\relax}{#6}}{#5}}%
6061     {\romannumeral0\xintimul {#7}{\xintDSH {\the\numexpr -#2+#1\relax}{#4}}}%
6062     }%
6063     {#1}%
6064 }%
6065 \def\XINT_fsub_C #1#2#3%
6066 {%
6067     \expandafter\XINT_fsub_D\expandafter {#2}{#3}{#1}%
6068 }%
6069 \def\XINT_fsub_D #1#2{\XINT_outfrac {#2}{#1}}%
```

24.31 \xintSum, \xintSumExpr

```
6070 \def\xintSum {\romannumeral0\xintsum }%
6071 \def\xintsum #1{\xintsumexpr #1\relax }%
6072 \def\xintSumExpr {\romannumeral0\xintsumexpr }%
6073 \def\xintsumexpr {\expandafter\XINT_fsumexpr\romannumeral-`0}%
```

```
\def\XINT_fsumexpr {\XINT_fsum_loop_a {0/1[0]}}%
\def\XINT_fsum_loop_a #1#2%
{%
    \expandafter\XINT_fsum_loop_b \romannumeral-`0#2\Z {#1}%
}%
\def\XINT_fsum_loop_b #1%
{%
    \xint_gob_til_relax #1\XINT_fsum_finished\relax
    \XINT_fsum_loop_c #1%
}%
\def\XINT_fsum_loop_c #1\Z #2%
{%
    \expandafter\XINT_fsum_loop_a\expandafter{\romannumeral0\xintadd {#2}{#1}}%
}%
\def\XINT_fsum_finished #1\Z #2{ #2}%
```

24.32 \xintMul

```
\def\xintMul {\romannumeral0\xintmul }%
\def\xintmul #1%
{%
    \expandafter\xint_fmul\expandafter {\romannumeral0\XINT_infrac {#1}}%
}%
\def\xint_fmul #1#2%
   {\expandafter\XINT_fmul_A\romannumeral0\XINT_infrac {#2}#1}%
\def\XINT_fmul_A #1#2#3#4#5#6%
{%
    \expandafter\XINT_fmul_B
    \expandafter{\the\numexpr #1+#4\expandafter}%
    \expandafter{\romannumeral0\xintimul {#6}{#3}}%
    {\romannumeral0\xintimul {#5}{#2}}%
}%
\def\XINT_fmul_B #1#2#3%
{%
    \expandafter \XINT_fmul_C \expandafter{#3}{#1}{#2}%
}%
\def\XINT_fmul_C #1#2{\XINT_outfrac {#2}{#1}}%
```

24.33 \xintSqr

```
\def\xintSqr {\romannumeral0\xintsqr }%
\def\xintsqr #1%
{%
    \expandafter\xint_fsqr\expandafter{\romannumeral0\XINT_infrac {#1}}%
}%
\def\xint_fsqr #1{\XINT_fmul_A #1#1}%
```

24.34 \xintPow

```
Modified in 1.06 to give the exponent to a \numexpr.
With 1.07 and for use within the \xintexpr parser, we must allow fractions (which
```

```
  are integers in disguise) as input to the exponent, so we must have a variant
  which uses \xintNum and not only \numexpr for normalizing the input. Hence the
  \xintfPow here. 1.08b: well actually I think that with xintfrac.sty loaded the
  exponent should always be allowed to be a fraction giving an integer. So I do
  as for \xintFac, and remove here the duplicated. The \xintexpr can thus use di-
  rectly \xintPow.

\def\xintPow {\romannumeral0\xintpow }%
\def\xintpow #1%
{%
    \expandafter\xint_fpow\expandafter {\romannumeral0\XINT_infrac {#1}}%
}%
\def\xint_fpow #1#2%
{%
    \expandafter\XINT_fpow_fork\the\numexpr \xintNum{#2}\relax\Z #1%
}%
\def\XINT_fpow_fork #1#2\Z
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_fpow_zero
      0#1\dummy  \XINT_fpow_neg
       0-\dummy  {\XINT_fpow_pos #1}%
    \krof
    {#2}%
}%
\def\XINT_fpow_zero #1#2#3#4%
{%
    \space 1/1[0]%
}%
\def\XINT_fpow_pos #1#2#3#4#5%
{%
    \expandafter\XINT_fpow_pos_A\expandafter
    {\the\numexpr #1#2*#3\expandafter}\expandafter
    {\romannumeral0\xintipow {#5}{#1#2}}%
    {\romannumeral0\xintipow {#4}{#1#2}}%
}%
\def\XINT_fpow_neg #1#2#3#4%
{%
    \expandafter\XINT_fpow_pos_A\expandafter
    {\the\numexpr -#1*#2\expandafter}\expandafter
    {\romannumeral0\xintipow {#3}{#1}}%
    {\romannumeral0\xintipow {#4}{#1}}%
}%
\def\XINT_fpow_pos_A #1#2#3%
{%
    \expandafter\XINT_fpow_pos_B\expandafter {#3}{#1}{#2}%
}%
\def\XINT_fpow_pos_B #1#2{\XINT_outfrac {#2}{#1}}%
```

24.35 \xintFac

1.07: to be used by the \xintexpr scanner which needs to be able to apply \xintFac to a fraction which is an integer in disguise; so we use \xintNum and not only \numexpr. Je modifie cela dans 1.08b, au lieu d'avoir un \xintfFac spécialement pour \xintexpr, tout simplement j'étends \xintFac comme les autres macros, pour qu'elle utilise \xintNum.

```
\def\xintFac {\romannumeral0\xintfac }%
\def\xintfac #1%
{%
    \expandafter\XINT_fac_fork\expandafter{\the\numexpr \xintNum{#1}}%
}%
```

24.36 \xintPrd, \xintPrdExpr

```
\def\xintPrd {\romannumeral0\xintprd }%
\def\xintprd #1{\xintprdexpr #1\relax }%
\def\xintPrdExpr {\romannumeral0\xintprdexpr }%
\def\xintprdexpr {\expandafter\XINT_fprdexpr \romannumeral-`0}%
\def\XINT_fprdexpr {\XINT_fprod_loop_a {1/1[0]}}%
\def\XINT_fprod_loop_a #1#2%
{%
    \expandafter\XINT_fprod_loop_b \romannumeral-`0#2\Z {#1}%
}%
\def\XINT_fprod_loop_b #1%
{%
    \xint_gob_til_relax #1\XINT_fprod_finished\relax
    \XINT_fprod_loop_c #1%
}%
\def\XINT_fprod_loop_c #1\Z #2%
{%
  \expandafter\XINT_fprod_loop_a\expandafter{\romannumeral0\xintmul {#1}{#2}}%
}%
\def\XINT_fprod_finished #1\Z #2{ #2}%
```

24.37 \xintDiv

```
\def\xintDiv {\romannumeral0\xintdiv }%
\def\xintdiv #1%
{%
    \expandafter\xint_fdiv\expandafter {\romannumeral0\XINT_infrac {#1}}%
}%
\def\xint_fdiv #1#2%
   {\expandafter\XINT_fdiv_A\romannumeral0\XINT_infrac {#2}#1}%
\def\XINT_fdiv_A #1#2#3#4#5#6%
{%
    \expandafter\XINT_fdiv_B
    \expandafter{\the\numexpr #4-#1\expandafter}%
    \expandafter{\romannumeral0\xintimul {#2}{#6}}%
```

```
    {\romannumeral0\xintimul {#3}{#5}}%
}%
\def\XINT_fdiv_B #1#2#3%
{%
    \expandafter\XINT_fdiv_C
    \expandafter{#3}{#1}{#2}%
}%
\def\XINT_fdiv_C #1#2{\XINT_outfrac {#2}{#1}}%
```

24.38 \xintGeq

Rewritten completely in 1.08a to be less dumb when comparing fractions having big powers of tens.

```
\def\xintGeq {\romannumeral0\xintgeq }%
\def\xintgeq #1%
{%
    \expandafter\xint_fgeq\expandafter {\romannumeral0\xintabs {#1}}%
}%
\def\xint_fgeq #1#2%
{%
    \expandafter\XINT_fgeq_A \romannumeral0\xintabs {#2}#1%
}%
\def\XINT_fgeq_A #1%
{%
    \xint_gob_til_zero #1\XINT_fgeq_Zii 0%
    \XINT_fgeq_B #1%
}%
\def\XINT_fgeq_Zii 0\XINT_fgeq_B #1[#2]#3[#4]{ 1}%
\def\XINT_fgeq_B #1/#2[#3]#4#5/#6[#7]%
{%
    \xint_gob_til_zero #4\XINT_fgeq_Zi 0%
    \expandafter\XINT_fgeq_C\expandafter
    {\the\numexpr #7-#3\expandafter}\expandafter
    {\romannumeral0\xintimul {#4#5}{#2}}%
    {\romannumeral0\xintimul {#6}{#1}}%
}%
\def\XINT_fgeq_Zi 0#1#2#3#4#5#6#7{ 0}%
\def\XINT_fgeq_C #1#2#3%
{%
    \expandafter\XINT_fgeq_D\expandafter
    {#3}{#1}{#2}%
}%
\def\XINT_fgeq_D #1#2#3%
{%
    \xintSgnFork
    {\xintiSgn{\the\numexpr #2+\xintLength{#3}-\xintLength{#1}\relax}}%
    { 0}{\XINT_fgeq_E #2\Z {#3}{#1}}{ 1}%
}%
\def\XINT_fgeq_E #1%
```

```
{%
    \xint_UDsignfork
        #1\dummy  \XINT_fgeq_Fd
         -\dummy {\XINT_fgeq_Fn #1}%
    \krof
}%
\def\XINT_fgeq_Fd #1\Z #2#3%
{%
    \expandafter\XINT_fgeq_Fe\expandafter
    {\romannumeral0\XINT_dsx_addzerosnofuss {#1}{#3}}{#2}%
}%
\def\XINT_fgeq_Fe #1#2{\XINT_geq_pre {#2}{#1}}%
\def\XINT_fgeq_Fn #1\Z #2#3%
{%
    \expandafter\XINT_geq_pre\expandafter
    {\romannumeral0\XINT_dsx_addzerosnofuss {#1}{#2}}{#3}%
}%
```

24.39 \xintMax

Rewritten completely in 1.08a.

```
\def\xintMax {\romannumeral0\xintmax }%
\def\xintmax #1%
{%
    \expandafter\xint_fmax\expandafter {\romannumeral0\xintraw {#1}}%
}%
\def\xint_fmax #1#2%
{%
    \expandafter\XINT_fmax_A\romannumeral0\xintraw {#2}#1%
}%
\def\XINT_fmax_A #1#2/#3[#4]#5#6/#7[#8]%
{%
    \xint_UDsignsfork
      #1#5\dummy \XINT_fmax_minusminus
       -#5\dummy \XINT_fmax_firstneg
       #1-\dummy \XINT_fmax_secondneg
        --\dummy \XINT_fmax_nonneg_a
    \krof
    #1#5{#2/#3[#4]}{#6/#7[#8]}%
}%
\def\XINT_fmax_minusminus --%
   {\expandafter\xint_minus_andstop\romannumeral0\XINT_fmin_nonneg_b }%
\def\XINT_fmax_firstneg #1-#2#3{ #1#2}%
\def\XINT_fmax_secondneg -#1#2#3{ #1#3}%
\def\XINT_fmax_nonneg_a #1#2#3#4%
{%
    \XINT_fmax_nonneg_b {#1#3}{#2#4}%
}%
```

```
\def\XINT_fmax_nonneg_b #1#2%
{%
    \ifcase\romannumeral0\XINT_fgeq_A #1#2
        \xint_afterfi{ #1}%
    \or \xint_afterfi{ #2}%
    \fi
}%
```

24.40 \xintMin

Rewritten completely in 1.08a.

```
\def\xintMin {\romannumeral0\xintmin }%
\def\xintmin #1%
{%
    \expandafter\xint_fmin\expandafter {\romannumeral0\xintraw {#1}}%
}%
\def\xint_fmin #1#2%
{%
    \expandafter\XINT_fmin_A\romannumeral0\xintraw {#2}#1%
}%
\def\XINT_fmin_A #1#2/#3[#4]#5#6/#7[#8]%
{%
    \xint_UDsignsfork
      #1#5\dummy \XINT_fmin_minusminus
       -#5\dummy \XINT_fmin_firstneg
       #1-\dummy \XINT_fmin_secondneg
        --\dummy \XINT_fmin_nonneg_a
    \krof
    #1#5{#2/#3[#4]}{#6/#7[#8]}%
}%
\def\XINT_fmin_minusminus --%
   {\expandafter\xint_minus_andstop\romannumeral0\XINT_fmax_nonneg_b }%
\def\XINT_fmin_firstneg #1-#2#3{ -#3}%
\def\XINT_fmin_secondneg -#1#2#3{ -#2}%
\def\XINT_fmin_nonneg_a #1#2#3#4%
{%
    \XINT_fmin_nonneg_b {#1#3}{#2#4}%
}%
\def\XINT_fmin_nonneg_b #1#2%
{%
    \ifcase\romannumeral0\XINT_fgeq_A #1#2
        \xint_afterfi{ #2}%
    \or \xint_afterfi{ #1}%
    \fi
}%
```

24.41 \xintCmp

Rewritten completely in 1.08a to be less dumb when comparing fractions having big powers of tens.

```
\def\xintCmp {\romannumeral0\xintcmp }%
\def\xintcmp #1%
{%
    \expandafter\xint_fcmp\expandafter {\romannumeral0\xintraw {#1}}%
}%
\def\xint_fcmp #1#2%
{%
    \expandafter\XINT_fcmp_A\romannumeral0\xintraw {#2}#1%
}%
\def\XINT_fcmp_A #1#2/#3[#4]#5#6/#7[#8]%
{%
    \xint_UDsignsfork
      #1#5\dummy \XINT_fcmp_minusminus
       -#5\dummy \XINT_fcmp_firstneg
       #1-\dummy \XINT_fcmp_secondneg
        --\dummy \XINT_fcmp_nonneg_a
    \krof
    #1#5{#2/#3[#4]}{#6/#7[#8]}%
}%
\def\XINT_fcmp_minusminus --#1#2{\XINT_fcmp_B #2#1}%
\def\XINT_fcmp_firstneg #1-#2#3{ -1}%
\def\XINT_fcmp_secondneg -#1#2#3{ 1}%
\def\XINT_fcmp_nonneg_a #1#2%
{%
    \xint_UDzerosfork
      #1#2\dummy \XINT_fcmp_zerozero
       0#2\dummy \XINT_fcmp_firstzero
       #10\dummy \XINT_fcmp_secondzero
        00\dummy \XINT_fcmp_pos
    \krof
    #1#2%
}%
\def\XINT_fcmp_zerozero   #1[#2]#3[#4]{ 0}%
\def\XINT_fcmp_firstzero  #1[#2]#3[#4]{ -1}%
\def\XINT_fcmp_secondzero #1[#2]#3[#4]{ 1}%
\def\XINT_fcmp_pos #1#2#3#4%
{%
    \XINT_fcmp_B #1#3#2#4%
}%
\def\XINT_fcmp_B #1/#2[#3]#4/#5[#6]%
{%
    \expandafter\XINT_fcmp_C\expandafter
    {\the\numexpr #6-#3\expandafter}\expandafter
    {\romannumeral0\xintimul {#4}{#2}}%
```

```
    {\romannumeral0\xintimul {#5}{#1}}%
}%
\def\XINT_fcmp_C #1#2#3%
{%
    \expandafter\XINT_fcmp_D\expandafter
    {#3}{#1}{#2}%
}%
\def\XINT_fcmp_D #1#2#3%
{%
    \xintSgnFork
    {\xintiSgn{\the\numexpr #2+\xintLength{#3}-\xintLength{#1}\relax}}%
    { -1}{\XINT_fcmp_E #2\Z {#3}{#1}}{ 1}%
}%
\def\XINT_fcmp_E #1%
{%
    \xint_UDsignfork
        #1\dummy  \XINT_fcmp_Fd
         -\dummy {\XINT_fcmp_Fn #1}%
    \krof
}%
\def\XINT_fcmp_Fd #1\Z #2#3%
{%
    \expandafter\XINT_fcmp_Fe\expandafter
    {\romannumeral0\XINT_dsx_addzerosnofuss {#1}{#3}}{#2}%
}%
\def\XINT_fcmp_Fe #1#2{\XINT_cmp_pre {#2}{#1}}%
\def\XINT_fcmp_Fn #1\Z #2#3%
{%
    \expandafter\XINT_cmp_pre\expandafter
    {\romannumeral0\XINT_dsx_addzerosnofuss {#1}{#2}}{#3}%
}%
```

24.42 \xintAbs

```
\def\xintAbs {\romannumeral0\xintabs }%
\def\xintabs #1%
{%
    \expandafter\xint_fabs\romannumeral0\XINT_infrac {#1}%
}%
\def\xint_fabs #1#2%
{%
    \expandafter\XINT_outfrac\expandafter
    {\the\numexpr #1\expandafter}\expandafter
    {\romannumeral0\XINT_abs #2}%
}%
```

24.43 \xintOpp

```
\def\xintOpp {\romannumeral0\xintopp }%
\def\xintopp #1%
```

```
{%
    \expandafter\xint_fopp\romannumeral0\XINT_infrac {#1}%
}%
\def\xint_fopp #1#2%
{%
    \expandafter\XINT_outfrac\expandafter
    {\the\numexpr #1\expandafter}\expandafter
    {\romannumeral0\XINT_opp #2}%
}%
```

24.44 \xintSgn

```
\def\xintSgn {\romannumeral0\xintsgn }%
\def\xintsgn #1%
{%
    \expandafter\xint_fsgn\romannumeral0\XINT_infrac {#1}%
}%
\def\xint_fsgn #1#2#3{\xintisgn {#2}}%
```

24.45 \xintDivision, \xintQuo, \xintRem

```
\def\xintDivision {\romannumeral0\xintdivision }%
\def\xintdivision #1%
{%
    \expandafter\xint_xdivision\expandafter{\romannumeral0\xintnum {#1}}%
}%
\def\xint_xdivision #1#2%
{%
    \expandafter\XINT_div_fork\romannumeral0\xintnum {#2}\Z #1\Z
}%
\def\xintQuo {\romannumeral0\xintquo }%
\def\xintRem {\romannumeral0\xintrem }%
\def\xintquo {\expandafter\xint_firstoftwo_andstop
                \romannumeral0\xintdivision }%
\def\xintrem {\expandafter\xint_secondoftwo_andstop
                \romannumeral0\xintdivision }%
```

24.46 \xintFDg, \xintLDg, \xintMON, \xintMMON, \xintOdd

```
\def\xintFDg {\romannumeral0\xintfdg }%
\def\xintfdg #1%
{%
    \expandafter\XINT_fdg\romannumeral0\xintnum {#1}\W\Z
}%
\def\xintLDg {\romannumeral0\xintldg }%
\def\xintldg #1%
{%
    \expandafter\XINT_ldg\expandafter{\romannumeral0\xintnum {#1}}%
}%
\def\xintMON {\romannumeral0\xintmon }%
\def\xintmon #1%
```

```
{%
    \ifodd\xintLDg {#1}
        \xint_afterfi{ -1}%
    \else
        \xint_afterfi{ 1}%
    \fi
}%
\def\xintMMON {\romannumeral0\xintmmon }%
\def\xintmmon #1%
{%
    \ifodd\xintLDg {#1}
        \xint_afterfi{ 1}%
    \else
        \xint_afterfi{ -1}%
    \fi
}%
\def\xintOdd {\romannumeral0\xintodd }%
\def\xintodd #1%
{%
    \ifodd\xintLDg{#1}
        \xint_afterfi{ 1}%
    \else
        \xint_afterfi{ 0}%
    \fi
}%
```

24.47 \xintFloatAdd

1.07

```
\def\xintFloatAdd      {\romannumeral0\xintfloatadd }%
\def\xintfloatadd    #1{\XINT_fladd_chkopt \xintfloat #1\Z }%
\def\XINTinFloatAdd   {\romannumeral-`0\XINTinfloatadd }%
\def\XINTinfloatadd #1{\XINT_fladd_chkopt \XINT_inFloat #1\Z }%
\def\XINT_fladd_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_fladd_opt
       \else\expandafter\XINT_fladd_noopt
    \fi  #1#2%
}%
\def\XINT_fladd_noopt #1#2\Z #3%
{%
    #1[\XINT_digits]{\XINT_FL_Add {\XINT_digits+2}{#2}{#3}}%
}%
\def\XINT_fladd_opt #1[\Z #2]#3#4%
{%
    #1[#2]{\XINT_FL_Add {#2+2}{#3}{#4}}%
}%
\def\XINT_FL_Add #1#2%
{%
```

```
6495     \expandafter\XINT_FL_Add_a\expandafter{\the\numexpr #1\expandafter}%
6496     \expandafter{\romannumeral-`0\XINT_inFloat [#1]{#2}}%
6497 }%
6498 \def\XINT_FL_Add_a #1#2#3%
6499 {%
6500     \expandafter\XINT_FL_Add_b\romannumeral-`0\XINT_inFloat [#1]{#3}#2{#1}%
6501 }%
6502 \def\XINT_FL_Add_b #1%
6503 {%
6504     \xint_gob_til_zero #1\XINT_FL_Add_zero 0\XINT_FL_Add_c #1%
6505 }%
6506 \def\XINT_FL_Add_c #1[#2]#3%
6507 {%
6508     \xint_gob_til_zero #3\XINT_FL_Add_zerobis 0\XINT_FL_Add_d #1[#2]#3%
6509 }%
6510 \def\XINT_FL_Add_d #1[#2]#3[#4]#5%
6511 {%
6512     \xintSgnFork {\ifnum \numexpr #2-#4-#5>1 \expandafter 1%
6513                   \else\ifnum \numexpr #4-#2-#5>1
6514                        \xint_afterfi {\expandafter-\expandafter1}%
6515                        \else \expandafter\expandafter\expandafter0%
6516                        \fi
6517                   \fi}%
6518     {#3[#4]}{\xintAdd {#1[#2]}{#3[#4]}}{#1[#2]}%
6519 }%
6520 \def\XINT_FL_Add_zero 0\XINT_FL_Add_c 0[0]#1[#2]#3{#1[#2]}%
6521 \def\XINT_FL_Add_zerobis 0\XINT_FL_Add_d #1[#2]0[0]#3{#1[#2]}%
```

24.48 \xintFloatSub

1.07

```
6522 \def\xintFloatSub {\romannumeral0\xintfloatsub }%
6523 \def\xintfloatsub    #1{\XINT_flsub_chkopt \xintfloat #1\Z }%
6524 \def\XINTinFloatSub {\romannumeral-`0\XINTinfloatsub }%
6525 \def\XINTinfloatsub #1{\XINT_flsub_chkopt \XINT_inFloat #1\Z }%
6526 \def\XINT_flsub_chkopt #1#2%
6527 {%
6528     \ifx [#2\expandafter\XINT_flsub_opt
6529        \else\expandafter\XINT_flsub_noopt
6530     \fi  #1#2%
6531 }%
6532 \def\XINT_flsub_noopt #1#2\Z #3%
6533 {%
6534     #1[\XINT_digits]{\XINT_FL_Add {\XINT_digits+2}{#2}{\xintOpp{#3}}}%
6535 }%
6536 \def\XINT_flsub_opt #1[\Z #2]#3#4%
6537 {%
6538     #1[#2]{\XINT_FL_Add {#2+2}{#3}{\xintOpp{#4}}}%
```

```
}%
```

24.49 \xintFloatMul

1.07

```
\def\xintFloatMul    {\romannumeral0\xintfloatmul}%
\def\xintfloatmul    #1{\XINT_flmul_chkopt \xintfloat #1\Z }%
\def\XINTinFloatMul {\romannumeral-`0\XINTinfloatmul }%
\def\XINTinfloatmul #1{\XINT_flmul_chkopt \XINT_inFloat #1\Z }%
\def\XINT_flmul_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_flmul_opt
       \else\expandafter\XINT_flmul_noopt
    \fi  #1#2%
}%
\def\XINT_flmul_noopt #1#2\Z #3%
{%
    #1[\XINT_digits]{\XINT_FL_Mul {\XINT_digits+2}{#2}{#3}}%
}%
\def\XINT_flmul_opt #1[\Z #2]#3#4%
{%
    #1[#2]{\XINT_FL_Mul {#2+2}{#3}{#4}}%
}%
\def\XINT_FL_Mul #1#2%
{%
    \expandafter\XINT_FL_Mul_a\expandafter{\the\numexpr #1\expandafter}%
    \expandafter{\romannumeral-`0\XINT_inFloat [#1]{#2}}%
}%
\def\XINT_FL_Mul_a #1#2#3%
{%
    \expandafter\XINT_FL_Mul_b\romannumeral-`0\XINT_inFloat [#1]{#3}#2%
}%
\def\XINT_FL_Mul_b #1[#2]#3[#4]{\xintE{\xintiMul {#1}{#3}}{#2+#4}}%
```

24.50 \xintFloatDiv

1.07

```
\def\xintFloatDiv    {\romannumeral0\xintfloatdiv}%
\def\xintfloatdiv    #1{\XINT_fldiv_chkopt \xintfloat #1\Z }%
\def\XINTinFloatDiv  {\romannumeral-`0\XINTinfloatdiv }%
\def\XINTinfloatdiv  #1{\XINT_fldiv_chkopt \XINT_inFloat #1\Z }%
\def\XINT_fldiv_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_fldiv_opt
       \else\expandafter\XINT_fldiv_noopt
    \fi  #1#2%
```

```
}%
\def\XINT_fldiv_noopt #1#2\Z #3%
{%
    #1[\XINT_digits]{\XINT_FL_Div {\XINT_digits+2}{#2}{#3}}%
}%
\def\XINT_fldiv_opt #1[\Z #2]#3#4%
{%
    #1[#2]{\XINT_FL_Div {#2+2}{#3}{#4}}%
}%
\def\XINT_FL_Div #1#2%
{%
    \expandafter\XINT_FL_Div_a\expandafter{\the\numexpr #1\expandafter}%
    \expandafter{\romannumeral-`0\XINT_inFloat [#1]{#2}}%
}%
\def\XINT_FL_Div_a #1#2#3%
{%
    \expandafter\XINT_FL_Div_b\romannumeral-`0\XINT_inFloat [#1]{#3}#2%
}%
\def\XINT_FL_Div_b #1[#2]#3[#4]{\xintE{#3/#1}{#4-#2}}%
```

24.51 \xintFloatPow

1.07

```
\def\xintFloatPow {\romannumeral0\xintfloatpow}%
\def\xintfloatpow #1{\XINT_flpow_chkopt \xintfloat #1\Z }%
\def\XINTinFloatPow {\romannumeral-`0\XINTinfloatpow }%
\def\XINTinfloatpow #1{\XINT_flpow_chkopt \XINT_inFloat #1\Z }%
\def\XINT_flpow_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_flpow_opt
       \else\expandafter\XINT_flpow_noopt
    \fi
     #1#2%
}%
\def\XINT_flpow_noopt  #1#2\Z #3%
{%
   \expandafter\XINT_flpow_checkB_start\expandafter
                {\the\numexpr #3\expandafter}\expandafter
                {\the\numexpr \XINT_digits}{#2}{#1[\XINT_digits]}%
}%
\def\XINT_flpow_opt #1[\Z #2]#3#4%
{%
   \expandafter\XINT_flpow_checkB_start\expandafter
               {\the\numexpr #4\expandafter}\expandafter
               {\the\numexpr #2}{#3}{#1[#2]}%
}%
\def\XINT_flpow_checkB_start #1{\XINT_flpow_checkB_a #1\Z }%
\def\XINT_flpow_checkB_a #1%
```

```
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_flpow_BisZero
      0#1\dummy  {\XINT_flpow_checkB_b 1}%
       0-\dummy  {\XINT_flpow_checkB_b 0#1}%
    \krof
}%
\def\XINT_flpow_BisZero \Z #1#2#3{#3{1/1[0]}}%
\def\XINT_flpow_checkB_b #1#2\Z #3%
{%
    \expandafter\XINT_flpow_checkB_c \expandafter
    {\romannumeral0\XINT_length{#2}}{#3}{#2}#1%
}%
\def\XINT_flpow_checkB_c #1#2%
{%
    \expandafter\XINT_flpow_checkB_d \expandafter
    {\the\numexpr \expandafter\XINT_Length\expandafter
                  {\the\numexpr #1*20/3}+#1+#2+1}%
}%
\def\XINT_flpow_checkB_d #1#2#3#4%
{%
    \expandafter \XINT_flpow_a
    \romannumeral-`0\XINT_inFloat [#1]{#4}{#1}{#2}#3%
}%
\def\XINT_flpow_a #1%
{%
    \xint_UDzerominusfork
      #1-\dummy \XINT_flpow_zero
      0#1\dummy {\XINT_flpow_b 1}%
       0-\dummy {\XINT_flpow_b 0#1}%
    \krof
}%
\def\XINT_flpow_zero [#1]#2#3#4#5%
{%
    \if #41 \xint_afterfi {\xintError:DivisionByZero\space 1.e2147483647}%
    \else \xint_afterfi { 0.e0}\fi
}%
\def\XINT_flpow_b #1#2[#3]#4#5%
{%
    \XINT_flpow_c {#4}{#5}{#2[#3]}{#1*\ifodd #5 1\else 0\fi}%
}%
\def\XINT_flpow_c #1#2#3#4%
{%
    \XINT_flpow_loop {#1}{#2}{#3}{{#1}}\XINT_flpow_prd
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax {#4}%
}%
```

```
\def\XINT_flpow_loop #1#2#3%
{%
    \ifnum #2 = 1
        \expandafter\XINT_flpow_loop_end
    \else
        \xint_afterfi{\expandafter\XINT_flpow_loop_a
            \expandafter{\the\numexpr 2*(#2/2)-#2\expandafter }% b mod 2
            \expandafter{\the\numexpr #2-#2/2\expandafter }%     [b/2]
            \expandafter{\romannumeral-`0\XINTinfloatmul [#1]{#3}{#3}}}%
    \fi
    {#1}{{#3}}%
}%
\def\XINT_flpow_loop_a #1#2#3#4%
{%
    \ifnum #1 = 1
        \expandafter\XINT_flpow_loop
    \else
        \expandafter\XINT_flpow_loop_throwaway
    \fi
    {#4}{#2}{#3}%
}%
\def\XINT_flpow_loop_throwaway #1#2#3#4%
{%
   \XINT_flpow_loop {#1}{#2}{#3}%
}%
\def\XINT_flpow_loop_end #1{\romannumeral0\XINT_rord_main {}\relax }%
\def\XINT_flpow_prd #1#2%
{%
    \XINT_flpow_prd_getnext {#2}{#1}%
}%
\def\XINT_flpow_prd_getnext #1#2#3%
{%
    \XINT_flpow_prd_checkiffinished #3\Z {#1}{#2}%
}%
\def\XINT_flpow_prd_checkiffinished #1%
{%
    \xint_gob_til_relax #1\XINT_flpow_prd_end\relax
    \XINT_flpow_prd_compute #1%
}%
\def\XINT_flpow_prd_compute #1\Z #2#3%
{%
    \expandafter\XINT_flpow_prd_getnext\expandafter
    {\romannumeral-`0\XINTinfloatmul [#3]{#1}{#2}}{#3}%
}%
\def\XINT_flpow_prd_end\relax\XINT_flpow_prd_compute
    \relax\Z #1#2#3%
{%
    \expandafter\XINT_flpow_conclude \the\numexpr #3\relax #1%
}%
```

```
\def\XINT_flpow_conclude #1#2[#3]#4%
{%
    \expandafter\XINT_flpow_conclude_really\expandafter
    {\the\numexpr\if #41 -\fi#3\expandafter}%
    \xint_UDzerofork
        #4\dummy {{#2}}%
         0\dummy {{1/#2}}%
    \krof #1%
}%
\def\XINT_flpow_conclude_really #1#2#3#4%
{%
    \xint_UDzerofork
    #3\dummy {#4{#2[#1]}}%
     0\dummy {#4{-#2[#1]}}%
    \krof
}%
```

24.52 \xintFloatPower

1.07

```
\def\xintFloatPower {\romannumeral0\xintfloatpower}%
\def\xintfloatpower #1{\XINT_flpower_chkopt \xintfloat #1\Z }%
\def\XINTinFloatPower {\romannumeral-`0\XINTinfloatpower}%
\def\XINTinfloatpower #1{\XINT_flpower_chkopt \XINT_inFloat #1\Z }%
\def\XINT_flpower_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_flpower_opt
       \else\expandafter\XINT_flpower_noopt
    \fi
     #1#2%
}%
\def\XINT_flpower_noopt  #1#2\Z #3%
{%
   \expandafter\XINT_flpower_checkB_start\expandafter
                {\the\numexpr \XINT_digits\expandafter}\expandafter
                {\romannumeral0\xintnum{#3}}{#2}{#1[\XINT_digits]}%
}%
\def\XINT_flpower_opt #1[\Z #2]#3#4%
{%
   \expandafter\XINT_flpower_checkB_start\expandafter
               {\the\numexpr #2\expandafter}\expandafter
               {\romannumeral0\xintnum{#4}}{#3}{#1[#2]}%
}%
\def\XINT_flpower_checkB_start #1#2{\XINT_flpower_checkB_a #2\Z {#1}}%
\def\XINT_flpower_checkB_a #1%
{%
    \xint_UDzerominusfork
      #1-\dummy  \XINT_flpower_BisZero
```

```
      0#1\dummy  {\XINT_flpower_checkB_b 1}%
       0-\dummy  {\XINT_flpower_checkB_b 0#1}%
    \krof
}%
\def\XINT_flpower_BisZero \Z #1#2#3{#3{1/1[0]}}%
\def\XINT_flpower_checkB_b #1#2\Z #3%
{%
    \expandafter\XINT_flpower_checkB_c \expandafter
    {\romannumeral0\XINT_length{#2}}{#3}{#2}#1%
}%
\def\XINT_flpower_checkB_c #1#2%
{%
    \expandafter\XINT_flpower_checkB_d \expandafter
    {\the\numexpr \expandafter\XINT_Length\expandafter
                  {\the\numexpr #1*20/3}+#1+#2+1}%
}%
\def\XINT_flpower_checkB_d #1#2#3#4%
{%
    \expandafter \XINT_flpower_a
    \romannumeral-`0\XINT_inFloat [#1]{#4}{#1}{#2}#3%
}%
\def\XINT_flpower_a #1%
{%
    \xint_UDzerominusfork
      #1-\dummy \XINT_flpower_zero
      0#1\dummy {\XINT_flpower_b 1}%
       0-\dummy {\XINT_flpower_b 0#1}%
    \krof
}%
\def\XINT_flpower_zero [#1]#2#3#4#5%
{%
    \if #41
          \xint_afterfi {\xintError:DivisionByZero\space 1.e2147483647}%
    \else \xint_afterfi { 0.e0}\fi
}%
\def\XINT_flpower_b #1#2[#3]#4#5%
{%
    \XINT_flpower_c {#4}{#5}{#2[#3]}{#1*\xintOdd {#5}}%
}%
\def\XINT_flpower_c #1#2#3#4%
{%
    \XINT_flpower_loop {#1}{#2}{#3}{{#1}}\XINT_flpow_prd
      \xint_relax
        \xint_undef\xint_undef\xint_undef\xint_undef
        \xint_undef\xint_undef\xint_undef\xint_undef
      \xint_relax {#4}%
}%
\def\XINT_flpower_loop #1#2#3%
{%
```

```
    \ifcase\XINT_isOne {#2}
        \xint_afterfi{\expandafter\XINT_flpower_loop_x\expandafter
            {\romannumeral-`0\XINTinfloatmul [#1]{#3}{#3}}%
            {\romannumeral0\xintdivision {#2}{2}}}%
    \or \expandafter\XINT_flpow_loop_end
    \fi
    {#1}{{#3}}%
}%
\def\XINT_flpower_loop_x #1#2{\expandafter\XINT_flpower_loop_a #2{#1}}%
\def\XINT_flpower_loop_a #1#2#3#4%
{%
    \ifnum #2 = 1
        \expandafter\XINT_flpower_loop
    \else
        \expandafter\XINT_flpower_loop_throwaway
    \fi
    {#4}{#1}{#3}%
}%
\def\XINT_flpower_loop_throwaway #1#2#3#4%
{%
   \XINT_flpower_loop {#1}{#2}{#3}%
}%
```

24.53 \xintFloatSqrt

1.08

```
\def\xintFloatSqrt     {\romannumeral0\xintfloatsqrt }%
\def\xintfloatsqrt   #1{\XINT_flsqrt_chkopt \xintfloat #1\Z }%
\def\XINTinFloatSqrt   {\romannumeral-`0\XINTinfloatsqrt }%
\def\XINTinfloatsqrt #1{\XINT_flsqrt_chkopt \XINT_inFloat #1\Z }%
\def\XINT_flsqrt_chkopt #1#2%
{%
    \ifx [#2\expandafter\XINT_flsqrt_opt
       \else\expandafter\XINT_flsqrt_noopt
    \fi  #1#2%
}%
\def\XINT_flsqrt_noopt #1#2\Z
{%
    #1[\XINT_digits]{\XINT_FL_sqrt \XINT_digits {#2}}%
}%
\def\XINT_flsqrt_opt #1[\Z #2]#3%
{%
    #1[#2]{\XINT_FL_sqrt {#2}{#3}}%
}%
\def\XINT_FL_sqrt #1%
{%
    \ifnum\numexpr #1<\xint_c_xviii
        \xint_afterfi {\XINT_FL_sqrt_a\xint_c_xviii}%
```

```
    \else
        \xint_afterfi {\XINT_FL_sqrt_a {#1+\xint_c_i}}%
    \fi
}%
\def\XINT_FL_sqrt_a #1#2%
{%
    \expandafter\XINT_FL_sqrt_checkifzeroorneg
    \romannumeral-`0\XINT_inFloat [#1]{#2}%
}%
\def\XINT_FL_sqrt_checkifzeroorneg #1%
{%
    \xint_UDzerominusfork
     #1-\dummy  \XINT_FL_sqrt_iszero
     0#1\dummy  \XINT_FL_sqrt_isneg
      0-\dummy {\XINT_FL_sqrt_b #1}%
    \krof
}%
\def\XINT_FL_sqrt_iszero #1[#2]{0[0]}%
\def\XINT_FL_sqrt_isneg  #1[#2]{\xintError:RootOfNegative 0[0]}%
\def\XINT_FL_sqrt_b #1[#2]%
{%
    \ifodd #2
        \xint_afterfi{\XINT_FL_sqrt_c 01}%
    \else
        \xint_afterfi{\XINT_FL_sqrt_c {}0}%
    \fi
    {#1}{#2}%
}%
\def\XINT_FL_sqrt_c #1#2#3#4%
{%
    \expandafter\XINT_flsqrt\expandafter {\the\numexpr #4-#2}{#3#1}%
}%
\def\XINT_flsqrt #1#2%
{%
    \expandafter\XINT_sqrt_a
    \expandafter{\romannumeral0\XINT_length {#2}}\XINT_flsqrt_big_d {#2}{#1}%
}%
\def\XINT_flsqrt_big_d #1\or #2\fi #3%
{%
   \fi
   \ifodd #3
     \xint_afterfi{\expandafter\XINT_flsqrt_big_eB}%
   \else
     \xint_afterfi{\expandafter\XINT_flsqrt_big_eA}%
   \fi
   \expandafter {\the\numexpr (#3-\xint_c_i)/\xint_c_ii }{#1}%
}%
\def\XINT_flsqrt_big_eA  #1#2#3%
{%
```

```
    \XINT_flsqrt_big_eA_a #3\Z {#2}{#1}{#3}%
}%
\def\XINT_flsqrt_big_eA_a #1#2#3#4#5#6#7#8#9\Z
{%
    \XINT_flsqrt_big_eA_b {#1#2#3#4#5#6#7#8}%
}%
\def\XINT_flsqrt_big_eA_b #1#2%
{%
    \expandafter\XINT_flsqrt_big_f
    \romannumeral0\XINT_flsqrt_small_e {#2001}{#1}%
}%
\def\XINT_flsqrt_big_eB #1#2#3%
{%
    \XINT_flsqrt_big_eB_a #3\Z {#2}{#1}{#3}%
}%
\def\XINT_flsqrt_big_eB_a #1#2#3#4#5#6#7#8#9%
{%
    \XINT_flsqrt_big_eB_b {#1#2#3#4#5#6#7#8#9}%
}%
\def\XINT_flsqrt_big_eB_b #1#2\Z #3%
{%
    \expandafter\XINT_flsqrt_big_f
    \romannumeral0\XINT_flsqrt_small_e {#30001}{#1}%
}%
\def\XINT_flsqrt_small_e #1#2%
{%
   \expandafter\XINT_flsqrt_small_f\expandafter
   {\the\numexpr #1*#1-#2-\xint_c_i}{#1}%
}%
\def\XINT_flsqrt_small_f #1#2%
{%
   \expandafter\XINT_flsqrt_small_g\expandafter
   {\the\numexpr (#1+#2)/(2*#2)-\xint_c_i }{#1}{#2}%
}%
\def\XINT_flsqrt_small_g #1%
{%
    \ifnum #1>\xint_c_
       \expandafter\XINT_flsqrt_small_h
    \else
       \expandafter\XINT_flsqrt_small_end
    \fi
    {#1}%
}%
\def\XINT_flsqrt_small_h #1#2#3%
{%
    \expandafter\XINT_flsqrt_small_f\expandafter
    {\the\numexpr #2-\xint_c_ii*#1*#3+#1*#1\expandafter}\expandafter
    {\the\numexpr #3-#1}%
}%
```

```
\def\XINT_flsqrt_small_end #1#2#3%
{%
    \expandafter\space\expandafter
    {\the\numexpr \xint_c_i+#3*\xint_c_x^iv-
                       (#2*\xint_c_x^iv+#3)/(\xint_c_ii*#3)}%
}%
\def\XINT_flsqrt_big_f #1%
{%
    \expandafter\XINT_flsqrt_big_fa\expandafter
    {\romannumeral0\xintisqr {#1}}{#1}%
}%
\def\XINT_flsqrt_big_fa #1#2#3#4%
{%
    \expandafter\XINT_flsqrt_big_fb\expandafter
    {\romannumeral-`0\XINT_dsx_addzerosnofuss
                      {\numexpr #3-\xint_c_viii\relax}{#2}}%
    {\romannumeral0\xintisub
      {\XINT_dsx_addzerosnofuss
           {\numexpr \xint_c_ii*(#3-\xint_c_viii)\relax}{#1}}{#4}}%
    {#3}%
}%
\def\XINT_flsqrt_big_fb #1#2%
{%
    \expandafter\XINT_flsqrt_big_g\expandafter {#2}{#1}%
}%
\def\XINT_flsqrt_big_g #1#2%
{%
    \expandafter\XINT_flsqrt_big_j
    \romannumeral0\xintidivision
    {#1}{\romannumeral0\XINT_dbl_pos #2\R\R\R\R\R\R\R\Z \W\W\W\W\W\W\W }{#2}%
}%
\def\XINT_flsqrt_big_j #1%
{%
    \ifcase\XINT_Sgn {#1}
        \expandafter \XINT_flsqrt_big_end_a
    \or \expandafter \XINT_flsqrt_big_k
    \fi {#1}%
}%
\def\XINT_flsqrt_big_k #1#2#3%
{%
    \expandafter\XINT_flsqrt_big_l\expandafter
    {\romannumeral0\XINT_sub_pre {#3}{#1}}%
    {\romannumeral0\xintiadd {#2}{\romannumeral0\XINT_sqr {#1}}}%
}%
\def\XINT_flsqrt_big_l #1#2%
{%
   \expandafter\XINT_flsqrt_big_g\expandafter
   {#2}{#1}%
}%
```

```
\def\XINT_flsqrt_big_end_a #1#2#3#4#5%
{%
   \expandafter\XINT_flsqrt_big_end_b\expandafter
   {\the\numexpr -#4+#5/\xint_c_ii\expandafter}\expandafter
   {\romannumeral0\xintisub
    {\XINT_dsx_addzerosnofuss {#4}{#3}}%
    {\xintHalf{\xintiQuo{\XINT_dsx_addzerosnofuss {#4}{#2}}{#3}}}}%
}%
\def\XINT_flsqrt_big_end_b #1#2{#2[#1]}%
\XINT_frac_restorecatcodes_endinput%
```

25 Package xintseries implementation

The commenting is currently (2013/06/16) very sparse.

Contents

25.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the xintfrac package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \def\space { }%
  \let\z\endgroup
  \expandafter\let\expandafter\x\csname ver@xintseries.sty\endcsname
  \expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
  \expandafter
```

```
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \expandafter
  \ifx\csname numexpr\endcsname\relax
     \y{xintseries}{\numexpr not available, aborting input}%
     \aftergroup\endinput
  \else
    \ifx\x\relax   % plain-TeX, first loading of xintseries.sty
      \ifx\w\relax % but xintfrac.sty not yet loaded.
         \y{xintseries}{Package xintfrac is required}%
         \y{xintseries}{Will try \string\input\space xintfrac.sty}%
         \def\z{\endgroup\input xintfrac.sty\relax}%
      \fi
    \else
      \def\empty {}%
      \ifx\x\empty % LaTeX, first loading,
      % variable is initialized, but \ProvidesPackage not yet seen
          \ifx\w\relax % xintfrac.sty not yet loaded.
            \y{xintseries}{Package xintfrac is required}%
            \y{xintseries}{Will try \string\RequirePackage{xintfrac}}%
            \def\z{\endgroup\RequirePackage{xintfrac}}%
          \fi
      \else
        \y{xintseries}{I was already loaded, aborting input}%
        \aftergroup\endinput
      \fi
    \fi
  \fi
\z%
```

25.2 Confirmation of xintfrac loading

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
```

```
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \def\empty {}%
  \expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
  \ifx\w\relax % Plain TeX, user gave a file name at the prompt
     \y{xintseries}{Loading of package xintfrac failed, aborting input}%
     \aftergroup\endinput
  \fi
  \ifx\w\empty % LaTeX, user gave a file name at the prompt
     \y{xintseries}{Loading of package xintfrac failed, aborting input}%
     \aftergroup\endinput
  \fi
\endgroup%
```

25.3 Catcodes

Perhaps catcodes have changed after the loading of **xint** and **xintfrac** and prior to the current loading of **xintseries**, so we can not employ the `\XINT_restorecatcodes_endinput` in this style file. But there is no problem using `\XINT_setcatcodes`.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_series_restorecatcodes_endinput
      {%
        \catcode93=\the\catcode93   % ]
        \catcode91=\the\catcode91   % [
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
```

```
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
      \catcode91=12 % [
      \catcode93=12 % ]
  }%
\x
```

25.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xintseries.sty\endcsname
\ProvidesPackage{xintseries}%
  [2013/06/14 v1.08b Expandable partial sums with xint package (jfB)]%
```

25.5 \xintSeries

Modified in 1.06 to give the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that. 1.08a adds the forgotten optimization following that previous change.

```
\def\xintSeries {\romannumeral0\xintseries }%
\def\xintseries #1#2%
{%
    \expandafter\XINT_series\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
```

```
\def\XINT_series #1#2#3%
{%
   \ifnum #2<#1
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi {\XINT_series_loop {#1}{0}{#2}{#3}}%
   \fi
}%
\def\XINT_series_loop #1#2#3#4%
{%
    \ifnum #3>#1 \else \XINT_series_exit \fi
    \expandafter\XINT_series_loop\expandafter
    {\the\numexpr #1+1\expandafter }\expandafter
    {\romannumeral0\xintadd {#2}{#4{#1}}}%
    {#3}{#4}%
}%
\def\XINT_series_exit \fi #1#2#3#4#5#6#7#8%
{%
    \fi\xint_gobble_ii #6%
}%
```

25.6 \xintiSeries

Modified in 1.06 to give the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that. 1.08a adds the forgotten optimization following that previous change.

```
\def\xintiSeries {\romannumeral0\xintiseries }%
\def\xintiseries #1#2%
{%
    \expandafter\XINT_iseries\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_iseries #1#2#3%
{%
   \ifnum #2<#1
      \xint_afterfi { 0}%
   \else
      \xint_afterfi {\XINT_iseries_loop {#1}{0}{#2}{#3}}%
   \fi
}%
\def\XINT_iseries_loop #1#2#3#4%
{%
    \ifnum #3>#1 \else \XINT_iseries_exit \fi
    \expandafter\XINT_iseries_loop\expandafter
    {\the\numexpr #1+1\expandafter }\expandafter
    {\romannumeral0\xintiadd {#2}{#4{#1}}}%
    {#3}{#4}%
}%
```

```
\def\XINT_iseries_exit \fi #1#2#3#4#5#6#7#8%
{%
    \fi\xint_gobble_ii #6%
}%
```

25.7 \xintPowerSeries

The 1.03 version was very lame and created a build-up of denominators. The Horner scheme for polynomial evaluation is used in 1.04, this cures the denominator problem and drastically improves the efficiency of the macro. Modified in 1.06 to give the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that. 1.08a adds the forgotten optimization following that previous change.

```
\def\xintPowerSeries {\romannumeral0\xintpowerseries }%
\def\xintpowerseries #1#2%
{%
    \expandafter\XINT_powseries\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_powseries #1#2#3#4%
{%
   \ifnum #2<#1
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi
      {\XINT_powseries_loop_i {#3{#2}}{#1}{#2}{#3}{#4}}%
   \fi
}%
\def\XINT_powseries_loop_i #1#2#3#4#5%
{%
    \ifnum #3>#2 \else\XINT_powseries_exit_i\fi
    \expandafter\XINT_powseries_loop_ii\expandafter
    {\the\numexpr #3-1\expandafter}\expandafter
    {\romannumeral0\xintmul {#1}{#5}}{#2}{#4}{#5}%
}%
\def\XINT_powseries_loop_ii #1#2#3#4%
{%
   \expandafter\XINT_powseries_loop_i\expandafter
   {\romannumeral0\xintadd {#4{#1}}{#2}}{#3}{#1}{#4}%
}%
\def\XINT_powseries_exit_i\fi #1#2#3#4#5#6#7#8#9%
{%
    \fi \XINT_powseries_exit_ii  #6{#7}%
}%
\def\XINT_powseries_exit_ii #1#2#3#4#5#6%
{%
    \xintmul{\xintPow {#5}{#6}}{#4}%
}%
```

25.8 \xintPowerSeriesX

```
Same as \xintPowerSeries except for the initial expansion of the x parameter.
Modified in 1.06 to give the indices first to a \numexpr rather than expand-
ing twice. I just use \the\numexpr and maintain the previous code after that.
1.08a adds the forgotten optimization following that previous change.
```

```
\def\xintPowerSeriesX {\romannumeral0\xintpowerseriesx }%
\def\xintpowerseriesx #1#2%
{%
    \expandafter\XINT_powseriesx\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_powseriesx #1#2#3#4%
{%
   \ifnum #2<#1
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi
      {\expandafter\XINT_powseriesx_pre\expandafter
                  {\romannumeral-‘0#4}{#1}{#2}{#3}%
      }%
   \fi
}%
\def\XINT_powseriesx_pre #1#2#3#4%
{%
    \XINT_powseries_loop_i {#4{#3}}{#2}{#3}{#4}{#1}%
}%
```

25.9 \xintRationalSeries

```
This computes F(a)+...+F(b) on the basis of the value of F(a) and the ratios
F(n)/F(n-1). As in \xintPowerSeries we use an iterative scheme which has the
great advantage to avoid denominator build-up. This makes exact computations
possible with exponential type series, which would be completely inaccessible
to \xintSeries. #1=a, #2=b, #3=F(a), #4=ratio function Modified in 1.06 to give
the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr
and maintain the previous code after that. 1.08a adds the forgotten optimiza-
tion following that previous change.
```

```
\def\xintRationalSeries {\romannumeral0\xintratseries }%
\def\xintratseries #1#2%
{%
    \expandafter\XINT_ratseries\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_ratseries #1#2#3#4%
{%
   \ifnum #2<#1
```

```
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi
      {\XINT_ratseries_loop {#2}{1}{#1}{#4}{#3}}%
   \fi
}%
\def\XINT_ratseries_loop #1#2#3#4%
{%
    \ifnum #1>#3 \else\XINT_ratseries_exit_i\fi
    \expandafter\XINT_ratseries_loop\expandafter
    {\the\numexpr #1-1\expandafter}\expandafter
    {\romannumeral0\xintadd {1}{\xintMul {#2}{#4{#1}}}}{#3}{#4}%
}%
\def\XINT_ratseries_exit_i\fi #1#2#3#4#5#6#7#8%
{%
    \fi \XINT_ratseries_exit_ii  #6%
}%
\def\XINT_ratseries_exit_ii #1#2#3#4#5%
{%
    \XINT_ratseries_exit_iii #5%
}%
\def\XINT_ratseries_exit_iii #1#2#3#4%
{%
    \xintmul{#2}{#4}%
}%
```

25.10 \xintRationalSeriesX

a,b,initial,ratiofunction,x
This computes F(a,x)+...+F(b,x) on the basis of the value of F(a,x) and the ratios F(n,x)/F(n-1,x). The argument x is first expanded and it is the value resulting from this which is used then throughout. The initial term F(a,x) must be defined as one-parameter macro which will be given x. Modified in 1.06 to give the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that. 1.08a adds the forgotten optimization following that previous change.

```
\def\xintRationalSeriesX {\romannumeral0\xintratseriesx }%
\def\xintratseriesx #1#2%
{%
    \expandafter\XINT_ratseriesx\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_ratseriesx #1#2#3#4#5%
{%
   \ifnum #2<#1
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi
```

```
      {\expandafter\XINT_ratseriesx_pre\expandafter
                    {\romannumeral-`0#5}{#2}{#1}{#4}{#3}%
      }%
   \fi
}%
\def\XINT_ratseriesx_pre #1#2#3#4#5%
{%
    \XINT_ratseries_loop {#2}{1}{#3}{#4{#1}}{#5{#1}}%
}%
```

25.11 \xintFxPtPowerSeries

I am not two happy with this piece of code. Will make it more economical another day. Modified in 1.06 to give the indices first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that. 1.08a: forgot last time some optimization from the change to \numexpr.

```
\def\xintFxPtPowerSeries {\romannumeral0\xintfxptpowerseries }%
\def\xintfxptpowerseries #1#2%
{%
    \expandafter\XINT_fppowseries\expandafter
    {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
}%
\def\XINT_fppowseries #1#2#3#4#5%
{%
   \ifnum #2<#1
      \xint_afterfi { 0}%
   \else
      \xint_afterfi
        {\expandafter\XINT_fppowseries_loop_pre\expandafter
           {\romannumeral0\xinttrunc {#5}{\xintPow {#4}{#1}}}%
          {#1}{#4}{#2}{#3}{#5}%
        }%
   \fi
}%
\def\XINT_fppowseries_loop_pre #1#2#3#4#5#6%
{%
    \ifnum #4>#2 \else\XINT_fppowseries_dont_i \fi
    \expandafter\XINT_fppowseries_loop_i\expandafter
    {\the\numexpr #2+\xint_c_i\expandafter}\expandafter
    {\romannumeral0\xintitrunc {#6}{\xintMul {#5{#2}}{#1}}}%
    {#1}{#3}{#4}{#5}{#6}%
}%
\def\XINT_fppowseries_dont_i \fi\expandafter\XINT_fppowseries_loop_i
    {\fi \expandafter\XINT_fppowseries_dont_ii }%
\def\XINT_fppowseries_dont_ii #1#2#3#4#5#6#7{\xinttrunc {#7}{#2[-#7]}}%
\def\XINT_fppowseries_loop_i #1#2#3#4#5#6#7%
{%
    \ifnum #5>#1 \else \XINT_fppowseries_exit_i \fi
```

```
7347     \expandafter\XINT_fppowseries_loop_ii\expandafter
7348     {\romannumeral0\xinttrunc {#7}{\xintMul {#3}{#4}}}%
7349     {#1}{#4}{#2}{#5}{#6}{#7}%
7350 }%
7351 \def\XINT_fppowseries_loop_ii #1#2#3#4#5#6#7%
7352 {%
7353     \expandafter\XINT_fppowseries_loop_i\expandafter
7354     {\the\numexpr #2+\xint_c_i\expandafter}\expandafter
7355     {\romannumeral0\xintiadd {#4}{\xintiTrunc {#7}{\xintMul {#6{#2}}{#1}}}}%
7356     {#1}{#3}{#5}{#6}{#7}%
7357 }%
7358 \def\XINT_fppowseries_exit_i\fi\expandafter\XINT_fppowseries_loop_ii
7359     {\fi \expandafter\XINT_fppowseries_exit_ii }%
7360 \def\XINT_fppowseries_exit_ii #1#2#3#4#5#6#7%
7361 {%
7362     \xinttrunc {#7}
7363     {\xintiAdd {#4}{\xintiTrunc {#7}{\xintMul {#6{#2}}{#1}}}[-#7]}%
7364 }%
```

25.12 \xintFxPtPowerSeriesX

```
a,b,coeff,x,D
Modified in 1.06 to give the indices first to a \numexpr rather than expand-
ing twice. I just use \the\numexpr and maintain the previous code after that.
1.08a adds the forgotten optimization following that previous change.
```

```
7365 \def\xintFxPtPowerSeriesX {\romannumeral0\xintfxptpowerseriesx }%
7366 \def\xintfxptpowerseriesx #1#2%
7367 {%
7368     \expandafter\XINT_fppowseriesx\expandafter
7369     {\the\numexpr #1\expandafter}\expandafter{\the\numexpr #2}%
7370 }%
7371 \def\XINT_fppowseriesx #1#2#3#4#5%
7372 {%
7373    \ifnum #2<#1
7374       \xint_afterfi { 0}%
7375    \else
7376       \xint_afterfi
7377         {\expandafter \XINT_fppowseriesx_pre \expandafter
7378          {\romannumeral-`0#4}{#1}{#2}{#3}{#5}%
7379         }%
7380    \fi
7381 }%
7382 \def\XINT_fppowseriesx_pre #1#2#3#4#5%
7383 {%
7384     \expandafter\XINT_fppowseries_loop_pre\expandafter
7385        {\romannumeral0\xinttrunc {#5}{\xintPow {#1}{#2}}}%
7386        {#2}{#1}{#3}{#4}{#5}%
7387 }%
```

25.13 \xintFloatPowerSeries

1.08a. I still have to re-visit \xintFxPtPowerSeries; temporarily I just adapted the code to the case of floats.

```
\def\xintFloatPowerSeries {\romannumeral0\xintfloatpowerseries }%
\def\xintfloatpowerseries #1{\XINT_flpowseries_chkopt #1\Z }%
\def\XINT_flpowseries_chkopt #1%
{%
    \ifx [#1\expandafter\XINT_flpowseries_opt
       \else\expandafter\XINT_flpowseries_noopt
    \fi
    #1%
}%
\def\XINT_flpowseries_noopt  #1\Z #2%
{%
    \expandafter\XINT_flpowseries\expandafter
    {\the\numexpr #1\expandafter}\expandafter
    {\the\numexpr #2}\XINT_digits
}%
\def\XINT_flpowseries_opt [\Z #1]#2#3%
{%
    \expandafter\XINT_flpowseries\expandafter
    {\the\numexpr #2\expandafter}\expandafter
    {\the\numexpr #3\expandafter}{\the\numexpr #1}%
}%
\def\XINT_flpowseries #1#2#3#4#5%
{%
   \ifnum #2<#1
      \xint_afterfi { 0.e0}%
   \else
      \xint_afterfi
        {\expandafter\XINT_flpowseries_loop_pre\expandafter
           {\romannumeral-`0\XINTinfloatpow [#3]{#5}{#1}}%
         {#1}{#5}{#2}{#4}{#3}%
        }%
   \fi
}%
\def\XINT_flpowseries_loop_pre #1#2#3#4#5#6%
{%
    \ifnum #4>#2 \else\XINT_flpowseries_dont_i \fi
    \expandafter\XINT_flpowseries_loop_i\expandafter
    {\the\numexpr #2+\xint_c_i\expandafter}\expandafter
    {\romannumeral-`0\XINTinfloatmul [#6]{#5{#2}}{#1}}%
    {#1}{#3}{#4}{#5}{#6}%
}%
\def\XINT_flpowseries_dont_i \fi\expandafter\XINT_flpowseries_loop_i
    {\fi \expandafter\XINT_flpowseries_dont_ii }%
\def\XINT_flpowseries_dont_ii #1#2#3#4#5#6#7{\xintfloat [#7]{#2}}%
```

```
\def\XINT_flpowseries_loop_i #1#2#3#4#5#6#7%
{%
    \ifnum #5>#1 \else \XINT_flpowseries_exit_i \fi
    \expandafter\XINT_flpowseries_loop_ii\expandafter
    {\romannumeral-`0\XINTinfloatmul [#7]{#3}{#4}}%
    {#1}{#4}{#2}{#5}{#6}{#7}%
}%
\def\XINT_flpowseries_loop_ii #1#2#3#4#5#6#7%
{%
    \expandafter\XINT_flpowseries_loop_i\expandafter
    {\the\numexpr #2+\xint_c_i\expandafter}\expandafter
    {\romannumeral-`0\XINTinfloatadd [#7]{#4}%
                          {\XINTinfloatmul [#7]{#6{#2}}{#1}}}%
    {#1}{#3}{#5}{#6}{#7}%
}%
\def\XINT_flpowseries_exit_i\fi\expandafter\XINT_flpowseries_loop_ii
    {\fi \expandafter\XINT_flpowseries_exit_ii }%
\def\XINT_flpowseries_exit_ii #1#2#3#4#5#6#7%
{%
    \xintfloatadd [#7]{#4}{\XINTinfloatmul [#7]{#6{#2}}{#1}}%
}%
```

25.14 \xintFloatPowerSeriesX

1.08a

```
\def\xintFloatPowerSeriesX {\romannumeral0\xintfloatpowerseriesx }%
\def\xintfloatpowerseriesx #1{\XINT_flpowseriesx_chkopt #1\Z }%
\def\XINT_flpowseriesx_chkopt #1%
{%
    \ifx [#1\expandafter\XINT_flpowseriesx_opt
       \else\expandafter\XINT_flpowseriesx_noopt
    \fi
    #1%
}%
\def\XINT_flpowseriesx_noopt  #1\Z #2%
{%
    \expandafter\XINT_flpowseriesx\expandafter
    {\the\numexpr #1\expandafter}\expandafter
    {\the\numexpr #2}\XINT_digits
}%
\def\XINT_flpowseriesx_opt [\Z #1]#2#3%
{%
    \expandafter\XINT_flpowseriesx\expandafter
    {\the\numexpr #2\expandafter}\expandafter
    {\the\numexpr #3\expandafter}{\the\numexpr #1}%
}%
\def\XINT_flpowseriesx #1#2#3#4#5%
{%
```

```
    \ifnum #2<#1
       \xint_afterfi { 0.e0}%
    \else
       \xint_afterfi
         {\expandafter \XINT_flpowseriesx_pre \expandafter
          {\romannumeral-`0#5}{#1}{#2}{#4}{#3}%
         }%
    \fi
}%
\def\XINT_flpowseriesx_pre #1#2#3#4#5%
{%
     \expandafter\XINT_flpowseries_loop_pre\expandafter
        {\romannumeral-`0\XINTinfloatpow [#5]{#1}{#2}}%
        {#2}{#1}{#3}{#4}{#5}%
}%
\XINT_series_restorecatcodes_endinput%
```

26 Package xintcfrac implementation

The commenting is currently (2013/06/16) very sparse.

Contents

26.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the xintfrac package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
```

```
\endlinechar=13 %
\catcode123=1   % {
\catcode125=2   % }
\catcode64=11   % @
\catcode35=6    % #
\catcode44=12   % ,
\catcode45=12   % -
\catcode46=12   % .
\catcode58=12   % :
\def\space { }%
\let\z\endgroup
\expandafter\let\expandafter\x\csname ver@xintcfrac.sty\endcsname
\expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
\expandafter
  \ifx\csname PackageInfo\endcsname\relax
    \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
  \else
    \def\y#1#2{\PackageInfo{#1}{#2}}%
  \fi
\expandafter
\ifx\csname numexpr\endcsname\relax
   \y{xintcfrac}{\numexpr not available, aborting input}%
   \aftergroup\endinput
\else
  \ifx\x\relax   % plain-TeX, first loading of xintcfrac.sty
    \ifx\w\relax % but xintfrac.sty not yet loaded.
       \y{xintcfrac}{Package xintfrac is required}%
       \y{xintcfrac}{Will try \string\input\space xintfrac.sty}%
       \def\z{\endgroup\input xintfrac.sty\relax}%
    \fi
  \else
    \def\empty {}%
    \ifx\x\empty % LaTeX, first loading,
    % variable is initialized, but \ProvidesPackage not yet seen
        \ifx\w\relax % xintfrac.sty not yet loaded.
          \y{xintcfrac}{Package xintfrac is required}%
          \y{xintcfrac}{Will try \string\RequirePackage{xintfrac}}%
          \def\z{\endgroup\RequirePackage{xintfrac}}%
        \fi
    \else
      \y{xintcfrac}{I was already loaded, aborting input}%
      \aftergroup\endinput
    \fi
  \fi
\fi
\z%
```

26.2 Confirmation of xintfrac loading

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \def\empty {}%
  \expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
  \ifx\w\relax % Plain TeX, user gave a file name at the prompt
      \y{xintcfrac}{Loading of package xintfrac failed, aborting input}%
      \aftergroup\endinput
  \fi
  \ifx\w\empty % LaTeX, user gave a file name at the prompt
      \y{xintcfrac}{Loading of package xintfrac failed, aborting input}%
      \aftergroup\endinput
  \fi
\endgroup%
```

26.3 Catcodes

Perhaps catcodes have changed after the loading of **xint** and **xintfrac** and prior to the current loading of **xintcfrac**, so we can not employ the `\XINT_restorecatcodes_endinput` in this style file. But there is no problem using `\XINT_setcatcodes`.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_cfrac_restorecatcodes_endinput
      {%
        \catcode93=\the\catcode93   % ]
        \catcode91=\the\catcode91   % [
        \catcode94=\the\catcode94   % ^
        \catcode96=\the\catcode96   % `
```

```
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
      \catcode91=12 % [
      \catcode93=12 % ]
  }%
\x
```

26.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
  \fi
\expandafter\x\csname ver@xintcfrac.sty\endcsname
```

```
\ProvidesPackage{xintcfrac}%
  [2013/06/14 v1.08b Expandable continued fractions with xint package (jfB)]%
```

26.5 \xintCFrac

```
\def\xintCFrac {\romannumeral0\xintcfrac }%
\def\xintcfrac #1%
{%
    \XINT_cfrac_opt_a #1\Z
}%
\def\XINT_cfrac_opt_a #1%
{%
    \ifx[#1\XINT_cfrac_opt_b\fi \XINT_cfrac_noopt #1%
}%
\def\XINT_cfrac_noopt #1\Z
{%
    \expandafter\XINT_cfrac_A\romannumeral0\xintrawwithzeros {#1}\Z
    \relax\relax
}%
\def\XINT_cfrac_opt_b\fi\XINT_cfrac_noopt [\Z #1]%
{%
    \fi\csname XINT_cfrac_opt#1\endcsname
}%
\def\XINT_cfrac_optl #1%
{%
    \expandafter\XINT_cfrac_A\romannumeral0\xintrawwithzeros {#1}\Z
    \relax\hfill
}%
\def\XINT_cfrac_optc #1%
{%
    \expandafter\XINT_cfrac_A\romannumeral0\xintrawwithzeros {#1}\Z
    \relax\relax
}%
\def\XINT_cfrac_optr #1%
{%
    \expandafter\XINT_cfrac_A\romannumeral0\xintrawwithzeros {#1}\Z
    \hfill\relax
}%
\def\XINT_cfrac_A #1/#2\Z
{%
    \expandafter\XINT_cfrac_B\romannumeral0\xintidivision {#1}{#2}{#2}%
}%
\def\XINT_cfrac_B #1#2%
{%
    \XINT_cfrac_C #2\Z {#1}%
}%
\def\XINT_cfrac_C #1%
{%
    \xint_gob_til_zero #1\XINT_cfrac_integer 0\XINT_cfrac_D #1%
}%
```

```
\def\XINT_cfrac_integer 0\XINT_cfrac_D 0#1\Z #2#3#4#5{ #2}%
\def\XINT_cfrac_D #1\Z #2#3{\XINT_cfrac_loop_a {#1}{#3}{#1}{{#2}}}%
\def\XINT_cfrac_loop_a
{%
    \expandafter\XINT_cfrac_loop_d\romannumeral0\XINT_div_prepare
}%
\def\XINT_cfrac_loop_d #1#2%
{%
    \XINT_cfrac_loop_e #2.{#1}%
}%
\def\XINT_cfrac_loop_e #1%
{%
    \xint_gob_til_zero #1\xint_cfrac_loop_exit0\XINT_cfrac_loop_f #1%
}%
\def\XINT_cfrac_loop_f #1.#2#3#4%
{%
    \XINT_cfrac_loop_a {#1}{#3}{#1}{{#2}#4}%
}%
\def\xint_cfrac_loop_exit0\XINT_cfrac_loop_f #1.#2#3#4#5#6%
   {\XINT_cfrac_T #5#6{#2}#4\Z }%
\def\XINT_cfrac_T #1#2#3#4%
{%
  \xint_gob_til_Z #4\XINT_cfrac_end\Z\XINT_cfrac_T #1#2{#4+\cfrac{#11#2}{#3}}%
}%
\def\XINT_cfrac_end\Z\XINT_cfrac_T #1#2#3%
{%
    \XINT_cfrac_end_b #3%
}%
\def\XINT_cfrac_end_b \Z+\cfrac#1#2{ #2}%
```

26.6 \xintGCFrac

```
\def\xintGCFrac {\romannumeral0\xintgcfrac }%
\def\xintgcfrac #1{\XINT_gcfrac_opt_a #1\Z }%
\def\XINT_gcfrac_opt_a #1%
{%
    \ifx[#1\XINT_gcfrac_opt_b\fi \XINT_gcfrac_noopt #1%
}%
\def\XINT_gcfrac_noopt #1\Z
{%
    \XINT_gcfrac #1+\W/\relax\relax
}%
\def\XINT_gcfrac_opt_b\fi\XINT_gcfrac_noopt [\Z #1]%
{%
    \fi\csname XINT_gcfrac_opt#1\endcsname
}%
\def\XINT_gcfrac_optl #1%
{%
    \XINT_gcfrac #1+\W/\relax\hfill
}%
```

```
\def\XINT_gcfrac_optc #1%
{%
    \XINT_gcfrac #1+\W/\relax\relax
}%
\def\XINT_gcfrac_optr #1%
{%
    \XINT_gcfrac #1+\W/\hfill\relax
}%
\def\XINT_gcfrac
{%
    \expandafter\XINT_gcfrac_enter\romannumeral-`0%
}%
\def\XINT_gcfrac_enter {\XINT_gcfrac_loop {}}%
\def\XINT_gcfrac_loop #1#2+#3/%
{%
    \xint_gob_til_W #3\XINT_gcfrac_endloop\W
    \XINT_gcfrac_loop {{#3}{#2}#1}%
}%
\def\XINT_gcfrac_endloop\W\XINT_gcfrac_loop #1#2#3%
{%
    \XINT_gcfrac_T #2#3#1\Z\Z
}%
\def\XINT_gcfrac_T #1#2#3#4{\XINT_gcfrac_U #1#2{\xintFrac{#4}}}%
\def\XINT_gcfrac_U #1#2#3#4#5%
{%
    \xint_gob_til_Z #5\XINT_gcfrac_end\Z\XINT_gcfrac_U
                #1#2{\xintFrac{#5}%
                 \ifcase\xintSgn{#4}
                 +\or+\else-\fi
                 \cfrac{#1\xintFrac{\xintAbs{#4}}#2}{#3}}%
}%
\def\XINT_gcfrac_end\Z\XINT_gcfrac_U #1#2#3%
{%
    \XINT_gcfrac_end_b #3%
}%
\def\XINT_gcfrac_end_b #1\cfrac#2#3{ #3}%
```

26.7 \xintGCtoGCx

```
\def\xintGCtoGCx {\romannumeral0\xintgctogcx }%
\def\xintgctogcx #1#2#3%
{%
    \expandafter\XINT_gctgcx_start\expandafter {\romannumeral-`0#3}{#1}{#2}%
}%
\def\XINT_gctgcx_start #1#2#3{\XINT_gctgcx_loop_a {}{#2}{#3}#1+\W/}%
\def\XINT_gctgcx_loop_a #1#2#3#4+#5/%
{%
    \xint_gob_til_W #5\XINT_gctgcx_end\W
    \XINT_gctgcx_loop_b {#1{#4}}{#2{#5}#3}{#2}{#3}%
}%
```

```
\def\XINT_gctgcx_loop_b #1#2%
{%
    \XINT_gctgcx_loop_a {#1#2}%
}%
\def\XINT_gctgcx_end\W\XINT_gctgcx_loop_b #1#2#3#4{ #1}%
```

26.8 \xintFtoCs

```
\def\xintFtoCs {\romannumeral0\xintftocs }%
\def\xintftocs #1%
{%
    \expandafter\XINT_ftc_A\romannumeral0\xintrawwithzeros {#1}\Z
}%
\def\XINT_ftc_A #1/#2\Z
{%
    \expandafter\XINT_ftc_B\romannumeral0\xintidivision {#1}{#2}{#2}%
}%
\def\XINT_ftc_B #1#2%
{%
    \XINT_ftc_C #2.{#1}%
}%
\def\XINT_ftc_C #1%
{%
    \xint_gob_til_zero #1\XINT_ftc_integer 0\XINT_ftc_D #1%
}%
\def\XINT_ftc_integer 0\XINT_ftc_D 0#1.#2#3{ #2}%
\def\XINT_ftc_D #1.#2#3{\XINT_ftc_loop_a {#1}{#3}{#1}{#2,}}%
\def\XINT_ftc_loop_a
{%
    \expandafter\XINT_ftc_loop_d\romannumeral0\XINT_div_prepare
}%
\def\XINT_ftc_loop_d #1#2%
{%
    \XINT_ftc_loop_e #2.{#1}%
}%
\def\XINT_ftc_loop_e #1%
{%
    \xint_gob_til_zero #1\xint_ftc_loop_exit0\XINT_ftc_loop_f #1%
}%
\def\XINT_ftc_loop_f #1.#2#3#4%
{%
    \XINT_ftc_loop_a {#1}{#3}{#1}{#4#2,}%
}%
\def\xint_ftc_loop_exit0\XINT_ftc_loop_f #1.#2#3#4{ #4#2}%
```

26.9 \xintFtoCx

```
\def\xintFtoCx {\romannumeral0\xintftocx }%
\def\xintftocx #1#2%
{%
    \expandafter\XINT_ftcx_A\romannumeral0\xintrawwithzeros {#2}\Z {#1}%
```

```
}%
\def\XINT_ftcx_A #1/#2\Z
{%
    \expandafter\XINT_ftcx_B\romannumeral0\xintidivision {#1}{#2}{#2}%
}%
\def\XINT_ftcx_B #1#2%
{%
    \XINT_ftcx_C #2.{#1}%
}%
\def\XINT_ftcx_C #1%
{%
    \xint_gob_til_zero #1\XINT_ftcx_integer 0\XINT_ftcx_D #1%
}%
\def\XINT_ftcx_integer 0\XINT_ftcx_D 0#1.#2#3#4{ #2}%
\def\XINT_ftcx_D #1.#2#3#4{\XINT_ftcx_loop_a {#1}{#3}{#1}{#2#4}{#4}}%
\def\XINT_ftcx_loop_a
{%
    \expandafter\XINT_ftcx_loop_d\romannumeral0\XINT_div_prepare
}%
\def\XINT_ftcx_loop_d #1#2%
{%
    \XINT_ftcx_loop_e #2.{#1}%
}%
\def\XINT_ftcx_loop_e #1%
{%
    \xint_gob_til_zero #1\xint_ftcx_loop_exit0\XINT_ftcx_loop_f #1%
}%
\def\XINT_ftcx_loop_f #1.#2#3#4#5%
{%
    \XINT_ftcx_loop_a {#1}{#3}{#1}{#4{#2}#5}{#5}%
}%
\def\xint_ftcx_loop_exit0\XINT_ftcx_loop_f #1.#2#3#4#5{ #4{#2}}%
```

26.10 \xintFtoGC

```
\def\xintFtoGC {\romannumeral0\xintftogc }%
\def\xintftogc {\xintftocx {+1/}}%
```

26.11 \xintFtoCC

```
\def\xintFtoCC {\romannumeral0\xintftocc }%
\def\xintftocc #1%
{%
    \expandafter\XINT_ftcc_A\expandafter {\romannumeral0\xintrawwithzeros {#1}}%
}%
\def\XINT_ftcc_A #1%
{%
    \expandafter\XINT_ftcc_B
    \romannumeral0\xintrawwithzeros {\xintAdd {1/2[0]}{#1[0]}}\Z {#1[0]}%
}%
\def\XINT_ftcc_B #1/#2\Z
```

```
{%
    \expandafter\XINT_ftcc_C\expandafter {\romannumeral0\xintiquo {#1}{#2}}%
}%
\def\XINT_ftcc_C #1#2%
{%
    \expandafter\XINT_ftcc_D\romannumeral0\xintsub {#2}{#1}\Z {#1}%
}%
\def\XINT_ftcc_D #1%
{%
    \xint_UDzerominusfork
      #1-\dummy \XINT_ftcc_integer
      0#1\dummy \XINT_ftcc_En
       0-\dummy {\XINT_ftcc_Ep #1}%
    \krof
}%
\def\XINT_ftcc_Ep #1\Z #2%
{%
    \expandafter\XINT_ftcc_loop_a\expandafter
    {\romannumeral0\xintdiv {1[0]}{#1}}{#2+1/}%
}%
\def\XINT_ftcc_En #1\Z #2%
{%
    \expandafter\XINT_ftcc_loop_a\expandafter
    {\romannumeral0\xintdiv {1[0]}{#1}}{#2+-1/}%
}%
\def\XINT_ftcc_integer #1\Z #2{ #2}%
\def\XINT_ftcc_loop_a #1%
{%
    \expandafter\XINT_ftcc_loop_b
    \romannumeral0\xintrawwithzeros {\xintAdd {1/2[0]}{#1}}\Z {#1}%
}%
\def\XINT_ftcc_loop_b #1/#2\Z
{%
    \expandafter\XINT_ftcc_loop_c\expandafter
    {\romannumeral0\xintiquo {#1}{#2}}%
}%
\def\XINT_ftcc_loop_c #1#2%
{%
    \expandafter\XINT_ftcc_loop_d
    \romannumeral0\xintsub {#2}{#1[0]}\Z {#1}%
}%
\def\XINT_ftcc_loop_d #1%
{%
    \xint_UDzerominusfork
      #1-\dummy \XINT_ftcc_end
      0#1\dummy \XINT_ftcc_loop_N
       0-\dummy {\XINT_ftcc_loop_P #1}%
    \krof
}%
```

```
\def\XINT_ftcc_end #1\Z #2#3{ #3#2}%
\def\XINT_ftcc_loop_P #1\Z #2#3%
{%
    \expandafter\XINT_ftcc_loop_a\expandafter
    {\romannumeral0\xintdiv {1[0]}{#1}}{#3#2+1/}%
}%
\def\XINT_ftcc_loop_N #1\Z #2#3%
{%
    \expandafter\XINT_ftcc_loop_a\expandafter
    {\romannumeral0\xintdiv {1[0]}{#1}}{#3#2+-1/}%
}%
```

26.12 \xintFtoCv

```
\def\xintFtoCv {\romannumeral0\xintftocv }%
\def\xintftocv #1%
{%
    \xinticstocv {\xintFtoCs {#1}}%
}%
```

26.13 \xintFtoCCv

```
\def\xintFtoCCv {\romannumeral0\xintftoccv }%
\def\xintftoccv #1%
{%
    \xintigctocv {\xintFtoCC {#1}}%
}%
```

26.14 \xintCstoF

```
\def\xintCstoF {\romannumeral0\xintcstof }%
\def\xintcstof #1%
{%
    \expandafter\XINT_cstf_prep \romannumeral-`0#1,\W,%
}%
\def\XINT_cstf_prep
{%
    \XINT_cstf_loop_a 1001%
}%
\def\XINT_cstf_loop_a #1#2#3#4#5,%
{%
    \xint_gob_til_W #5\XINT_cstf_end\W
    \expandafter\XINT_cstf_loop_b
    \romannumeral0\xintrawwithzeros {#5}.{#1}{#2}{#3}{#4}%
}%
\def\XINT_cstf_loop_b #1/#2.#3#4#5#6%
{%
    \expandafter\XINT_cstf_loop_c\expandafter
    {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
    {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#6}}{\XINT_Mul {#1}{#4}}}%
```

```
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#5}}{\XINT_Mul {#1}{#3}}}%
}%
\def\XINT_cstf_loop_c #1#2%
{%
    \expandafter\XINT_cstf_loop_d\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_cstf_loop_d #1#2%
{%
    \expandafter\XINT_cstf_loop_e\expandafter {\expandafter{#2}#1}%
}%
\def\XINT_cstf_loop_e #1#2%
{%
    \expandafter\XINT_cstf_loop_a\expandafter{#2}#1%
}%
\def\XINT_cstf_end #1.#2#3#4#5{\xintrawwithzeros {#2/#3}[0]}%
```

26.15 \xintiCstoF

```
\def\xintiCstoF {\romannumeral0\xinticstof }%
\def\xinticstof #1%
{%
    \expandafter\XINT_icstf_prep \romannumeral-`0#1,\W,%
}%
\def\XINT_icstf_prep
{%
    \XINT_icstf_loop_a 1001%
}%
\def\XINT_icstf_loop_a #1#2#3#4#5,%
{%
    \xint_gob_til_W #5\XINT_icstf_end\W
    \expandafter
    \XINT_icstf_loop_b \romannumeral-`0#5.{#1}{#2}{#3}{#4}%
}%
\def\XINT_icstf_loop_b #1.#2#3#4#5%
{%
    \expandafter\XINT_icstf_loop_c\expandafter
    {\romannumeral0\xintiadd {#5}{\XINT_Mul {#1}{#3}}}%
    {\romannumeral0\xintiadd {#4}{\XINT_Mul {#1}{#2}}}%
    {#2}{#3}%
}%
\def\XINT_icstf_loop_c #1#2%
{%
    \expandafter\XINT_icstf_loop_a\expandafter {#2}{#1}%
}%
\def\XINT_icstf_end#1.#2#3#4#5{\xintrawwithzeros {#2/#3}[0]}%
```

26.16 \xintGCtoF

```
\def\xintGCtoF {\romannumeral0\xintgctof }%
\def\xintgctof #1%
{%
```

```
7996     \expandafter\XINT_gctf_prep \romannumeral-`0#1+\W/%
7997 }%
7998 \def\XINT_gctf_prep
7999 {%
8000     \XINT_gctf_loop_a 1001%
8001 }%
8002 \def\XINT_gctf_loop_a #1#2#3#4#5+%
8003 {%
8004     \expandafter\XINT_gctf_loop_b
8005     \romannumeral0\xintrawwithzeros {#5}.{#1}{#2}{#3}{#4}%
8006 }%
8007 \def\XINT_gctf_loop_b #1/#2.#3#4#5#6%
8008 {%
8009     \expandafter\XINT_gctf_loop_c\expandafter
8010     {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
8011     {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
8012     {\romannumeral0\xintiadd {\XINT_Mul {#2}{#6}}{\XINT_Mul {#1}{#4}}}%
8013     {\romannumeral0\xintiadd {\XINT_Mul {#2}{#5}}{\XINT_Mul {#1}{#3}}}%
8014 }%
8015 \def\XINT_gctf_loop_c #1#2%
8016 {%
8017     \expandafter\XINT_gctf_loop_d\expandafter {\expandafter{#2}{#1}}%
8018 }%
8019 \def\XINT_gctf_loop_d #1#2%
8020 {%
8021     \expandafter\XINT_gctf_loop_e\expandafter {\expandafter{#2}#1}%
8022 }%
8023 \def\XINT_gctf_loop_e #1#2%
8024 {%
8025     \expandafter\XINT_gctf_loop_f\expandafter {\expandafter{#2}#1}%
8026 }%
8027 \def\XINT_gctf_loop_f #1#2/%
8028 {%
8029     \xint_gob_til_W #2\XINT_gctf_end\W
8030     \expandafter\XINT_gctf_loop_g
8031     \romannumeral0\xintrawwithzeros {#2}.#1%
8032 }%
8033 \def\XINT_gctf_loop_g #1/#2.#3#4#5#6%
8034 {%
8035     \expandafter\XINT_gctf_loop_h\expandafter
8036     {\romannumeral0\XINT_mul_fork #1\Z #6\Z }%
8037     {\romannumeral0\XINT_mul_fork #1\Z #5\Z }%
8038     {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
8039     {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
8040 }%
8041 \def\XINT_gctf_loop_h #1#2%
8042 {%
8043     \expandafter\XINT_gctf_loop_i\expandafter {\expandafter{#2}{#1}}%
8044 }%
```

```
\def\XINT_gctf_loop_i #1#2%
{%
    \expandafter\XINT_gctf_loop_j\expandafter {\expandafter{#2}#1}%
}%
\def\XINT_gctf_loop_j #1#2%
{%
    \expandafter\XINT_gctf_loop_a\expandafter {#2}#1%
}%
\def\XINT_gctf_end #1.#2#3#4#5{\xintrawwithzeros {#2/#3}[0]}%
```

26.17 \xintiGCtoF

```
\def\xintiGCtoF {\romannumeral0\xintigctof }%
\def\xintigctof #1%
{%
    \expandafter\XINT_igctf_prep \romannumeral-`0#1+\W/%
}%
\def\XINT_igctf_prep
{%
    \XINT_igctf_loop_a 1001%
}%
\def\XINT_igctf_loop_a #1#2#3#4#5+%
{%
    \expandafter\XINT_igctf_loop_b
    \romannumeral-`0#5.{#1}{#2}{#3}{#4}%
}%
\def\XINT_igctf_loop_b #1.#2#3#4#5%
{%
    \expandafter\XINT_igctf_loop_c\expandafter
    {\romannumeral0\xintiadd {#5}{\XINT_Mul {#1}{#3}}}%
    {\romannumeral0\xintiadd {#4}{\XINT_Mul {#1}{#2}}}%
    {#2}{#3}%
}%
\def\XINT_igctf_loop_c #1#2%
{%
    \expandafter\XINT_igctf_loop_f\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_igctf_loop_f #1#2#3#4/%
{%
    \xint_gob_til_W #4\XINT_igctf_end\W
    \expandafter\XINT_igctf_loop_g
    \romannumeral-`0#4.{#2}{#3}#1%
}%
\def\XINT_igctf_loop_g #1.#2#3%
{%
    \expandafter\XINT_igctf_loop_h\expandafter
    {\romannumeral0\XINT_mul_fork #1\Z #3\Z }%
    {\romannumeral0\XINT_mul_fork #1\Z #2\Z }%
}%
\def\XINT_igctf_loop_h #1#2%
```

```
{%
    \expandafter\XINT_igctf_loop_i\expandafter {#2}{#1}%
}%
\def\XINT_igctf_loop_i #1#2#3#4%
{%
    \XINT_igctf_loop_a {#3}{#4}{#1}{#2}%
}%
\def\XINT_igctf_end #1.#2#3#4#5{\xintrawwithzeros {#4/#5}[0]}%
```

26.18 \xintCstoCv

```
\def\xintCstoCv {\romannumeral0\xintcstocv }%
\def\xintcstocv #1%
{%
    \expandafter\XINT_cstcv_prep \romannumeral-`0#1,\W,%
}%
\def\XINT_cstcv_prep
{%
    \XINT_cstcv_loop_a {}1001%
}%
\def\XINT_cstcv_loop_a #1#2#3#4#5#6,%
{%
    \xint_gob_til_W #6\XINT_cstcv_end\W
    \expandafter\XINT_cstcv_loop_b
    \romannumeral0\xintrawwithzeros {#6}.{#2}{#3}{#4}{#5}{#1}%
}%
\def\XINT_cstcv_loop_b #1/#2.#3#4#5#6%
{%
    \expandafter\XINT_cstcv_loop_c\expandafter
    {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
    {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#6}}{\XINT_Mul {#1}{#4}}}%
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#5}}{\XINT_Mul {#1}{#3}}}%
}%
\def\XINT_cstcv_loop_c #1#2%
{%
    \expandafter\XINT_cstcv_loop_d\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_cstcv_loop_d #1#2%
{%
    \expandafter\XINT_cstcv_loop_e\expandafter {\expandafter{#2}#1}%
}%
\def\XINT_cstcv_loop_e #1#2%
{%
    \expandafter\XINT_cstcv_loop_f\expandafter{#2}#1%
}%
\def\XINT_cstcv_loop_f #1#2#3#4#5%
{%
    \expandafter\XINT_cstcv_loop_g\expandafter
    {\romannumeral0\xintrawwithzeros {#1/#2}}{#5}{#1}{#2}{#3}{#4}%
```

```
}%
\def\XINT_cstcv_loop_g #1#2{\XINT_cstcv_loop_a {#2{#1[0]}}}%
\def\XINT_cstcv_end #1.#2#3#4#5#6{ #6}%
```

26.19 \xintiCstoCv

```
\def\xintiCstoCv {\romannumeral0\xinticstocv }%
\def\xinticstocv #1%
{%
    \expandafter\XINT_icstcv_prep \romannumeral-`0#1,\W,%
}%
\def\XINT_icstcv_prep
{%
    \XINT_icstcv_loop_a {}1001%
}%
\def\XINT_icstcv_loop_a #1#2#3#4#5#6,%
{%
    \xint_gob_til_W #6\XINT_icstcv_end\W
    \expandafter
    \XINT_icstcv_loop_b \romannumeral-`0#6.{#2}{#3}{#4}{#5}{#1}%
}%
\def\XINT_icstcv_loop_b #1.#2#3#4#5%
{%
    \expandafter\XINT_icstcv_loop_c\expandafter
    {\romannumeral0\xintiadd {#5}{\XINT_Mul {#1}{#3}}}%
    {\romannumeral0\xintiadd {#4}{\XINT_Mul {#1}{#2}}}%
    {{#2}{#3}}%
}%
\def\XINT_icstcv_loop_c #1#2%
{%
    \expandafter\XINT_icstcv_loop_d\expandafter {#2}{#1}%
}%
\def\XINT_icstcv_loop_d #1#2%
{%
    \expandafter\XINT_icstcv_loop_e\expandafter
    {\romannumeral0\xintrawwithzeros {#1/#2}}{{#1}{#2}}%
}%
\def\XINT_icstcv_loop_e #1#2#3#4{\XINT_icstcv_loop_a {#4{#1[0]}}#2#3}%
\def\XINT_icstcv_end #1.#2#3#4#5#6{ #6}%
```

26.20 \xintGCtoCv

```
\def\xintGCtoCv {\romannumeral0\xintgctocv }%
\def\xintgctocv #1%
{%
    \expandafter\XINT_gctcv_prep \romannumeral-`0#1+\W/%
}%
\def\XINT_gctcv_prep
{%
    \XINT_gctcv_loop_a {}1001%
}%
```

```
\def\XINT_gctcv_loop_a #1#2#3#4#5#6+%
{%
    \expandafter\XINT_gctcv_loop_b
    \romannumeral0\xintrawwithzeros {#6}.{#2}{#3}{#4}{#5}{#1}%
}%
\def\XINT_gctcv_loop_b #1/#2.#3#4#5#6%
{%
    \expandafter\XINT_gctcv_loop_c\expandafter
    {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
    {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#6}}{\XINT_Mul {#1}{#4}}}%
    {\romannumeral0\xintiadd {\XINT_Mul {#2}{#5}}{\XINT_Mul {#1}{#3}}}%
}%
\def\XINT_gctcv_loop_c #1#2%
{%
    \expandafter\XINT_gctcv_loop_d\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_gctcv_loop_d #1#2%
{%
    \expandafter\XINT_gctcv_loop_e\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_gctcv_loop_e #1#2%
{%
    \expandafter\XINT_gctcv_loop_f\expandafter {#2}#1%
}%
\def\XINT_gctcv_loop_f #1#2%
{%
    \expandafter\XINT_gctcv_loop_g\expandafter
    {\romannumeral0\xintrawwithzeros {#1/#2}}{{#1}{#2}}%
}%
\def\XINT_gctcv_loop_g #1#2#3#4%
{%
    \XINT_gctcv_loop_h {#4{#1[0]}}{#2#3}%
}%
\def\XINT_gctcv_loop_h #1#2#3/%
{%
    \xint_gob_til_W #3\XINT_gctcv_end\W
    \expandafter\XINT_gctcv_loop_i
    \romannumeral0\xintrawwithzeros {#3}.#2{#1}%
}%
\def\XINT_gctcv_loop_i #1/#2.#3#4#5#6%
{%
    \expandafter\XINT_gctcv_loop_j\expandafter
    {\romannumeral0\XINT_mul_fork #1\Z #6\Z }%
    {\romannumeral0\XINT_mul_fork #1\Z #5\Z }%
    {\romannumeral0\XINT_mul_fork #2\Z #4\Z }%
    {\romannumeral0\XINT_mul_fork #2\Z #3\Z }%
}%
\def\XINT_gctcv_loop_j #1#2%
```

```
{%
    \expandafter\XINT_gctcv_loop_k\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_gctcv_loop_k #1#2%
{%
    \expandafter\XINT_gctcv_loop_l\expandafter {\expandafter{#2}#1}%
}%
\def\XINT_gctcv_loop_l #1#2%
{%
    \expandafter\XINT_gctcv_loop_m\expandafter {\expandafter{#2}#1}%
}%
\def\XINT_gctcv_loop_m #1#2{\XINT_gctcv_loop_a {#2}#1}%
\def\XINT_gctcv_end #1.#2#3#4#5#6{ #6}%
```

26.21 \xintiGCtoCv

```
\def\xintiGCtoCv {\romannumeral0\xintigctocv }%
\def\xintigctocv #1%
{%
    \expandafter\XINT_igctcv_prep \romannumeral-`0#1+\W/%
}%
\def\XINT_igctcv_prep
{%
    \XINT_igctcv_loop_a {}1001%
}%
\def\XINT_igctcv_loop_a #1#2#3#4#5#6+%
{%
    \expandafter\XINT_igctcv_loop_b
    \romannumeral-`0#6.{#2}{#3}{#4}{#5}{#1}%
}%
\def\XINT_igctcv_loop_b #1.#2#3#4#5%
{%
    \expandafter\XINT_igctcv_loop_c\expandafter
    {\romannumeral0\xintiadd {#5}{\XINT_Mul {#1}{#3}}}%
    {\romannumeral0\xintiadd {#4}{\XINT_Mul {#1}{#2}}}%
    {{#2}{#3}}%
}%
\def\XINT_igctcv_loop_c #1#2%
{%
    \expandafter\XINT_igctcv_loop_f\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_igctcv_loop_f #1#2#3#4/%
{%
    \xint_gob_til_W #4\XINT_igctcv_end_a\W
    \expandafter\XINT_igctcv_loop_g
    \romannumeral-`0#4.#1#2{#3}%
}%
\def\XINT_igctcv_loop_g #1.#2#3#4#5%
{%
    \expandafter\XINT_igctcv_loop_h\expandafter
```

```
    {\romannumeral0\XINT_mul_fork #1\Z #5\Z }%
    {\romannumeral0\XINT_mul_fork #1\Z #4\Z }%
    {{#2}{#3}}%
}%
\def\XINT_igctcv_loop_h #1#2%
{%
    \expandafter\XINT_igctcv_loop_i\expandafter {\expandafter{#2}{#1}}%
}%
\def\XINT_igctcv_loop_i #1#2{\XINT_igctcv_loop_k #2{#2#1}}%
\def\XINT_igctcv_loop_k #1#2%
{%
    \expandafter\XINT_igctcv_loop_l\expandafter
    {\romannumeral0\xintrawwithzeros {#1/#2}}%
}%
\def\XINT_igctcv_loop_l #1#2#3{\XINT_igctcv_loop_a {#3{#1[0]}}#2}%
\def\XINT_igctcv_end_a #1.#2#3#4#5%
{%
    \expandafter\XINT_igctcv_end_b\expandafter
    {\romannumeral0\xintrawwithzeros {#2/#3}}%
}%
\def\XINT_igctcv_end_b #1#2{ #2{#1[0]}}%
```

26.22 \xintCntoF

Modified in 1.06 to give the N first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that.

```
\def\xintCntoF {\romannumeral0\xintcntof }%
\def\xintcntof #1%
{%
    \expandafter\XINT_cntf\expandafter {\the\numexpr #1}%
}%
\def\XINT_cntf #1#2%
{%
   \ifnum #1>\xint_c_
      \xint_afterfi {\expandafter\XINT_cntf_loop\expandafter
                     {\the\numexpr #1-1\expandafter}\expandafter
                     {\romannumeral-`0#2{#1}}{#2}}%
   \else
      \xint_afterfi
         {\ifnum #1=\xint_c_
              \xint_afterfi {\expandafter\space \romannumeral-`0#2{0}}%
          \else \xint_afterfi { 0/1[0]}%
          \fi}%
   \fi
}%
\def\XINT_cntf_loop #1#2#3%
{%
    \ifnum #1>\xint_c_ \else \XINT_cntf_exit \fi
    \expandafter\XINT_cntf_loop\expandafter
```

```
    {\the\numexpr #1-1\expandafter }\expandafter
    {\romannumeral0\xintadd {\xintDiv {1[0]}{#2}}{#3{#1}}}%
    {#3}%
}%
\def\XINT_cntf_exit \fi
    \expandafter\XINT_cntf_loop\expandafter
    #1\expandafter #2#3%
{%
    \fi\xint_gobble_ii #2%
}%
```

26.23 \xintGCntoF

Modified in 1.06 to give the N first to a \numexpr rather than expanding twice. I just use \the\numexpr and maintain the previous code after that.

```
\def\xintGCntoF {\romannumeral0\xintgcntof }%
\def\xintgcntof #1%
{%
    \expandafter\XINT_gcntf\expandafter {\the\numexpr #1}%
}%
\def\XINT_gcntf #1#2#3%
{%
   \ifnum #1>\xint_c_
      \xint_afterfi {\expandafter\XINT_gcntf_loop\expandafter
                     {\the\numexpr #1-1\expandafter}\expandafter
                     {\romannumeral-`0#2{#1}}{#2}{#3}}%
   \else
      \xint_afterfi
         {\ifnum #1=\xint_c_
              \xint_afterfi {\expandafter\space\romannumeral-`0#2{0}}%
          \else \xint_afterfi { 0/1[0]}%
          \fi}%
   \fi
}%
\def\XINT_gcntf_loop #1#2#3#4%
{%
    \ifnum #1>\xint_c_ \else \XINT_gcntf_exit \fi
    \expandafter\XINT_gcntf_loop\expandafter
    {\the\numexpr #1-1\expandafter }\expandafter
    {\romannumeral0\xintadd {\xintDiv {#4{#1}}{#2}}{#3{#1}}}%
    {#3}{#4}%
}%
\def\XINT_gcntf_exit \fi
    \expandafter\XINT_gcntf_loop\expandafter
    #1\expandafter #2#3#4%
{%
    \fi\xint_gobble_ii #2%
}%
```

26.24 \xintCntoCs

```
Modified in 1.06 to give the N first to a \numexpr rather than expanding twice.
I just use \the\numexpr and maintain the previous code after that.
```

```
\def\xintCntoCs {\romannumeral0\xintcntocs }%
\def\xintcntocs #1%
{%
    \expandafter\XINT_cntcs\expandafter {\the\numexpr #1}%
}%
\def\XINT_cntcs #1#2%
{%
   \ifnum #1<0
      \xint_afterfi { 0/1[0]}%
   \else
      \xint_afterfi {\expandafter\XINT_cntcs_loop\expandafter
                     {\the\numexpr #1-1\expandafter}\expandafter
                     {\expandafter{\romannumeral-`0#2{#1}}}{#2}}%
   \fi
}%
\def\XINT_cntcs_loop #1#2#3%
{%
    \ifnum #1>-1 \else \XINT_cntcs_exit \fi
    \expandafter\XINT_cntcs_loop\expandafter
    {\the\numexpr #1-1\expandafter }\expandafter
    {\expandafter{\romannumeral-`0#3{#1}},#2}{#3}%
}%
\def\XINT_cntcs_exit \fi
    \expandafter\XINT_cntcs_loop\expandafter
    #1\expandafter #2#3%
{%
    \fi\XINT_cntcs_exit_b #2%
}%
\def\XINT_cntcs_exit_b #1,{ }%
```

26.25 \xintCntoGC

```
Modified in 1.06 to give the N first to a \numexpr rather than expanding twice.
I just use \the\numexpr and maintain the previous code after that.
```

```
\def\xintCntoGC {\romannumeral0\xintcntogc }%
\def\xintcntogc #1%
{%
    \expandafter\XINT_cntgc\expandafter {\the\numexpr #1}%
}%
\def\XINT_cntgc #1#2%
{%
   \ifnum #1<0
      \xint_afterfi { 0/1[0]}%
```

```
8405    \else
8406       \xint_afterfi {\expandafter\XINT_cntgc_loop\expandafter
8407                      {\the\numexpr #1-1\expandafter}\expandafter
8408                      {\expandafter{\romannumeral-`0#2{#1}}}{#2}}%
8409    \fi
8410 }%
8411 \def\XINT_cntgc_loop #1#2#3%
8412 {%
8413     \ifnum #1>-1 \else \XINT_cntgc_exit \fi
8414     \expandafter\XINT_cntgc_loop\expandafter
8415     {\the\numexpr #1-1\expandafter }\expandafter
8416     {\expandafter{\romannumeral-`0#3{#1}}+1/#2}{#3}%
8417 }%
8418 \def\XINT_cntgc_exit \fi
8419     \expandafter\XINT_cntgc_loop\expandafter
8420     #1\expandafter #2#3%
8421 {%
8422     \fi\XINT_cntgc_exit_b #2%
8423 }%
8424 \def\XINT_cntgc_exit_b #1+1/{ }%
```

26.26 \xintGCntoGC

```
Modified in 1.06 to give the N first to a \numexpr rather than expanding twice.
I just use \the\numexpr and maintain the previous code after that.
```

```
8425 \def\xintGCntoGC {\romannumeral0\xintgcntogc }%
8426 \def\xintgcntogc #1%
8427 {%
8428     \expandafter\XINT_gcntgc\expandafter {\the\numexpr #1}%
8429 }%
8430 \def\XINT_gcntgc #1#2#3%
8431 {%
8432    \ifnum #1<0
8433       \xint_afterfi { {0/1[0]}}%
8434    \else
8435       \xint_afterfi {\expandafter\XINT_gcntgc_loop\expandafter
8436                      {\the\numexpr #1-1\expandafter}\expandafter
8437                      {\expandafter{\romannumeral-`0#2{#1}}}{#2}{#3}}%
8438    \fi
8439 }%
8440 \def\XINT_gcntgc_loop #1#2#3#4%
8441 {%
8442     \ifnum #1>-1 \else \XINT_gcntgc_exit \fi
8443     \expandafter\XINT_gcntgc_loop_b\expandafter
8444     {\expandafter{\romannumeral-`0#4{#1}}/#2}{#3{#1}}{#1}{#3}{#4}%
8445 }%
8446 \def\XINT_gcntgc_loop_b #1#2#3%
8447 {%
```

```
8448     \expandafter\XINT_gcntgc_loop\expandafter
8449     {\the\numexpr #3-1\expandafter}\expandafter
8450     {\expandafter{\romannumeral-`0#2}+#1}%
8451 }%
8452 \def\XINT_gcntgc_exit \fi
8453     \expandafter\XINT_gcntgc_loop_b\expandafter #1#2#3#4#5%
8454 {%
8455     \fi\XINT_gcntgc_exit_b #1%
8456 }%
8457 \def\XINT_gcntgc_exit_b #1/{ }%
```

26.27 \xintCstoGC

```
8458 \def\xintCstoGC {\romannumeral0\xintcstogc }%
8459 \def\xintcstogc #1%
8460 {%
8461     \expandafter\XINT_cstc_prep \romannumeral-`0#1,\W,%
8462 }%
8463 \def\XINT_cstc_prep #1,{\XINT_cstc_loop_a {{#1}}}%
8464 \def\XINT_cstc_loop_a #1#2,%
8465 {%
8466     \xint_gob_til_W #2\XINT_cstc_end\W
8467     \XINT_cstc_loop_b {#1}{#2}%
8468 }%
8469 \def\XINT_cstc_loop_b #1#2{\XINT_cstc_loop_a {#1+1/{#2}}}%
8470 \def\XINT_cstc_end\W\XINT_cstc_loop_b #1#2{ #1}%
```

26.28 \xintGCtoGC

```
8471 \def\xintGCtoGC {\romannumeral0\xintgctogc }%
8472 \def\xintgctogc #1%
8473 {%
8474     \expandafter\XINT_gctgc_start \romannumeral-`0#1+\W/%
8475 }%
8476 \def\XINT_gctgc_start {\XINT_gctgc_loop_a {}}%
8477 \def\XINT_gctgc_loop_a #1#2+#3/%
8478 {%
8479     \xint_gob_til_W #3\XINT_gctgc_end\W
8480     \expandafter\XINT_gctgc_loop_b\expandafter
8481     {\romannumeral-`0#2}{#3}{#1}%
8482 }%
8483 \def\XINT_gctgc_loop_b #1#2%
8484 {%
8485     \expandafter\XINT_gctgc_loop_c\expandafter
8486     {\romannumeral-`0#2}{#1}%
8487 }%
8488 \def\XINT_gctgc_loop_c #1#2#3%
8489 {%
8490     \XINT_gctgc_loop_a {#3{#2}+{#1}/}%
8491 }%
```

```
\def\XINT_gctgc_end\W\expandafter\XINT_gctgc_loop_b
{%
    \expandafter\XINT_gctgc_end_b
}%
\def\XINT_gctgc_end_b #1#2#3{ #3{#1}}%
\XINT_cfrac_restorecatcodes_endinput%
```

27 Package xintexpr implementation

The commenting is currently (2013/06/16) very sparse. I was greatly helped in the task of writing this expandable parser by the comments provided in `l3fp-parse.dtx`. One will recognize in particular the idea of the 'until' macros; but I have not looked into the actual `l3fp` code beyond the very useful comments provided in its documentation. My main hurdle was that my data has no a priori bound on its size; this led me to experiment with a technique of storing and retrieving data expandably as *names* of control sequences. Also brace pairs have a special rôle related to the parsing of `A/B[n]` fractions; this is *experimental* and perhaps I will opt for another solution at a later stage, for example one where such fractions should be user-prefixed by some marker, for example `!` (which could not be confused there with its other use as postfix symbol for the factorial function). There are thus some essential differences of principle with the `l3fp` workplan. Of course, my task was on the other hand simplified by the fact that I do not implement boolean operators nor function names. To circumvent the potential hash-table impact I have provided the macro creators `\xintNewExpr` and `\xintNewFloatExpr`.

Version `1.08b` tries to correct a problem originating in the attempt to attribute a special rôle to braces: expansion could be stopped by space tokens, as various macros tried to expand without grabbing what came next. They now have a doubled `\romannumeral-'0`.

Contents

27.1 Catcodes, ε-TEX and reload detection

The code for reload detection is copied from Heiko Oberdiek's packages, and adapted here to check for previous loading of the xintfrac package.

The method for catcodes is slightly different, but still directly inspired by these packages.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
```

```
\endlinechar=13 %
\catcode123=1   % {
\catcode125=2   % }
\catcode64=11   % @
\catcode35=6    % #
\catcode44=12   % ,
\catcode45=12   % -
\catcode46=12   % .
\catcode58=12   % :
\def\space { }%
\let\z\endgroup
\expandafter\let\expandafter\x\csname ver@xintexpr.sty\endcsname
\expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
\expandafter
  \ifx\csname PackageInfo\endcsname\relax
    \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
  \else
    \def\y#1#2{\PackageInfo{#1}{#2}}%
  \fi
\expandafter
\ifx\csname numexpr\endcsname\relax
   \y{xintexpr}{\numexpr not available, aborting input}%
   \aftergroup\endinput
\else
  \ifx\x\relax   % plain-TeX, first loading of xintexpr.sty
    \ifx\w\relax % but xintfrac.sty not yet loaded.
       \y{xintexpr}{Package xintfrac is required}%
       \y{xintexpr}{Will try \string\input\space xintfrac.sty}%
       \def\z{\endgroup\input xintfrac.sty\relax}%
    \fi
  \else
    \def\empty {}%
    \ifx\x\empty % LaTeX, first loading,
    % variable is initialized, but \ProvidesPackage not yet seen
        \ifx\w\relax % xintfrac.sty not yet loaded.
          \y{xintexpr}{Package xintfrac is required}%
          \y{xintexpr}{Will try \string\RequirePackage{xintfrac}}%
          \def\z{\endgroup\RequirePackage{xintfrac}}%
        \fi
    \else
      \y{xintexpr}{I was already loaded, aborting input}%
      \aftergroup\endinput
    \fi
  \fi
\fi
\z%
```

27.2 Confirmation of xintfrac loading

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode64=11   % @
  \catcode35=6    % #
  \catcode44=12   % ,
  \catcode45=12   % -
  \catcode46=12   % .
  \catcode58=12   % :
  \expandafter
    \ifx\csname PackageInfo\endcsname\relax
      \def\y#1#2{\immediate\write-1{Package #1 Info: #2.}}%
    \else
      \def\y#1#2{\PackageInfo{#1}{#2}}%
    \fi
  \def\empty {}%
  \expandafter\let\expandafter\w\csname ver@xintfrac.sty\endcsname
  \ifx\w\relax % Plain TeX, user gave a file name at the prompt
      \y{xintexpr}{Loading of package xintfrac failed, aborting input}%
      \aftergroup\endinput
  \fi
  \ifx\w\empty % LaTeX, user gave a file name at the prompt
      \y{xintexpr}{Loading of package xintfrac failed, aborting input}%
      \aftergroup\endinput
  \fi
\endgroup%
```

27.3 Catcodes

Perhaps catcodes have changed after the loading of **xint** and **xintfrac** and prior to the current loading of **xintexpr**, so we can not employ the `\XINT_restorecatcodes_endinput` in this style file. But there is no problem using `\XINT_setcatcodes`.

```
\begingroup\catcode61\catcode48\catcode32=10\relax%
  \catcode13=5    % ^^M
  \endlinechar=13 %
  \catcode123=1   % {
  \catcode125=2   % }
  \catcode95=11   % _
  \def\x
  {%
      \endgroup
      \edef\XINT_expr_restorecatcodes_endinput
      {%
        \catcode33=\the\catcode33   % !
        \catcode93=\the\catcode93   % ]
        \catcode91=\the\catcode91   % [
        \catcode94=\the\catcode94   % ^
```

```
        \catcode96=\the\catcode96   % `
        \catcode47=\the\catcode47   % /
        \catcode41=\the\catcode41   % )
        \catcode40=\the\catcode40   % (
        \catcode42=\the\catcode42   % *
        \catcode43=\the\catcode43   % +
        \catcode62=\the\catcode62   % >
        \catcode60=\the\catcode60   % <
        \catcode58=\the\catcode58   % :
        \catcode46=\the\catcode46   % .
        \catcode45=\the\catcode45   % -
        \catcode44=\the\catcode44   % ,
        \catcode35=\the\catcode35   % #
        \catcode95=\the\catcode95   % _
        \catcode125=\the\catcode125 % }
        \catcode123=\the\catcode123 % {
        \endlinechar=\the\endlinechar
        \catcode13=\the\catcode13   % ^^M
        \catcode32=\the\catcode32   %
        \catcode61=\the\catcode61\relax   % =
        \noexpand\endinput
      }%
      \XINT_setcatcodes % defined in xint.sty
      \catcode91=12 % [
      \catcode93=12 % ]
      \catcode33=11 % !
  }%
\x
```

27.4 Package identification

```
\begingroup
  \catcode64=11 % @
  \catcode58=12 % :
  \expandafter\ifx\csname ProvidesPackage\endcsname\relax
    \def\x#1#2#3[#4]{\endgroup
      \immediate\write-1{Package: #3 #4}%
      \xdef#1{#4}%
    }%
  \else
    \def\x#1#2[#3]{\endgroup
      #2[{#3}]%
      \ifx#1\@undefined
        \xdef#1{#3}%
      \fi
      \ifx#1\relax
        \xdef#1{#3}%
      \fi
    }%
```

```
  \fi
\expandafter\x\csname ver@xintexpr.sty\endcsname
\ProvidesPackage{xintexpr}%
  [2013/06/14 v1.08b Expandable expression parser (jfB)]%
```

27.5 Helper macros

```
\def\xint_gob_til_dot #1.{}%
\def\xint_gob_til_dot_andstop #1.{ }%
\def\xint_gob_til_! #1!{}% ! of catcode 11
\def\XINT_expr_string {\expandafter\xint_gob_til_dot\string }%
\def\XINT_expr_unexpectedtoken {\xintError:ignored }%
```

27.6 \xintexpr, \xinttheexpr, \xintthe

```
\def\xintexpr {\romannumeral0\xinteval }%
\def\xinteval
{%
    \expandafter\XINT_expr_until_end\romannumeral-‘0%
    \expandafter\XINT_expr_checkifprefix_ii\romannumeral-‘0%
    \XINT_expr_getnext
}%
\def\xinttheexpr {\romannumeral0\xinttheeval }%
\def\xinttheeval {\expandafter\XINT_expr_the\romannumeral0\xinteval }%
\def\XINT_expr_the #1#2#3{\xintraw{\XINT_expr_string #3}}%
\def\xintthe #1{\ifx#1\xintexpr \expandafter\xinttheexpr
                \else\expandafter\xintthefloatexpr\fi}%
```

27.7 Parenthesized expressions

```
\def\XINT_expr_until_end #1%
{%
    \ifcase#1%
          \expandafter\xint_gobble_vi
    \or
          \expandafter\XINT_expr_extra_closing_paren
    \fi
    \expandafter\XINT_expr_until_end\romannumeral-‘0\romannumeral-‘0%
}%
\def\XINT_expr_extra_closing_paren {\xintError:removed }%
\def\XINT_expr_endofexpr {!\XINT_illegaluse }%
\def\XINT_illegaluse
   {Illegal_here_use_xintthe\xintError:use_xintthe!\xint_gobble_i }%
\def\XINT_expr_oparen
{%
    \expandafter\XINT_expr_until_cparen\romannumeral-‘0%
    \expandafter\XINT_expr_checkifprefix_ii\romannumeral-‘0%
    \XINT_expr_getnext
}%
\def\XINT_expr_until_cparen #1%
{%
```

```
    \ifcase#1%
          \expandafter\XINT_expr_missing_cparen
    \or
    \else \xint_afterfi
    {\expandafter\XINT_expr_until_cparen\romannumeral-`0\romannumeral-`0}%
    \fi
}%
\def\XINT_expr_missing_cparen #1%
{%
    \xintError:inserted \xint_c_ \XINT_expr_endofexpr
}%
```

27.8 Infix operators, minus as prefix, scientific notation

```
\def\xint_tmp_def #1#2#3%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_expr_op_#1\expandafter\endcsname
    \csname XINT_expr_until_#1\expandafter\endcsname
    \csname XINT_expr_checkifprefix_#2\expandafter\endcsname
    \csname XINT_expr_precedence_#1\expandafter\endcsname
    \csname xint_c_#2\expandafter\endcsname
    \csname xint#3\endcsname
}%
\def\xint_tmp_do_defs #1#2#3#4#5#6%
{%
    \def #1##1% \XINT_expr_op_?
    {%
        \expandafter #2\expandafter ##1\romannumeral-`0\expandafter
        #3\romannumeral-`0\XINT_expr_getnext
    }%
    \def #2##1##2##3##4% \XINT_expr_until_?
    {%
      \ifnum ##2>#5%
        \xint_afterfi {\expandafter #2\expandafter ##1\romannumeral-`0##3##4}%
      \else
        \xint_afterfi
        {\expandafter ##2\expandafter ##3%
         \csname .#6{\XINT_expr_string ##1}{\XINT_expr_string ##4}\endcsname }%
      \fi
    }%
    \let #4#5%
}%
\xint_tmp_def +{ii}{Add}%
\xint_tmp_def -{ii}{Sub}%
\xint_tmp_def *{iii}{Mul}%
\xint_tmp_def /{iii}{Div}%
\xint_tmp_def ^{iv}{Pow}%
\xint_tmp_def  e{v}{fE}%
\xint_tmp_def  E{v}{fE}%
```

```
\def\xint_tmp_def #1%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_expr_checkifprefix_#1\expandafter\endcsname
    \csname XINT_expr_op_-#1\endcsname
}%
\def\xint_tmp_do_defs #1#2%
{%
    \def #1##1%
    {\xint_UDsignfork
        ##1\dummy #2%
          -\dummy ##1%
     \krof }%
}%
\xint_tmp_def {ii}%
\xint_tmp_def {iii}%
\xint_tmp_def {iv}%
\xint_tmp_def {v}%
\def\xint_tmp_def #1%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_expr_op_-#1\expandafter\endcsname
    \csname XINT_expr_until_-#1\expandafter\endcsname
    \csname XINT_expr_checkifprefix_#1\expandafter\endcsname
    \csname xint_c_#1\endcsname
}%
\def\xint_tmp_do_defs #1#2#3#4%
{%
    \def #1% \XINT_expr_op_-ii,iii,iv,v
    {%
        \expandafter #2\romannumeral-`0\expandafter
        #3\romannumeral-`0\XINT_expr_getnext
    }%
    \def #2##1##2##3% \XINT_expr_until_-ii,iii,iv,v
    {%
        \ifnum ##1>#4%
         \xint_afterfi {\expandafter #2\romannumeral-`0##2##3}%
        \else
         \xint_afterfi {\expandafter ##1\expandafter ##2%
                        \csname .\xintOpp{\XINT_expr_string ##3}\endcsname }%
        \fi
    }%
}%
\xint_tmp_def {ii}%
\xint_tmp_def {iii}%
\xint_tmp_def {iv}%
\xint_tmp_def {v}%
```

27.9 Get next infix operator or closing parenthesis or factorial or expression end

June 14 (1.08b): I add here a second \romannumeral-‘0, as in \XINT_expr_getnext and other macros which are trying to expand the next token but without grabbing it.

```
\def\XINT_expr_getop #1%
{%
    \expandafter\XINT_expr_getop_a\expandafter #1%
    \romannumeral-‘0\romannumeral-‘0%
}%
\def\XINT_expr_getop_a #1#2%
{%
    \ifcat #2\relax
        \ifx #2\relax
             \expandafter\expandafter\expandafter
             \XINT_expr_foundendofexpr
        \else
             \XINT_expr_unexpectedtoken
             \expandafter\expandafter\expandafter
             \XINT_expr_getop
        \fi
    \else
        \expandafter\XINT_expr_op_found\expandafter #2%
    \fi
    #1%
}%
\def\XINT_expr_foundendofexpr {\xint_c_ \XINT_expr_endofexpr }%
\def\XINT_expr_op_found #1%
{%
    \ifcsname XINT_expr_precedence_\string #1\endcsname
        \expandafter\xint_afterfi\expandafter
        {\csname XINT_expr_precedence_\string #1\expandafter\endcsname
         \csname XINT_expr_op_\string #1\endcsname }%
    \else
        \XINT_expr_unexpectedtoken
        \expandafter\XINT_expr_getop
    \fi
}%
\expandafter\let\csname XINT_expr_precedence_)\endcsname \xint_c_i
\expandafter\let\csname XINT_expr_op_)\endcsname\XINT_expr_getop
\def\xint_tmp_def
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_expr_precedence_!\expandafter\endcsname
    \csname XINT_expr_op_!\endcsname
}%
\def\xint_tmp_do_defs #1#2%
{%
```

```
8814     \def #1##1##2%
8815     {\ifx ##1#2%
8816          \expandafter\xint_firstoftwo
8817     \else\expandafter\xint_secondoftwo
8818     \fi{\expandafter\XINT_expr_getop}{\expandafter\XINT_flexpr_getop}%
8819     \csname .\xintFac{\XINT_expr_string ##2}/1[0]\endcsname }%
8820     \let#2\empty
8821 }%
8822 \xint_tmp_def
```

27.10 Get next opening parenthesis or minus prefix or decimal number or braced fraction or sub-xintexpression

June 14: 1.08b adds a second \romannumeral-‘0 to \XINT_expr_getnext in an attempt to solve a problem with space tokens stopping the \romannumeral and thus preventing expansion of the following token. For example: 1+ \the\cnta caused a problem, as ‘\the’ was not expanded. I did not define \XINT_expr_getnext as a macro with parameter (which would have cured preventively this), precisely to try to recognize brace pairs. The second \romannumeral-‘0 is added here for the same reason in other places: \XINT_expr_scannum_intpart_b, \XINT_expr_scannum_transition, \XINT_expr_scannum_decpart_b, and \XINT_expr_getop.

```
8823 \def\XINT_expr_getnext
8824 {%
8825     \expandafter\XINT_expr_getnext_checkforbraced_a
8826     \romannumeral-‘0\romannumeral-‘0%
8827 }%
8828 \def\XINT_expr_getnext_checkforbraced_a #1%
8829 {%
8830     \XINT_expr_getnext_checkforbraced_b #1\W\Z {#1}%
8831 }%
8832 \def\XINT_expr_getnext_checkforbraced_b #1#2%
8833 {%
8834     \xint_UDwfork
8835        #1\dummy \XINT_expr_getnext_emptybracepair
8836        #2\dummy \XINT_expr_getnext_onetoken_perhaps
8837        \W\dummy \XINT_expr_getnext_gotbracedstuff
8838     \krof
8839 }%
8840 \def\XINT_expr_getnext_onetoken_perhaps\Z #1%
8841 {%
8842     \expandafter\XINT_expr_getnext_checkforbraced_c\expandafter
8843     {\romannumeral-‘0#1}%
8844 }%
8845 \def\XINT_expr_getnext_checkforbraced_c #1%
8846 {%
8847     \XINT_expr_getnext_checkforbraced_d #1\W\Z {#1}%
8848 }%
8849 \def\XINT_expr_getnext_checkforbraced_d #1#2%
```

```
{%
    \xint_UDwfork
       #1\dummy \XINT_expr_getnext_emptybracepair
       #2\dummy \XINT_expr_getnext_onetoken_wehope
       \W\dummy \XINT_expr_getnext_gotbracedstuff
    \krof
}%
\def\XINT_expr_getnext_emptybracepair #1{\XINT_expr_getnext }%
\def\XINT_expr_getnext_gotbracedstuff #1\W\Z #2%
{%
    \expandafter\XINT_expr_getop\csname .#2\endcsname
}%
\def\XINT_expr_getnext_onetoken_wehope\Z #1%
{%
    \xint_gob_til_! #1\XINT_expr_subexpr !%
    \expandafter\XINT_expr_getnext_onetoken_fork\string #1%
}%
\def\XINT_expr_subexpr !#1!{\expandafter\XINT_expr_getop\xint_gobble_i }%
\begingroup
\lccode`*=`_
\lowercase{\endgroup
\def\XINT_expr_sixwayfork #1(-.+*\dummy #2#3\krof {#2}%
\def\XINT_expr_getnext_onetoken_fork #1%
{%
    \XINT_expr_sixwayfork
        #1-.+*\dummy   \XINT_expr_oparen
        (#1.+*\dummy   -%
        (-#1+*\dummy  {\XINT_expr_scannum_start\XINT_expr_scannum_decpart_b.}%
        (-.#1*\dummy   \XINT_expr_getnext%
         (-.+#1\dummy {\XINT_expr_scannum_start\XINT_expr_scannum_decpart_b*}%
         (-.+*\dummy  {\XINT_expr_scannum_check #1}%
    \krof
}}%
\def\XINT_expr_scannum_check #1%
{%
    \ifnum \xint_c_ix<1#1
        \expandafter\XINT_expr_scannum_start
    \else
        \xint_afterfi{\XINT_expr_unexpectedtoken
                      \expandafter\XINT_expr_getnext\xint_gobble_ii}%
    \fi \XINT_expr_scannum_intpart_b #1%
}%
\def\XINT_expr_scannum_stopscan {!}% ! catcode 11
\def\XINT_expr_gathernum #1!%        ! with catcode 11
{%
    \expandafter\space\csname .#1\endcsname
}%
\def\XINT_expr_scannum_start #1%
{%
```

```
8899     \expandafter\XINT_expr_getop
8900     \romannumeral-`0\expandafter\XINT_expr_gathernum
8901     \romannumeral-`0#1%
8902 }%
8903 \def\XINT_expr_scannum_intpart_a #1%
8904 {%
8905     \ifnum \xint_c_ix<1\string#1
8906        \expandafter\expandafter\expandafter
8907           \XINT_expr_scannum_intpart_b
8908        \expandafter\string
8909     \else
8910        \if #1.%
8911            \expandafter\expandafter\expandafter
8912            \XINT_expr_scannum_transition
8913        \else
8914            \expandafter\expandafter\expandafter
8915            \XINT_expr_scannum_stopscan
8916        \fi
8917     \fi
8918     #1%
8919 }%
8920 \def\XINT_expr_scannum_intpart_b #1%
8921 {%
8922     \expandafter #1\romannumeral-`0\expandafter
8923     \XINT_expr_scannum_intpart_a\romannumeral-`0\romannumeral-`0%
8924 }%
8925 \def\XINT_expr_scannum_transition #1%
8926 {%
8927     \expandafter.\romannumeral-`0\expandafter
8928     \XINT_expr_scannum_decpart_a\romannumeral-`0\romannumeral-`0%
8929 }%
8930 \def\XINT_expr_scannum_decpart_a #1%
8931 {%
8932     \ifnum \xint_c_ix<1\string#1
8933        \expandafter\expandafter\expandafter
8934        \XINT_expr_scannum_decpart_b\expandafter\string
8935     \else
8936        \expandafter \XINT_expr_scannum_stopscan
8937     \fi
8938     #1%
8939 }%
8940 \def\XINT_expr_scannum_decpart_b #1%
8941 {%
8942     \expandafter #1\romannumeral-`0\expandafter
8943     \XINT_expr_scannum_decpart_a\romannumeral-`0\romannumeral-`0%
8944 }%
```

27.11 \xintfloatexpr, \xintthefloatexpr

1.08b: various doublings of \romannumeral-‘0 to avoid some expansion/space token problems

```
\def\xintfloatexpr {\romannumeral0\xintfloateval }%
\def\xintfloateval
{%
    \expandafter\XINT_expr_until_end\romannumeral-‘0%
    \expandafter\XINT_flexpr_checkifprefix_ii\romannumeral-‘0%
    \XINT_flexpr_getnext
}%
\def\xintthefloatexpr {\romannumeral0\xintthefloateval }%
\def\xintthefloateval
    {\expandafter\XINT_flexpr_the\romannumeral0\xintfloateval }%
\def\XINT_flexpr_the #1#2#3{\xintfloat{\XINT_expr_string #3}}%
\def\XINT_flexpr_oparen
{%
    \expandafter\XINT_expr_until_cparen\romannumeral-‘0%
    \expandafter\XINT_flexpr_checkifprefix_ii\romannumeral-‘0%
    \XINT_flexpr_getnext
}%
\def\xint_tmp_def #1#2#3%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_flexpr_op_#1\expandafter\endcsname
    \csname XINT_flexpr_until_#1\expandafter\endcsname
    \csname XINT_flexpr_checkifprefix_#2\expandafter\endcsname
    \csname XINT_expr_precedence_#1\expandafter\endcsname
    \csname xint_c_#2\expandafter\endcsname
    \csname XINTinFloat#3\endcsname
}%
\def\xint_tmp_do_defs #1#2#3#4#5#6%
{%
    \def #1##1% \XINT_flexpr_op_?
    {%
        \expandafter #2\expandafter ##1\romannumeral-‘0\expandafter
        #3\romannumeral-‘0\XINT_flexpr_getnext
    }%
    \def #2##1##2##3##4% \XINT_flexpr_until_?
    {%
      \ifnum ##2>#5%
        \xint_afterfi {\expandafter #2\expandafter ##1\romannumeral-‘0##3##4}%
      \else
        \xint_afterfi
        {\expandafter ##2\expandafter ##3%
         \csname .#6{\XINT_expr_string ##1}%
                    {\XINT_expr_string ##4}\endcsname }%
      \fi
```

```
    }%
}%
\xint_tmp_def +{ii}{Add}%
\xint_tmp_def -{ii}{Sub}%
\xint_tmp_def *{iii}{Mul}%
\xint_tmp_def /{iii}{Div}%
\xint_tmp_def ^{iv}{Power}%
\xint_tmp_def  e{v}{fE}%
\xint_tmp_def  E{v}{fE}%
\def\xint_tmp_def #1%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_flexpr_checkifprefix_#1\expandafter\endcsname
    \csname XINT_flexpr_op_-#1\endcsname
}%
\def\xint_tmp_do_defs #1#2%
{%
    \def #1##1%
    {\xint_UDsignfork
        ##1\dummy #2%
          -\dummy ##1%
     \krof }%
}%
\xint_tmp_def {ii}%
\xint_tmp_def {iii}%
\xint_tmp_def {iv}%
\xint_tmp_def {v}%
\def\xint_tmp_def #1%
{%
    \expandafter\xint_tmp_do_defs
    \csname XINT_flexpr_op_-#1\expandafter\endcsname
    \csname XINT_expr_until_-#1\expandafter\endcsname
    \csname XINT_flexpr_checkifprefix_#1\expandafter\endcsname
    \csname xint_c_#1\endcsname
}%
\def\xint_tmp_do_defs #1#2#3#4%
{%
    \def #1% \XINT_flexpr_op_-ii,iii,iv,v
    {%
        \expandafter #2\romannumeral-‘0\expandafter
        #3\romannumeral-‘0\XINT_flexpr_getnext
    }%
}%
\xint_tmp_def {ii}%
\xint_tmp_def {iii}%
\xint_tmp_def {iv}%
\xint_tmp_def {v}%
\let\xint_tmp_def\empty
\let\xint_tmp_do_defs\empty
```

```
\def\XINT_flexpr_getop #1%
{%
    \expandafter\XINT_flexpr_getop_a\expandafter #1%
    \romannumeral-`0\romannumeral-`0%
}%
\def\XINT_flexpr_getop_a #1#2%
{%
    \ifcat #2\relax
        \ifx #2\relax
             \expandafter\expandafter\expandafter
             \XINT_expr_foundendofexpr
        \else
             \XINT_expr_unexpectedtoken
             \expandafter\expandafter\expandafter
             \XINT_flexpr_getop
        \fi
    \else
        \expandafter\XINT_flexpr_op_found\expandafter #2%
    \fi
    #1%
}%
\def\XINT_flexpr_op_found #1%
{%
    \ifcsname XINT_expr_precedence_\string #1\endcsname
        \expandafter\xint_afterfi\expandafter
        {\csname XINT_expr_precedence_\string #1\expandafter\endcsname
         \csname XINT_flexpr_op_\string #1\endcsname }%
    \else
        \XINT_expr_unexpectedtoken
        \expandafter\XINT_flexpr_getop
    \fi
}%
\expandafter\let\csname XINT_flexpr_op_)\endcsname\XINT_flexpr_getop
\def\XINT_flexpr_getnext
{%
    \expandafter\XINT_flexpr_getnext_checkforbraced_a
    \romannumeral-`0\romannumeral-`0%
}%
\def\XINT_flexpr_getnext_checkforbraced_a #1%
{%
    \XINT_flexpr_getnext_checkforbraced_b #1\W\Z {#1}%
}%
\def\XINT_flexpr_getnext_checkforbraced_b #1#2%
{%
    \xint_UDwfork
       #1\dummy \XINT_flexpr_getnext_emptybracepair
       #2\dummy \XINT_flexpr_getnext_onetoken_perhaps
       \W\dummy \XINT_flexpr_getnext_gotbracedstuff
    \krof
```

```
}%
\def\XINT_flexpr_getnext_onetoken_perhaps\Z #1%
{%
    \expandafter\XINT_flexpr_getnext_checkforbraced_c\expandafter
    {\romannumeral-`0#1}%
}%
\def\XINT_flexpr_getnext_checkforbraced_c #1%
{%
    \XINT_flexpr_getnext_checkforbraced_d #1\W\Z {#1}%
}%
\def\XINT_flexpr_getnext_checkforbraced_d #1#2%
{%
    \xint_UDwfork
       #1\dummy \XINT_flexpr_getnext_emptybracepair
       #2\dummy \XINT_flexpr_getnext_onetoken_wehope
       \W\dummy \XINT_flexpr_getnext_gotbracedstuff
    \krof
}%
\def\XINT_flexpr_getnext_emptybracepair #1{\XINT_flexpr_getnext }%
\def\XINT_flexpr_getnext_gotbracedstuff #1\W\Z #2%
{%
    \expandafter\XINT_flexpr_getop\csname .#2\endcsname
}%
\def\XINT_flexpr_getnext_onetoken_wehope\Z #1%
{%
    \xint_gob_til_! #1\XINT_flexpr_subexpr !%
    \expandafter\XINT_flexpr_getnext_onetoken_fork\string #1%
}%
\def\XINT_flexpr_subexpr !#1!{\expandafter\XINT_flexpr_getop\xint_gobble_i }%
\begingroup
\lccode`*=`_
\lowercase{\endgroup
\def\XINT_flexpr_getnext_onetoken_fork #1%
{%
    \XINT_expr_sixwayfork
      #1-.+*\dummy   \XINT_flexpr_oparen
      (#1.+*\dummy   -%
      (-#1+*\dummy  {\XINT_flexpr_scannum_start\XINT_expr_scannum_decpart_b.}%
      (-.#1*\dummy   \XINT_flexpr_getnext%
      (-.+#1\dummy  {\XINT_flexpr_scannum_start\XINT_expr_scannum_decpart_b*}%
      (-.+*\dummy   {\XINT_flexpr_scannum_check #1}%
    \krof
}}%
\def\XINT_flexpr_scannum_check #1%
{%
    \ifnum \xint_c_ix<1#1
        \expandafter\XINT_flexpr_scannum_start
    \else
        \xint_afterfi
```

```
9136        {\XINT_expr_unexpectedtoken
9137         \expandafter\XINT_flexpr_getnext\xint_gobble_ii}%
9138     \fi \XINT_expr_scannum_intpart_b #1%
9139 }%
9140 \def\XINT_flexpr_scannum_start #1%
9141 {%
9142     \expandafter\XINT_flexpr_getop
9143     \romannumeral-`0\expandafter\XINT_expr_gathernum
9144     \romannumeral-`0#1%
9145 }%
```

27.12 \xintNewExpr

```
9146 \catcode`* 13
9147 \def\xintNewExpr #1[#2]#3%
9148 {%
9149     \begingroup
9150     \ifcase #2\relax
9151         \toks0 {\xdef #1}%
9152     \or \toks0 {\xdef #1##1}%
9153     \or \toks0 {\xdef #1##1##2}%
9154     \or \toks0 {\xdef #1##1##2##3}%
9155     \or \toks0 {\xdef #1##1##2##3##4}%
9156     \or \toks0 {\xdef #1##1##2##3##4##5}%
9157     \or \toks0 {\xdef #1##1##2##3##4##5##6}%
9158     \or \toks0 {\xdef #1##1##2##3##4##5##6##7}%
9159     \or \toks0 {\xdef #1##1##2##3##4##5##6##7##8}%
9160     \or \toks0 {\xdef #1##1##2##3##4##5##6##7##8##9}%
9161     \else
9162        \immediate\write-1{Package xintexpr Error! illegal number of macro
9163          parameters.}%
9164     \fi
9165         \def\xintAdd  {:xintAdd}%
9166         \def\xintSub  {:xintSub}%
9167         \def\xintMul  {:xintMul}%
9168         \def\xintDiv  {:xintDiv}%
9169         \def\xintPow  {:xintPow}%
9170         \def\xintFac  {:xintFac}%
9171         \def\xintOpp  {:xintOpp}%
9172         \def\xintfE   {:xintfE}%
9173         \def\xintraw  { :romannumeral0:xintraw}%
9174         \def\XINT_expr_the ##1##2##3%
9175            {\expandafter\xintraw
9176             \expandafter{\romannumeral-`0\XINT_expr_string ##3}}%
9177     \lccode`\*=`: \lowercase {\def*}{!noexpand!}%
9178     \catcode`: 13
9179     \endlinechar -1
9180     \everyeof {\noexpand }%
9181     \edef\xintNewExprtmp
```

```
        {\scantokens
         \expandafter{\romannumeral0\xinttheeval #3\relax}}%
    \lccode`\*=`_ \lowercase {\def*}{####}%
    \catcode`_ 13  \catcode`! 0 \catcode`: 11
    \the\toks0 {\scantokens\expandafter{\xintNewExprtmp }}%
\endgroup
}%
```

27.13 \xintNewFloatExpr

```
\def\xintNewFloatExpr #1[#2]#3%
{%
    \begingroup
    \ifcase #2\relax
        \toks0 {\xdef #1}%
    \or \toks0 {\xdef #1##1}%
    \or \toks0 {\xdef #1##1##2}%
    \or \toks0 {\xdef #1##1##2##3}%
    \or \toks0 {\xdef #1##1##2##3##4}%
    \or \toks0 {\xdef #1##1##2##3##4##5}%
    \or \toks0 {\xdef #1##1##2##3##4##5##6}%
    \or \toks0 {\xdef #1##1##2##3##4##5##6##7}%
    \or \toks0 {\xdef #1##1##2##3##4##5##6##7##8}%
    \or \toks0 {\xdef #1##1##2##3##4##5##6##7##8##9}%
    \else
       \immediate\write-1{Package xintexpr Error! illegal number of macro
        parameters.}%
    \fi
        \def\XINTinFloatAdd   {:XINTinFloatAdd}%
        \def\XINTinFloatSub   {:XINTinFloatSub}%
        \def\XINTinFloatMul   {:XINTinFloatMul}%
        \def\XINTinFloatDiv   {:XINTinFloatDiv}%
        \def\XINTinFloatPower {:XINTinFloatPower}%
        \def\xintFac     {:xintFac}%
        \def\xintOpp     {:xintOpp}%
        \def\XINTinFloatfE    {:XINTinFloatfE}%
        \def\xintfloat  { :romannumeral0:xintfloat}%
        \def\XINT_flexpr_the ##1##2##3%
           {\expandafter\xintfloat
            \expandafter{\romannumeral-`0\XINT_expr_string ##3}}%
    \lccode`\*=`: \lowercase {\def*}{!noexpand!}%
    \catcode`: 13
    \endlinechar -1
    \everyeof {\noexpand }%
    \edef\xintNewExprtmp
        {\scantokens
         \expandafter{\romannumeral0\xintthefloateval #3\relax}}%
    \lccode`\*=`_ \lowercase {\def*}{####}%
    \catcode`_ 13  \catcode`! 0 \catcode`: 11
    \the\toks0 {\scantokens\expandafter{\xintNewExprtmp }}%
```

```
\endgroup
}%
\XINT_expr_restorecatcodes_endinput%
```