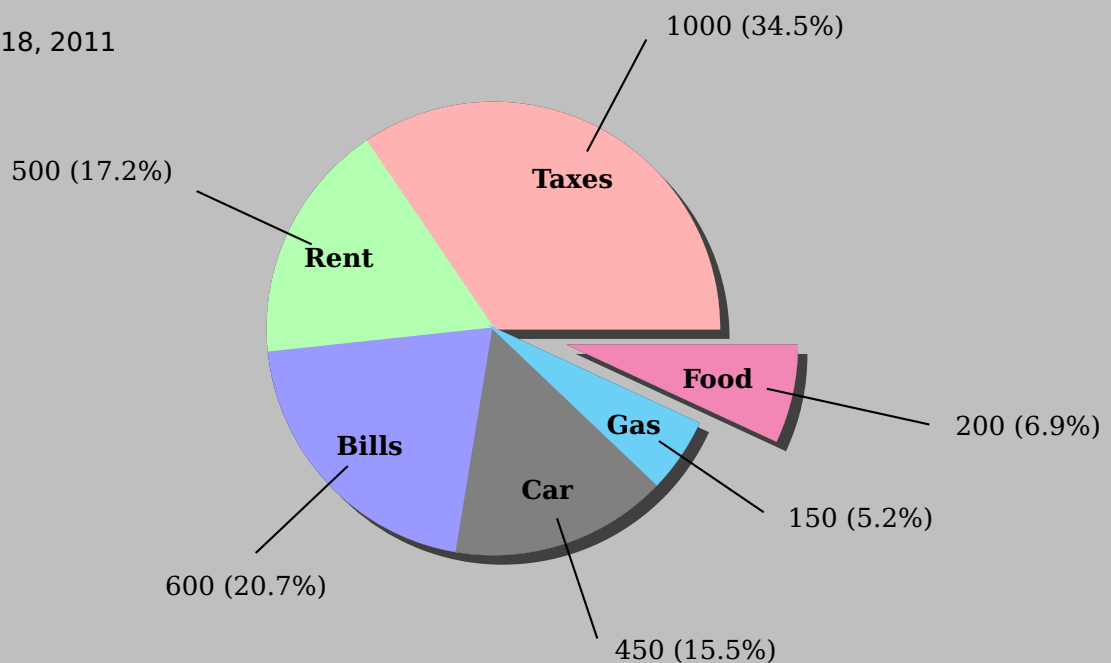


PSTricks

pstricks-add additional Macros for pstricks v.3.49

January 18, 2011



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This version of `pstricks-add` needs `pstricks.tex` version `>1.04` from June 2004, otherwise the additional macros may not work as expected. The ellipsis material and the option `asolid` (renamed to `eofill`) are now part of the new `pstricks.tex` package, available on CTAN. `pstricks-add` will forever be an experimental and dynamical package, try it at your own risk.

- It is important to load `pstricks-add` as the **last** PSTricks related package, otherwise a lot of the macros won't work in the expected way.
- `pstricks-add` uses the extended version of the `keyval` package. So be sure that you have installed `pst-xkey` which is part of the `xkeyval`-package, and that all packages that use the old `keyval` interface are loaded **before** the `xkeyval`.[\[1\]](#)
- the option `tickstyle` from `pst-plot` is no longer supported; use `ticksize` instead.
- the option `xyLabel` is no longer supported; use the option `labelFontSize` instead.
- if `pstricks-add` is loaded together with the package `pst-func` then `InsideArrow` of the `\psbezier` macro doesn't work!

Thanks to: Hendri Adriaens; Stefano Baroni; Martin Chicoine; Gerry Coombes; Ulrich Dirr; Christophe Fourey; Hubert Gäßlein; Jürgen Gilg; Denis Girou; Pablo Gonzáles; Peter Hutnick; Christophe Jorssen; Uwe Kern; Manuel Luque; Jens-Uwe Morawski; Tobias Nähring; Rolf Niepraschk; Alan Ristow; Christine Römer; Arnaud Schmittbuhl; John Smith; Timothy Van Zandt

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1. \psGetSlope and \psGetDistance

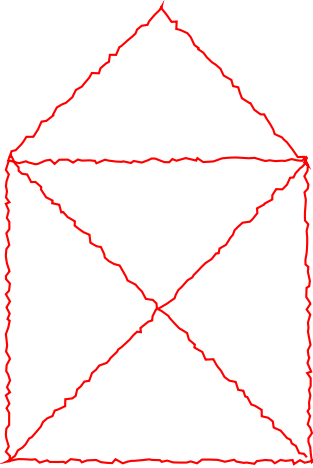
$\backslash\text{psGetSlope}(x_1, y_1)(x_2, y_2)\backslash\langle\text{macro}\rangle$ $\backslash\text{psGetDistance}(x_1, y_1)(x_2, y_2)\backslash\langle\text{macro}\rangle$

0.0 0.85759
 2.0 0.55055
 -0.2 1.10112
 0.00615

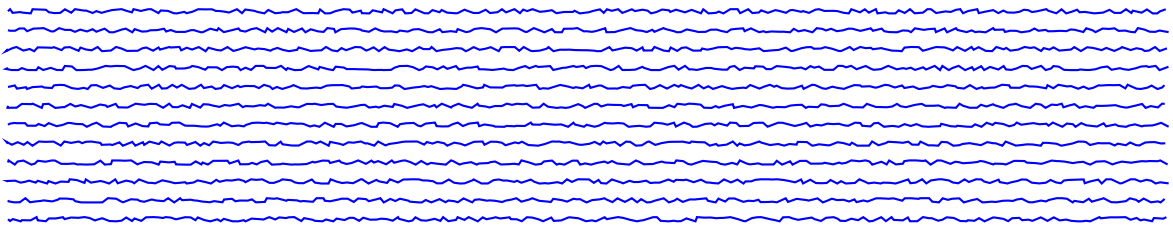
$\backslash\text{psGetSlope}(-2,1)(3,1)\backslash\text{SlopeVal} \backslash\text{SlopeVal} \backslash\text{quad}$ $\backslash\text{psGetDistance}(-2,1)(3,1)\backslash\text{DVal} \backslash\text{DVal}\backslash\backslash$ $\backslash\text{psGetSlope}(-2,1)(-3,-1)\backslash\text{SlopeVal} \backslash\text{SlopeVal}\backslash\text{quad}$ $\backslash\text{psGetDistance}(-2,1)(-3,-1)\backslash\text{DVal} \backslash\text{DVal}\backslash\backslash$ $\backslash\text{psGetSlope}(-2,0)(3,-1)\backslash\text{SlopeVal} \backslash\text{SlopeVal}\backslash\text{quad}$ $\backslash\text{psGetDistance}(-2,0)(3,-1)\backslash\text{DVal} \backslash\text{DVal}\backslash\backslash$ $\backslash\text{psGetSlope}(-2111,-12)(3,1)\backslash\text{SlopeVal} \backslash\text{SlopeVal}\backslash\text{quad}$ $\% \backslash\text{psGetDistance}(-2111,-12)(3,1)\backslash\text{DVal} ==> \text{Overflow!}$

2. "Handmade" lines :-)

```
\pslineByHand [Options] (x1,y1)(x2,y2)(x3,y3) ...
```

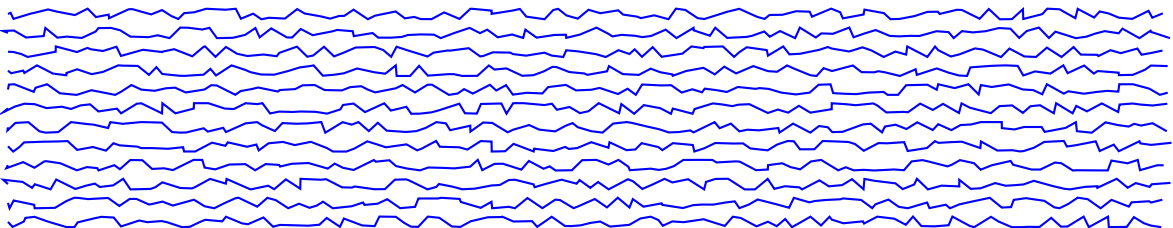


```
\begin{pspicture}(4,6)
\psset{unit=2cm}
\pslineByHand[linecolor=red](0,0)(0,2)(2,2)
(2,0)(0,0)(2,2)(1,3)(0,2)(2,0)
\end{pspicture}
```



```
\begin{pspicture}(\linewidth,3)
\multido{\rA=0.00+0.25}{12}{\pslineByHand[linecolor=blue](0,\rA)(\linewidth,\rA)}
}
\end{pspicture}
```

The amplitude and the width can be changed by the optional arguments `varsteptol` and `VarStepEpsilon`. Both are preset to `VarStepEpsilon=2`, `varsteptol=0.8`.

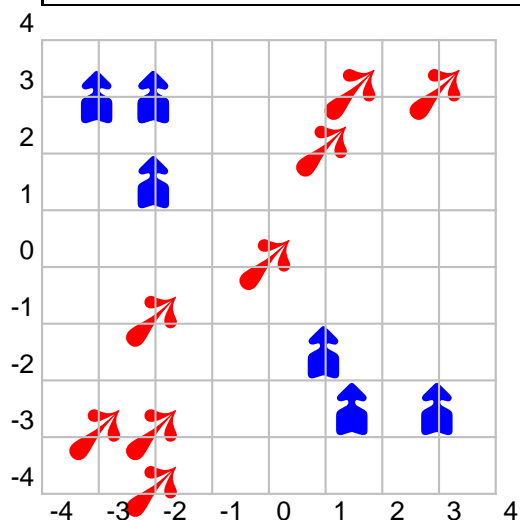


```
\begin{pspicture}(\linewidth,3)
\multido{\rA=0.00+0.25}{12}{%
\pslineByHand[linecolor=blue,VarStepEpsilon=4,varsteptol=2](0,\rA)(\linewidth,\rA)}
}
\end{pspicture}
```

3. \rmultiput: a multiple \rput

PSTricks already has a `\multirput`, which puts a box n times with a difference of dx and dy relative to each other. It is not possible to put it with a different distance from one point to the next. This is possible with `\rmultiput`:

`\rmultiput` * [Options] {any material}(x_1, y_1)(x_2, y_2)... (x_n, y_n)

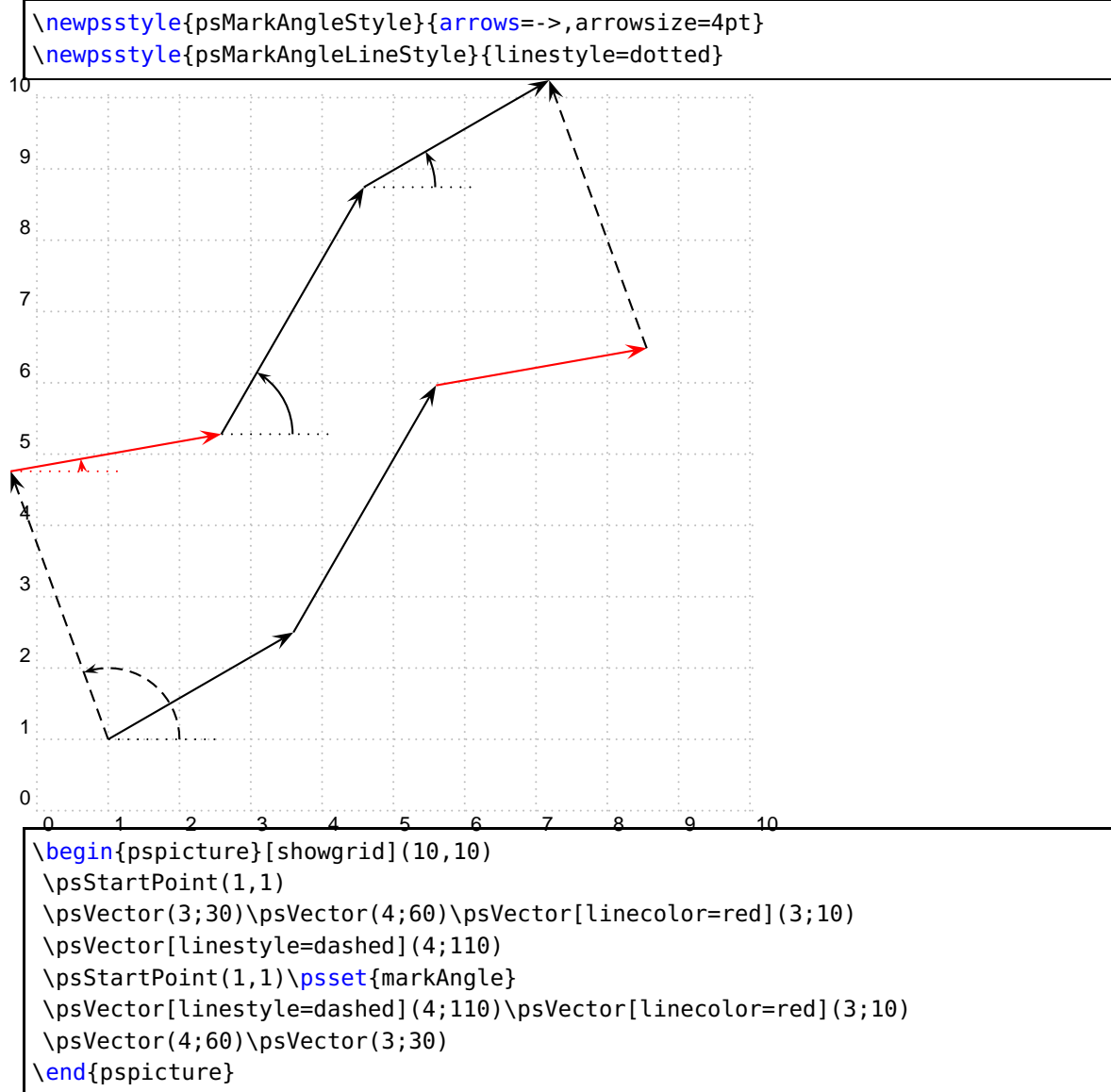


```
\psset{unit=0.75}
\begin{pspicture}(-4,-4)(4,4)
\rmultiput[rot=45]{\red\psscalebox{3}{\ding
{250}}}%
(-2,-4)(-2,-3)(-3,-3)(-2,-1)(0,0)(1,2)
(1.5,3)(3,3)
\rmultiput[rot=90,ref=lc]{\blue\psscalebox
{2}{\ding{253}}}%
(-2,2.5)(-2,2.5)(-3,2.5)(-2,1)(1,-2)
(1.5,-3)(3,-3)
\psgrid[subgriddiv=0,gridcolor=lightgray]
\end{pspicture}
```

4. \psVector: Drawing relative vector lines

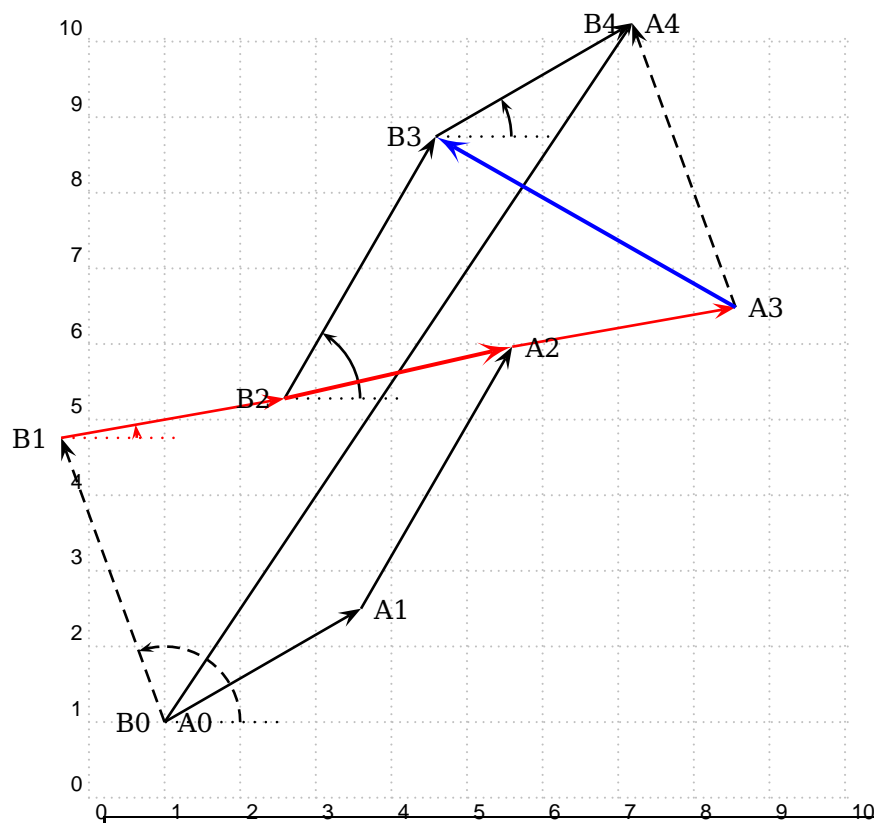
The new macros `\psStartPoint` and `\psVector` allow to draw a series of vectors which start point refers to the endpoint of the last drawn vector. The coordinates of the end-point are *always* interpreted relative to the last the vector. The first vector refers to the coordinates set by `\psStartPoint`. With the boolean argument one can draw the horizontal angle of the vector.

The style of the angle arc is saved in `psMarkAngleStyle` and the style for the horizontal line in `psMarkAngleLineStyle` and preset to



All end points of the vectors are saved in node names with the preset name `Vector#`, where `#` is the consecutive number of the nodes. `Vector0` ist the starting point of the first `\psVector`. With the macro `\psStartPoint` one can set the starting point and with optional argument the name of the nodes. `Vector3` is the default node name of the endpoint of the third vector or the name of the starting point of the forth vector.

`\psStartPoint [node basename] (x,y)`



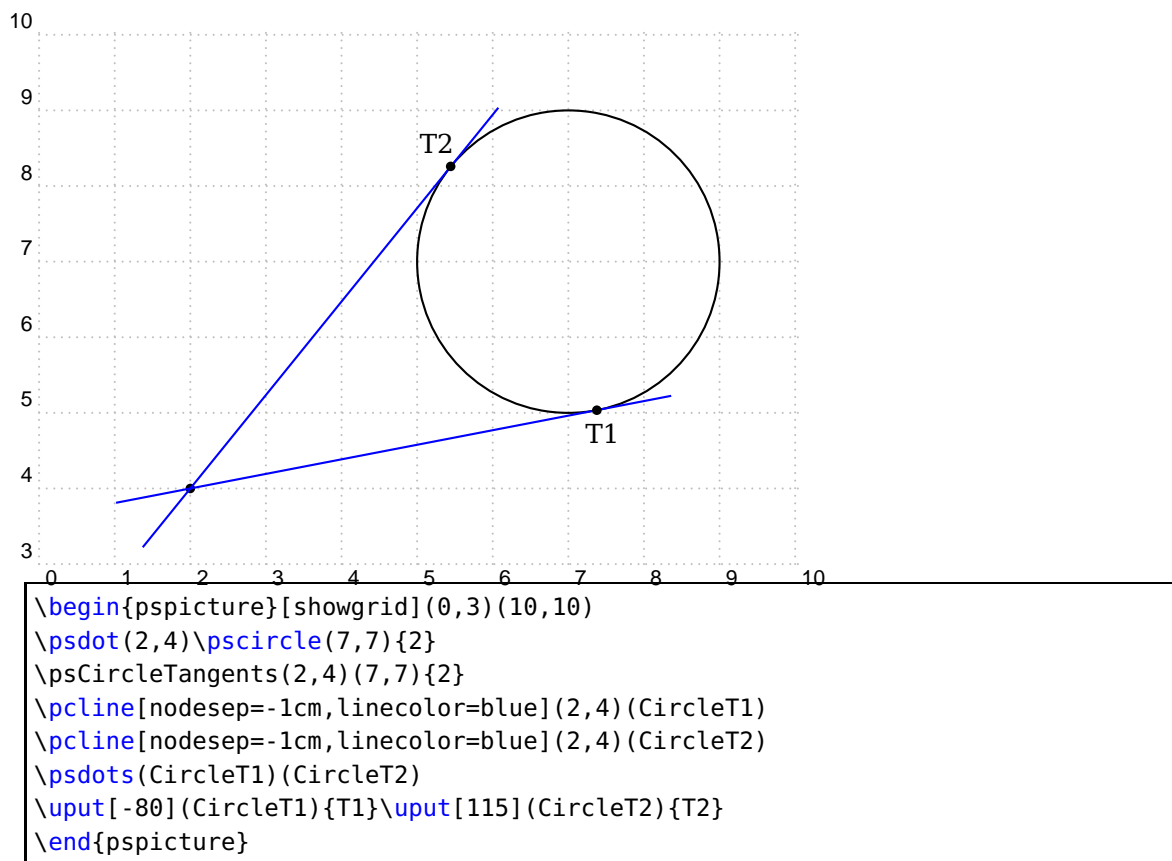
```
\begin{pspicture}[showgrid,linewidth=1pt](10,10.4)
\psStartPoint[A](1,1)% nodes have the base name A
\psVector(3;30)\psVector(4;60)\psVector[linecolor=red](3;10)
\psVector[linestyle=dashed](4;110)
\psline{->}(A0)(A4)
\psStartPoint[B](1,1)\psset{markAngle}% nodes have the base name B
\psVector[linestyle=dashed](4;110)
\psVector[linecolor=red](3;10)
\psVector(4;60)\psVector(3;30)
\psline[arrows=-D>,arrowscale=2,linewidth=1.5pt,linecolor=red](B2)(A2)
\psline[arrows=-D>,arrowscale=2,linewidth=1.5pt,linecolor=blue](A3)(B3)
\multido{\iA=0+1}{5}{\uput[0](A\iA){A\iA}\uput[180](B\iA){B\iA}}
\end{pspicture}
```

5. \psCircleTangents: Calculating tangent lines of circles

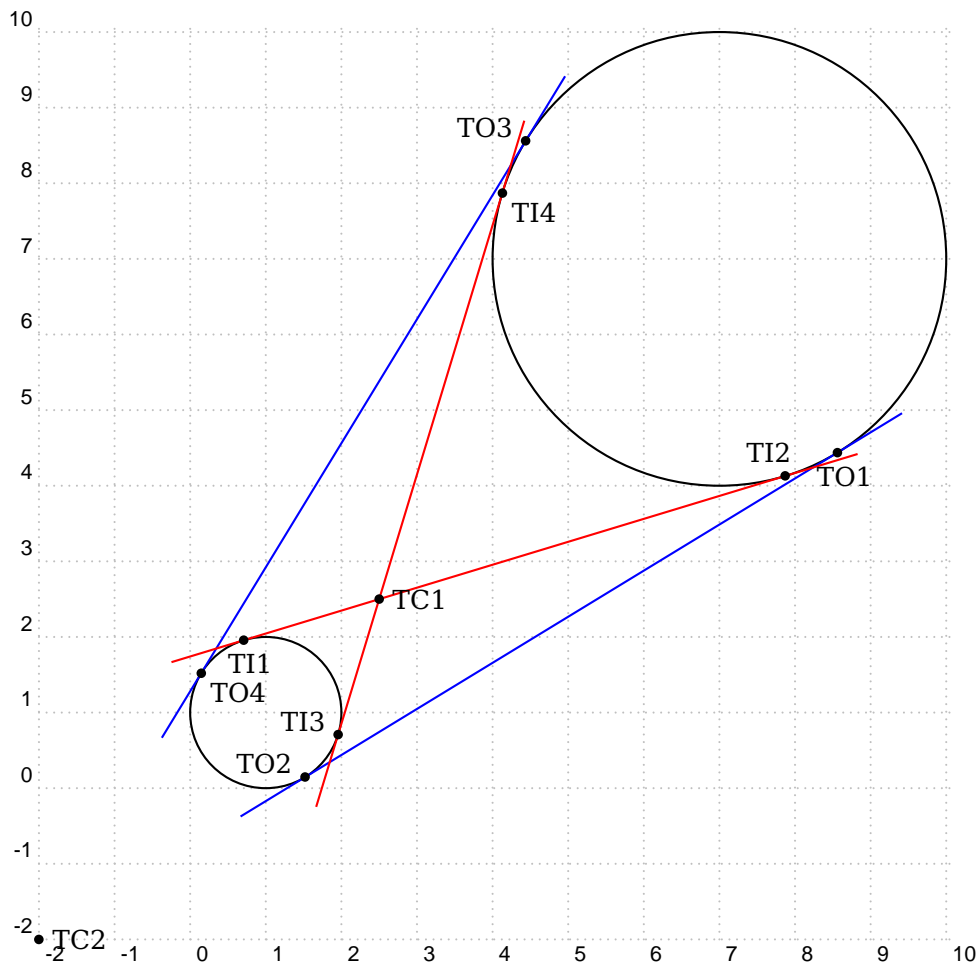
The macro calculates the points on a circle where tangent lines from another point or another circle are drawn.

```
\psCircleTangents( $x_1, y_1$ ) ( $x_2, y_2$ ) {Radius}
\psCircleTangents( $x_1, y_1$ ) {Radius} ( $x_2, y_2$ ) {Radius}
```

In the first case the coordinates of a point and the center and the radius of a circle must be given. The names of the calculates node names are CircleT1 and CircleT2.



When using the other variant of the macro two circles must be given. The macro then defines ten nodes, named CircleTC1 and CircleTC2 for the two intersection points, CircleT01, CircleT02, CircleT03, and CircleT04 for the four nodes of the outer tangent lines and CircleTI1, CircleTI2, CircleTI3, and CircleTI4 for the four nodes of the inner tangent lines.



```

\begin{pspicture}[showgrid](-2,-2)(10,10)
\pscircle(1,1){1}\pscircle(7,7){3}
\psCircleTangents(1,1){1}(7,7){3}
\pcline[nodesep=-1cm,linecolor=blue](CircleT01)(CircleT02)
\pcline[nodesep=-1cm,linecolor=blue](CircleT03)(CircleT04)
\pcline[nodesep=-1cm,linecolor=red](CircleTI1)(CircleTI2)
\pcline[nodesep=-1cm,linecolor=red](CircleTI3)(CircleTI4)
\psdots(CircleTC1)\psdots(CircleTC2)%
(CircleT01)(CircleT02)(CircleT03)(CircleT04)%
(CircleTI1)(CircleTI2)(CircleTI3)(CircleTI4)%
\uput[0](CircleTC1){TC1}\uput[0](CircleTC2){TC2}
\uput[-80](CircleTI1){TI1}\uput[115](CircleTI2){TI2}
\uput[150](CircleTI3){TI3}\uput[-45](CircleTI4){TI4}
\uput[-80](CircleT01){T01}\uput[150](CircleT02){T02}
\uput[150](CircleT03){T03}\uput[-45](CircleT04){T04}
\end{pspicture}

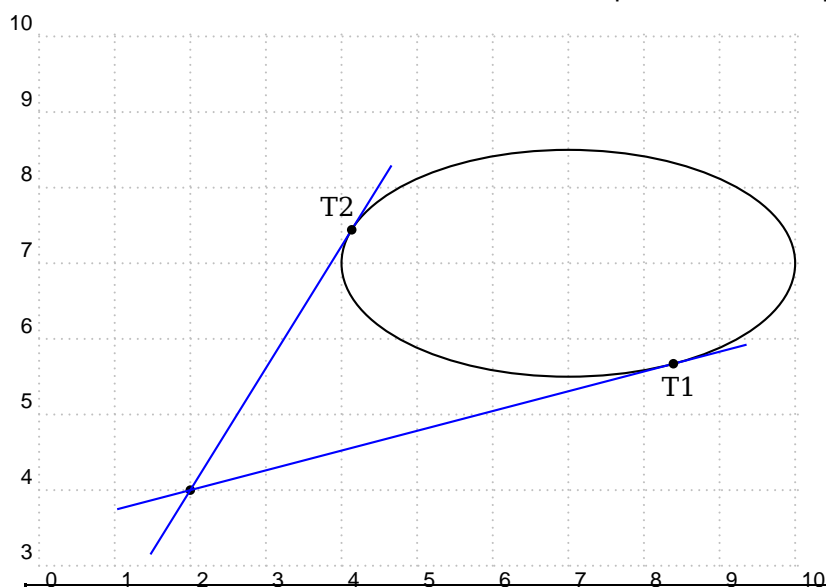
```

6. \psEllipseTangents: Calculating tangent lines of an ellipse

The macro calculates the two points on an ellipse where tangent lines from an outside point are drawn.

$\text{\psEllipseTangents}(x_0, y_0)(a, b)(x_p, y_p)$

The first two pairs of coordinates are the same as the ones for the default ellipse. The names of the calculates node names are EllipseT1 and EllipseT2.



```

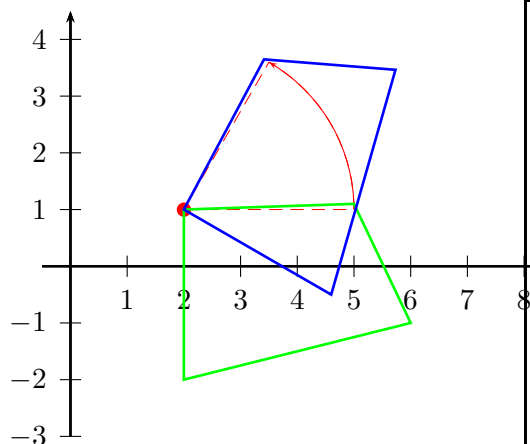
\begin{pspicture}[showgrid](0,3)(10,10)
\psdot(2,4)\psellipse(7,7)(3,1.5)
\psEllipseTangents(7,7)(3,1.5)(2,4)
\pcline[nodesep=-1cm,linecolor=blue](2,4)(EllipseT1)
\pcline[nodesep=-1cm,linecolor=blue](2,4)(EllipseT2)
\psdots(EllipseT1)(EllipseT2)
\uput[-80](EllipseT1){T1}\uput[115](EllipseT2){T2}
\end{pspicture}

```

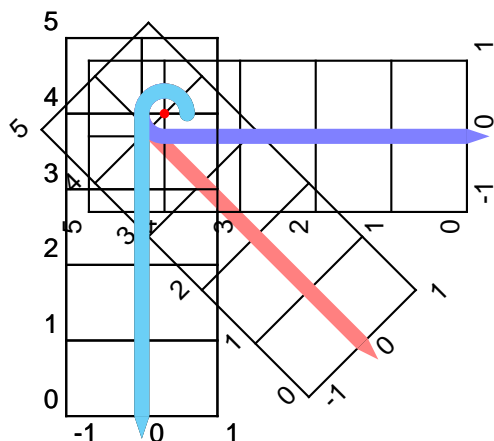
7. \psrotate: Rotating objects

\rput also has an optional argument for rotating objects, but it always depends on the \rput coordinates. With \psrotate the rotating center can be placed anywhere. The rotation is done with \pscustom, all optional arguments are only valid if they are part of the \pscustom macro.

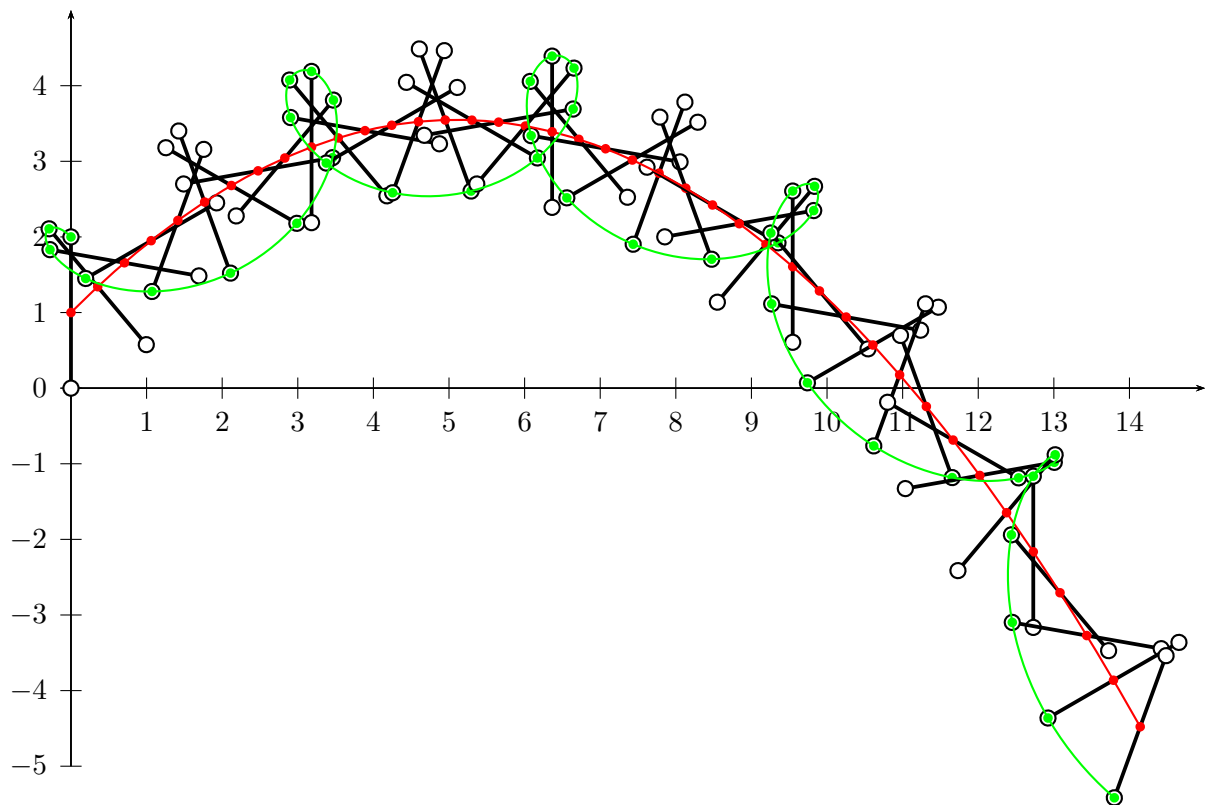
`\psrotate [Options] (x,y){rot angle}{object}`



```
\psset{unit=0.75}
\begin{pspicture}(-0.5,-3.5)(8.5,4.5)
  \psaxes{->}(0,0)(-0.5,-3)(8.5,4.5)
  \psdots[linecolor=red,dotscale=1.5](2,1)
  \psarc[linecolor=red,linewidth=0.4pt,
    showpoints=true]
    {->}(2,1){3}{0}{60}
  \pspolygon[linecolor=green,linewidth=1pt]
    (2,1)(5,1.1)(6,-1)(2,-2)
  \psrotate(2,1){60}{%
    \pspolygon[linecolor=blue,linewidth=1pt]
      (2,1)(5,1.1)(6,-1)(2,-2)}
\end{pspicture}
```



```
\begin{pspicture}(-1,-1)(3,6)
\def\canne{% Idea by Manuel Luque
  \psgrid[subgriddiv=0](-1,0)(1,5)
  \pscustom[linewidth=2mm]{\psline(0,4)\psarcn
    (0.3,4){0.3}{180}{360}}%
  \pscircle*(0.6,4){0.1}\pstriangle*(0,0)
    (0.2,-0.3)}
\def\Object{}
  \canne
  \psrotate(0.3,4){45}{\psset{linecolor=red
    !50}\canne}
  \psrotate(0.3,4){90}{\psset{linecolor=blue
    !50}\canne}
  \psrotate(0.3,4){360}{\psset{linecolor=cyan
    !50}\canne}
  \psdot[linecolor=red](0.3,4)
\end{pspicture}
```



```

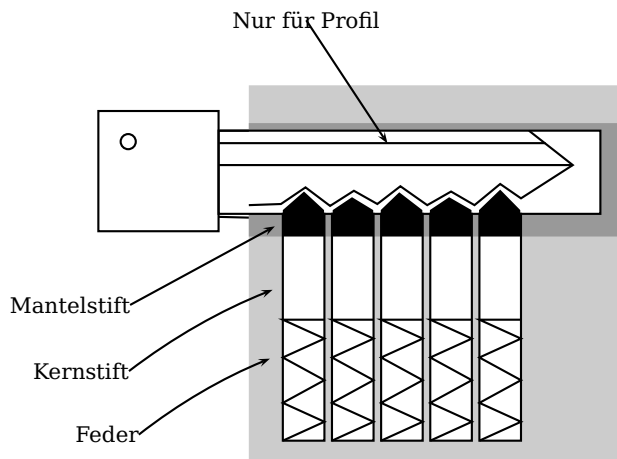
\begin{pspicture}(0,-6)(15,5)
\def\majorette{\psline[linewidth=0.5mm](0,2)% Idea by Manuel Luque
\pscircle[fillstyle=solid]{0.1}
\pscircle[fillstyle=solid](0,2){0.1}}
\psaxes[linewidth=0.5pt]{->}(0,0)(0,-5)(15,5)
\pstVerb{/V0 10 def /Alpha 45 def}% vitesse initiale, angle de lancement
\multido{\nT=0.0+0.05,\iA=0+40}{41}{%
\pstVerb{/nT \nT\space def}%
\rput(!V0 Alpha cos mul nT mul -9.81 2 div nT dup mul mul V0 Alpha sin mul nT
mul add){%
\psrotate(0,1){\iA}{\majorette\psdot[linecolor=red](0,1)\psdot[linecolor=
green](0,2)}}}
\parametricplot[linecolor=red]{0}{2}{% trajectoire du milieu
V0 Alpha cos mul t mul -9.81 2 div t dup mul mul V0 Alpha sin mul t mul add 1
add}
\parametricplot[linecolor=green,plotpoints=360]{0}{2}{% d'une extremite
V0 Alpha cos mul t mul 800 t mul sin sub % x(t)
-9.81 2 div t dup mul mul V0 Alpha sin mul t mul add 1 add 800 t mul cos add
}%y(t)
\end{pspicture}

```

8. \psComment: comments to a graphic

<code>\psComment</code> * <code>[Options]</code> <code>{arrows}</code> $(x_0, y_0)(x_1, y_1)$ <code>{Text}</code> <code>[line macro]</code> <code>[put macro]</code>
--

By default the macro uses the `\ncline` macro to draw a line from the first to the second point, it can be changed with the first additional optional argument. The label is put by default with `\rput`, which can be changed with the last optional argument. If this is used, then the line macro has also be defined, eg `\psComment(A)(B){text}[\ncarc][\ncput]`. At least, leave the argument empty.



```

\SpecialCoor\newpsstyle{weiss}{fillstyle=solid,fillcolor=white}
\footnotesize\psset{unit=0.5cm,dimen=middle}
\begin{pspicture}(-12,-4)(6,10)
\psframe*[linecolor=black!20](-5,-3)(5,7) \psframe*[linecolor=black!40](-5,3)(5,6)
\pscircle(-8.19,5.51){0.2}
\psframe[fillcolor=white,fillstyle=solid](-5.8,3.6)(4.3,5.8)
\psframe(-8.98,3.14)(-5.8,6.32)
\multido{\rA=-4.1+1.3}{5}{\rput(\rA,-2.4){\psframe[style=weiss](1.1,6)
\psline(0,0)(1.1,0.5)(0,1)(1.1,1.6)(0,2.2)(1.1,2.7)(0,3.2)(1.1,3.2)}}
\pspolygon*(-4.1,3.7)(-4.1,3)(-3,3)(-3.01,3.7)(-3.54,4.19)
\pspolygon*(1.09,3.7)(1.1,3)(2.2,3)(2.18,3.7)(1.65,4.24)
\pspolygon*(-2.78,3.7)(-2.8,3)(-1.7,3)(-1.71,3.7)(-2.27,4.04)
\pspolygon*(-1.51,3.7)(-1.5,3)(-0.4,3)(-0.41,3.7)(-1.02,4.17)
\pspolygon*(-0.21,3.7)(-0.2,3)(0.9,3)(0.89,3.7)(0.3,4.04)
\psline(-5,3.83)(-4.15,3.86)(-3.5,4.3)(-2.85,3.81)(-2.22,4.21)(-1.6,3.86)(-0.99,4.33)
(-0.28,3.83)(0.35,4.19)(0.97,3.83)(1.65,4.39)(2.2,4.01)(3.57,4.89)(2.41,5.8)
\psline(-5,5.8)(-5.78,5.8) \psline(-5.78,5.47)(2.85,5.47)
\psline(-5.8,3.52)(-5,3.5) \psline(3.57,4.89)(-5.8,4.89)
\psComment*[ref=r]{->}(-8.14,1.19)(-4.31,3.27){Mantelstift}
\psComment*[ref=r]{->}(-8.17,-0.56)(-4.37,1.59){Kernstift}[\ncarc]
\psComment*[ref=r]{->}(-7.91,-2.24)(-4.44,-0.23){Feder}[\ncarc]
\psComment[npos=-0.1]{->}(-3.48,8.72)(-1.33,5.46){Nur für Profil}
\end{pspicture}

```

9. \psChart: a pie chart

<code>\psChart</code>	<code>[Options]</code>	<code>{comma separated value list}</code>	<code>{comma separated value list}</code>	<code>{radius}</code>
-----------------------	------------------------	---	---	-----------------------

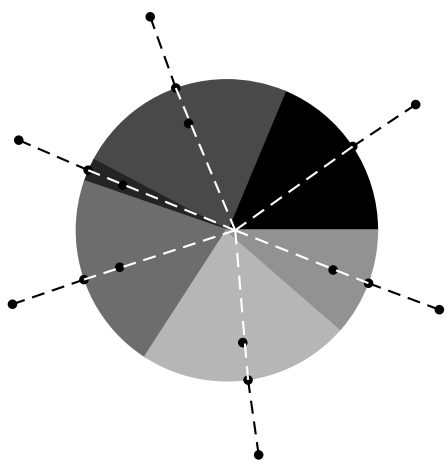
The special optional arguments for the `\psChart` macro are as follows:

<i>name</i>	<i>description</i>	<i>default</i>
<code>chartSep</code>	distance from the pie chart center to an outraged pie piece	10pt
<code>chartColor</code>	gray or colored pie (values are: gray or color)	gray
<code>userColor</code>	a comma separated list of user defined colors for the pie	{}

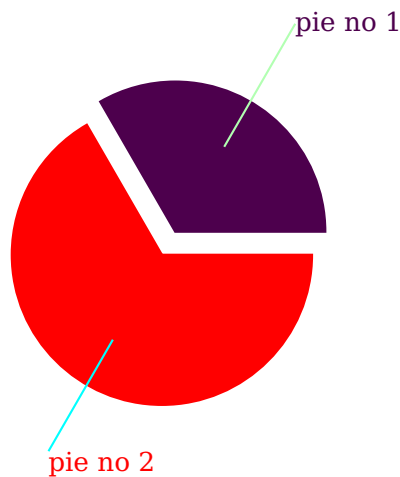
The first mandatory argument is the list of the values and may not be empty. The second one is a list of outraged pieces, numbered consecutively from 1 to up the total number of values. The list of user defined colors must be enclosed in braces!

The macro `\psChart` defines for every value three nodes at the half angle and in distances from 0.75, 1, and 1.25 times of the radius from the origin. The nodes are named as `psChartI?`, `psChart?`, and `psChartO?`, where ? is the number of the pie. The letter I leads to the inner node and the letter O to the outer node. The distance can be changed with the optional arguments `chartNodeI` and `chartNodeO` in the usual way with `\psset{chartNodeI=...,chartNodeO=...}`.

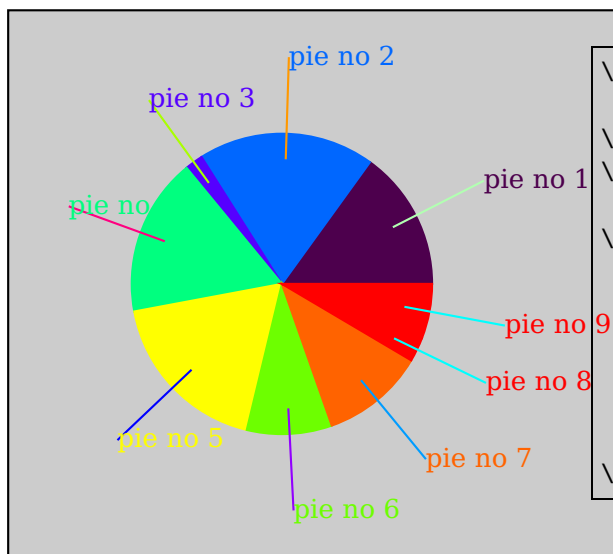
The other one is the node on the circle line. The origin is by default (0,0). Moving the pie to another position can be done as usual with the `\rput`-macro. The used colors are named internally as `chartFillColor?` and can be used by the user for coloring lines or text.



```
\begin{pspicture}(-3,-3)(3,3)
\psChart{ 23, 29, 3, 26, 28, 14 }{}{2}
\multido{\iA=1+1}{6}{%
  \psdot(psChart\iA)\psdot(psChartI\iA)\psdot(
    psChartO\iA)%
  \psline[linestyle=dashed,linecolor=white](
    psChart\iA)
  \psline[linestyle=dashed](psChart\iA)(
    psChartO\iA)}
\end{pspicture}
```

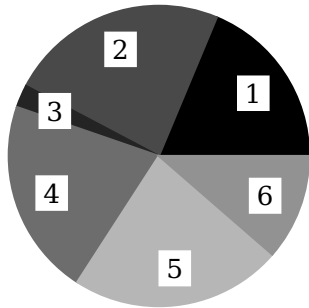
```
\begin{pspicture}(-3,-3)(3,3)
\psChart[chartColor=color]{45,90}{1}{2}
\ncline[linecolor=-chartFillColor1,
nodesepB=-20pt]{psChart01}{psChart1}
\rput[l](psChart01){%
\textcolor{chartFillColor1}{pie no 1}}
\ncline[linecolor=-chartFillColor2,
nodesepB=-20pt]{psChart02}{psChart2}
\rput[lt](psChart02){%
\textcolor{chartFillColor2}{pie no 2}}
\end{pspicture}
```



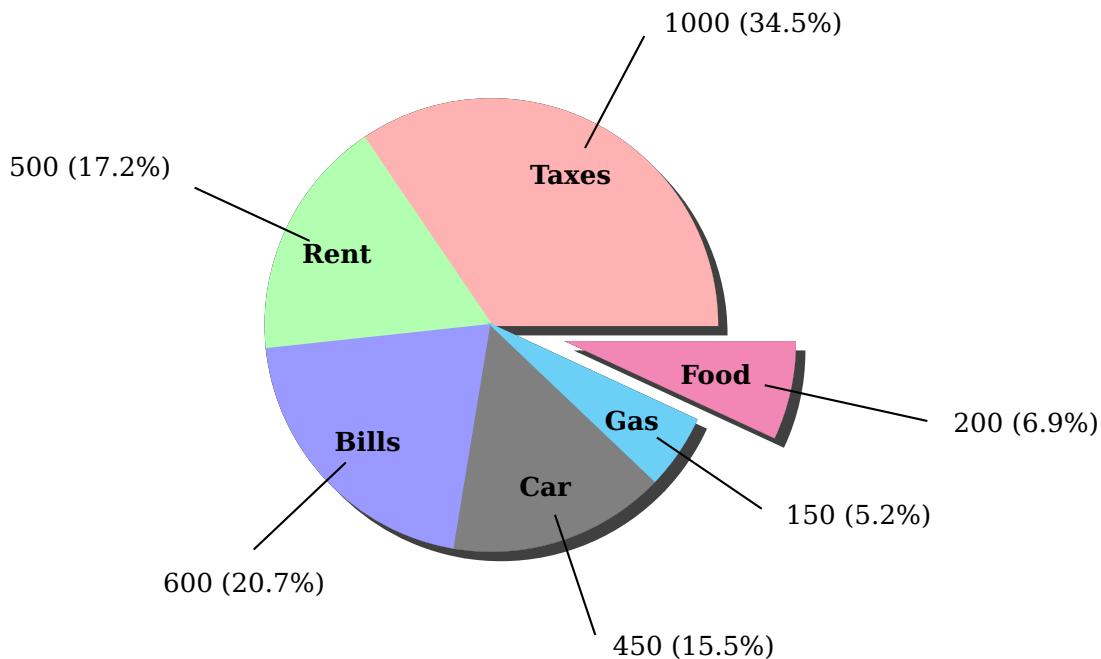
```
\psframebox[fillcolor=black!20,
fillstyle=solid]{%
\begin{pspicture}(-3.5,-3.5)(4.25,3.5)
\psChart[chartColor=color]%
{23, 29, 3, 26, 28, 14, 17, 4, 9}{2}
\multido{\iA=1+1}{9}{%
\ncline[linecolor=-chartFillColor\iA,
nodesepB=-10pt]{psChart0\iA}{psChart
\iA}
\rput[l](psChart0\iA){%
\textcolor{chartFillColor\iA}{pie no
\iA}}}
\end{pspicture}}
```



```
\begin{pspicture}(-3,-3)(3,3)
\psChart[userColor={red!30,green!30,
blue!40,gray,magenta!60,cyan}]%
{ 23, 29, 3, 26, 28, 14 }{1,4}{2}
\end{pspicture}
```



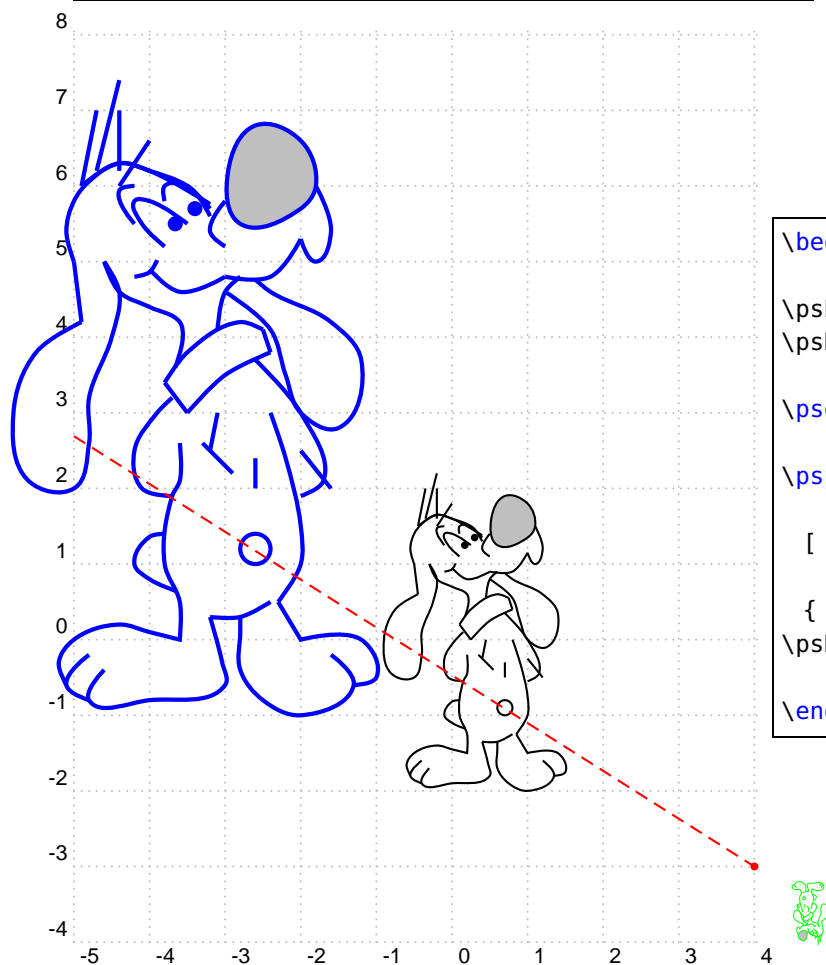
```
\begin{pspicture}(-3,-2.5)(3,2.5)
\psChart{ 23, 29, 3, 26, 28, 14 }{{2}}
\multido{\iA=1+1}{6}{\rput*(psChartI\iA){\iA}}
\end{pspicture}
```



```
\psset{unit=1.5}
\begin{pspicture}(-3,-3)(3,3)
\psChart[userColor={red!30,green!30,blue!40,gray,cyan!50,
magenta!60,cyan},chartSep=30pt,shadow=true,shadowsize=5pt
]{34.5,17.2,20.7,15.5,5.2,6.9}{6}{2}
\psset{nodesepA=5pt,nodesepB=-10pt}
\ncline{psChart01}{psChart1}\nput{0}{psChart01}{1000 (34.5\%)}
\ncline{psChart02}{psChart2}\nput{150}{psChart02}{500 (17.2\%)}
\ncline{psChart03}{psChart3}\nput{-90}{psChart03}{600 (20.7\%)}
\ncline{psChart04}{psChart4}\nput{0}{psChart04}{450 (15.5\%)}
\ncline{psChart05}{psChart5}\nput{0}{psChart05}{150 (5.2\%)}
\ncline{psChart06}{psChart6}\nput{0}{psChart06}{200 (6.9\%)}
\bfseries%
\rput(psChartI1){Taxes}\rput(psChartI2){Rent}\rput(psChartI3){Bills}
\rput(psChartI4){Car}\rput(psChartI5){Gas}\rput(psChartI6){Food}
\end{pspicture}
```

10. \psHomothetie: central dilatation

`\psHomothetie [Options] (center){factor}{object}`

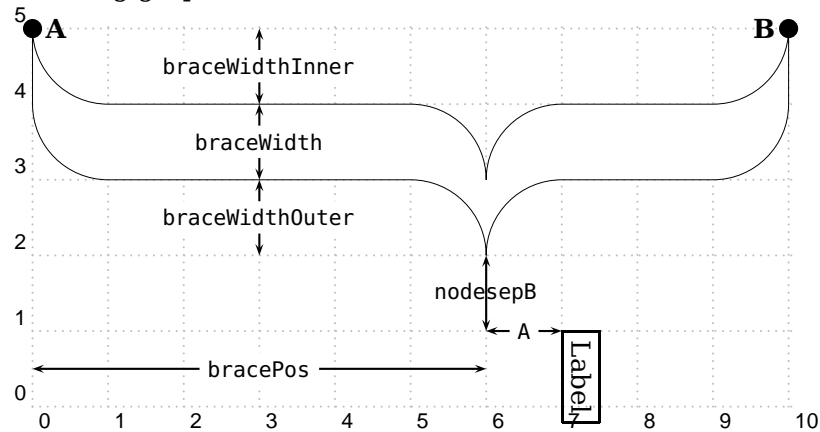


```
\begin{pspicture}[showgrid=true](-5,-4)(4,8)
\psBill% needs package pst-fun
\psHomothetie[linecolor=blue](4,-3){2}{\psBill}
\psdots[dotsize=3pt,linecolor=red](4,-3)
\psplot[linestyle=dashed,linecolor=red]{-5}{4}%
[ /m -3 -0.85 sub 4 0.6 sub div def ]
{ m x mul m 4 mul sub 3 sub }%
\psHomothetie[linecolor=green](4,-3){-0.2}{\psBill}
\end{pspicture}
```

11. \psbrace

`\psbrace * [Options] (A) (B) {text}`

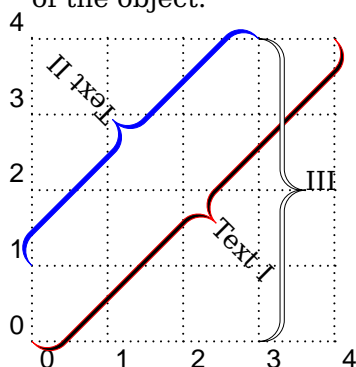
Additional to all other available options from `pstricks` or the other related packages, there are two new option, named `braceWidth` and `bracePos`. All important ones are shown in the following graphics and table.



A positive value for `nodeSepA` and `nodeSepB` shifts the label to the upper right and a negative value to the lower left. This does not depends on the value for the rotating of the label!

name	meaning
<code>braceWidth</code>	default is <code>\pslinewidth</code>
<code>braceWidthInner</code>	default is <code>10\pslinewidth</code>
<code>braceWidthOuter</code>	default is <code>10\pslinewidth</code>
<code>bracePos</code>	relative position (default is 0.5)
<code>nodeSepA</code>	x-separation (default is <code>0pt</code>)
<code>nodeSepB</code>	y-separation (default is <code>0pt</code>)
<code>rot</code>	additional rotating for the text (default is 0)
<code>ref</code>	reference point for the text (default is c)
<code>fillcolor</code>	default is black

By default the text is written perpendicular to the brace line and can be changed with the `pstricks` option `rot=...`. The text parameter can take any object and may also be empty. The reference point can be any value of the combination of l (left) or r (right) and b (bottom) or B (Baseline) or C (center) or t (top), where the default is c, the center of the object.



```
\begin{pspicture}(4,4)
\psgrid[subgriddiv=0,griddots=10]
\pnode(0,0){A}
\pnode(4,4){B}
\psbrace[linecolor=red,ref=lC](A)(B){Text I}
\psbrace*[linecolor=blue,ref=lC](3,4)(0,1){Text II}
\psbrace[fillcolor=white](3,0)(3,4){III}
\end{pspicture}
```

The option `\specialCoor` is enabled, so that all types of coordinates are possible, `(nodename)`, `(x,y)`, `(nodeA|nodeB)`, ... The star version fills the inner of the brace with the current linecolor. With the fillcolor white or any other background color the brace can be "unfilled".

The diagram illustrates the flexibility of the `\psbrace` command through three distinct examples, each showing a visual result and its corresponding LaTeX code.

Example 1: Text Braces

Visual: A sequence of four right-facing curly braces, each containing the word "Text". The last brace is also accompanied by a left-facing curly brace.

Code:

```
\begin{pspicture}(8,2.5)
\psbrace(0,0)(0,2){\fbox{Text}}%
\psbrace[nodesepA=10pt](2,0)(2,2){\fbox{Text}}
\psbrace[ref=lC](4,0)(4,2){\fbox{Text}}
\psbrace[ref=lt,rot=90,nodesepB=-15pt](6,0)(6,2){\fbox{Text}}
\psbrace[ref=lt,rot=90,nodesepA=-5pt,nodesepB=15pt](8,2)(8,0){\fbox{Text}}
\end{pspicture}
```

Example 2: Mathematical Braces

Visual: Three mathematical expressions, each enclosed in a brace. The first is $\int_1^\infty \frac{1}{x^2} dx = 1$. The second is $\int_1^\infty \frac{1}{x^2} dx = 1$. The third is $\int_1^\infty \frac{1}{x^2} dx = 1$.

Code:

```
\def\someMath{\int\limits_1^{\infty}\frac{1}{x^2}\,dx=1}
\begin{pspicture}(8,2.5)
\psbrace[ref=lC](0,0)(0,2){\someMath}%
\psbrace[rot=90](2,0)(2,2){\someMath}
\psbrace[ref=lC](4,0)(4,2){\someMath}
\psbrace[ref=lt,rot=90,nodesepB=-30pt](6,0)(6,2){\someMath}
\psbrace[ref=lt,rot=90,nodesepB=30pt](8,2)(8,0){\someMath}
\end{pspicture}
```

Example 3: Long Text Braces

Visual: Three long horizontal braces. The first contains the text "some very, very long wonderful Text". The second contains the word "Text". The third contains the word "Text".

Code:

```
\begin{pspicture}(\linewidth,5)
\psbrace(0,0.5)(\linewidth,0.5){\fbox{Text}}%
\psbrace[bracePos=0.25,nodesepB=10pt,rot=90](0,2)(\linewidth,2){\fbox{Text}}
\psbrace[ref=lC,nodesepA=-3.5cm,nodesepB=15pt,rot=90](0,4)(\linewidth,4){%
\fbox{some very, very long wonderful Text}}
\end{pspicture}
```


It is also possible to put a vertical brace around a default paragraph. This works by setting two invisible nodes at the beginning and the end of the paragraph. Indentation is possible with a minipage.

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense.

[illegible]

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense.

[illegible]

Some nonsense text, which is nothing more than nonsense.
Some nonsense text, which is nothing more than nonsense.

```
\noindent\rnode{A}{}%
```

$$\backslash\mathrm{vspace}\{ -1\mathrm{ex}\}$$
[illegible]
$$\text{\vspace*{-2ex}\noindent\textcolor{blue}{\text{\node{B}{}}\textcolor{blue}{\text{\psbrace[linecolor=red]{A}{B}}}}$$

Some nonsense text, which is nothing more than nonsense.
Some nonsense text, which is nothing more than nonsense.

```
\medskip\hfill\begin{minipage}{0.95\linewidth}
\noindent\rnode{A}{}
```

$$\backslash\mathrm{vspace}\ast\{-1\mathrm{ex}\}$$
[illegible]

Some nonsense text, which is nothing more than nonsense.

```
\vspace*{-2ex}\noindent\rnode{B}{}\psbrace[linecolor=red](A)(B){}  
\end{minipage}
```

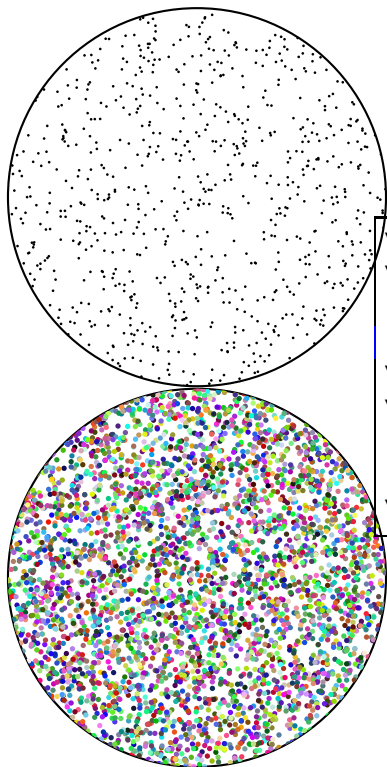

12. Random dots

The syntax of the new macro `\psRandom` is:

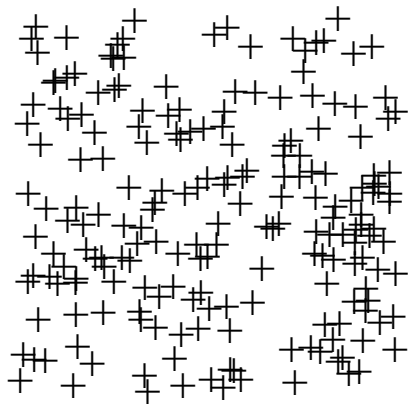
```
\psRandom [Options] {}
\psRandom [Options] ( $x_{Min}, y_{Min}$ ) ( $x_{Max}, y_{Max}$ ) {clip path}
```

If there is no area for the dots defined, then $(0,0)(1,1)$ in the current scale setting is used for placing the dots. If there is only one (x_{Max}, y_{Max}) defined, then $(0,0)$ is used for the other point. This area should be greater than the clipping path to be sure that the dots are placed over the full area. The clipping path can be everything. If no clipping path is given, then the frame $(0,0)(1,1)$ in user coordinates is used. The new options are:

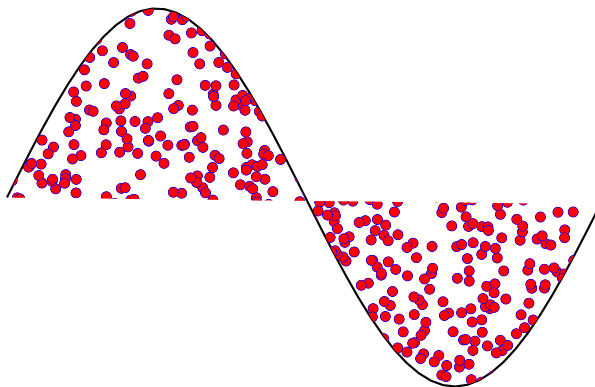
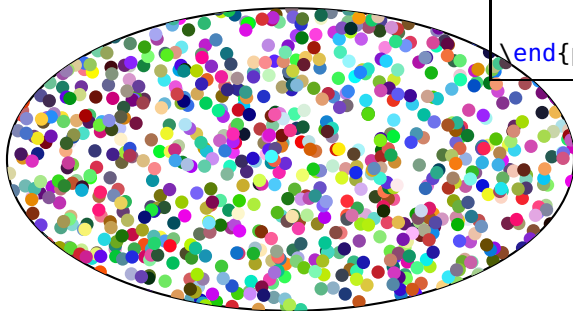
name	default	
randomPoints	1000	number of random dots
color	false	random color



```
\psset{unit=5cm}
\begin{pspicture}(1,1)
  \psRandom[dotsize=1pt,fillstyle=solid](1,1){\pscircle
    (0.5,0.5){0.5}}
\end{pspicture}
\begin{pspicture}(1,1)
  \psRandom[dotsize=2pt,randomPoints=5000,color,%
    fillstyle=solid](1,1){\pscircle(0.5,0.5){0.5}}
\end{pspicture}
```



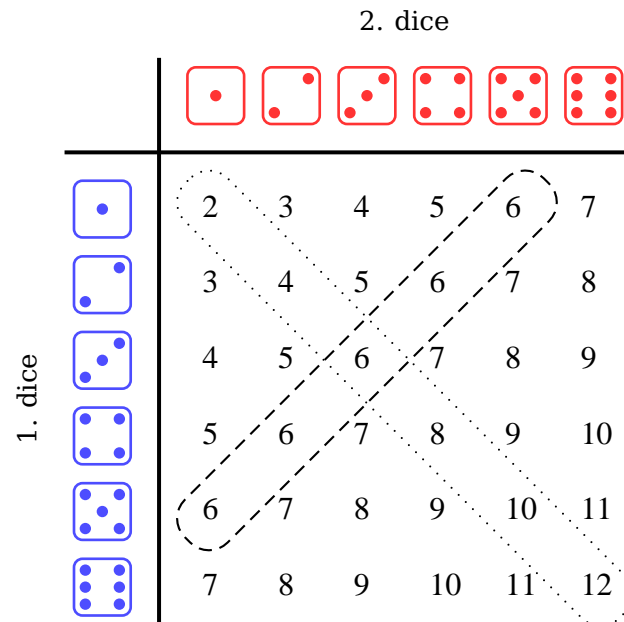
```
\psset{unit=5cm}
\begin{pspicture}(1,1)
  \psRandom[randomPoints=200,dotsize=8pt,
    dotstyle=+]{ }
\end{pspicture}
\begin{pspicture}(1.5,1)
  \psRandom[dotsize=5pt,color](0,0)(1.5,0.8){\
    \psellipse(0.75,0.4)(0.75,0.4)}
\end{pspicture}
```



```
\psset{unit=2.5cm}
\begin{pspicture}(0,-1)(3,1)
  \psRandom[dotsize=4pt,dotstyle=o,
    linecolor=blue,fillcolor=red,%
    fillstyle=solid,randomPoints=1000]
    (0,-1)(3,1){\psplot{0}{3.14}{ x
      114 mul sin }}
\end{pspicture}
```

13. \psDice

\psdice creates the view of a dice. The number on the dice is the only parameter. The optional parameters, like the color can be used as usual. The macro is a box of dimension zero and is placed at the current point. Use the \rput macro to place it anywhere. The optional argument unit can be used to scale the dice. the default size of the dice $1\text{cm} \times 1\text{cm}$.



```
\begin{pspicture}(-1,-1)(8,8)
\multido{\iA=1+1}{6}{%
\rput(\iA,7.5){\Huge\psdice[unit=0.75,linecolor=red!80]{\iA}}
\rput(! -0.5 7 \iA\space sub){\Huge\psdice[unit=0.75,linecolor=blue!70]{\iA}}
%
\multido{\iB=1+1}{6}{%
\rput(! \iA\space 7 \iB\space sub){%
\rnode[c]{p\iA\iB}{\makebox[1em][l]{\strut\psPrintValue[fontscale=12]{\iA\space \iB\space add}}}%
}}}
\ncbox[lineararc=0.35,nodesep=0.2,linestyle=dotted]{p11}{p66}
\ncbox[lineararc=0.35,nodesep=0.2,linestyle=dashed]{p15}{p51}
\rput{90}(-1.5,3.5){1. dice}
\rput{0}(3.5,8.5){2. dice}
\psline[linewidth=1.5pt](0.25,0.5)(0.25,8)
\psline[linewidth=1.5pt](-1,6.75)(6.5,6.75)
\end{pspicture}
```

14. \psFormatInt

There exist some packages and a lot of code to format an integer like 1 000 000 or 1,234,567 (in Europe 1.234.567). But all packages expect a real number as argument and cannot handle macros as an argument. For this case pstricks-add has a macro \psFormatInt which can handle both:

1,234,567	\psFormatInt{1234567}\\
1,234,567	\psFormatInt[intSeparator={,}]{1234567}\\
1.234.567	\psFormatInt[intSeparator=.]{1234567}\\
1·234·567	\psFormatInt[intSeparator=\$\cdot\$]{1234567}\\
965,432	\def\temp{965432} \psFormatInt{\temp}

With the option intSeparator the symbol can be changed to any any non-number character.

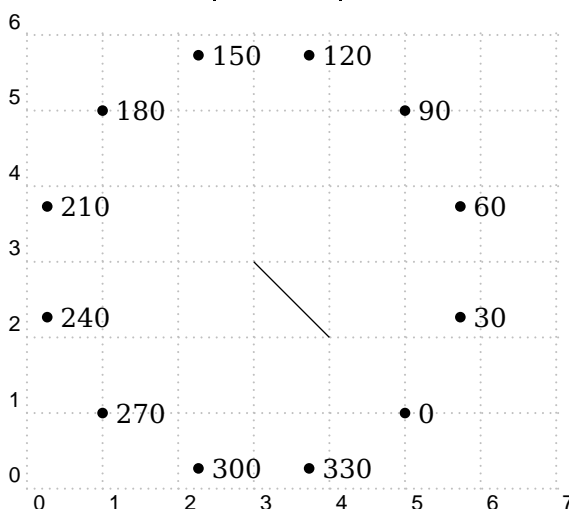
15. \psRelNode and \psDefPSPNodes

With these macros it is possible to put a node relative to a given line or given pspicture-environment. In the first case the parameters are the angle and the length factor:

`\psRelNode[P0][P1]{length factor}{end node name}`
`\psDefPSPNodes`

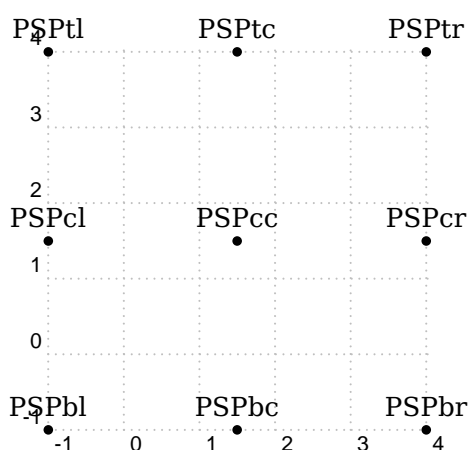
The length factor relates to the distance $\overline{P_0P_1}$ and the end node name must be a valid nodename and shouldn't contain any of the special PostScript characters. There are two valid options:

name	default	meaning
angle	0	angle between the given line $\overline{P_0P_1}$ and the new one $\overline{P_0P_{endNode}}$
trueAngle	false	defines whether the angle refers to the seen line or to the mathematical one, which respect the scaling factors xunit and yunit.



```
\begin{pspicture}[showgrid](7,6)
  \nnode(3,3){A}\nnode(4,2){B}
  \psline[nodesep=-3,linewidth=0.5pt](A)(B)
  \multido{\iA=0+30}{12}{%
    \psRelNode[angle=\iA](A)(B){2}{C}%
    \qdisk(C){2pt}
    \uput[0](C){\iA}}
\end{pspicture}
```

In the second case the new macro `\psDefPSPNodes` defines nine nodes that corresponds to nine particular points (namely bottom left, bottom center, bottom right, center left, center center, center right, top left, top center, top right) of the pspicture box.



```
\begin{pspicture}[showgrid=true](-1,-1)(4,4)
  \psDefPSPNodes
  \psdots(PSPbl)(PSPbc)(PSPbr)
  (PSPcl)(PSPcc)(PSPcr)(PSPtl)(PSPtc)(PSPtr)
  \uput[90](PSPbl){PSPbl} \uput[90](PSPbc){
    PSPbc}
  \uput[90](PSPbr){PSPbr} \uput[90](PSPcl){
    PSPcl}
  \uput[90](PSPcc){PSPcc} \uput[90](PSPcr){
    PSPcr}
  \uput[90](PSPtl){PSPtl} \uput[90](PSPtc){
    PSPtc}
  \uput[90](PSPtr){PSPtr}
\end{pspicture}
```

The name of the nodes are predefined as:

```
\psset[pst-PSPNodes]{bName=PSPbl,bcName=PSPbc,brName=PSPbr,
  clName=PSPcl,ccName=PSPcc,crName=PSPcr,tlName=PSPtl,tcName=PSPtc,trName=PSPtr}
```

and can be modified in the same way.

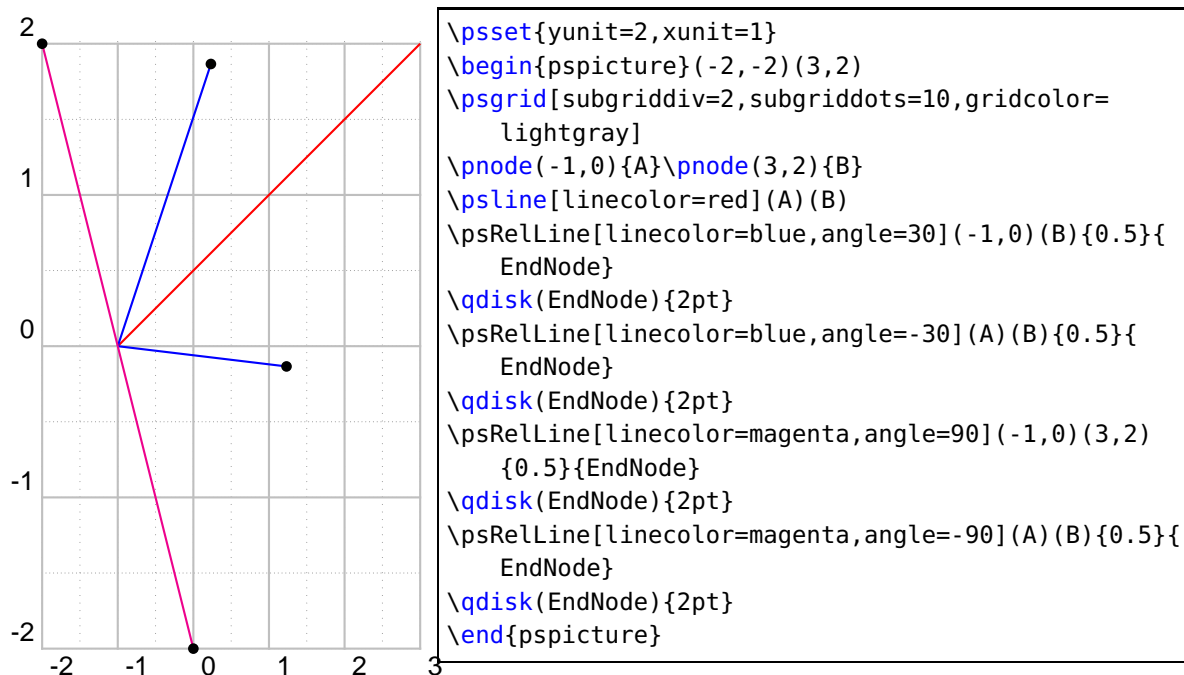
16. \psRelLine

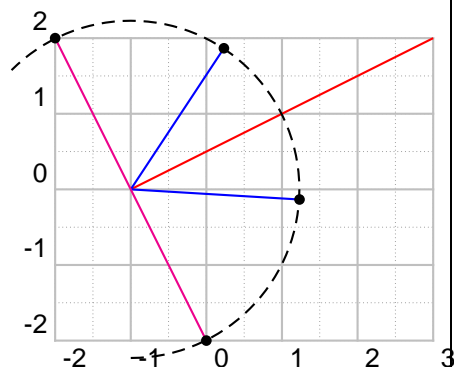
With this macro it is possible to plot lines relative to a given one. Parameter are the angle and the length factor:

```
\psRelLine(P0)(P1){length factor}{<end node name>}
\psRelLine [{arrows}] (P0)(P1){length factor}{end node name}
\psRelLine [Options] (P0)(P1){length factor}{end node name}
\psRelLine [Options] [{arrows}] (P0)(P1){length factor}{end node name}
```

The length factor relates to the distance $\overline{P_0P_1}$ and the end node name must be a valid nodename and shouldn't contain any of the special PostScript characters. There are two valid options which are described in the foregoing section for \psRelNode.

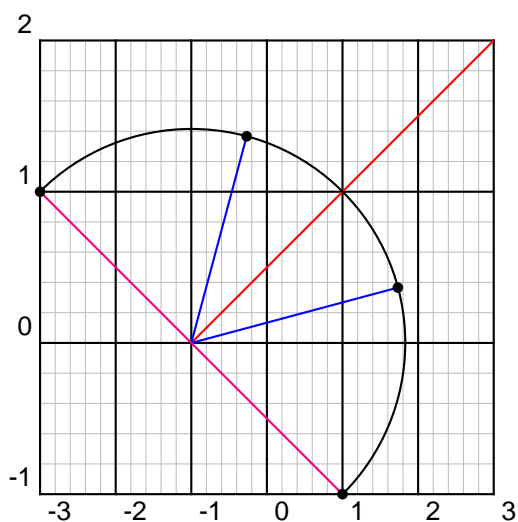
The following two figures show the same, the first one with a scaling different to 1 : 1, this is the reason why the end points are on an ellipse and not on a circle like in the second figure.





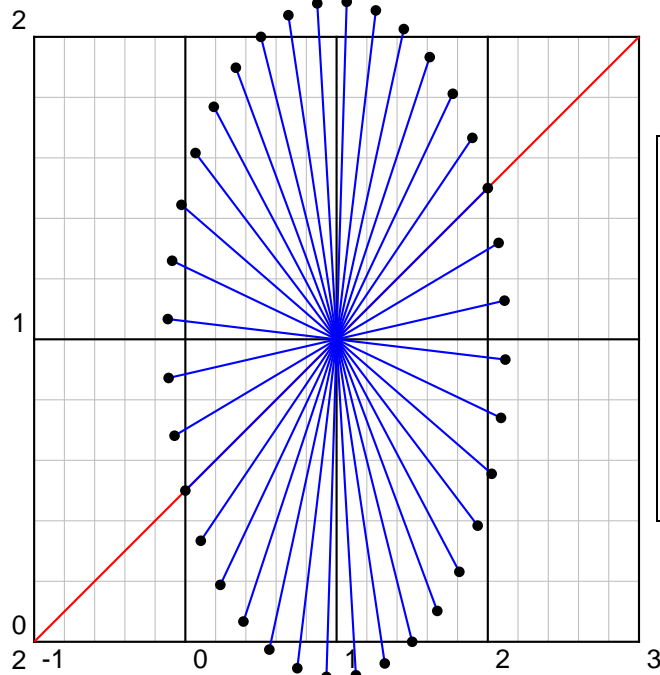
```
\begin{pspicture}(-2,-2)(3,2)
\psgrid[subgriddiv=2,subgriddots=10,gridcolor=
lightgray]
\node(-1,0){A}\node(3,2){B}
\psline[linecolor=red](A)(B)
\psarc[linestyle=dashed](A){2.23}{-90}{135}
\psRelLine[linecolor=blue,angle=30](-1,0)(B){0.5}{
EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=blue,angle=-30](A)(B){0.5}{
EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=magenta,angle=90](-1,0)(3,2)
{0.5}{EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=magenta,angle=-90](A)(B){0.5}{
EndNode}
\qdisk(EndNode){2pt}
\end{pspicture}
```

The following figure has also a different scaling, but has set the option `trueAngle`, all angles refer to "what you see".

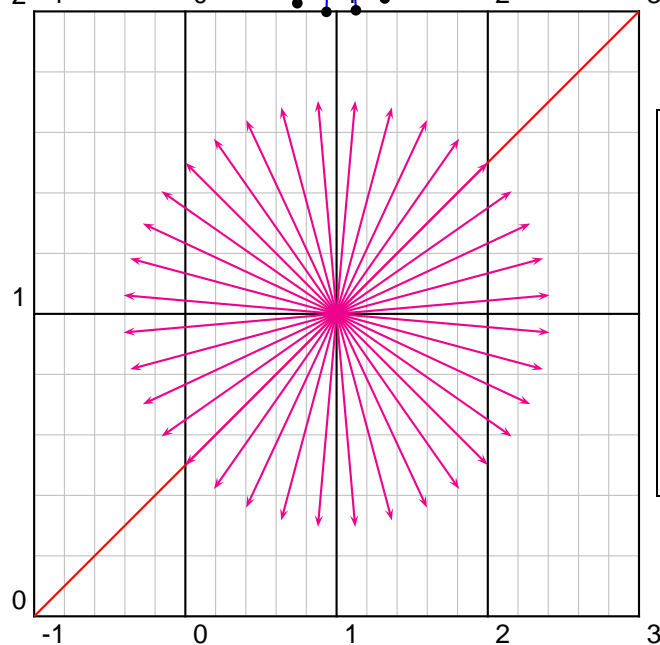


```
\psset{yunit=2,xunit=1}
\begin{pspicture}(-3,-1)(3,2)\psgrid[
subgridcolor=lightgray]
\node(-1,0){A}\node(3,2){B}
\psline[linecolor=red](A)(B)
\psarc(A){2.83}{-45}{135}
\psRelLine[linecolor=blue,angle=30,trueAngle
](A)(B){0.5}{EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=blue,angle=-30,
trueAngle](A)(B){0.5}{EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=magenta,angle=90,
trueAngle](A)(B){0.5}{EndNode}
\qdisk(EndNode){2pt}
\psRelLine[linecolor=magenta,angle=-90,
trueAngle](A)(B){0.5}{EndNode}
\qdisk(EndNode){2pt}
\end{pspicture}
```

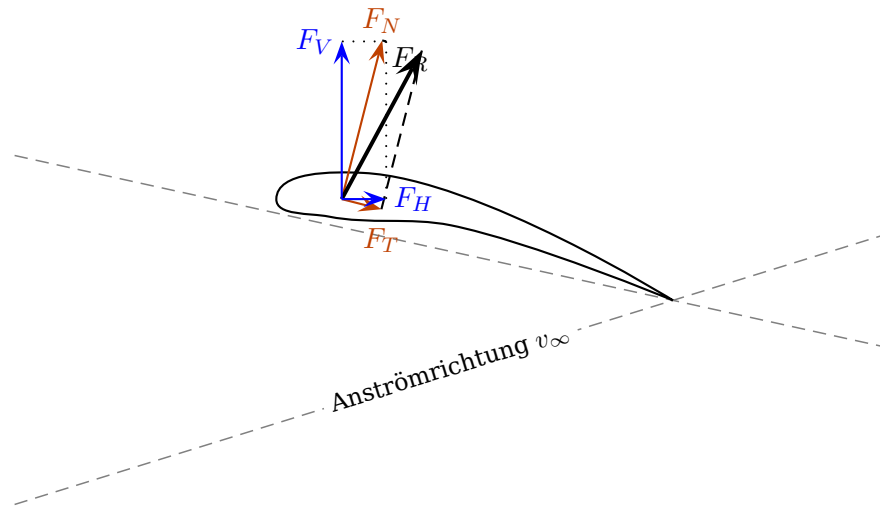
Two examples using `\multido` to show the behaviour of the options `trueAngle` and `angle`.



```
\psset{yunit=4,xunit=2}
\begin{pspicture}(-1,0)(3,2)\psgrid[
  subgridcolor=lightgray]
\pnode(-1,0){A}\pnode(1,1){B}
\psline[linecolor=red](A)(3,2)
\multido{\iA=0+10}{36}{%
  \psRelLine[linecolor=blue,angle=\iA
    ](B)(A){-0.5}{EndNode}
  \qdisk(EndNode){2pt}
}
\end{pspicture}
```



```
\psset{yunit=4,xunit=2}
\begin{pspicture}(-1,0)(3,2)\psgrid[
  subgridcolor=lightgray]
\pnode(-1,0){A}\pnode(1,1){B}
\psline[linecolor=red](A)(3,2)
\multido{\iA=0+10}{36}{%
  \psRelLine[linecolor=magenta,angle
    =\iA,trueAngle]{->}(B)(A)
    {-0.5}{EndNode}
}
\end{pspicture}
```

```
\psset{xunit=0.75\linewidth,yunit=0.75\linewidth,trueAngle}%
\end{center}
\begin{pspicture}(1,0.6)%\psgrid
  \pnode(.3,.35){Vk} \pnode(.375,.35){D} \pnode(0,.4){DST1} \pnode(1,.18){DST2}
  \pnode(0,.1){A1} \pnode(1,.31){A1}
  { \psset{linewidth=.02,linestyle=dashed,linestyle=gray}%
    \pcline(DST1)(DST2) % <- Druckseitentangente
    \pcline(A2)(A1) % <- Anströmrichtung
    \lput*{:U}{\small Anströmrichtung  $v_\infty$ } }%
  \psIntersectionPoint(A1)(A2)(DST1)(DST2){Hk}
  \pscurve(Hk)(.4,.38)(Vk)(.36,.33)(.5,.32)(Hk)
  \psParallelline[linecolor=red!75!green,arrows=->,arrowscale=2](Vk)(Hk)(D)
    {.1}{FtE}
  \psRelLine[linecolor=red!75!green,arrows=->,arrowscale=2,angle=90](D)(FtE)
    {4}{Fn}% why "4"?
  \psParallelline[linestyle=dashed](D)(FtE)(Fn){.1}{Fnr1}
  \psRelLine[linestyle=dashed,angle=90](FtE)(D){-4}{Fnr2} % why "-4"?
  \psline[linewidth=1.5pt,arrows=->,arrowscale=2](D)(Fnr2)
  \psIntersectionPoint(D)([nodesep=2]D)(Fnr1)([offset=-4]Fnr1){Fh}
  \psIntersectionPoint(D)([offset=2]D)(Fnr1)([nodesep=4]Fnr1){Fv}
  \psline[linecolor=blue,arrows=->,arrowscale=2](D)(Fh)
  \psline[linecolor=blue,arrows=->,arrowscale=2](D)(Fv)
  \psline[linestyle=dotted](Fh)(Fnr1) \psline[linestyle=dotted](Fv)(Fnr1)
  \uput{.1}[0](Fh){\blue  $F_H$ } \uput{.1}[180](Fv){\blue  $F_V$ }
  \uput{.1}[-45](Fnr1){ $F_R$ } \uput{.1}[90](Fn){\color{red!75!green} $F_N$ }
  \uput{.25}[-90](FtE){\color{red!75!green} $F_T$ }
\end{pspicture}
```

17. \psParallelline

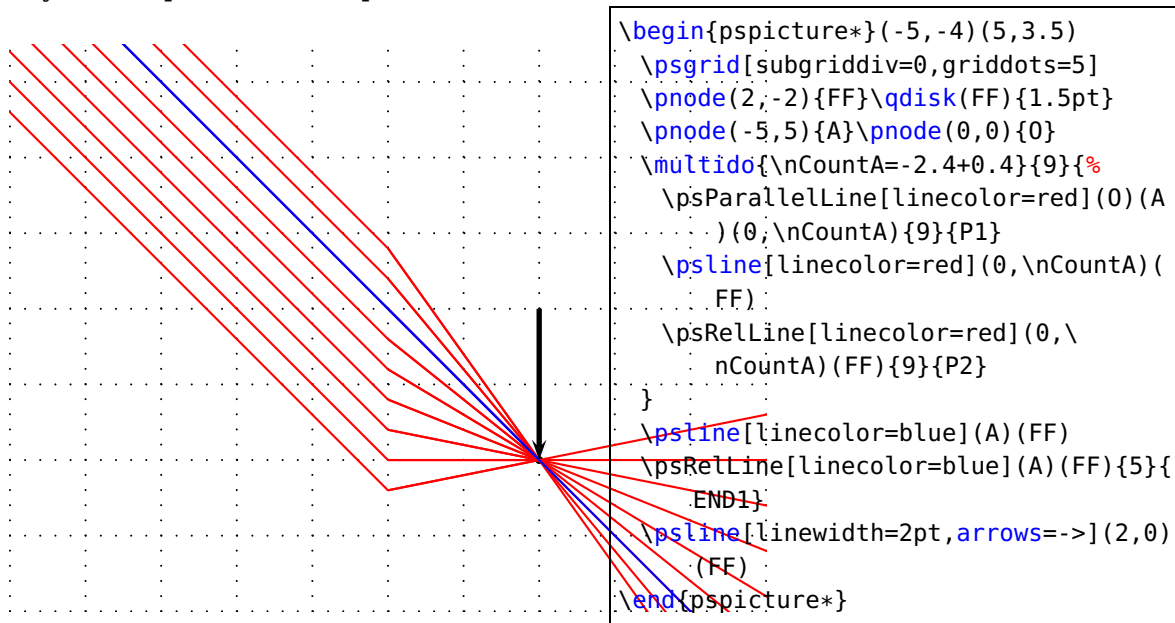
With this macro it is possible to plot lines relative to a given one, which is parallel. There is no special parameter here.

```

\psParallelLine(<P0>)(<P1>)(<P2>){<length>}{<end node name>}
\psParallelLine{<arrows>}( <P0>)( <P1>)( <P2>){<length>}{<end node name>}
\psParallelLine[<options>]( <P0>)( <P1>)( <P2>){<length>}{<end node name>}
\psParallelLine[<options>]{<arrows>}( <P0>)( <P1>)( <P2>){<length>}{<end node name>}

```

The line starts at P_2 , is parallel to $\overline{P_0P_1}$ and the length of this parallel line depends on the length factor. The end node name must be a valid nodename and shouldn't contain any of the special PostScript characters.



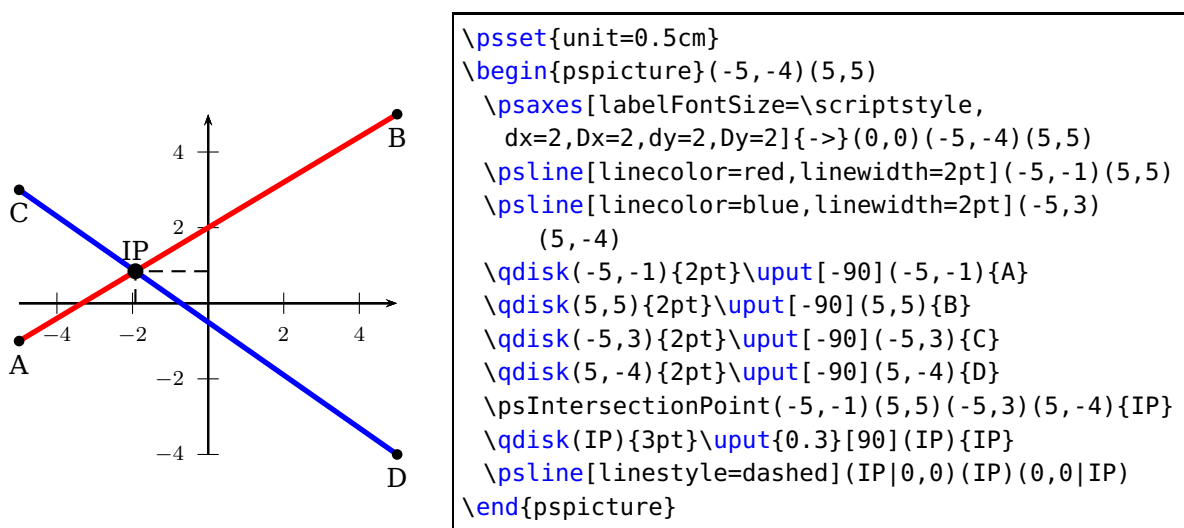
18. \psIntersectionPoint

This macro calculates the intersection point of two lines, given by the four coordinates. There is no special parameter here.

```

\psIntersectionPoint(<P0>)(<P1>)(<P2>)(<P3>){<node name>}

```

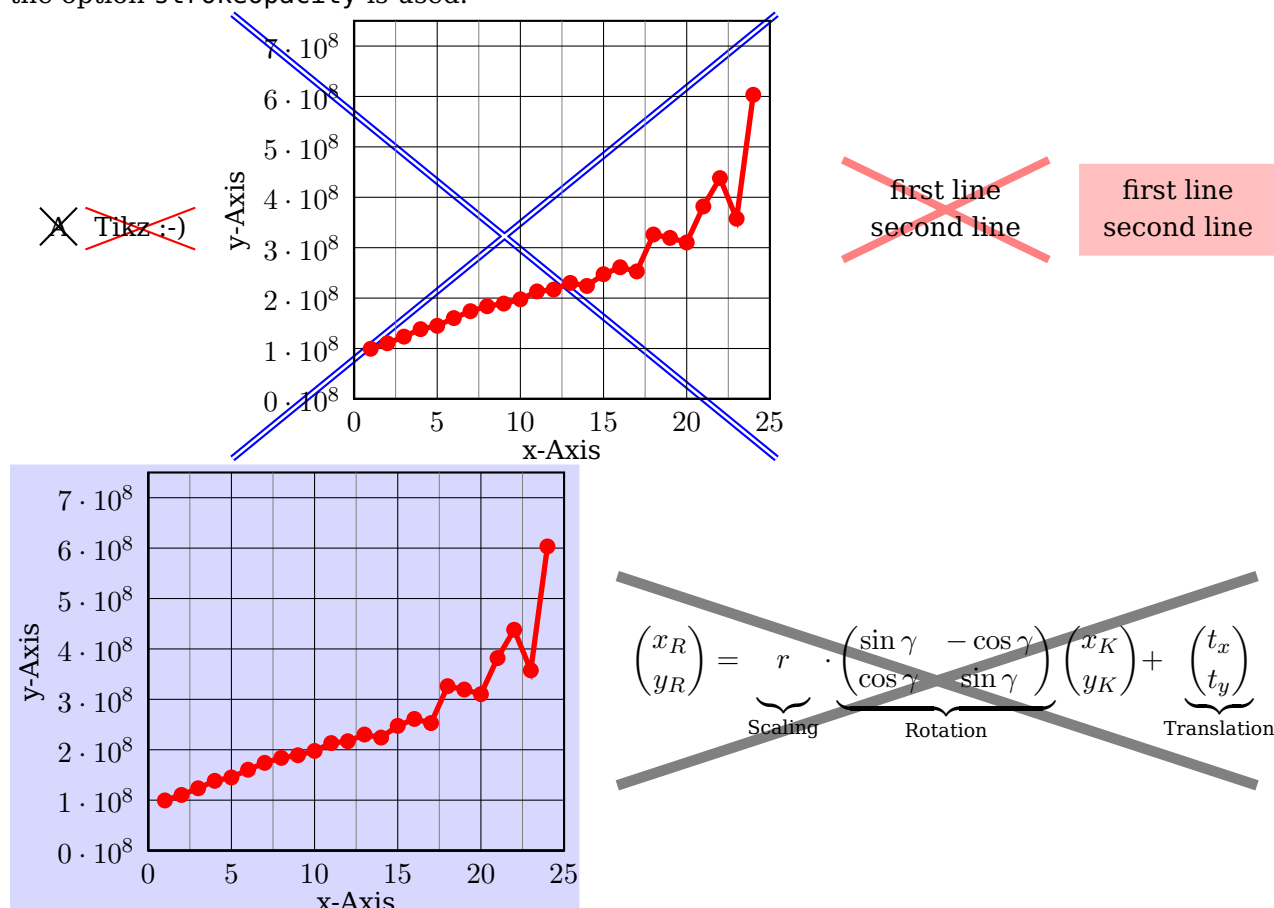


19. psCancel environment¹

This macro works like the `\cancel` macro from the package of the same name but it allows as argument any contents, not only letters but also a complex graphic.

`\psCancel` * `[Options]` `{contents}`

All optional arguments for lines and boxes are valid and can be used in the usual way. The star option fills the underlying box rectangle with the linecolor. This can be transparent if `opacity` is set to a value less than 1. This can be used in presentation to strike out words, equations, and graphic objects. Lines can also be transparent when the option `strokeopacity` is used.



```
\psCancel{A} \psCancel[linecolor=red]{Tikz :-)} \quad
\psCancel[linecolor=blue,doubleline=true]{%
  \readdata{\data}{demo1.data}
  \psset{shift=*,xAxisLabel=x-Axis,yAxisLabel=y-Axis,llx=-13mm,lly=-7mm,
    xAxisLabelPos={c,-1},yAxisLabelPos={-7,c}}
  \pstScalePoints(1,0.00000001){}{}
  \begin{psgraph}[axesstyle=frame,xticksize=0 7.5,yticksize=0 25,subticksize=1,
    ylabelFactor=\cdot 10^8,Dx=5,Dy=1,xsubticks=2](0,0)(25,7.5){5.5cm}{5cm}
```

¹ Thanks to by Stefano Baroni

```

\listplot[linecolor=red, linewidth=2pt, showpoints=true]{\data}
\end{psgraph}} \quad% end of Cancel
\psCancel[linecolor=red, linewidth=3pt, strokeopacity=0.5]{\tabular[b]{c}first line\\second line\endtabular}\quad
\psCancel*[linecolor=red!50, opacity=0.5]{\tabular[b]{c}first line\\second line\endtabular}
\quad
\psCancel*[linecolor=blue!30, opacity=0.5]{%
\readdata{\data}{demo1.data}
\psset{shift=*, xAxisLabel=x-Axis, yAxisLabel=y-Axis, llx=-15mm, lly=-7mm, urx=1mm
,
xAxisLabelPos={c, -1}, yAxisLabelPos={-7, c}}
\pstScalePoints(1, 0.00000001){}}
\begin{psgraph}[axesstyle=frame, xticksize=0 7.5, yticksize=0 25, subticksize=1,
ylabelFactor=\cdot 10^8, Dx=5, Dy=1, xsubticks=2](0,0)(25,7.5){5.5cm}{5cm}
\listplot[linecolor=red, linewidth=2pt, showpoints=true]{\data}
\end{psgraph}} \quad% end of Cancel
\psCancel[linecolor=red, linewidth=4pt, strokeopacity=0.5]{\parbox{8cm}{\[
\binom{x_R}{y_R} = \underbrace{r\sqrt{\phantom{A}}\sqrt{\phantom{B}}}_{\text{Scaling}}\sqrt{\phantom{A}}\sqrt{\phantom{B}}
\cdot
\underbrace{\begin{pmatrix}
\sin\gamma & -\cos\gamma \\
\cos\gamma & \sin\gamma
\end{pmatrix}}_{\text{Rotation}} \binom{x_K}{y_K} +
\underbrace{\binom{t_x}{t_y}}_{\text{Translation}} \]} }% end of psCancel

```

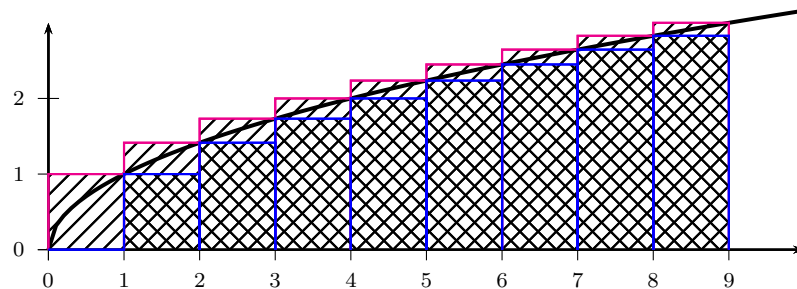
20. \psStep

\psStep calculates a step function for the upper or lower sum or the max/min of the Riemann integral definition of a given function. The available option is

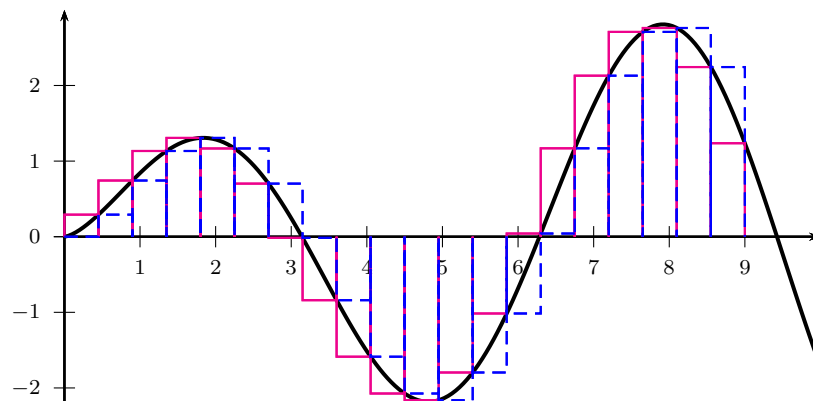
StepType=lower |upper|Riemann|infimum|supremum or alternative StepType=l |u|R|i|s with lower as the default setting. The syntax of the function is

```
\psStep [Options] ((x1,x2){n}{function})
```

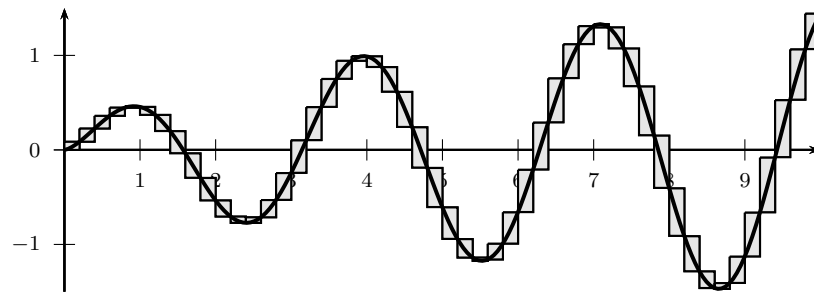
(x1,x2) is the given interval for the step wise calculated function, n is the number of the rectangles and *function* is the mathematical function in postfix or algebraic=true notation (with algebraic=true).



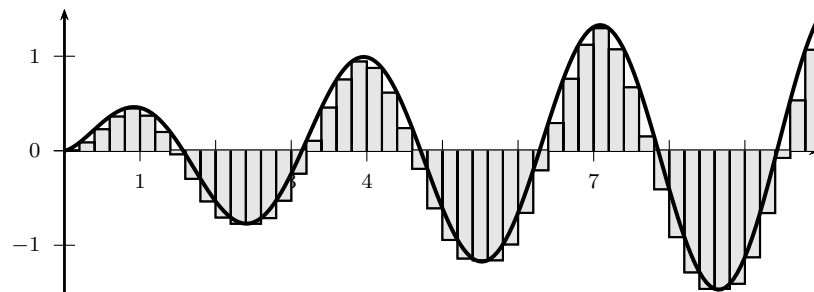
```
\begin{pspicture}(-0.5,-0.5)(10,3)
\psaxes[labelFontSize=\scriptstyle]{->}(10,3)
\psplot[plotpoints=100,linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)}
\psStep[linecolor=magenta,StepType=upper,fillstyle=hlines](0,9){9}{x sqrt}
\psStep[linecolor=blue,fillstyle=vlines](0,9){9}{x sqrt}
\end{pspicture}
```



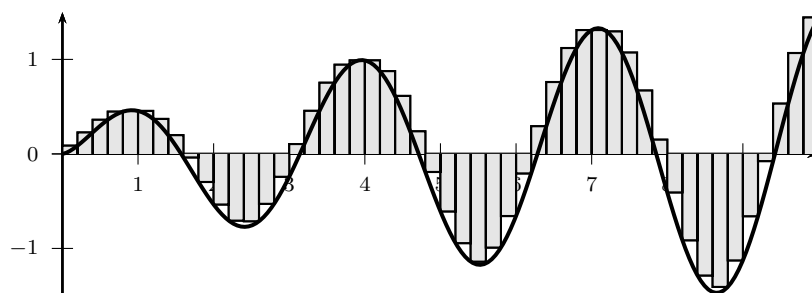
```
\psset{plotpoints=200}
\begin{pspicture}(-0.5,-2.25)(10,3)
\psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-2.25)(10,3)
\psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*sin(x)}
\psStep[algebraic=true,linecolor=magenta,StepType=upper](0,9){20}{sqrt(x)*sin(x)}
\psStep[linecolor=blue,linestyle=dashed](0,9){20}{x sqrt x RadtoDeg sin mul}
\end{pspicture}
```



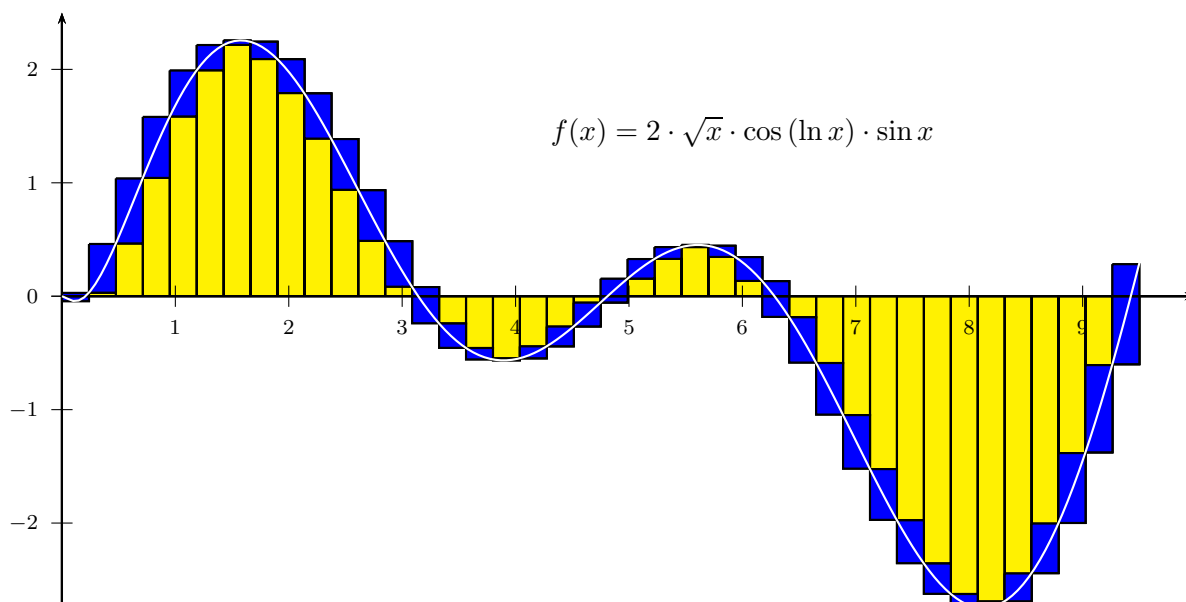
```
\psset{yunit=1.25cm,plotpoints=200}
\begin{pspicture}(-0.5,-1.5)(10,1.5)
\psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-1.5)(10,1.5)
\psStep[algebraic=true,StepType=Riemann,fillstyle=solid,fillcolor=black
!10](0,10){50}%
{sqrt(x)*cos(x)*sin(x)}
\psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*cos(x)*sin(x)}
\end{pspicture}
```



```
\psset{yunit=1.25cm,plotpoints=200}
\begin{pspicture}(-0.5,-1.5)(10,1.5)
\psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-1.5)(10,1.5)
\psStep[algebraic=true,StepType=infimum,fillstyle=solid,fillcolor=black
!10](0,10){50}%
{sqrt(x)*cos(x)*sin(x)}
\psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*cos(x)*sin(x)}
\end{pspicture}
```



```
\psset{yunit=1.25cm,plotpoints=200}
\begin{pspicture}(-0.5,-1.5)(10,1.5)
\psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-1.5)(10,1.5)
\psStep[algebraic=true,StepType=supremum,fillstyle=solid,fillcolor=black
!10](0,10){50}%
{sqrt(x)*cos(x)*sin(x)}
\psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*cos(x)*sin(x)}
\end{pspicture}
```



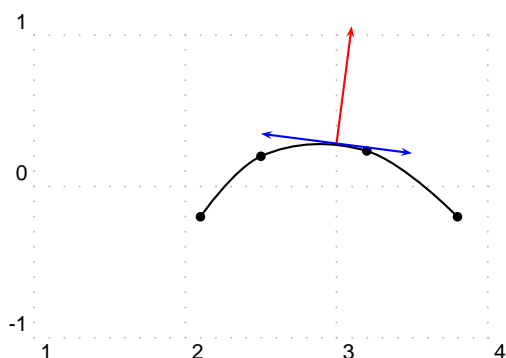
```
\psset{unit=1.5cm,plotpoints=200}
\begin{pspicture}[plotpoints=200](-0.5,-3)(10,2.5)
\psStep[algebraic=true,fillstyle=solid,fillcolor=yellow](0.001,9.5){40}{2*sqrt(
x)*cos(ln(x))*sin(x)}
\psStep[algebraic=true,StepType=Riemann,fillstyle=solid,fillcolor=blue
](0.001,9.5){40}{2*sqrt(x)*cos(ln(x))*sin(x)}
\psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-2.75)(10,2.5)
\psplot[algebraic=true,linecolor=white]{0.001}{9.75}{2*sqrt(x)*cos(ln(x))*sin(x
)}
\uput[90](6,1.2){$f(x)=2\cdot\sqrt{x}\cdot\cos(\ln{x})\cdot\sin{x}$}
\end{pspicture}
```

21. Tangent lines

There are two macros for plotting a tangent line or the tangent normal line. The first one is `\psTangentLine` which expects three pairs of coordinates, a x and a dx value. The second one is `\psplotTangent` which expects a function for the curve.

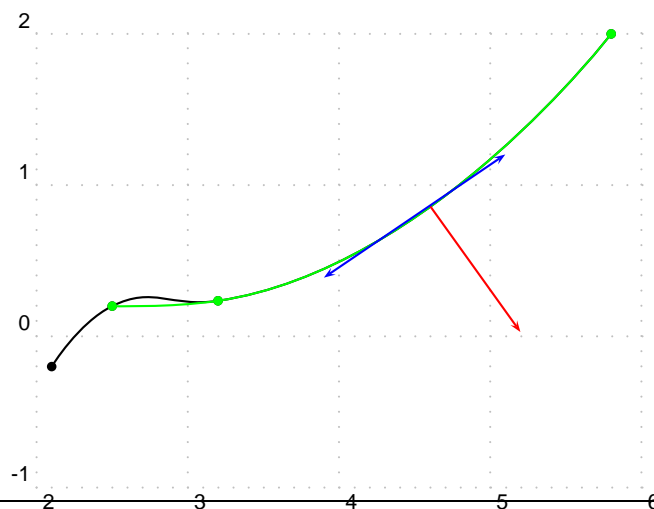
21.1. `\psTangentLine` and option `Tnormal`

`\psTangentLine` [Options] $(x_1, y_1)(x_2, y_2)(x_3, y_3)\{x\}\{dx\}$



```
\psset{unit=2}
\begin{pspicture}[showgrid=true](1,-1)(4,1)
\pscurve[showpoints=true]
(2.1,-0.2)(2.5,0.2)(3.2,0.235)(3.8,-0.2)
\psTangentLine[Tnormal,arrows=->,
linecolor=red](2.5,0.2)(3.2,0.235)%
(3.8,-0.2){3}{0.1}
\psTangentLine[arrows=<->,
linecolor=blue](2.5,0.2)(3.2,0.235)%
(3.8,-0.2){3}{0.5}
\end{pspicture}
```

In special cases one has to use `curvature=1 1 1` for the macro `\pscurve` to get the same equation for the curve as `\psplotTangentLine` does.



```
\psset{unit=2}
\begin{pspicture}[showgrid=true](2,-1)(6,2)
\pscurve[showpoints=true,
curvature=1 1 1](2.1,-0.2)(2.5,0.2)(3.2,0.235)(5.8,2)
\pscurve[showpoints=true,linecolor=green,
curvature=1 1 1](2.5,0.2)(3.2,0.235)(5.8,2)
\psTangentLine[Tnormal,arrows=->,linecolor=red](2.5,0.2)(3.2,0.235)(5.8,2){4.6}{0.6}
\psTangentLine[arrows=<->,linecolor=blue](2.5,0.2)(3.2,0.235)(5.8,2){4.5}{0.6}
\end{pspicture}
```


21.2. \psplotTangent and option Tnormal

There is an additional option, named `Derive` for an alternative function (see following example) to calculate the slope of the tangent. This will be in general the first derivative, but can also be any other function. If this option is different to the default value `Derive=default`, then this function is taken to calculate the slope. For the other cases, `psstricks-add` builds a secant with $-0.00005 < x < 0.00005$, calculates the slope and takes this for the tangent. This may be problematic in some cases of special functions or x values, then it may be appropriate to use the `Derive` option.

`\psplotTangent` * `[Options]` `{x}{dx}{function}`

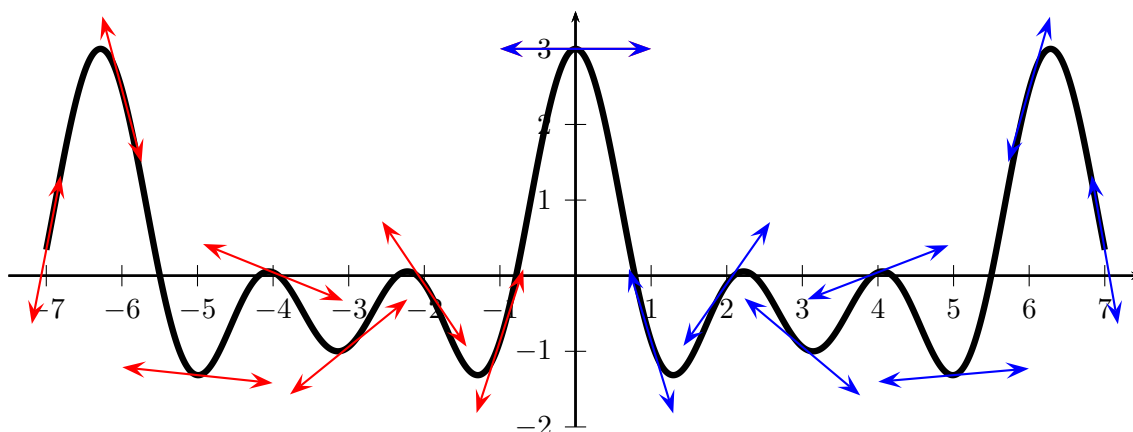
The macro expects three parameters:

x : the x value of the function for which the tangent should be calculated

dx : the dx to both sides of the x value

$f(x)$: the function in infix (with option `algebraic`) or the default postfix (PostScript) notation

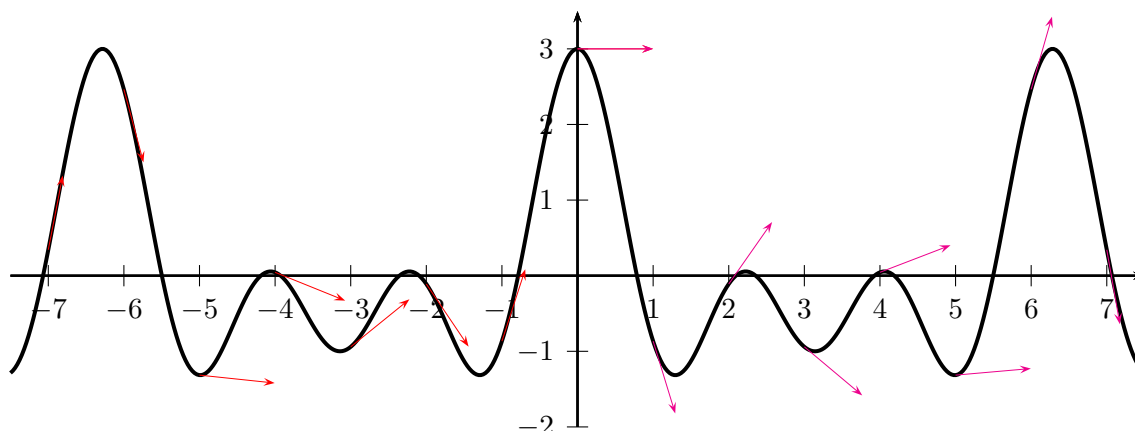
The following examples show the use of the `algebraic=true` option together with the `Derive` option. Remember that using the `algebraic` option implies that the angles have to be in the radian unit!



```
\def\F{x RadtoDeg dup dup cos exch 2 mul cos add exch 3 mul cos add}
\def\Fp{x RadtoDeg dup dup sin exch 2 mul sin 2 mul add exch 3 mul sin 3 mul
  add neg}
\psset{plotpoints=1001}
\begin{pspicture}(-7.5,-2.5)(7.5,4)%X\psgrid
  \psaxes{->}(0,0)(-7.5,-2)(7.5,3.5)
  \psplot[linewidth=3\pslinewidth]{-7}{7}{\F}
  \psset{linecolor=red, arrows=<->, arrowscale=2}
  \multido{\n=-7+1}{8}{\psplotTangent{\n}{1}{\F}}
  \psset{linecolor=magenta, arrows=<->, arrowscale=2}%
```

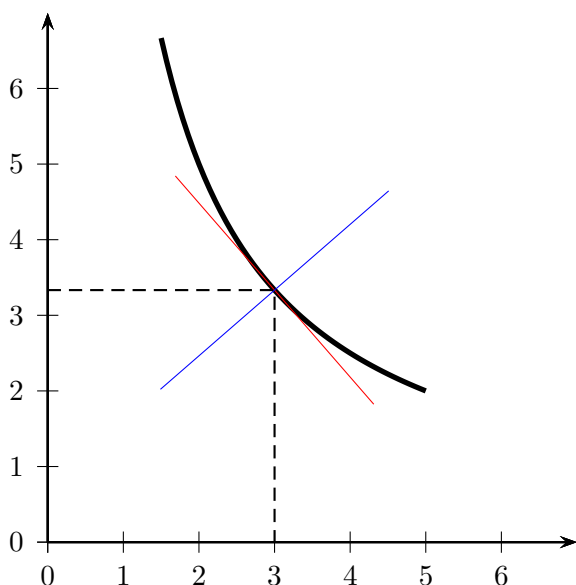
```
\multido{\n=0+1}{8}{\psplotTangent[linecolor=blue, Derive=\Fp]{\n}{1}{\F}}
\end{pspicture}
```

The star version plots only the tangent line in the positive x -direction:



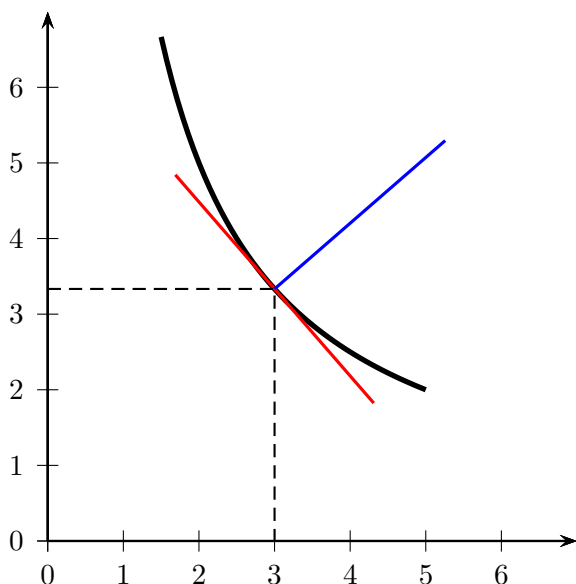
```
\def\Falg{cos(x)+cos(2*x)+cos(3*x)} \def\Fpalg{-sin(x)-2*sin(2*x)-3*sin(3*x)}
\begin{pspicture}(-7.5,-2.5)(7.5,4)%\psgrid
\psaxes{->}(0,0)(-7.5,-2)(7.5,3.5)
\psplot[linewidth=1.5pt,algebraic=true,plotpoints=500]{-7.5}{7.5}{\Falg}
\multido{\n=-7+1}{8}{\psplotTangent*[linecolor=red,arrows=->,arrowscale=2,
algebraic=true]{\n}{1}{\Falg}}
\multido{\n=0+1}{8}{\psplotTangent*[linecolor=magenta,%
arrows=->,arrowscale=2,algebraic=true,Derive={\Fpalg}]{\n}{1}{\Falg}}
\end{pspicture}
```

The next example shows the use of the Derive option to draw the perpendicular line to the tangent.



```
\begin{pspicture}(-0.5,-0.5)(7.25,7.25)
\def\Func{10 x div}
\psaxes[arrowscale=1.5]{->}(7,7)
\psplot[linewidth=2pt,algebraic=true]{1.5}{5}{10/x}
\psplotTangent[linewidth=.5\pslinewidth,
linecolor=red,algebraic=true]{3}{2}{10/x}
\psplotTangent[linewidth=.5\pslinewidth,
linecolor=blue,algebraic=true,Derive=(x*x)/10]{3}{2}{10/x}
\psline[linestyle=dashed](!0 /x 3 def \Func)
(!3 /x 3 def \Func)(3,0)
\end{pspicture}
```

By setting the optional argument `Tnormal` one can plot the normal of the tangent line. It always starts at the given point.

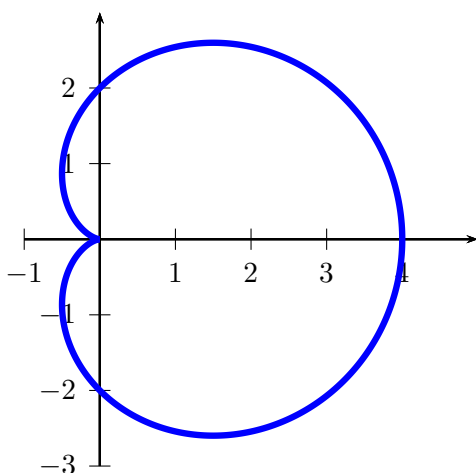


```
\begin{pspicture}(-0.5,-0.5)(7.25,7.25)
\def\Func{10 x div}
\psaxes[arrowscale=1.5]{->}(7,7)
\psplot[linewidth=2pt]{1.5}{5}{\Func}
\psplotTangent[linewidth=1.5\pslinewidth,
linecolor=red]{3}{2}{\Func}
\psplotTangent[linewidth=1.5\pslinewidth,
linecolor=blue,Tnormal]{3}{2}{\Func}
\psline[linestyle=dashed](!0 /x 3 def \Func)
(!3 /x 3 def \Func)(3,0)
\end{pspicture}
```

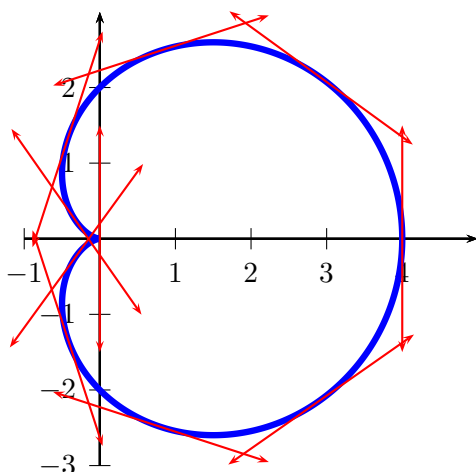
Let's work with the classical cardioid: $r = 2(1 + \cos(\theta))$ and $\frac{dr}{d\theta} = -2\sin(\theta)$. The `Derive` option always expects the $\frac{dr}{d\theta}$ value and uses internally the equation for the derivative of implicitly defined functions:

$$\frac{dy}{dx} = \frac{r' \cdot \sin \theta + x}{r' \cdot \cos \theta - y}$$

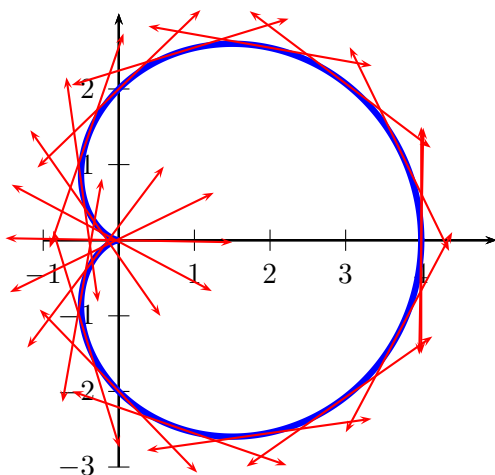
where $x = r \cdot \cos \theta$ and $y = r \cdot \sin \theta$



```
\begin{pspicture}(-1,-3)(5,3)%\psgrid[subgridcolor=
lightgray]
\psaxes{->}(0,0)(-1,-3)(5,3)
\psplot[polarplot,linewidth=3\pslinewidth,linecolor=blue
,%
plotpoints=500]{0}{360}{1 x cos add 2 mul}
\end{pspicture}
```



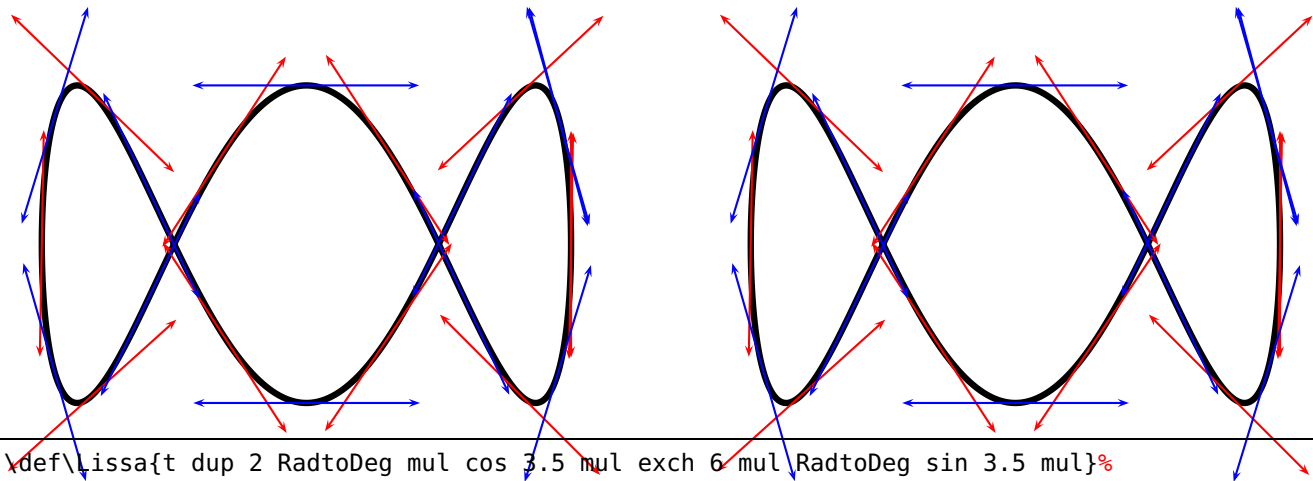
```
\begin{pspicture}(-1,-3)(5,3)%\psgrid[subgridcolor=
lightgray]
\psaxes{->}(0,0)(-1,-3)(5,3)
\psplot[polarplot,linewidth=3\pslinewidth,linecolor=blue
,plotpoints=500]{0}{360}{1 x cos add 2 mul}
\multido{\n=0+36}{10}{%
\psplotTangent[polarplot,linecolor=red,arrows=<->]{\n
}{1.5}{1 x cos add 2 mul} }
\end{pspicture}
```



```
\begin{pspicture}(-1,-3)(5,3)%\psgrid[subgridcolor=
lightgray]
\psaxes{->}(0,0)(-1,-3)(5,3)
\psplot[polarplot,linewidth=3\pslinewidth,linecolor=blue
,algebraic=true,plotpoints=500]{0}{6.289}{2*(1+cos(x
))}
\multido{\r=0.000+0.314}{21}{%
\psplotTangent[polarplot,Derive=-2*sin(x),algebraic=
true,linecolor=red,arrows=<->]{\r}{1.5}{2*(1+cos(x
))} }
\end{pspicture}
```

Let's work with a Lissajou curve: $\begin{cases} x = 3.5 \cos(2t) \\ y = 3.5 \sin(6t) \end{cases}$ whose derivative is: $\begin{cases} x = -7 \sin(2t) \\ y = 21 \cos(6t) \end{cases}$

The parameter must be the letter t instead of x and when using the `algebraic=true` option you must separate the two equations by a `|` (see example).



```

\def\Lissa{t dup 2 RadtoDeg mul cos 3.5 mul exch 6 mul RadtoDeg sin 3.5 mul}%
\psset{yunit=0.6}
\begin{pspicture}(-4,-4)(4,6)
\parametricplot[plotpoints=500,linewidth=3\pslinewidth]{0}{3.141592}{\Lissa}
\multido{\r=0.000+0.314}{11}{%
\psplotTangent[linecolor=red,arrows=<->]{\r}{1.5}{\Lissa} }
\multido{\r=0.157+0.314}{11}{%
\psplotTangent[linecolor=blue,arrows=<->]{\r}{1.5}{\Lissa} }
\end{pspicture}\hfill%
\def\LissaAlg{3.5*cos(2*t)|3.5*sin(6*t)} \def\LissaAlgDer{-7*sin(2*t)|21*cos(6*t)}%
\begin{pspicture}(-4,-4)(4,6)
\parametricplot[algebraic=true,plotpoints=500,linewidth=3\pslinewidth]{0}{3.141592}{\LissaAlg}
\multido{\r=0.000+0.314}{11}{%
\psplotTangent[algebraic=true,linecolor=red,arrows=<->]{\r}{1.5}{\LissaAlg} }
\multido{\r=0.157+0.314}{11}{%
\psplotTangent[algebraic=true,linecolor=blue,arrows=<->,%
Derive=\LissaAlgDer]{\r}{1.5}{\LissaAlg} }
\end{pspicture}

```

22. Successive derivatives of a function

The new PostScript function `Derive` has been added for plotting successive derivatives of a function. It must be used with the `algebraic=true` option. This function has two arguments:

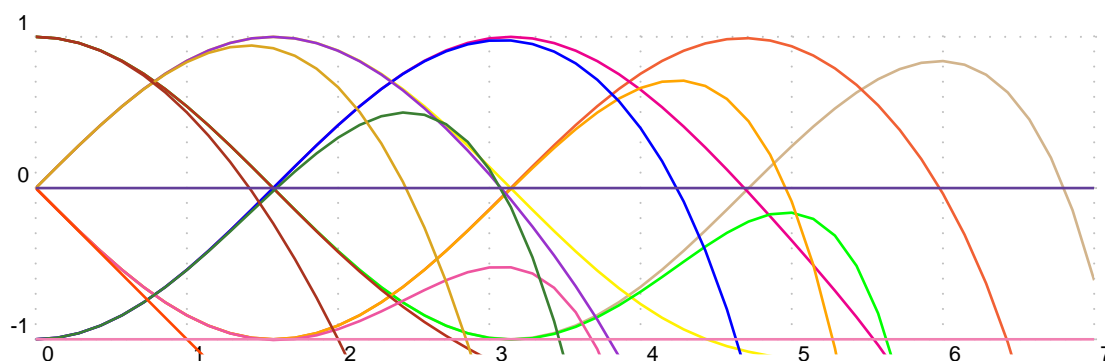
1. a positive integer which defines the order of the derivative; obviously 0 means the function itself!
2. a function of variable x which can be any function using common operators,

Do not think that the derivative is approximated, the internal PostScript engine will compute the real derivative using a formal derivative engine.

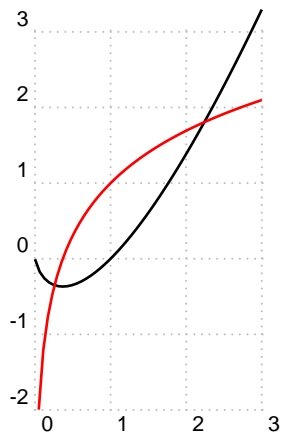
The following diagram contains the plot of the polynomial:

$$f(x) = \sum_{i=0}^{14} \frac{(-1)^i x^{2i}}{i!} = 1 - \frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \frac{x^8}{8!} - \frac{x^{10}}{10!} + \frac{x^{12}}{12!} - \frac{x^{14}}{14!}$$

and of its first 15 derivatives. It is the sequence definition of the cosine.



```
\psset{unit=2}
\def\getColor#1{\ifcase#1 Tan\or Red\orange\or magenta\or yellow\or green\or Orange\or blue\
or
DarkOrchid\or BrickRed\or Rhodamine\or OliveGreen\or Goldenrod\or Mahogany\or
OrangeRed\or CarnationPink\or RoyalPurple\or Lavender\fi}
\begin{pspicture}[showgrid=true](0,-1.2)(7,1.5)
\psclip{\psframe[linestyle=none](0,-1.1)(7,1.1)}
\multido{\in=0+1}{16}{%
\psplot[linewidth=1pt,algebraic=true,linecolor=\getColor{\in}]{0}{7}
{Derive(\in,1-x^2/2+x^4/24-x^6/720+x^8/40320-x^10/3628800+x^12/479001600-x
^14/87178291200)}}
\endpsclip
\end{pspicture}
```



```
\begin{pspicture}[shift=-2.5,showgrid=true,linewidth=1pt]
(0,-2)(3,3)
\psplot[algebraic=true]{.001}{3}{x*ln(x)} % f(x)
\psplot[algebraic=true,linecolor=red]{.05}{3}{Derive(1,x*ln
(x))} % f'(x)=1+ln(x)
\end{pspicture}
```

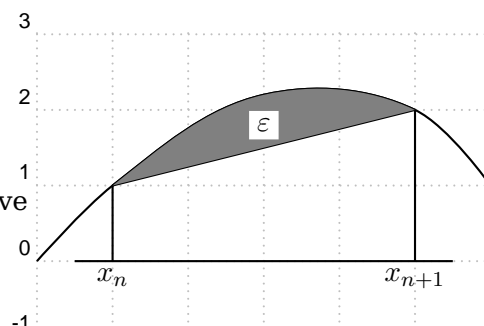
23. Variable step for plotting a curve

23.1. Theory

As you know with the `\psplot` macro, the curve is plotted using a piece-wise linear curve. The step is given by the parameter `plotpoints`. For each step between x_i and x_{i+1} , the area defined between the curve and its approximation (a segment) is majored by this formula :

$$|\varepsilon| \leq \frac{M_2(f)(x_{i+1} - x_i)^3}{12}$$

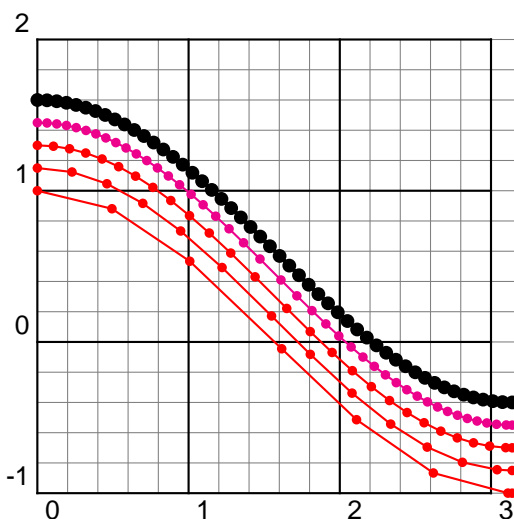
$M_2(f)$ is a majorant of the second derivative of f in the interval $[x_i; x_{i+1}]$.



The parameter `VarStep` (false by default) activates the variable step algorithm. It is set to a tolerance defined by the parameter `VarStepEpsilon` (default by default, accept real value). If this parameter is not set by the user, then it is automatically computed using the default first step given by the parameter `plotpoints`. Then, for each step, $f''(x_n)$ and $f''(x_{n+1})$ are computed and the smaller is used as $M_2(f)$, and then the step is approximated. This means that the step is constant for second order polynomials.

23.2. The cosine

Different value for the tolerance from 0.01 to 0.000 1, a factor 10 between each of them. In black, there is the classic `\psplot` behavior, and in magenta the default variable step behavior.



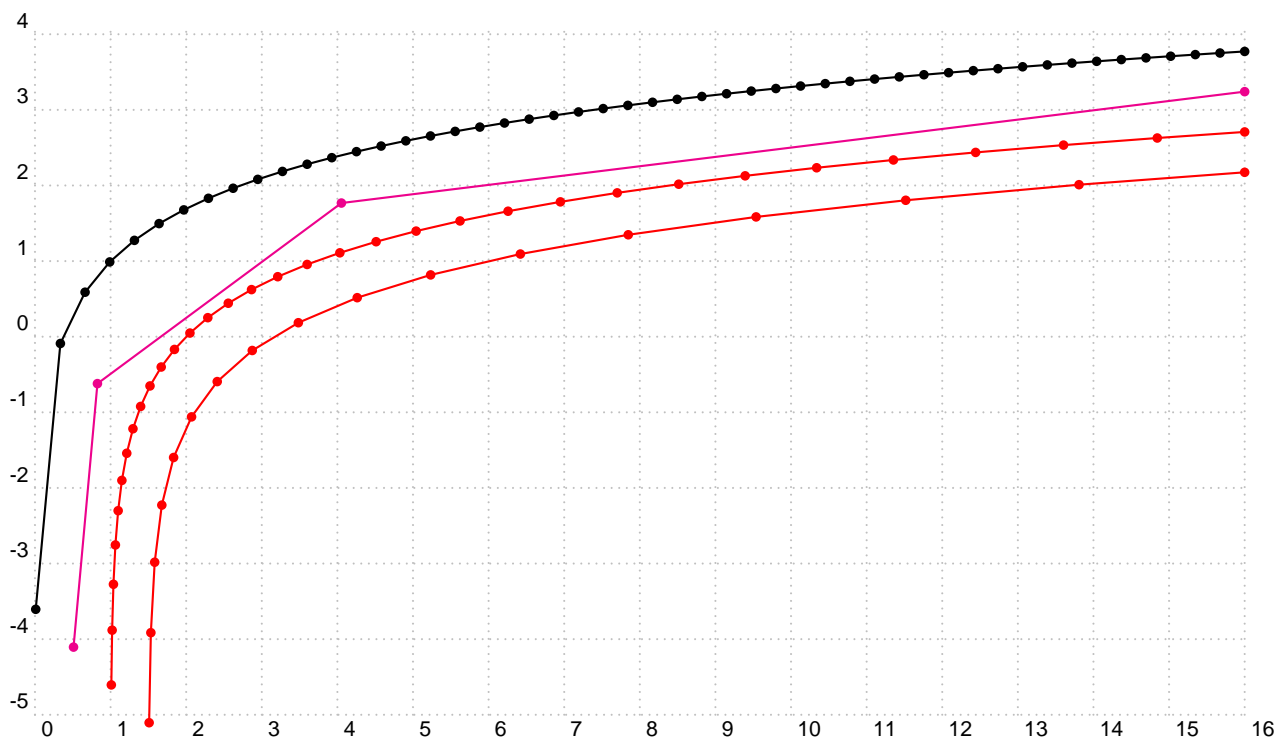
```
\psset{algebraic=true, VarStep=true, unit=2, showpoints=true, linecolor=red}
\begin{pspicture}[showgrid=true](-0,-1)(3.14,2)
  \psplot[VarStepEpsilon=.01]{0}{3.14}{cos(x)}
  \psplot[VarStepEpsilon=.001]{0}{3.14}{cos(x)+.15}
  \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}
```



```
\psplot[linecolor=magenta]{0}{3.14}{cos(x)+.45}
\psplot[VarStep=false,linewidth=1pt,linecolor=black]{-0}{3.14}{cos(x)+.6}
\end{pspicture}
```

23.3. The Napierian Logarithm

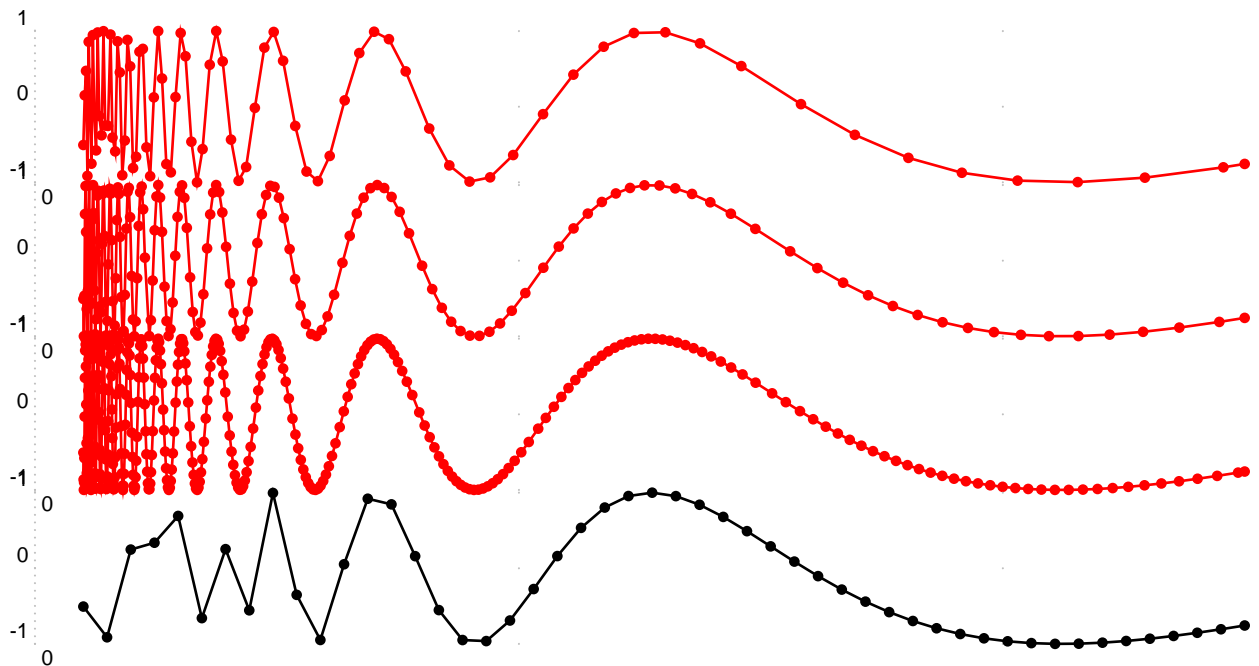
A really classic example which gives a bad beginning, the tolerance is set to 0.001.



```
\psset{algebraic=true, VarStep=true, linecolor=red, showpoints=true}
\begin{pspicture}[showgrid=true](0,-5)(16,4)
  \psplot[VarStep=false, linecolor=black]{.01}{16}{ln(x)+1}
  \psplot[linecolor=magenta]{.51}{16}{ln(x-1/2)+1/2}
  \psplot[VarStepEpsilon=.001]{1.01}{16}{ln(x-1)}
  \psplot[VarStepEpsilon=.01]{1.51}{16}{ln(x-1.5)-100/200}
\end{pspicture}
```

23.4. Sine of the inverse of x

Impossible to draw, but let's try!

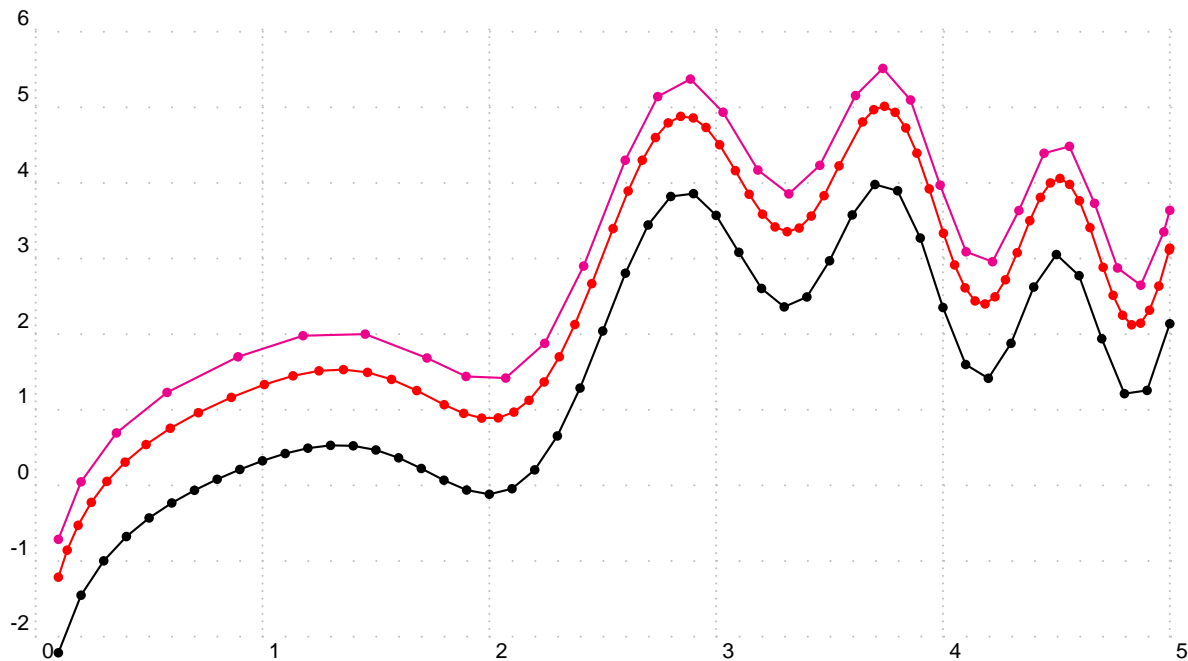


```
\psset{xunit=64,algebraic=true,VarStep,linecolor=red,showpoints=true,linewidth
=1pt}
\begin{pspicture}[showgrid=true](0,-1)(.5,1)
  \psplot[VarStepEpsilon=.0001]{.01}{.25}{sin(1/x)}
\end{pspicture}\\
\begin{pspicture}[showgrid=true](0,-1)(.5,1)
  \psplot[VarStepEpsilon=.00001]{.01}{.25}{sin(1/x)}
\end{pspicture}\\
\begin{pspicture}[showgrid=true](0,-1)(.5,1)
  \psplot[VarStepEpsilon=.000001]{.01}{.25}{sin(1/x)}
\end{pspicture}\\
\begin{pspicture}[showgrid=true](0,-1)(.5,1)
  \psplot[VarStep=false, linecolor=black]{.01}{.25}{sin(1/x)}
\end{pspicture}
```

23.5. A really complicated function

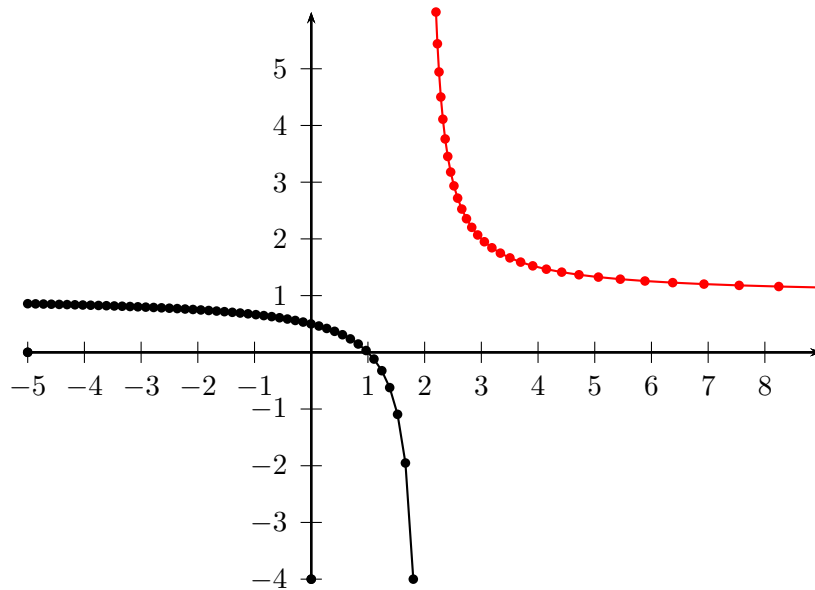
Just appreciate the difference between the normal behavior and the plotting with the `varStep` option. The function is:

$$f(x) = x - \frac{x^2}{10} + \ln(x) + \cos(2x) + \sin(x^2) - 1$$



```
\psset{xunit=3, algebraic=true, VarStep, showpoints=true}
\begin{pspicture}[showgrid=true](0,-2)(5,6)
  \psplot[VarStepEpsilon=.0005, linecolor=red]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+
    sin(x^2)}
  \psplot[linecolor=magenta]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+sin(x^2)+.5}
  \psplot[VarStep=false]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+sin(x^2)-1}
\end{pspicture}
```

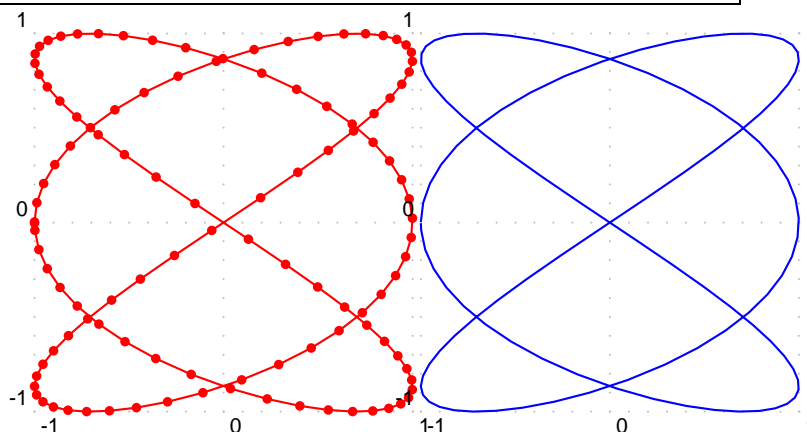
23.6. A hyperbola



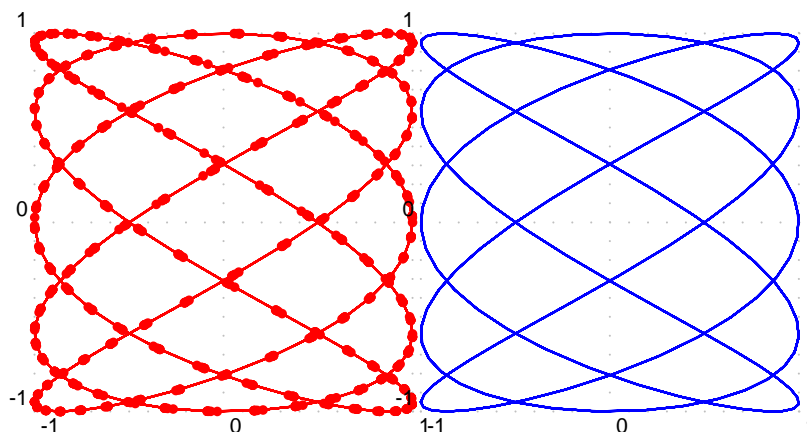
```
\psset{algebraic=true, showpoints=true, unit=0.75}
\begin{pspicture}(-5,-4)(9,6)
  \psplot[linecolor=black]{-5}{1.8}{(x-1)/(x-2)}
  \psplot[VarStep=true, VarStepEpsilon=.001, linecolor=red]{2.2}{9}{(x-1)/(x-2)}
}
\psaxes{->}(0,0)(-5,-4)(9,6)
\end{pspicture}
```

23.7. Using \psparametricplot

`\parametricplot` [Options] { t_0 }{ t_1 } [PS commands] { $x(t)$ $y(t)$ }

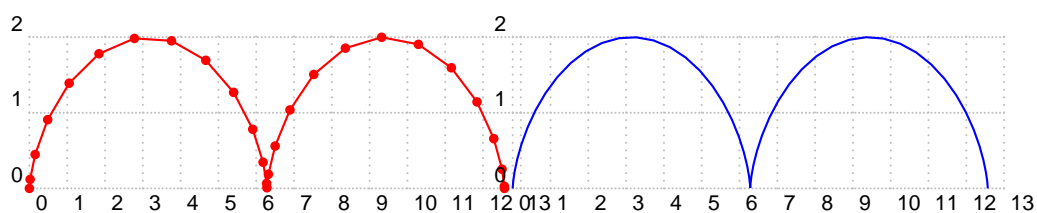


```
\psset{unit=3}
\begin{pspicture}[showgrid=true](-1,-1)(1,1)
\parametricplot[algebraic=true,linecolor=red,VarStep=true, showpoints=true,
  VarStepEpsilon=.0001]
  {-3.14}{3.14}{cos(3*t)|sin(2*t)}
\end{pspicture}
\begin{pspicture}[showgrid=true](-1,-1)(1,1)
\parametricplot[algebraic=true,linecolor=blue,VarStep=true, showpoints=false,
  VarStepEpsilon=.0001]
  {-3.14}{3.14}{cos(3*t)|sin(2*t)}
\end{pspicture}
```



```
\psset{unit=2.5}
\begin{pspicture}[showgrid=true](-1,-1)(1,1)
\parametricplot[algebraic=true,linecolor=red,VarStep=true, showpoints=true,
  VarStepEpsilon=.0001]
  {0}{47.115}{cos(5*t)|sin(3*t)}
\end{pspicture}
\begin{pspicture}[showgrid=true](-1,-1)(1,1)
\parametricplot[algebraic=true,linecolor=blue,VarStep=true, showpoints=false,
  VarStepEpsilon=.0001]
  {0}{47.115}{cos(5*t)|sin(3*t)}
\end{pspicture}
```

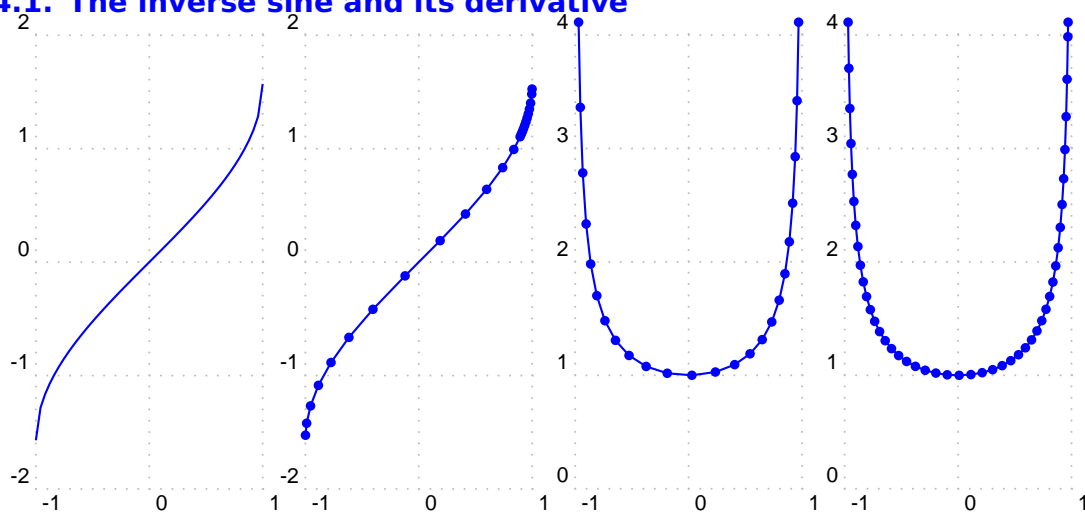
```
{0}{47.115}{cos(5*t)|sin(3*t)}
\end{pspicture}
```



```
\psset{xunit=.5}
\begin{pspicture}[showgrid=true](0,0)(12.566,2)
\parametricplot[algebraic=true,linecolor=red,VarStep, showpoints=true,
  VarStepEpsilon=.01]{0}{12.566}{t+cos(-t-Pi/2)|1+sin(-t-Pi/2)}
\end{pspicture}
%
\begin{pspicture}[showgrid=true](0,0)(12.566,2)
\parametricplot[algebraic=true,linecolor=blue,VarStep, showpoints=false,
  VarStepEpsilon=.001]{0}{12.566}{t+cos(-t-Pi/2)|1+sin(-t-Pi/2)}
\end{pspicture}
```

24. New math functions and their derivatives

24.1. The inverse sine and its derivative



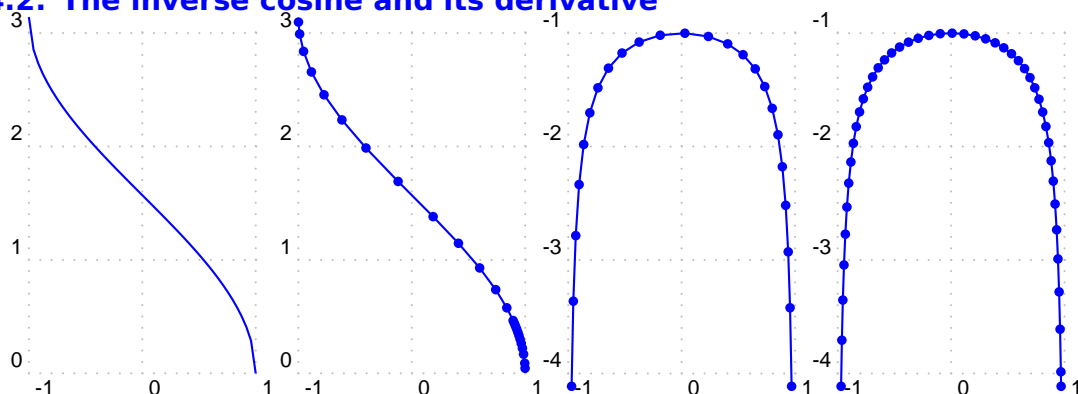
```
\psset{unit=1.5}
\begin{pspicture}[showgrid=true](-1,-2)(1,2)
\psplot[linecolor=blue,algebraic=true]{-1}{1}{asin(x)}
\end{pspicture}
\hspace{1em}
\psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
\begin{pspicture}[showgrid=true](-1,-2)(1,2)
\psplot[linecolor=blue]{-.999}{.999}{asin(x)}
\end{pspicture}
\hspace{1em}
```

```

\begin{pspicture}[showgrid=true](-1,0)(1,4)
  \psplot[linecolor=red]{-.97}{.97}{Derive(1,asin(x))}
\end{pspicture}
\hspace{1em}
\psset{algebraic=true, VarStep, VarStepEpsilon=.0001, showpoints=true}
\begin{pspicture}[showgrid=true](-1,0)(1,4)
  \psplot[linecolor=red]{-.97}{.97}{Derive(1,asin(x))}
\end{pspicture}

```

24.2. The inverse cosine and its derivative

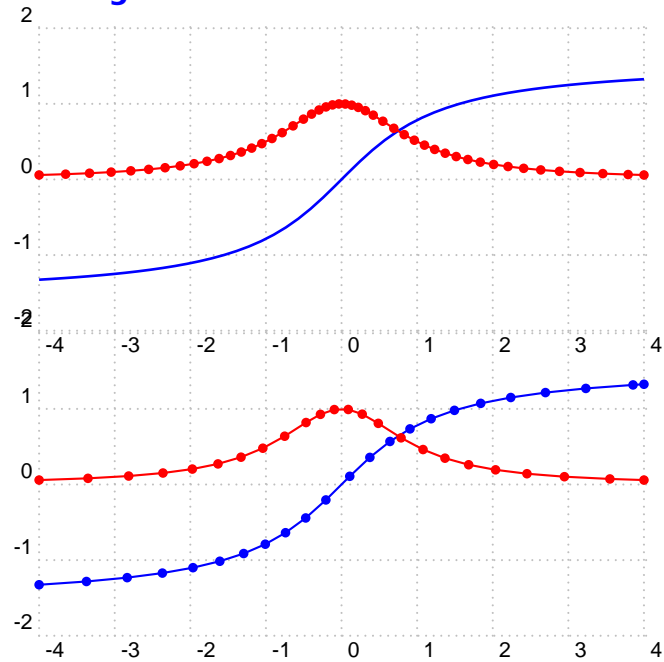


```

\psset{unit=1.5}
\begin{pspicture}[showgrid=true](-1,0)(1,3)
  \psplot[linecolor=blue,algebraic=true]{-1}{1}{acos(x)}
\end{pspicture}
\hspace{1em}
\psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
\begin{pspicture}[showgrid=true](-1,0)(1,3)
  \psplot[linecolor=blue]{-.999}{.999}{acos(x)}
\end{pspicture}
\hspace{1em}
\begin{pspicture}[showgrid=true](-1,-4)(1,-1)
  \psplot[linecolor=red]{-.97}{.97}{Derive(1,acos(x))}
\end{pspicture}
\hspace{1em}
\psset{algebraic=true, VarStep, VarStepEpsilon=.0001, showpoints=true}
\begin{pspicture}[showgrid=true](-1,-4)(1,-1)
  \psplot[linecolor=red]{-.97}{.97}{Derive(1,acos(x))}
\end{pspicture}

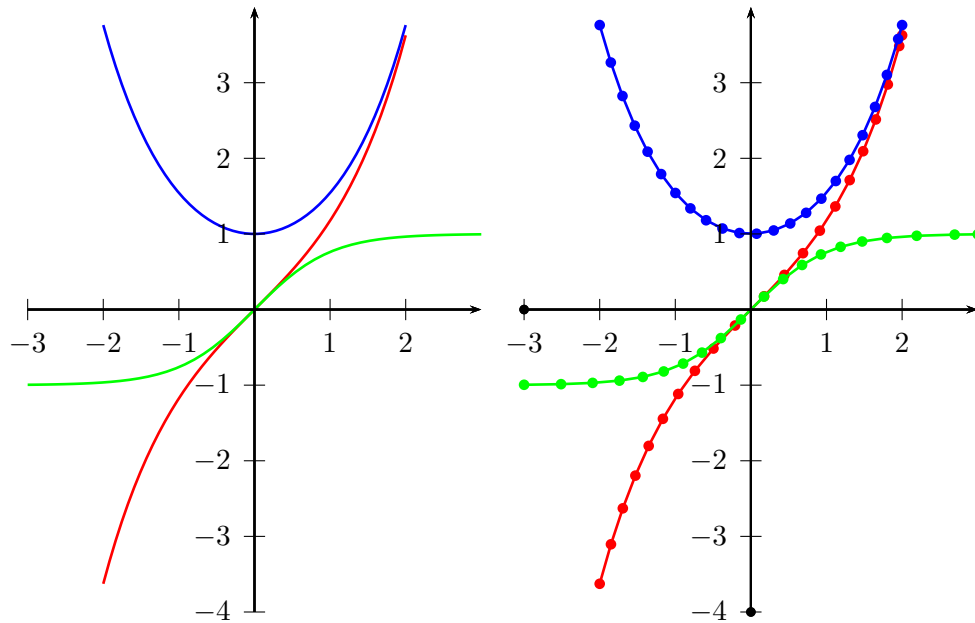
```

24.3. The inverse tangent and its derivative

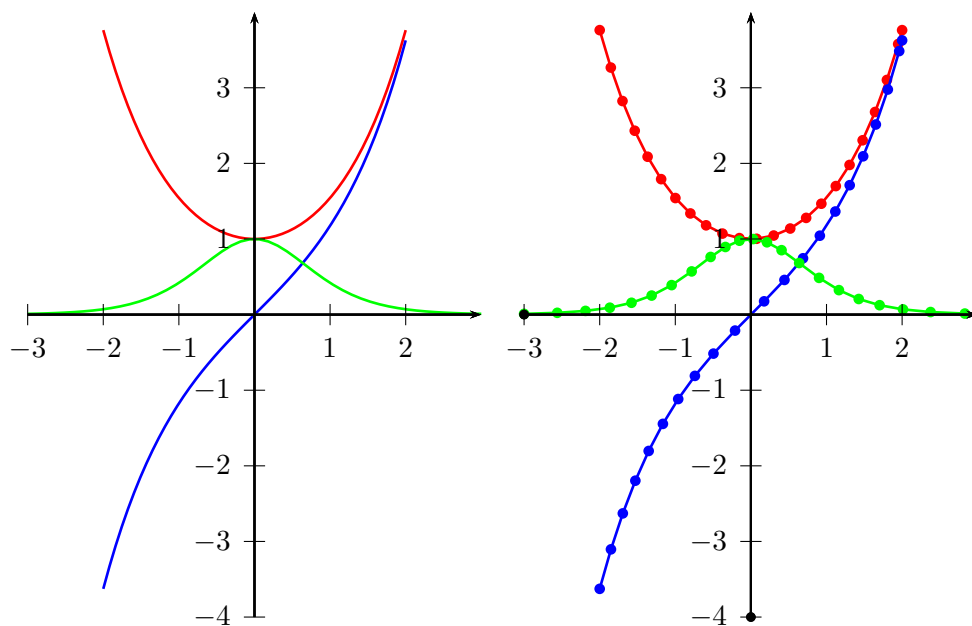


```
\begin{pspicture}[showgrid=true](-4,-2)(4,2)
\psset{algebraic=true}
\psplot[linecolor=blue,linewidth=1pt]{-4}{4}{atg(x)}
\psplot[linecolor=red,VarStep, VarStepEpsilon=.0001, showpoints=true]{-4}{4}{
  Derive(1,atg(x))}
\end{pspicture}
\hspace{1em}
\begin{pspicture}[showgrid=true](-4,-2)(4,2)
\psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
\psplot[linecolor=blue]{-4}{4}{atg(x)}
\psplot[linecolor=red]{-4}{4}{Derive(1,atg(x))}
\end{pspicture}
```


24.4. Hyperbolic functions



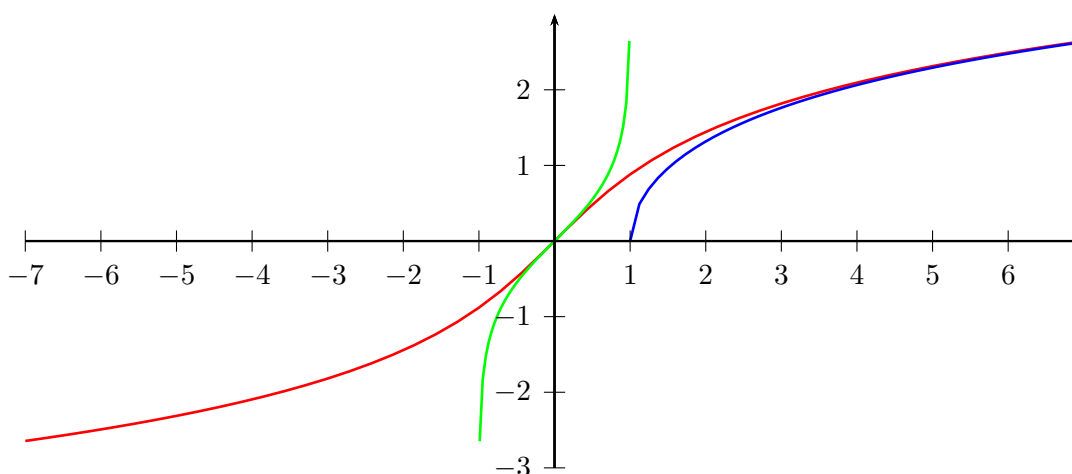
```
\begin{pspicture}(-3,-4)(3,4)
\psset{algebraic=true}
\psplot[linecolor=red,linewidth=1pt]{-2}{2}{sh(x)}
\psplot[linecolor=blue,linewidth=1pt]{-2}{2}{ch(x)}
\psplot[linecolor=green,linewidth=1pt]{-3}{3}{th(x)}
\psaxes{->}(0,0)(-3,-4)(3,4)
\end{pspicture}
\hspace{1em}
\begin{pspicture}(-3,-4)(3,4)
\psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
\psplot[linecolor=red,linewidth=1pt]{-2}{2}{sh(x)}
\psplot[linecolor=blue,linewidth=1pt]{-2}{2}{ch(x)}
\psplot[linecolor=green,linewidth=1pt]{-3}{3}{th(x)}
\psaxes{->}(0,0)(-3,-4)(3,4)
\end{pspicture}
```

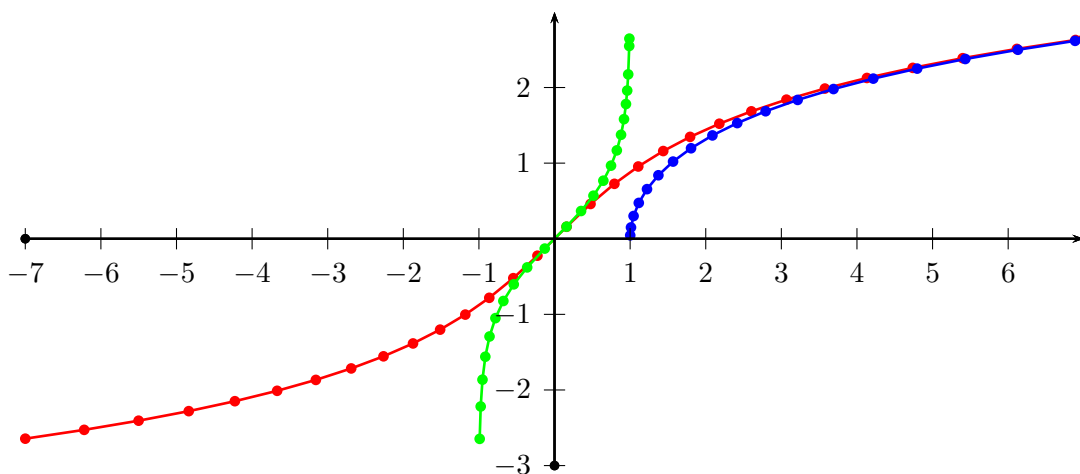


```

\begin{pspicture}(-3,-4)(3,4)
\psset{algebraic=true,linewidth=1pt}
\psplot[linecolor=red,linewidth=1pt]{-2}{2}{Derive(1,sh(x))}
\psplot[linecolor=blue,linewidth=1pt]{-2}{2}{Derive(1,ch(x))}
\psplot[linecolor=green,linewidth=1pt]{-3}{3}{Derive(1,th(x))}
\psaxes{->}(0,0)(-3,-4)(3,4)
\end{pspicture}
\hspace{1em}
\begin{pspicture}(-3,-4)(3,4)
\psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
\psplot[linecolor=red,linewidth=1pt]{-2}{2}{Derive(1,sh(x))}
\psplot[linecolor=blue,linewidth=1pt]{-2}{2}{Derive(1,ch(x))}
\psplot[linecolor=green,linewidth=1pt]{-3}{3}{Derive(1,th(x))}
\psaxes{->}(0,0)(-3,-4)(3,4)
\end{pspicture}

```

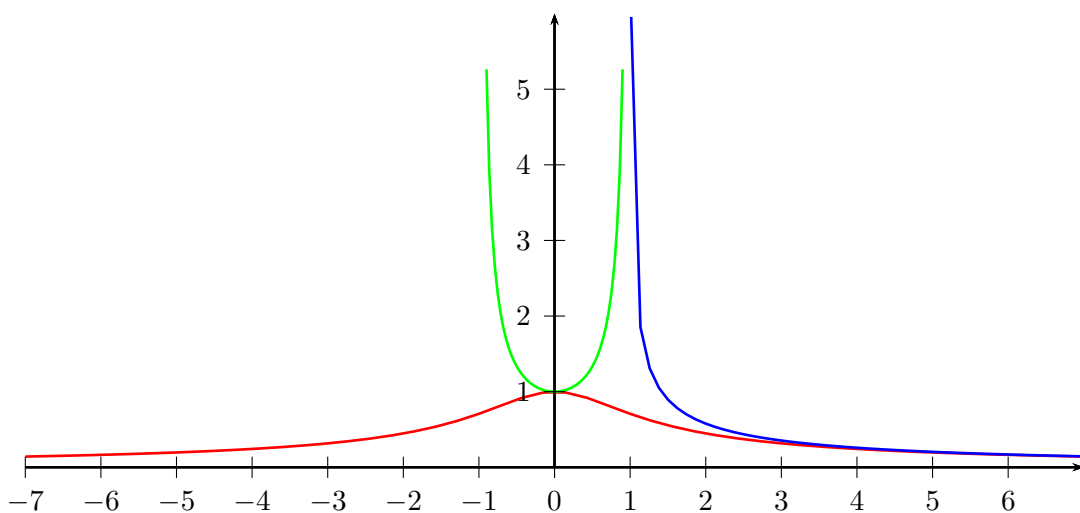


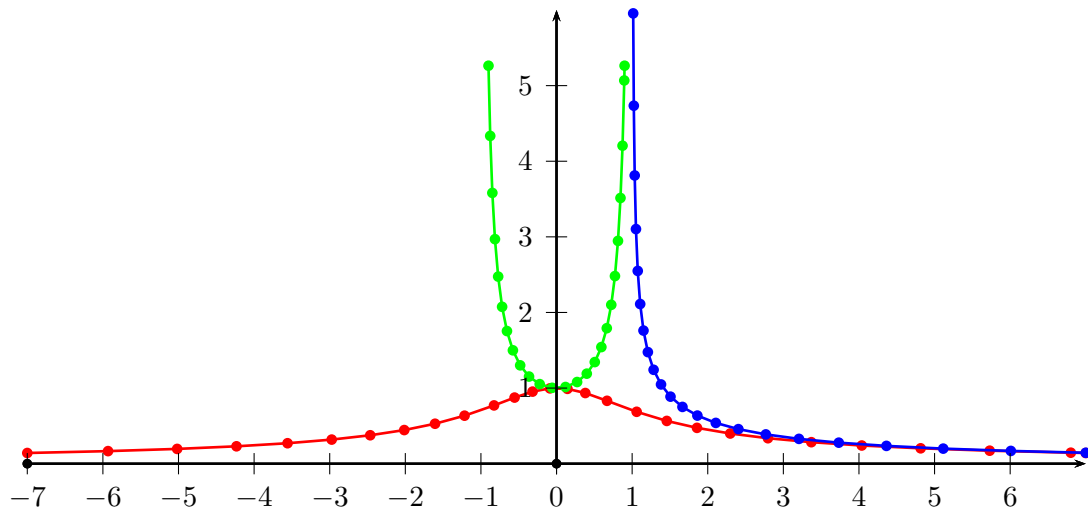


```

\begin{pspicture}(-7,-3)(7,3)
\psset{algebraic=true}
\psplot[linecolor=red,linewidth=1pt]{-7}{7}{Argsh(x)}
\psplot[linecolor=blue,linewidth=1pt]{1}{7}{Argch(x)}
\psplot[linecolor=green,linewidth=1pt]{-.99}{.99}{Argth(x)}
\psaxes{->}(0,0)(-7,-3)(7,3)
\end{pspicture}
\begin{pspicture}(-7,-3)(7,3)
\psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
\psplot[linecolor=red,linewidth=1pt]{-7}{7}{Argsh(x)}
\psplot[linecolor=blue,linewidth=1pt]{1.001}{7}{Argch(x)}
\psplot[linecolor=green,linewidth=1pt]{-.99}{.99}{Argth(x)}
\psaxes{->}(0,0)(-7,-3)(7,3)
\end{pspicture}

```





```

\begin{pspicture}(-7,-0.5)(7,6)
\psset{algebraic=true}
\psplot[linecolor=red,linewidth=1pt]{-7}{7}{Derive(1,Argsh(x))}
\psplot[linecolor=blue,linewidth=1pt]{1.014}{7}{Derive(1,Argch(x))}
\psplot[linecolor=green,linewidth=1pt]{-.9}{.9}{Derive(1,Argth(x))}
\psaxes{->}(0,0)(-7,0)(7,6)
\end{pspicture}\[\baselineskip]
\begin{pspicture}(-7,-0.5)(7,6)
\psset{algebraic=true}
\psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
\psplot[linecolor=red,linewidth=1pt]{-7}{7}{Derive(1,Argsh(x))}
\psplot[linecolor=blue,linewidth=1pt]{1.014}{7}{Derive(1,Argch(x))}
\psplot[linecolor=green,linewidth=1pt]{-.9}{.9}{Derive(1,Argth(x))}
\psaxes{->}(0,0)(-7,0)(7,6)
\end{pspicture}

```

25. \psplotDiffEqn – solving differential equations

A differential equation of first order is like

$$y' = f(x, y, y') \quad (1)$$

where y is a function of x . We define some vectors $Y = [y, y', \dots, y^{(n-1)}]$ and $Y' = [y', y'', \dots, y^{(n)}]$, depending on the order n . The syntax of the macro is

`\psplotDiffEqn [Options] {x0}{x1}{y0}{f(x,y,y',...)}{}`

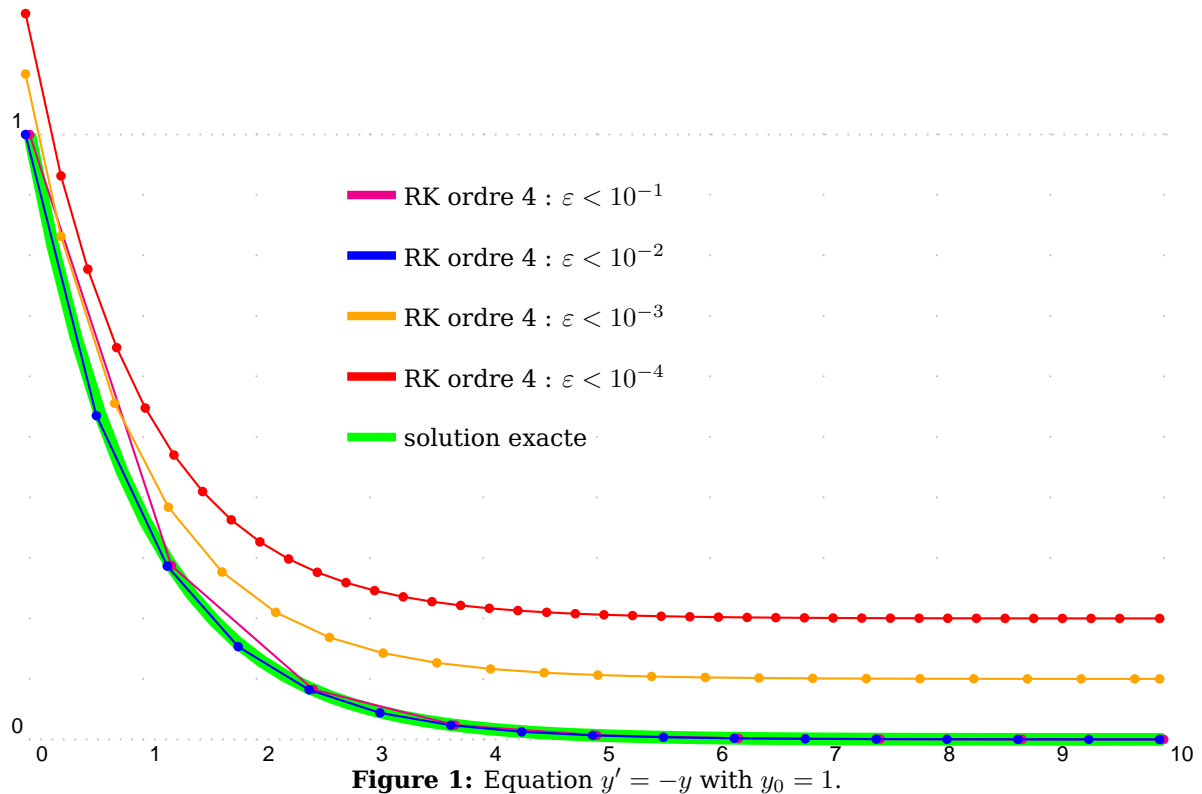
- options: the \psplotDiffEqn specific options and all other of PSTricks, which make sense;
- x_0 : the start value;
- x_1 : the end value of the definition interval;
- y_0 : the initial values for $y(x_0)$ $y'(x_0)$...;
- $f(x, y, y', \dots)$: the differential equation, depending to the number of initial values, e.g.: `{0 1}` for y_0 are two initial values, so that we have a differential equation of second order $f(x, y, y')$ and the macro leaves y y' on the stack.

The new options are:

- method: integration method (euler for order 1 euler method, rk4 for 4th order Runge-Kutta method);
- whichabs: select the abscissa for plotting the graph, by default it is x , but you can specify a number which represent a position in the vector y ;
- whichord: same as precedent for the ordinate, by default $y(0)$;
- plotfuncx: describe a ps function for the abscissa, parameter whichabs becomes useless;
- plotfuncy: idem for the ordinate;
- buildvector: boolean parameter for specifying the input-output of the f description:
 - true* (default): y is put on the stack element by element, y' must be given in the same way;
 - false* : y is put on the stack as a vector, y' must be returned in the same way;
- algebraic=true: algebraic=true description for f , buildvector parameter is useless when activating this option.

25.1. Variable step for differential equations

A new algorithm has been added for adjusting the step according to the variations of the curve. The parameter `method` has a new possible value : `varrkiv` to activate the Runge-Kutta method with variable step, then the parameter `varsteptol` (real value; .01 by default) can control the tolerance of the algorithm.



```
\def\Funct{neg}\def\FunctAlg{-y[0]}
\psset{xunit=1.5, yunit=8, showpoints=true}
\begin{pspicture}[showgrid=true](0,0)(10,1.2)
  \psplot[linewidth=6\pslinewidth, linecolor=green, showpoints=false]{0}{10}{
    Euler x neg exp}
  \psplotDiffEqn[linecolor=magenta, method=varrkiv, varsteptol=.1, plotpoints
    =2]{0}{10}{1}{\Funct}
  \rput(0,.0){\psplotDiffEqn[linecolor=blue, method=varrkiv, varsteptol=.01,
    plotpoints=2]{0}{10}{1}{\Funct}}
  \rput(0,.1){\psplotDiffEqn[linecolor=orange, method=varrkiv, varsteptol=.001,
    plotpoints=2]{0}{10}{1}{\Funct}}
  \rput(0,.2){\psplotDiffEqn[linecolor=red, method=varrkiv, varsteptol=.0001,
    plotpoints=2]{0}{10}{1}{\Funct}}
  \psset{linewidth=4\pslinewidth, showpoints=false}
  \rput*(3.3,.9){\psline[linecolor=magenta](-.75cm,0)}
  \rput*[l](3.3,.9){\small RK ordre 4 :  $\varepsilon < 10^{-1}$ }
  \rput*(3.3,.8){\psline[linecolor=blue](-.75cm,0)}
  \rput*[l](3.3,.8){\small RK ordre 4 :  $\varepsilon < 10^{-2}$ }
  \rput*(3.3,.7){\psline[linecolor=orange](-.75cm,0)}
```

```

\put*(l)(3.3,.7){\small RK ordre 4 :  $\varepsilon < 10^{-3}$ }
\put*(3.3,.6){\psline[linecolor=red](-.75cm,0)}
\put*(l)(3.3,.6){\small RK ordre 4 :  $\varepsilon < 10^{-4}$ }
\put*(3.3,.5){\psline[linecolor=green](-.75cm,0)}
\put*(l)(3.3,.5){\small solution exacte}
\end{pspicture}

```

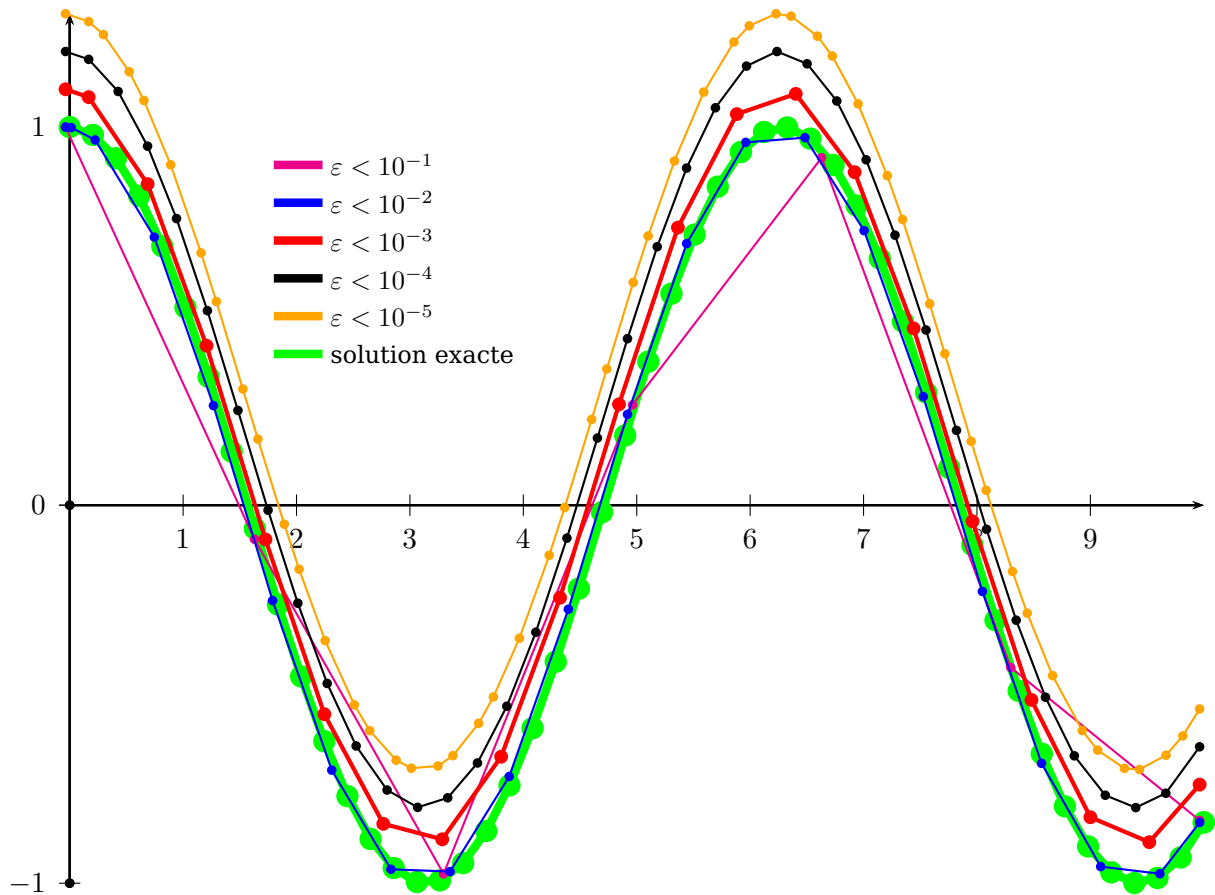


Figure 2: Equation $y'' = -y$

```

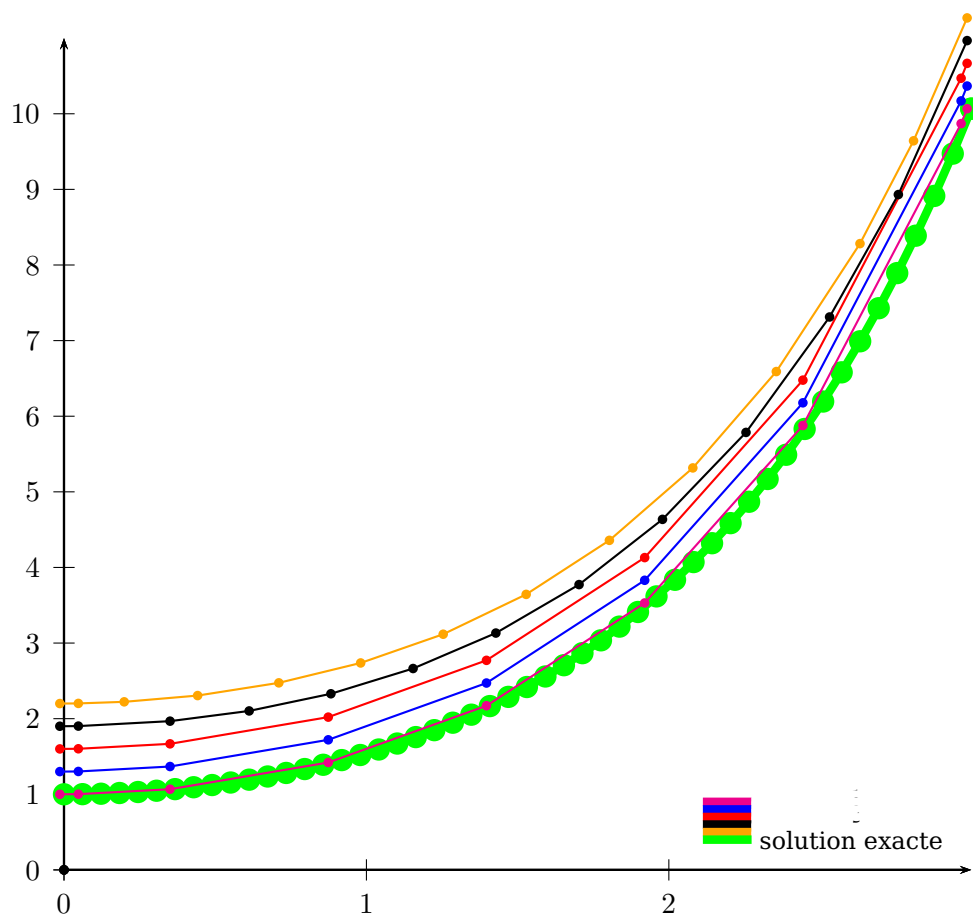
\def\Func{exch neg}
\psset{xunit=1.5, yunit=5, method=varrkiv, showpoints=true}%%
\def\quatrepi{12.5663706144}
\begin{pspicture}(0,-1)(10,1.3)
  \psaxes{>->}(0,0)(0,-1)(10,1.3)
  \psplot[linewidth=4\pslinewidth, linecolor=green, algebraic=true]{0}{10}{cos(
    x)}
  \rput(0,.0){\psplotDiffEqn[linecolor=magenta, plotpoints=7, varsteptol
    =.1]{0}{10}{1 0}{\Func}}
  \rput(0,.0){\psplotDiffEqn[linecolor=blue, plotpoints=201, varsteptol
    =.01]{0}{10}{1 0}{\Func}}
  \rput(0,.1){\psplotDiffEqn[linecolor=red, plotpoints=100, varsteptol
    =.001]{0}{10}{1 0}{\Func}}
  \rput(0,.2){\psplotDiffEqn[linecolor=black, plotpoints=1000, varsteptol=.0001]{0}{10}{1 0}{\Func}}
\end{pspicture}

```

```

\put(0,.3){\psplotDiffEqn[linecolor=orange, varsteptol=.00001]{0}{10}{1 0}{\
  Funct}}
\psset{linewidth=4\pslinewidth,showpoints=false}
\put*(2.3,.9){\psline[linecolor=magenta](-.75cm,0)}
\put*[l](2.3,.9){\small $\varepsilon<10^{-1}$}
\put*(2.3,.8){\psline[linecolor=blue](-.75cm,0)}
\put*[l](2.3,.8){\small $\varepsilon<10^{-2}$}
\put*(2.3,.7){\psline[linecolor=red](-.75cm,0)}
\put*[l](2.3,.7){\small $\varepsilon<10^{-3}$}
\put*(2.3,.6){\psline[linecolor=black](-.75cm,0)}
\put*[l](2.3,.6){\small $\varepsilon<10^{-4}$}
\put*(2.3,.5){\psline[linecolor=orange](-.75cm,0)}
\put*[l](2.3,.5){\small $\varepsilon<10^{-5}$}
\put*(2.3,.4){\psline[linecolor=green](-.75cm,0)}
\put*[l](2.3,.4){\small solution exacte}
\end{pspicture}

```

Figure 3: Equation $y'' = y$

```

\def\Funct{exch}
\psset{xunit=4, yunit=1, method=varrkiv, showpoints=true}%%
\def\quatrepi{12.5663706144}
\begin{pspicture}(0,-0.5)(3,11)

```



```

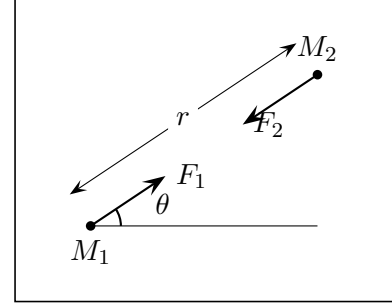
\psaxes{->}(0,0)(3,11)
\psplot[linewidth=4\pslinewidth, linecolor=green, algebraic=true]{0}{3}{ch(x)
}
\rput(0,.0){\psplotDiffEqn[linecolor=magenta, varsteptol=.1]{0}{3}{1 0}{\
Func}}
\rput(0,.3){\psplotDiffEqn[linecolor=blue, varsteptol=.01]{0}{3}{1 0}{\Func
}}
\rput(0,.6){\psplotDiffEqn[linecolor=red, varsteptol=.001]{0}{3}{1 0}{\Func
}}
\rput(0,.9){\psplotDiffEqn[linecolor=black, varsteptol=.0001]{0}{3}{1 0}{\
Func}}
\rput(0,1.2){\psplotDiffEqn[linecolor=Orange, varsteptol=.00001]{0}{3}{1 0}{\
Func}}
\psset{linewidth=4\pslinewidth, showpoints=false}
\rput*(2.3,.9){\psline[linecolor=magenta](-.75cm,0)}
\rput*[l](2.3,.9){\small $\varepsilon<10^{-1}$}
\rput*(2.3,.8){\psline[linecolor=blue](-.75cm,0)}
\rput*[l](2.3,.8){\small $\varepsilon<10^{-2}$}
\rput*(2.3,.7){\psline[linecolor=red](-.75cm,0)}
\rput*[l](2.3,.7){\small $\varepsilon<10^{-3}$}
\rput*(2.3,.6){\psline[linecolor=black](-.75cm,0)}
\rput*[l](2.3,.6){\small $\varepsilon<10^{-4}$}
\rput*(2.3,.5){\psline[linecolor=Orange](-.75cm,0)}
\rput*[l](2.3,.5){\small $\varepsilon<10^{-5}$}
\rput*(2.3,.4){\psline[linecolor=green](-.75cm,0)}
\rput*[l](2.3,.4){\small solution exacte}
\end{pspicture}

```

25.2. Equation of second order

Here is the traditional simulation of two stars attracting each other according to the classical gravitation law in $\frac{1}{r^2}$. In 2-Dimensions, the system to be solved is composed of four second order differential equations. In order to be described, each of them gives two first order equations, then we obtain a 8 sized vectorial equation. In the following example the masses of the stars are 1 and 20.

$$\begin{cases} x_1'' = \frac{M_2}{r^2} \cos(\theta) \\ y_1'' = \frac{M_2}{r^2} \sin(\theta) \\ x_2'' = \frac{M_1}{r^2} \cos(\theta) \\ y_2'' = \frac{M_1}{r^2} \sin(\theta) \end{cases} \text{ avec } \begin{cases} r^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2 \\ \cos(\theta) = \frac{(x_1 - x_2)}{r} \\ \sin(\theta) = \frac{(y_1 - y_2)}{r} \end{cases}$$



```

%% x1 y1 x'1 y'1 x2 y2 x'2 y'2
/yp2 exch def /xp2 exch def /ay2 exch def /ax2 exch def %% mise en variables
/yp1 exch def /xp1 exch def /ay1 exch def /ax1 exch def %% mise en variables
/ro2 ax2 ax1 sub dup mul ay2 ay1 sub dup mul add def %% calcul de r*r
xp1 yp1 %%
ax2 ax1 sub ro2 sqrt div ro2 div %% calcul de x''1
ay2 ay1 sub ro2 sqrt div ro2 div %% calcul de y''1
xp2 yp2 %%
3 index -20 mul %% calcul de x''2=-20x''1
3 index -20 mul %% calcul de y''2=-20y''1

```

Table 1: PostScript source code for the gravitational interaction

```

y[2]| %% y'[0]
y[3]| %% y'[1]
(y[4]-y[0])/((y[4]-y[0])^2+(y[5]-y[1])^2)^1.5| %% y'[2]=y''[0]
(y[5]-y[1])/((y[4]-y[0])^2+(y[5]-y[1])^2)^1.5| %% y'[3]=y''[1]
y[6]| %% y'[4]
y[7]| %% y'[5]
20*(y[0]-y[4])/((y[4]-y[0])^2+(y[5]-y[1])^2)^1.5| %% y'[6]=y''[4]
20*(y[1]-y[5])/((y[4]-y[0])^2+(y[5]-y[1])^2)^1.5| %% y'[7]=y''[5]

```

Table 2: Algebraic description for the gravitational interaction

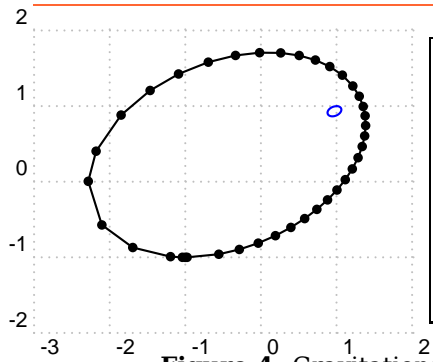


Figure 4: Gravitational interaction: fixed landmark, trajectory of the stars

```
\def\InitCond{ 1 1 .1 0 -1 -1 -2 0}
\begin{pspicture}[shift=-2,showgrid=true](-3,-1.75)(2,1.5)
\psplotDiffEqn[whichabs=0, whichord=1, linecolor=blue, method
=rk4, plotpoints=100]{0}{3.95}{\InitCond}{\Grav}
\psset{showpoints=true,whichabs=4, whichord=5}
\psplotDiffEqn[linecolor=black, method=varrkiv, varsteptol
=.0001, plotpoints=200]{0}{3.9}{\InitCond}{\Grav}
\end{pspicture}
```

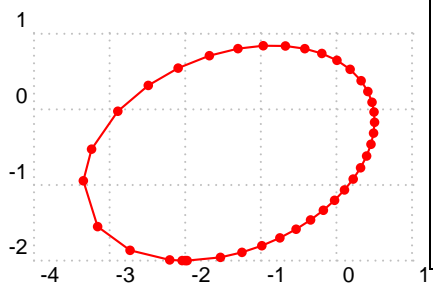


Figure 5: Gravitational interaction : landmark defined by one star

```
\def\InitCond{ 1 1 .1 0 -1 -1 -2 0}
\begin{pspicture}[shift=-1.5,showgrid=true](-4,-1.75)(1,1)
\psplotDiffEqn[linecolor=red, plotpoints=200,method=varrkiv,
varsteptol=.0001, showpoints=true,
plotfuncx=y dup 4 get exch 0 get sub,
plotfuncy=dup 5 get exch 1 get sub ]{0}{3.9}{\InitCond}{\Grav}
\end{pspicture}
```

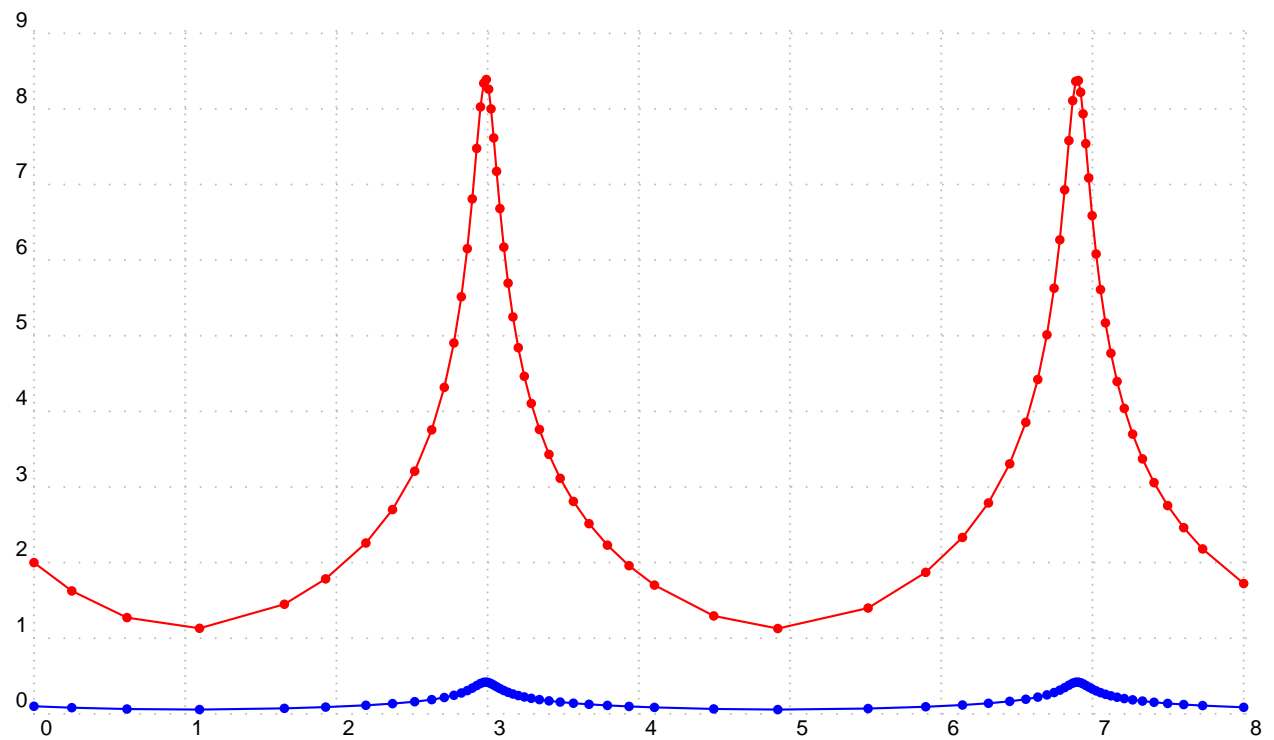


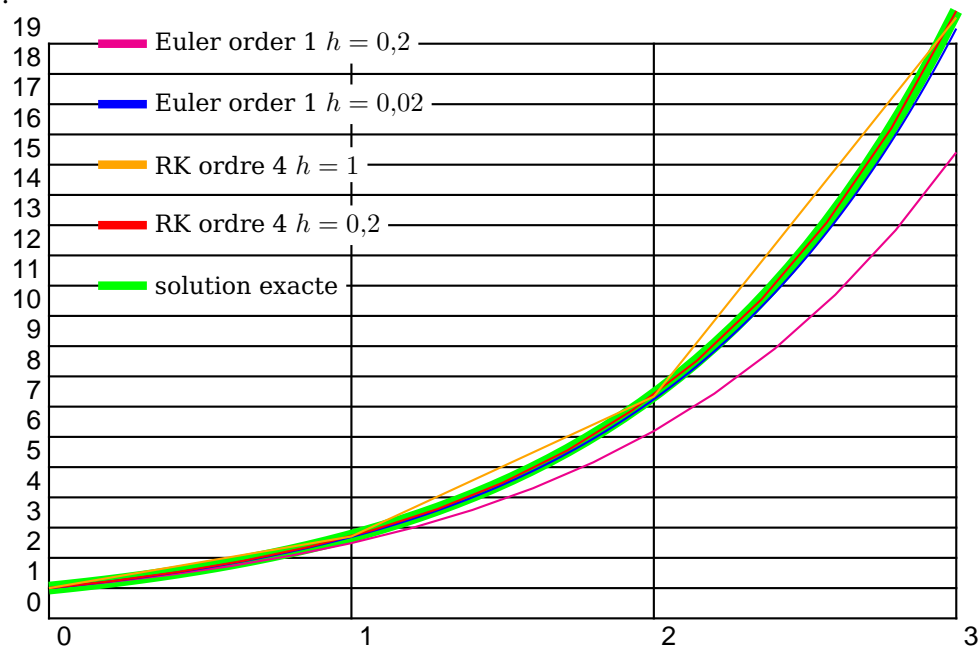
Figure 6: Gravitational interaction : speeds of the stars

```
\psset{xunit=2}
\begin{pspicture}[showgrid=true](0,0)(8,9)
\psset{showpoints=true}
```

```
\psplotDiffEqn[linecolor=red, method=varrkiv, plotpoints=2, varsteptol=.0001,  
  plotfuncy=dup 6 get dup mul exch 7 get dup mul add sqrt]{0}{8}{\InitCond  
  }{\Grav}  
\psplotDiffEqn[linecolor=blue, method=varrkiv, plotpoints=2, varsteptol  
  =.0001,  
  plotfuncy=dup 2 get dup mul exch 3 get dup mul add sqrt]{0}{8}{\InitCond  
  }{\Grav}  
\end{pspicture}
```

Simple equation of first order $y' = y$

For the initial value $y(0) = 1$ we have the solution $y(x) = e^x$. y is always on the stack, so we have to do nothing. Using the `algebraic=true` option, we write it as `y[0]`. The following example shows different solutions depending to the number of plotpoints with $y_0 = 1$:



```
\psset{xunit=4, yunit=.4}
\begin{pspicture}(3,19)\psgrid[subgriddiv=1]
  \psplot[linewidth=6\pslinewidth, linecolor=green]{0}{3}{Euler x exp}
  \psplotDiffEqn[linecolor=magenta,plotpoints=16,algebraic=true]{0}{3}{1}{y[0]}
  \psplotDiffEqn[linecolor=blue,plotpoints=151]{0}{3}{1}{y[0]}
  \psplotDiffEqn[linecolor=red,method=rk4,plotpoints=15]{0}{3}{1}{y[0]}
  \psplotDiffEqn[linecolor=orange,method=rk4,plotpoints=4]{0}{3}{1}{y[0]}
  \psset{linewidth=4\pslinewidth}
  \rput*(0.35,19){\psline[linecolor=magenta](-.75cm,0)}
  \rput*[l](0.35,19){\small Euler order 1 $h=0\{,\}2$}
  \rput*(0.35,17){\psline[linecolor=blue](-.75cm,0)}
  \rput*[l](0.35,17){\small Euler order 1 $h=0\{,\}02$}
  \rput*(0.35,15){\psline[linecolor=orange](-.75cm,0)}
  \rput*[l](0.35,15){\small RK ordre 4 $h=1$}
  \rput*(0.35,13){\psline[linecolor=red](-.75cm,0)}
  \rput*[l](0.35,13){\small RK ordre 4 $h=0\{,\}2$}
  \rput*(0.35,11){\psline[linecolor=green](-.75cm,0)}
  \rput*[l](0.35,11){\small solution exacte}
\end{pspicture}
```

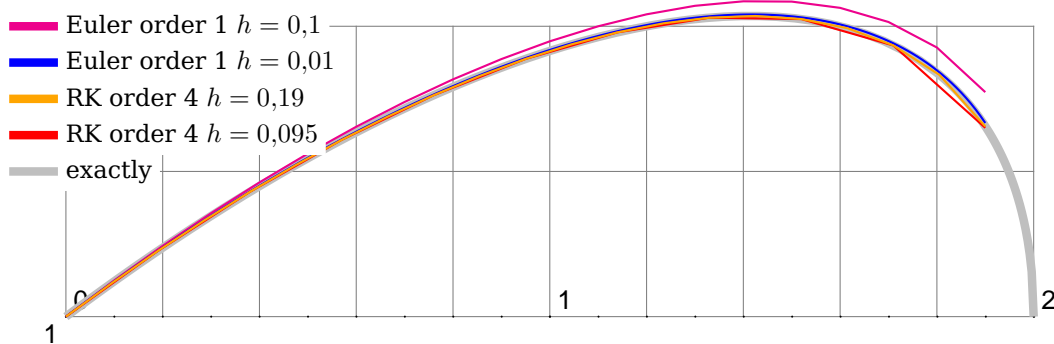
$$y' = \frac{2 - ty}{4 - t^2}$$

For the initial value $y(0) = 1$ the exact solution is $y(x) = \frac{t + \sqrt{4 - t^2}}{2}$. The function f described in PostScript code is like (y is still on the stack):

```
x          %% y x
mul        %% x*y
2 exch sub %% 2-x*y
4 x dup mul %% 2-x*y 4 x^2
sub        %% 2-x*y 4-x^2
div        %% (2-x*y)/(4-x^2)
```

The following example uses $y_0 = 1$.

```
\newcommand{\InitCond}{1}
\newcommand{\Func}{x mul 2 exch sub 4 x dup mul sub div}
\newcommand{\FuncAlg}{(2-x*y[0])/(4-x^2)}
```

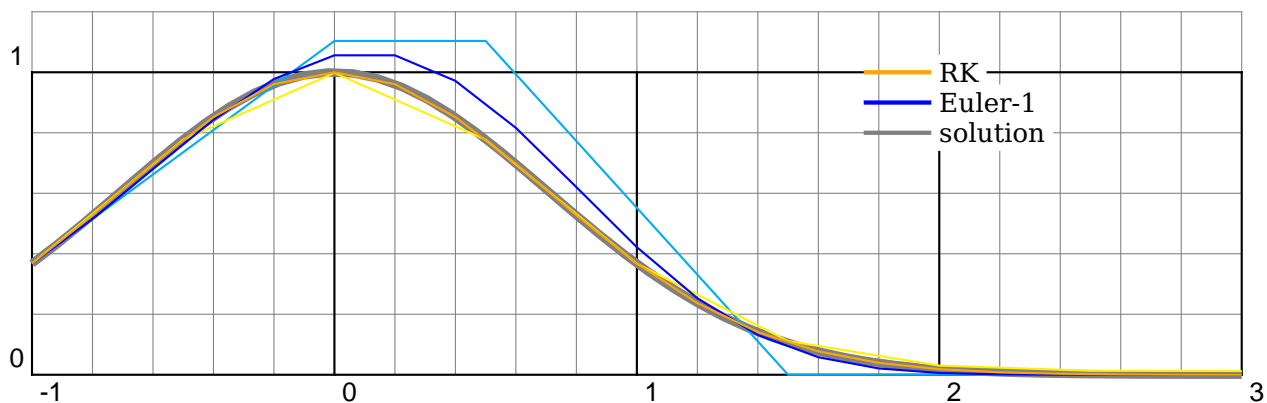


```
\psset{xunit=6.4, yunit=9.6, showpoints=false}
\begin{pspicture}(0,1)(2,1.7) \psgrid[subgriddiv=5]
{ \psset{linewidth=4\pslinewidth, linecolor=lightgray}
\psplot{0}{1.8}{x dup dup mul 4 exch sub sqrt add 2 div}
\psplot{1.8}{2}{x dup dup mul 4 exch sub sqrt add 2 div} }
\def\InitCond{1}
\def\Func{x mul 2 exch sub 4 x dup mul sub div}
\psplotDiffEqn[linecolor=magenta, plotpoints=20]{0}{1.9}{\InitCond}{\Func}
\psplotDiffEqn[linecolor=blue, plotpoints=191]{0}{1.9}{\InitCond}{\Func}
\psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11,%
algebraic=true]{0}{1.9}{\InitCond}{(2-x*y[0])/(4-x^2)}
\psplotDiffEqn[linecolor=orange, method=rk4, plotpoints=21,%
algebraic=true]{0}{1.9}{\InitCond}{(2-x*y[0])/(4-x^2)}
\psset{linewidth=4\pslinewidth}
\rput*(0.3,1.6){\psline[linecolor=magenta](-.75cm,0)}\rput*[l](0.3,1.6){\small Euler
order 1 $h=0\{, \}1\$}
\rput*(0.3,1.55){\psline[linecolor=blue](-.75cm,0)}\rput*[l](0.3,1.55){\small Euler order
1 $h=0\{, \}01\$}
\rput*(0.3,1.5){\psline[linecolor=orange](-.75cm,0)}\rput*[l](0.3,1.5){\small RK order 4
$h=0\{, \}19\$}
```

```
\rput*(0.3,1.45){\psline[linecolor=red](-.75cm,0)}\rput*[l](0.3,1.45){\small RK order 4 $  
h=0{,}095$}  
\rput*(0.3,1.4){\psline[linecolor=lightgray](-.75cm,0)}\rput*[l](0.3,1.4){\small exactly}  
\end{pspicture}
```

$$y' = -2xy$$

For $y(-1) = \frac{1}{e}$ we get $y(x) = e^{-x^2}$.



```
\psset{unit=4}
\begin{pspicture}(-1,0)(3,1.1)\psgrid
\psplot[linewidth=4\pslinewidth,linecolor=gray]{-1}{3}{Euler x dup mul neg
exp}
\psset{plotpoints=9}
\psplotDiffEqn[linecolor=cyan]{-1}{3}{1 Euler div}{x -2 mul mul}
\psplotDiffEqn[linecolor=yellow, method=rk4]{-1}{3}{1 Euler div}{x -2 mul mul}
\psset{plotpoints=21}
\psplotDiffEqn[linecolor=blue]{-1}{3}{1 Euler div}{x -2 mul mul}
\psplotDiffEqn[linecolor=orange, method=rk4]{-1}{3}{1 Euler div}{x -2 mul mul}
\psset{linewidth=2\pslinewidth}
\rput*(2,1){\psline[linecolor=orange](-0.25,0)}
\rput*[l](2,1){RK}
\rput*(2,.9){\psline[linecolor=blue](-0.25,0)}
\rput*[l](2,.9){\textsc{Euler}-1}
\rput*(2,.8){\psline[linecolor=gray](-0.25,0)}
\rput*[l](2,.8){solution}
\end{pspicture}
```


Spiral of Cornu

The integrals of Fresnel:

$$x = \int_0^t \cos \frac{\pi t^2}{2} dt \quad (2)$$

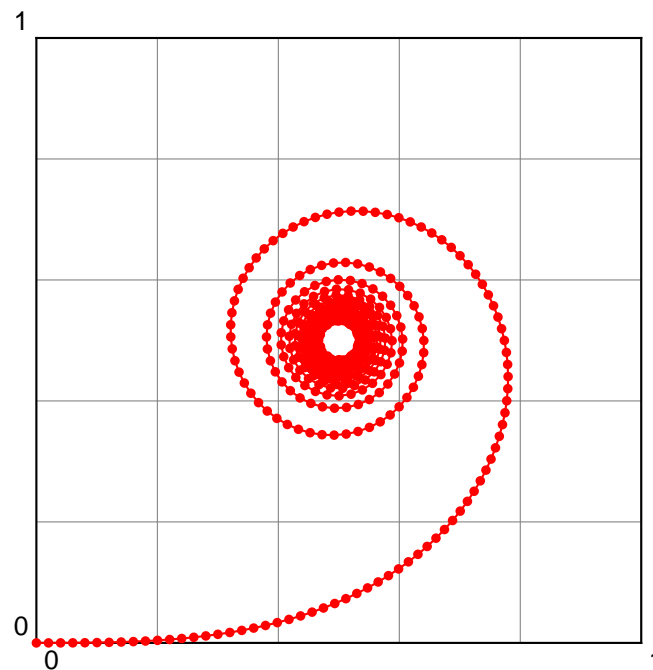
$$y = \int_0^t \sin \frac{\pi t^2}{2} dt \quad (3)$$

with

$$\dot{x} = \cos \frac{\pi t^2}{2} \quad (4)$$

$$\dot{y} = \sin \frac{\pi t^2}{2} \quad (5)$$

```
\psset{unit=8}
\begin{pspicture}(1,1)\psgrid[subgriddiv=5]
  \psplotDiffEqn[whichabs=0,whichord=1,linecolor=red,method=rk4,algebraic=true,
    %
    plotpoints=500,showpoints=true]{0}{10}{0 0}{cos(Pi*x^2/2)|sin(Pi*x^2/2)}
\end{pspicture}
```



Lotka-Volterra

The Lotka-Volterra model describes interactions between two species in an ecosystem, a predator and a prey. This represents our first multi-species model. Since we are considering two species, the model will involve two equations, one which describes how the prey population changes and the second which describes how the predator population changes.

For concreteness let us assume that the prey in our model are rabbits, and that the predators are foxes. If we let $R(t)$ and $F(t)$ represent the number of rabbits and foxes, respectively, that are alive at time t , then the Lotka-Volterra model is:

$$\dot{R} = a \cdot R - b \cdot R \cdot F \quad (6)$$

$$\dot{F} = e \cdot b \cdot R \cdot F - c \cdot F \quad (7)$$

where the parameters are defined by:

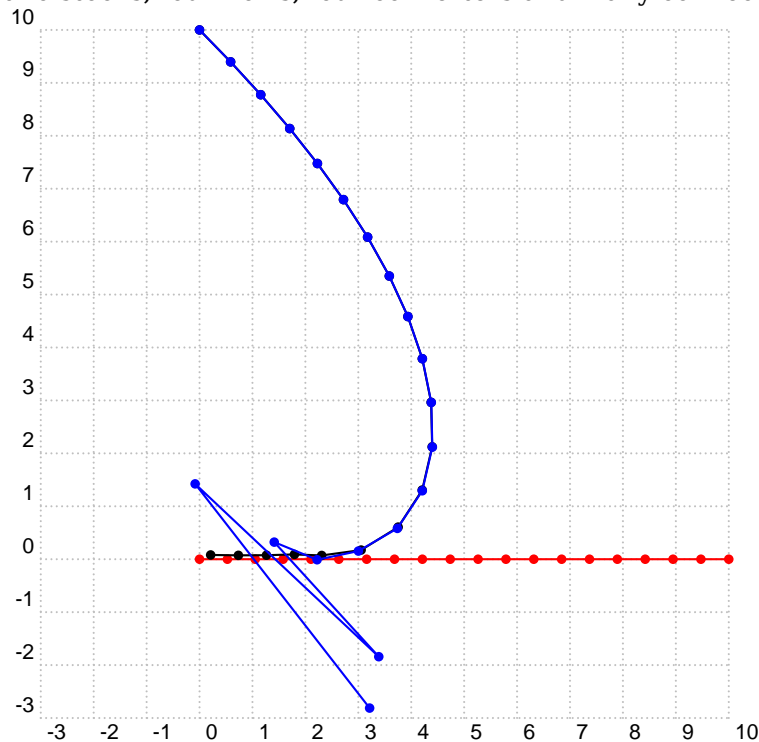
a is the natural growth rate of rabbits in the absence of predation,

c is the natural death rate of foxes in the absence of food (rabbits),

b is the death rate per encounter of rabbits due to predation,

e is the efficiency of turning predated rabbits into foxes.

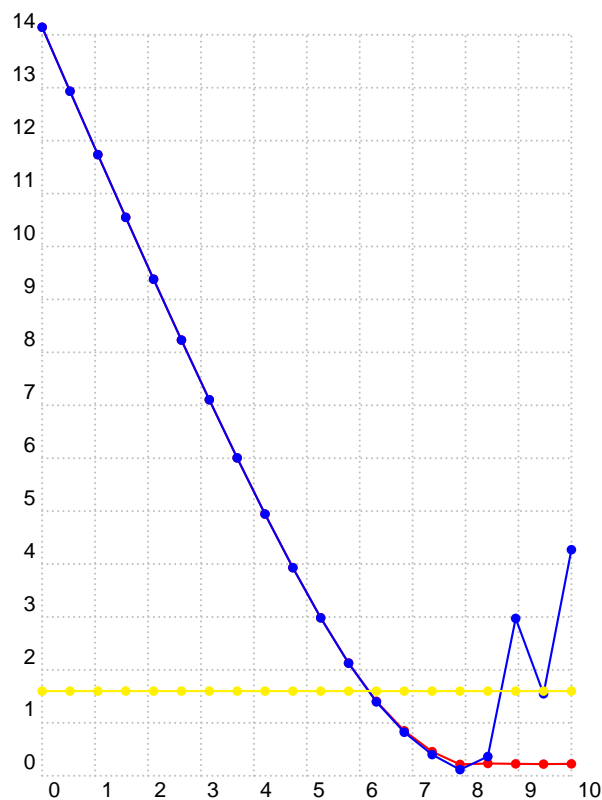
The Stella model representing the Lotka-Volterra model will be slightly more complex than the single species models we've dealt with before. The main difference is that our model will have two stocks (reservoirs), one for each species. Each species will have its own birth and death rates. In addition, the Lotka-Volterra model involves four parameters rather than two. All told, the Stella representation of the Lotka-Volterra model will use two stocks, four flows, four converters and many connectors.



```

\def\InitCond{ 0 10 10}%% xa ya xl
\def\Faiglelapin{\Vaigle*(y[2]-y[0])/sqrt(y[1]^2+(y[2]-y[0])^2)|%
  -\Vaigle*y[1]/sqrt(y[1]^2+(y[2]-y[0])^2)|%
  -\Vlapin}
\def\Vlapin{1} \def\Vaigle{1.6}
\psset{unit=.7,subgriddiv=0,gridcolor=lightgray,method=adams,algebraic=true,%
  plotpoints=20,showpoints=true}
\begin{pspicture}[showgrid=true](-3,-3)(10,10)
\psplotDiffEqn[plotfuncy=pop 0,whichabs=2,linecolor=red]{0}{10}{\InitCond}{\
  Faiglelapin}
\psplotDiffEqn[whichabs=0,whichord=1,linecolor=black,method=rk4]{0}{10}{\InitCond}{\
  Faiglelapin}
\psplotDiffEqn[whichabs=0,whichord=1,linecolor=blue]{0}{10}{\InitCond}{\Faiglelapin}
\end{pspicture}

```



```

\def\InitCond{ 0 10 10}%% xa ya xl
\def\Faiglelapin{\Vaigle*(y[2]-y[0])/sqrt(y[1]^2+(y[2]-y[0])^2)|%
  -\Vaigle*y[1]/sqrt(y[1]^2+(y[2]-y[0])^2)|%
  -\Vlapin}
\def\Vlapin{1} \def\Vaigle{1.6}
\psset{unit=.7,subgriddiv=0,gridcolor=lightgray,method=adams,algebraic=true,%
  plotpoints=20,showpoints=true}
\begin{pspicture}[showgrid=true](10,12)
\psplotDiffEqn[plotfuncy=dup 1 get dup mul exch dup 0 get exch 2 get sub dup
  mul add sqrt,linecolor=red,method=rk4]{0}{10}{\InitCond}{\Faiglelapin}
\psplotDiffEqn[plotfuncy=dup 1 get dup mul exch dup 0 get exch 2 get sub dup

```

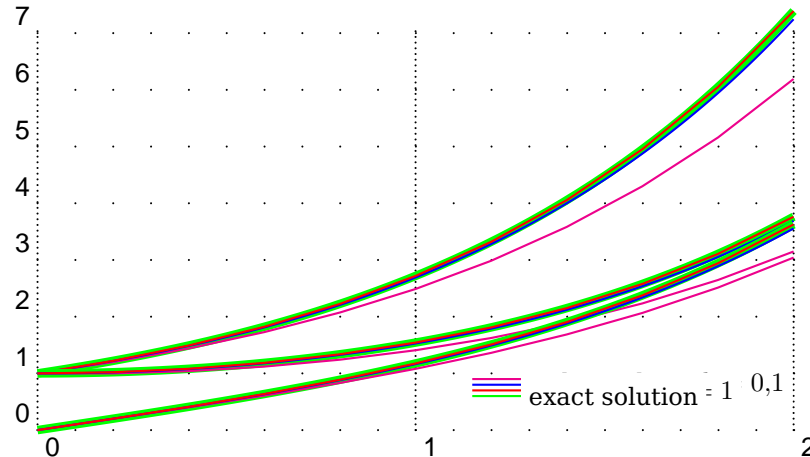
```

mul add sqrt,linecolor=blue]{0}{10}{\InitCond}{\Faiglelapin}
\psplotDiffEqn[plotfuncy=pop Func aload pop pop dup mul exch dup mul add sqrt,
linecolor=yellow]{0}{10}{\InitCond}{\Faiglelapin}
\end{pspicture}

```

$$y'' = y$$

Beginning with the initial equation $y(x) = Ae^x + Be^{-x}$ we get the hyperbolic trigonometrical functions.

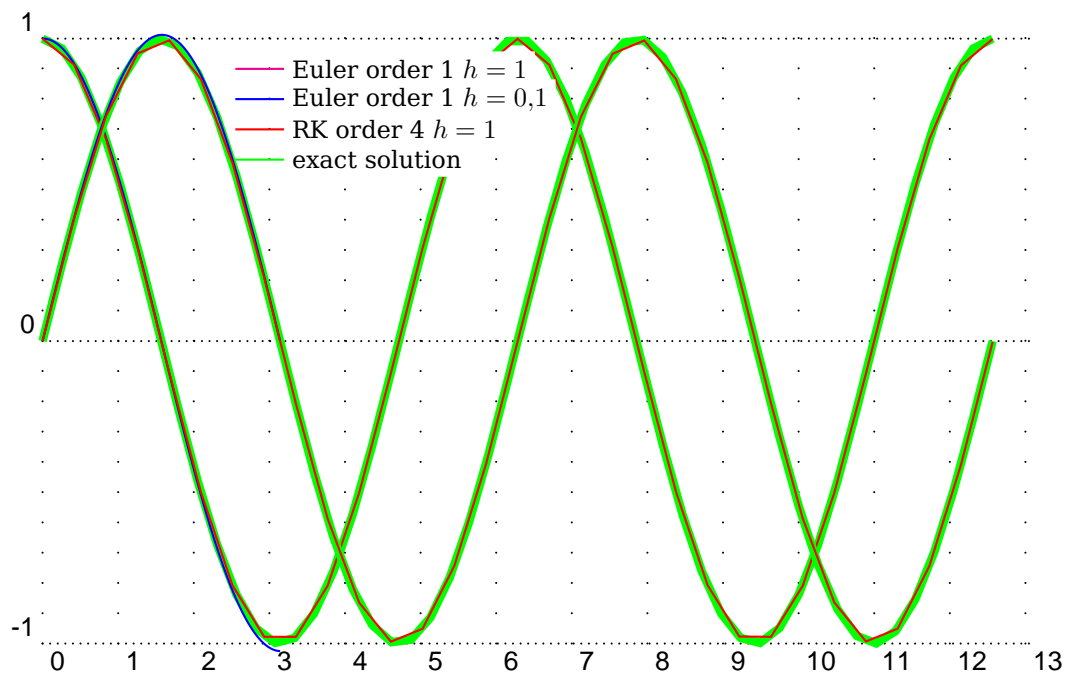


```

\def\Funct{exch} \psset{xunit=5cm, yunit=0.75cm}
\begin{pspicture}(0,-0.25)(2,7)\psgrid[subgriddiv=1,griddots=10]
\psplot[linecolor=green]{0}{2}{Euler x exp} %%e^x
\psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{1 1}{\Funct}
\psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{1 1}{\Funct}
\psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{1 1}{\Funct}
\psplot[linecolor=green]{0}{2}{Euler dup x exp %%ch(x)
exch x neg exp add 2 div}
\psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{1 0}{\Funct}
\psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{1 0}{\Funct}
\psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{1 0}{\Funct}
\psplot[linecolor=green]{0}{2}{Euler dup x exp
exch x neg exp sub 2 div} %%sh(x)
\psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{0 1}{\Funct}
\psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{0 1}{\Funct}
\psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{0 1}{\Funct}
\rput*(1.3,.9){\psline[linecolor=magenta](-.75cm,0)}\rput*[l](1.3,.9){\small\textsc{Euler}
order 1 $h=1$}
\rput*(1.3,.8){\psline[linecolor=blue](-.75cm,0)}\rput*[l](1.3,.8){\small\textsc{Euler}
order 1 $h=0{,}1$}
\rput*(1.3,.7){\psline[linecolor=red](-.75cm,0)}\rput*[l](1.3,.7){\small RK order 4 $h=1$}
\rput*(1.3,.6){\psline[linecolor=green](-.75cm,0)}\rput*[l](1.3,.6){\small exact
solution}
\end{pspicture}

```

$$y'' = -y$$



```

\def\Funct{exch neg}
\psset{xunit=1, yunit=4}
\def\quatrepi{12.5663706144}\psgrid[subgriddiv=1,griddots=10]
\begin{pspicture}(0,-1.25)(\quatrepi,1.25)\psgrid[subgriddiv=1,griddots=10]
\psplot[linewidth=4\pslinewidth,linecolor=green]{0}{\quatrepi}{x RadtoDeg cos}
  %\cos(x)
\psplotDiffEqn[linecolor=blue, plotpoints=201]{0}{3.1415926}{1 0}{\Funct}
\psplotDiffEqn[linecolor=red, method=rk4, plotpoints=31]{0}{\quatrepi}{1 0}{\Funct}
\psplot[linewidth=4\pslinewidth,linecolor=green]{0}{\quatrepi}{x RadtoDeg sin}
  %\sin(x)
\psplotDiffEqn[linecolor=blue,plotpoints=201]{0}{3.1415926}{0 1}{\Funct}
\psplotDiffEqn[linecolor=red,method=rk4, plotpoints=31]{0}{\quatrepi}{0 1}{\Funct}
\rput*(3.3,.9){\psline[linecolor=magenta]{-.75cm,0}}\rput*[l](3.3,.9){\small
  Euler order 1 $h=1$}
\rput*(3.3,.8){\psline[linecolor=blue]{-.75cm,0}}\rput*[l](3.3,.8){\small
  Euler order 1 $h=0{,}1$}
\rput*(3.3,.7){\psline[linecolor=red]{-.75cm,0}}\rput*[l](3.3,.7){\small RK
  order 4 $h=1$}
\rput*(3.3,.6){\psline[linecolor=green]{-.75cm,0}}\rput*[l](3.3,.6){\small
  exact solution}
\end{pspicture}

```

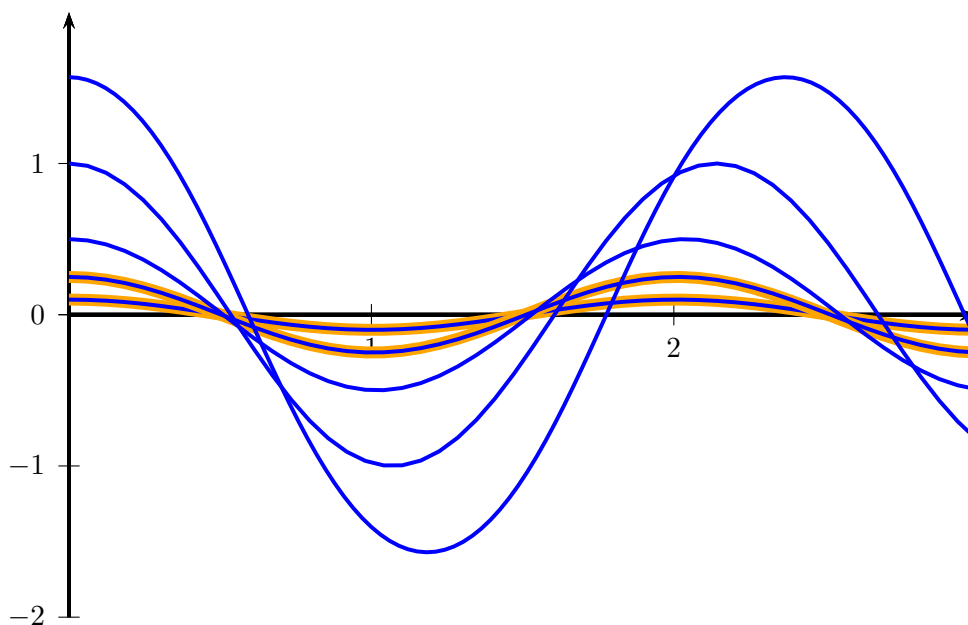
The mechanical pendulum: $y'' = -\frac{g}{l} \sin(y)$

For small oscillations $\sin(y) \simeq y$:

$$y(x) = y_0 \cos\left(\sqrt{\frac{g}{l}}x\right)$$

The function f is written in PostScript code:

```
exch RadtoDeg sin -9.8 mul %% y' -gsin(y)
```

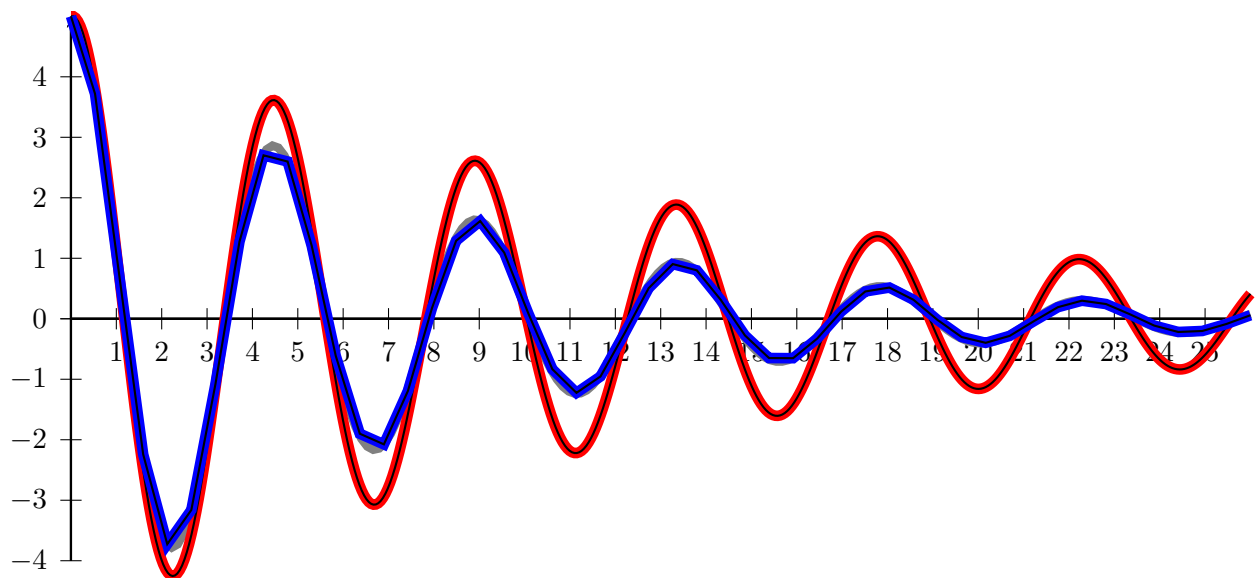


```
\def\Func{y[1]|-9.8*sin(y[0])}
\psset{yunit=2,xunit=4,algebraic=true,linewidth=1.5pt}
\begin{pspicture}(0,-2.25)(3,2.25)
  \psaxes{->}(0,0)(0,-2)(3,2)
  \psplot[linewidth=3\pslinewidth, linecolor=Orange]{0}{3}{.1*cos(sqrt(9.8)*x)}
  \psset{method=rk4,plotpoints=50,linecolor=blue}
  \psplotDiffEqn{0}{3}{.1 0}{\Func}
  \psplot[linewidth=3\pslinewidth,linecolor=Orange]{0}{3}{.25*cos(sqrt(9.8)*x)}
  \psplotDiffEqn{0}{3}{.25 0}{\Func}
  \psplotDiffEqn{0}{3}{.5 0}{\Func}
  \psplotDiffEqn{0}{3}{1 0}{\Func}
  \psplotDiffEqn[plotpoints=100]{0}{3}{Pi 2 div 0}{\Func}
\end{pspicture}
```

$$y'' = -\frac{y'}{4} - 2y$$

For $y_0 = 5$ and $y'_0 = 0$ the solution is:

$$5e^{-\frac{x}{8}} \left(\cos(\omega x) + \frac{\sin(\omega x)}{8\omega} \right) \text{ avec } \omega = \frac{\sqrt{127}}{8}$$

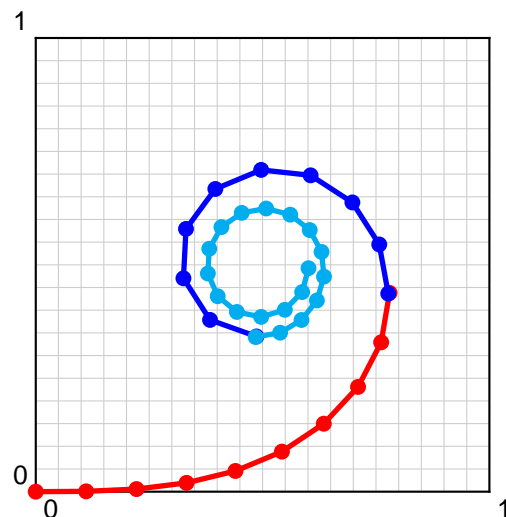


```
\psset{xunit=.6,yunit=0.8,plotpoints=500}
\begin{pspicture}(0,-4.25)(26,5.25)
  \psaxes{->}(0,0)(0,-4)(26,5)
  \psplot[plotpoints=200,linewidth=4\pslinewidth,linecolor=gray]{0}{26}{%
    Euler x -8 div exp x 127 sqrt 8 div mul RadtoDeg dup cos 5 mul exch sin 127
    sqrt div 5 mul add mul}
  \psplotDiffEqn[linecolor=red,linewidth=5\pslinewidth]{0}{26}{5 0}
    {dup 3 1 roll -4 div exch 2 mul sub}
  \psplotDiffEqn[linecolor=black,algebraic=true]{0}{26}{5 0} {y[1]|-y[1]/4-2*y
    [0]}
  \psset{method=rk4, plotpoints=50}
  \psplotDiffEqn[linecolor=blue,linewidth=5\pslinewidth]{0}{26}{5 0}{%
    dup 3 1 roll -4 div exch 2 mul sub}
  \psplotDiffEqn[linecolor=black,algebraic=true]{0}{26}{5 0}{y[1]|-y[1]/4-2*y
    [0]}
\end{pspicture}
```

25.3. Save final state of a equation

With the macros `\BeginSaveFinalState` and `\EndSaveFinalState` the end values of a differential equation can be saved and then used with the optional argument `GetFinalState` as starting values for another equation.

```
\psset{unit=10cm,linewidth=2pt}
\begin{pspicture}(1,1)\psgrid[subgridcolor=black!20,subgriddiv=20]
\BeginSaveFinalState
\psplotDiffEqn[
  whichabs=0,whichord=1,linecolor=red,method=rk4,
  plotpoints=10,showpoints=true]{0}{1}{0 0}{
    pop pop
    x dup mul 2 div 180 mul cos %% dx/dt
    x dup mul 2 div 180 mul sin %% dy/dt
  }
\psplotDiffEqn[GetFinalState,
  whichabs=0,whichord=1,linecolor=blue,method=rk4,%SaveFinalState,
  plotpoints=10,showpoints=true]{1}{2}{0 0}{
    pop pop
    x dup mul 2 div 180 mul cos %% dx/dt
    x dup mul 2 div 180 mul sin %% dy/dt
  }
\psplotDiffEqn[GetFinalState,
  whichabs=0,whichord=1,linecolor=cyan,method=rk4,%SaveFinalState,
  plotpoints=19,showpoints=true]{2}{3}{0 0 }{
    pop pop
    x dup mul 2 div 180 mul cos %% dx/dt
    x dup mul 2 div 180 mul sin %% dy/dt
  }
\EndSaveFinalState
\end{pspicture}
```



26. \psMatrixPlot

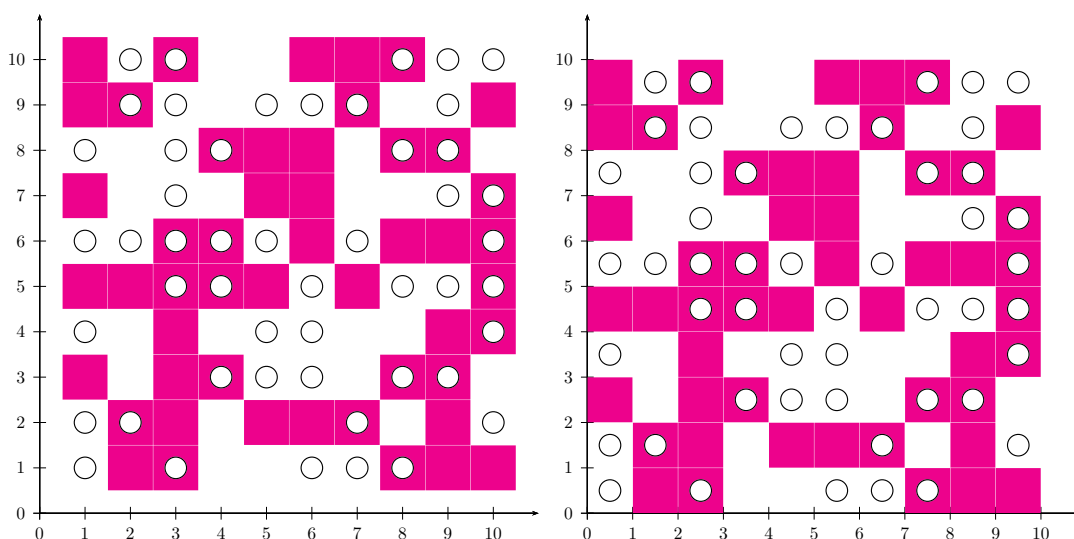
This macro allows you to visualize a matrix. The datafile must be defined as a PostScript matrix named dotmatrix:

```
/dotmatrix [ % <----- important line
0 1 1 0 0 0 0 1 1 1
0 1 1 0 1 1 1 0 1 0
1 0 1 1 0 0 0 1 1 0
0 0 1 0 0 0 0 0 1 1
1 1 1 1 1 0 1 0 0 1
0 0 1 1 0 1 0 1 1 1
1 0 0 0 1 1 0 0 0 1
0 0 0 1 1 1 0 1 1 0
1 1 0 0 0 0 1 0 0 1
1 0 1 0 0 1 1 1 0 0
] def      % <----- important line
```

Only the value 0 is important, in which case nothing happens, and for all other cases a dot is printed. The syntax of the macro is:

```
\psMatrixPlot [Options] {rows}{columns}{data file}
```

The matrix is scanned line by line from the the first one to the last. In general it appears as a bottom-to-top version of the above listed matrix, the first row 0110000111 is the first plotted line ($y = 1$). With the option `ChangeOrder=true` it looks exactly like the above view.

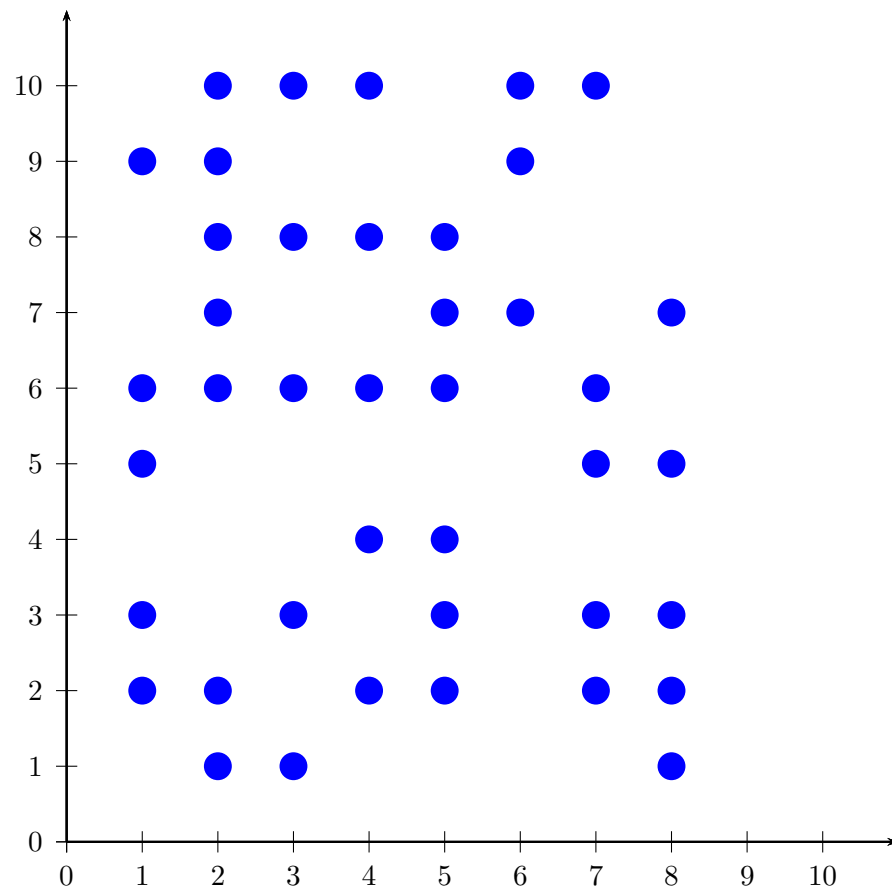


```
\psscalebox{0.6}{%
\begin{pspicture}(-0.5,-0.75)(11,11)
\psaxes{->}(11,11)
\psMatrixPlot[dotsize=1.1cm,dotstyle=square*,linecolor=magenta]%
{10}{10}{matrix.data}
\psMatrixPlot[dotsize=.5cm,dotstyle=o,ChangeOrder]{10}{10}{matrix.data}
```

```

\end{pspicture}}\quad
\psscalebox{0.6}{%
\begin{pspicture}(-0.5,-0.75)(11,11)
\psaxes{->}(11,11)
\psMatrixPlot[dotsize=1.1cm,dotstyle=square*,linecolor=magenta,XYoffset=-0.5]
%
{10}{10}{matrix.data}
\psMatrixPlot[dotsize=.5cm,dotstyle=o,ChangeOrder,XYoffset=-0.5]{10}{10}{
matrix.data}
\end{pspicture}}

```



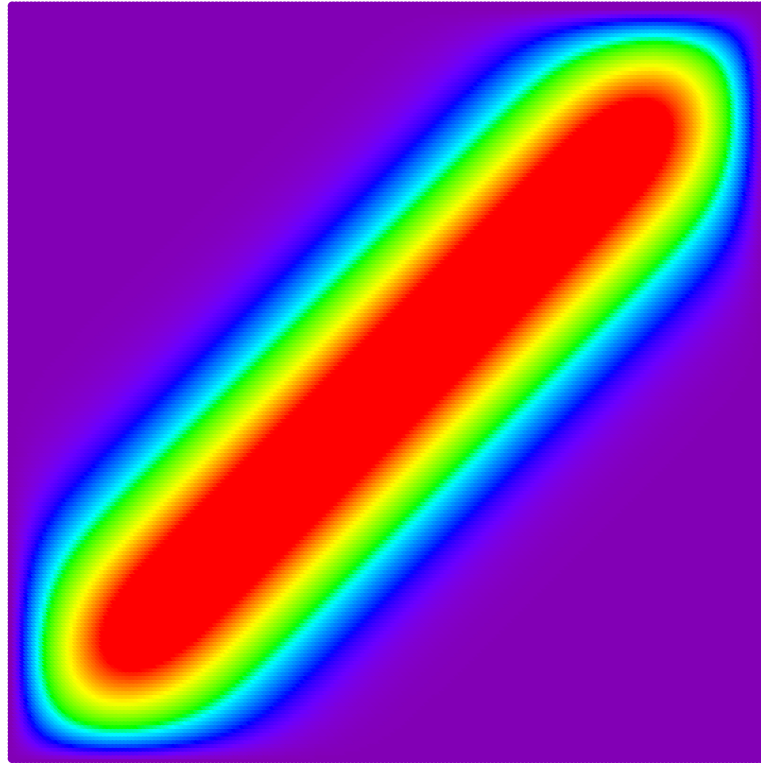
```

\begin{pspicture}(-0.5,-0.75)(11,11)
\psaxes{->}(11,11)
\psMatrixPlot[dotscale=3,dotstyle=*,linecolor=blue]{10}{8}{matrix.data}
\end{pspicture}

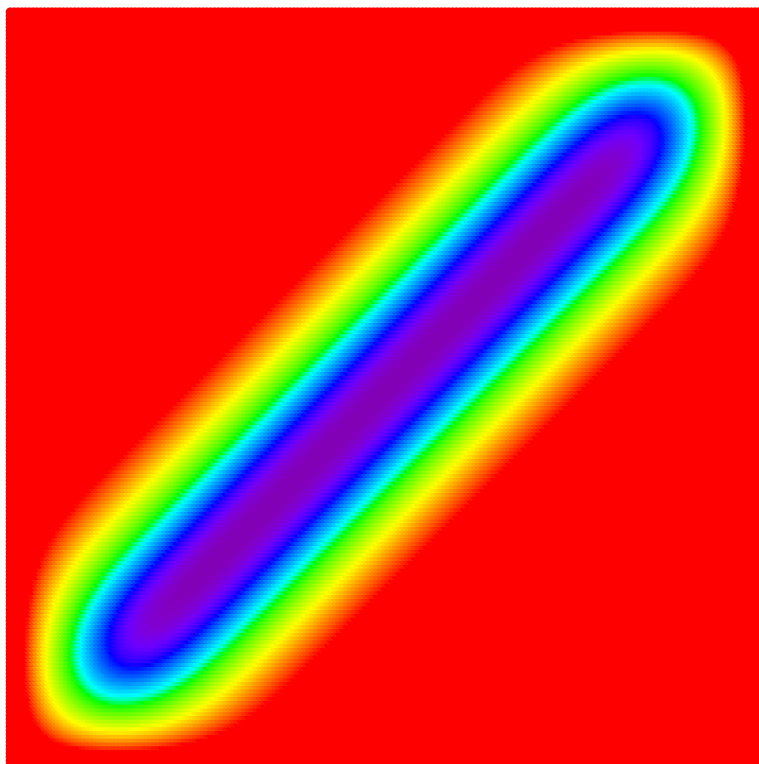
```

With the `colorType=1` the data is printed as continuous color in the range of the wavelength. The smallest value of the data array is set to red and the biggest value is set to violet. All other values are substituted by the corresponding color of the wavelength. `colorType=2` is the same, but vice versa with the color, from violet to red. `colorType=3` is the grayscale image and `colorType=4` the same invers.

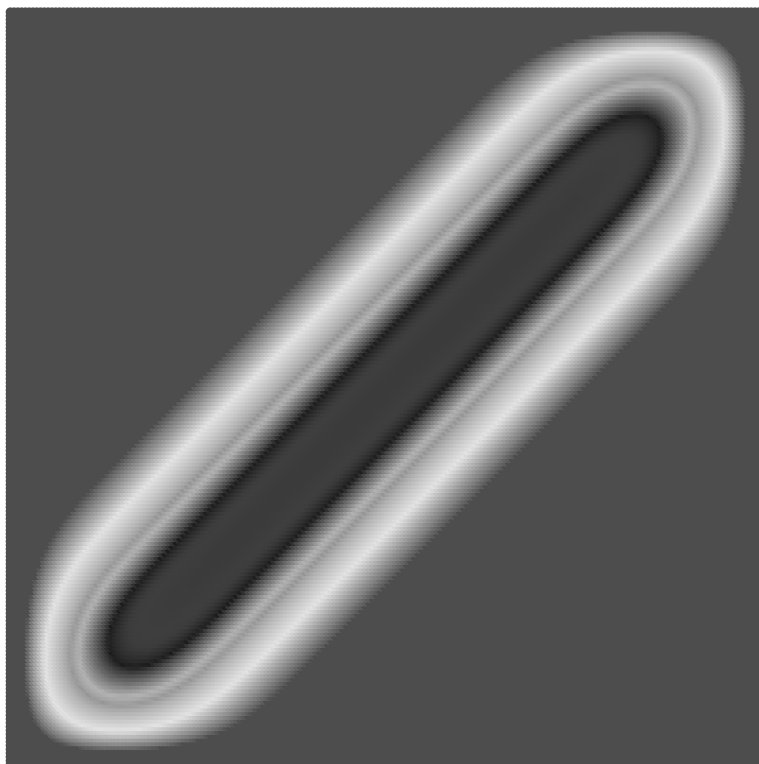
The following examples use a 200×200 matrix data, which is saved as `/dotmatrix [...]` in the file `pstricks-add-doc.dat`.



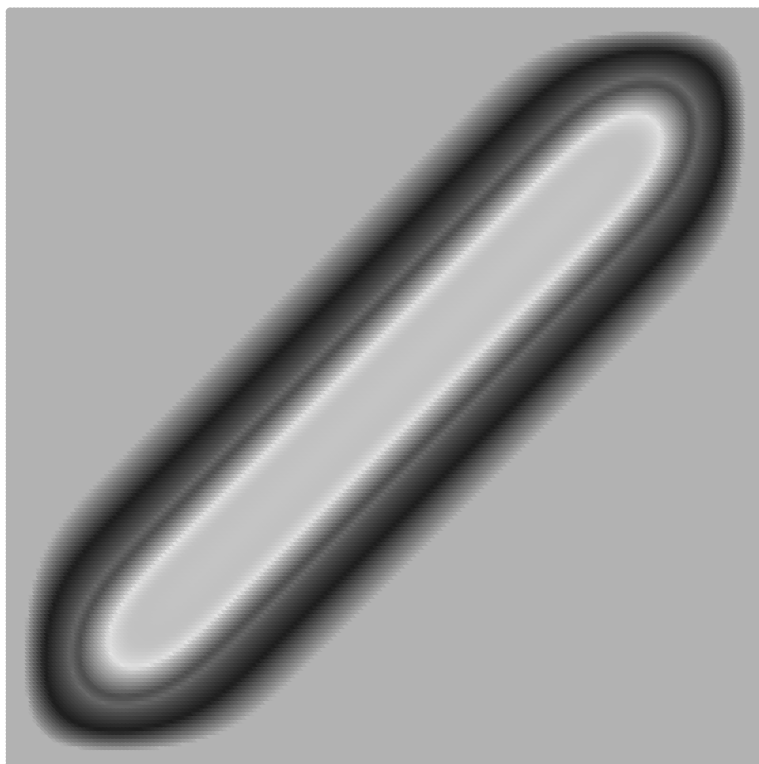
```
\begin{pspicture}(10,10)
  \psMatrixPlot[colorType=1,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}
\end{pspicture}
```



```
\begin{pspicture}(10,10)  
  \psMatrixPlot[colorType=2,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}  
\end{pspicture}
```



```
\begin{pspicture}(10,10)  
  \psMatrixPlot[colorType=3,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}  
\end{pspicture}
```

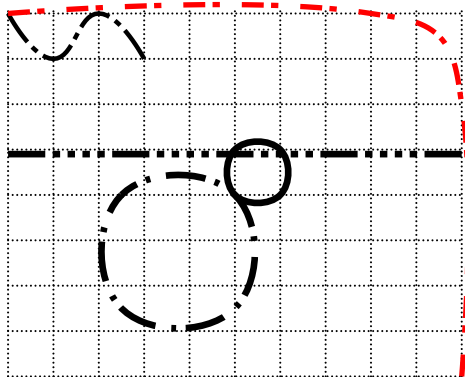


```
\begin{pspicture}(10,10)  
  \psMatrixPlot[colorType=4,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}  
\end{pspicture}
```

27. Dashed Lines

Tobias Nähring has implemented an enhanced feature for dashed lines. The number of arguments is no longer limited.

```
dash=value1 unit value2 unit ...
```



```
\psset{linewidth=2.5pt,unit=0.6}
\begin{pspicture}(-5,-4)(5,4)
\psgrid[subgriddiv=0,griddots=10,gridlabels=0
pt]
\psset{linestyle=dashed}
\pscurve[dash=5mm 1mm 1mm 1mm,linewidth
=0.1](-5,4)(-4,3)(-3,4)(-2,3)
\psline[dash=5mm 1mm 1mm 1mm 1mm 1mm 1mm 1mm
1mm 1mm](-5,0.9)(5,0.9)
\psccurve[linestyle=solid](0,0)(1,0)(1,1)
(0,1)
\psccurve[linestyle=dashed,dash=5mm 2mm 0.1
0.2,linetype=0](0,0)(-2.5,0)(-2.5,-2.5)
(0,-2.5)
\pscurve[dash=3mm 3mm 1mm 1mm,linecolor=red,
linewidth=2pt](5,-4)(5,2)(4.5,3.5)(3,4)
(-5,4)
\end{pspicture}
```

28. Arrows

28.1. Definition

pstricks-add defines the following "arrows":

Value	Example	Name
-		None
<->		Arrowheads.
>-<		Reverse arrowheads.
<<->>		Double arrowheads.
>>-<<		Double reverse arrowheads.
-		T-bars, flush to endpoints.
* - *		T-bars, centered on endpoints.
[-]		Square brackets.
] - [Reversed square brackets.
(-)		Rounded brackets.
) - (Reversed rounded brackets.
o - o		Circles, centered on endpoints.
* - *		Disks, centered on endpoints.
oo - oo		Circles, flush to endpoints.
** - **		Disks, flush to endpoints.
<->		T-bars and arrows.
>-<		T-bars and reverse arrows.
h - h		left/right hook arrows.
H - H		left/right hook arrows.
v - v		left/right inside vee arrows.
V - V		left/right outside vee arrows.
f - f		left/right inside filled arrows.
F - F		left/right outside filled arrows.
t - t		left/right inside slash arrows.
T - T		left/right outside slash arrows.

You can also mix and match, e.g., ->, *-) and [-> are all valid values of the arrows parameter. The parameter can be set with

```
\psset{arrows=<type>}
```

or for some macros with a special option, like

```
\psline[<general options>]{<arrow type>}(A)(B)
```

```
\psline[linecolor=red,linewidth=2pt]{|->}(0,0)(0,2)
```



28.2. Multiple arrows

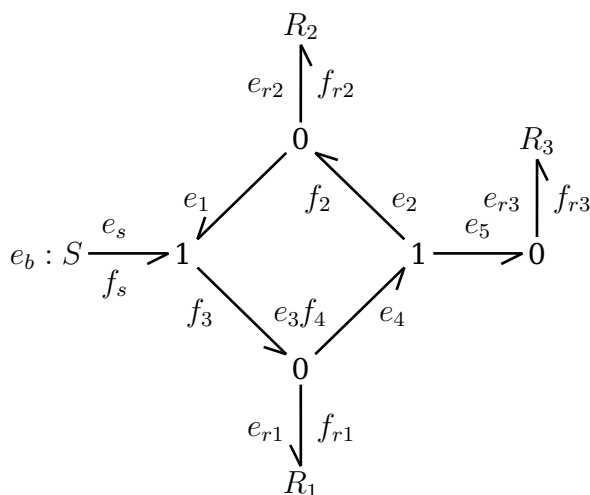
There are two new options which are only valid for the arrow type << or >>. nArrow sets both, the nArrowA and the nArrowB parameter. The meaning is declared in the following

tables. Without setting one of these parameters the behaviour is like the one described in the old PSTricks manual.

Value	Meaning
->>	-A
<<->>	A-A
<<-	A-
>>-	B-
-<<	-B
>>-<<	B-B
>>->>	B-A
<<-<<	A-B

Value	Example
<code>\psline{->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3]{->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=5]{->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline{<<-}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3]{<<-}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=5]{<<-}(0,1ex)(2.3,1ex)</code>	
<code>\psline{<<->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3]{<<->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=5]{<<->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline{<<- }(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3]{<<-<<}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=5]{<<-o}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3,nArrowsB=4]{<<-<<}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=3,nArrowsB=4]{>>->>}(0,1ex)(2.3,1ex)</code>	
<code>\psline[nArrowsA=1,nArrowsB=4]{>>->>}(0,1ex)(2.3,1ex)</code>	

28.3. hookarrow



`\psset{arrowsize=8pt,arrowlength=1,linewidth=1pt,nodesep=2pt,shortput=tablr}`

```

\large
\begin{psmatrix}[colsep=12mm,rowsep=10mm]
  & & $R_2$ & & \\
  & & 0 & & $R_3$ \\
$e_b:S$ & 1 & & 1 & 0 \\
  & & 0 & & \\
  & & $R_1$ & & \\
\end{psmatrix}
\ncline{-h}{1,3}{2,3}<{$e_{r2}$}>{$f_{r2}$}\ncline{-h}{2,3}{3,2}<{$e_{l1}$}
\ncline{-h}{3,1}{3,2}^{$e_s$}_{$f_s$}\ncline{-h}{3,2}{4,3}>{$e_3$}<{$f_3$}
\ncline{-h}{4,3}{3,4}>{$e_4$}<{$f_4$}\ncline{-h}{3,4}{2,3}>{$e_2$}<{$f_2$}
\ncline{-h}{3,4}{3,5}^{$e_5$}
\ncline{-h}{3,5}{2,5}<{$e_{r3}$}>{$f_{r3}$}
\ncline{-h}{4,3}{5,3}<{$e_{r1}$}>{$f_{r1}$}

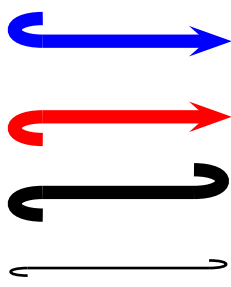
```

28.4. hookrightarrow and hookleftarrow

This is another type of arrow and is abbreviated with H. The length and width of the hook is set by the new options `hooklength` and `hookwidth`, which are by default set to

```
\psset{hooklength=3mm,hookwidth=1mm}
```

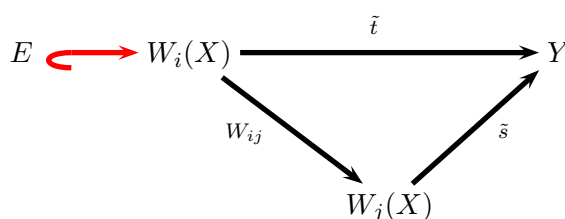
If the line begins with a right hook then the line ends with a left hook and vice versa:



```

\begin{pspicture}(3,4)
\psline[linewidth=5pt,linecolor=blue,hooklength=5mm,hookwidth=-3mm]{H->}(0,3.5)(3,3.5)
\psline[linewidth=5pt,linecolor=red,hooklength=5mm,hookwidth=3mm]{H->}(0,2.5)(3,2.5)
\psline[linewidth=5pt,hooklength=5mm,hookwidth=3mm]{H-H}(0,1.5)(3,1.5)
\psline[linewidth=1pt]{H-H}(0,0.5)(3,0.5)
\end{pspicture}

```
















```

$\begin{psmatrix}
E&W_i(X)&&Y\\
&&&&&\\
&&&&&\\
\psset{arrows=->,nodesep=3pt,linewidth=2pt}
\everypsbox{\scriptstyle}
\ncline[linecolor=red,arrows=H->,%hooklength=4mm,hookwidth=2mm]{1,1}{1,2}
\ncline{1,2}{1,4}^{\tilde{t}}
\ncline{1,2}{2,3}<{W_{ij}}
\ncline{2,3}{1,4}>{\tilde{s}}
\end{psmatrix}$

```

28.5. ArrowInside Option

It is now possible to have arrows inside lines and not only at the beginning or the end. The new defined options

Name	Example	Output
ArrowInside	<code>\psline[ArrowInside=->](0,0)(2,0)</code>	
ArrowInsidePos	<code>\psline[ArrowInside=->,% ArrowInsidePos=0.25](0,0)(2,0)</code>	
ArrowInsidePos	<code>\psline[ArrowInside=->,% ArrowInsidePos=10](0,0)(2,0)</code>	
ArrowInsideNo	<code>\psline[ArrowInside=->,% ArrowInsideNo=2](0,0)(2,0)</code>	
ArrowInsideOffset	<code>\psline[ArrowInside=->,% ArrowInsideNo=2,% ArrowInsideOffset=0.1](0,0)(2,0)</code>	
ArrowInside	<code>\psline[ArrowInside=->]{->}(0,0)(2,0)</code>	
ArrowInsidePos	<code>\psline[ArrowInside=->,% ArrowInsidePos=0.25]{->}(0,0)(2,0)</code>	
ArrowInsidePos	<code>\psline[ArrowInside=->,% ArrowInsidePos=10]{->}(0,0)(2,0)</code>	
ArrowInsideNo	<code>\psline[ArrowInside=->,% ArrowInsideNo=2]{->}(0,0)(2,0)</code>	
ArrowInsideOffset	<code>\psline[ArrowInside=->,% ArrowInsideNo=2,% ArrowInsideOffset=0.1]{->}(0,0)(2,0)</code>	
ArrowFill	<code>\psline[ArrowFill=false,% arrowinset=0]{->}(0,0)(2,0)</code>	
ArrowFill	<code>\psline[ArrowFill=false,% arrowinset=0]{<->}(0,0)(2,0)</code>	
ArrowFill	<code>\psline[ArrowInside=->,% arrowinset=0,% ArrowFill=false,% ArrowInsideNo=2,% ArrowInsideOffset=0.1]{->}(0,0)(2,0)</code>	

Without the default arrow definition there is only the one inside the line, defined by the type and the position. The position is relative to the length of the whole line. 0.25 means at 25% of the line length. The peak of the arrow gets the coordinates which are calculated by the macro. If you want arrows with an absolute position difference, then choose a value greater than 1, e.g. 10 which places an arrow every 10 pt. The default unit pt cannot be changed.

The `ArrowInside` takes only arrow definitions like `->` into account. Arrows from right to left (`<-`) are not possible and ignored. If you need such arrows, change the order of the pairs of coordinates for the line or curve macro.

28.6. ArrowFill Option

By default all arrows are filled polygons. With the option `ArrowFill=false` there are "white" arrows. Only for the beginning/end arrows are they empty, the inside arrows

are overpainted by the line.



```
\psset{arrowscale=2.5}
\psline[linecolor=red,arrowinset=0]{<->}(-1,0)(2,0)
```



```
\psset{arrowscale=2.5}
\psline[linecolor=red,arrowinset=0,ArrowFill=false]
{<->}(-1,0)(2,0)
```



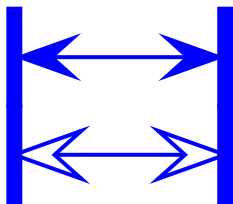
```
\psset{arrowscale=2.5}
\psline[linecolor=red,arrowinset=0,arrowsize=0.2,
ArrowFill=false]{<->}(-1,0)(2,0)
```



```
\psline[linecolor=blue,arrowscale=4,
ArrowFill]{>>->>}(-1,0)(2,0)
```



```
\psline[linecolor=blue,arrowscale=4,
ArrowFill=false]{>>->>}(-1,0)(2,0)
\rule{3cm}{0pt}\[30pt]
```



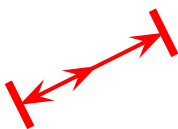
```
\psline[linecolor=blue,arrowscale=4,
ArrowFill]{>|->|}(-1,0)(2,0)
```

```
\psline[linecolor=blue,arrowscale=4,
ArrowFill=false]{>|->|}(-1,0)(2,0)%
```

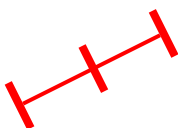
28.7. Examples

All examples are printed with `\psset{arrowscale=2,linecolor=red}`.

\psline




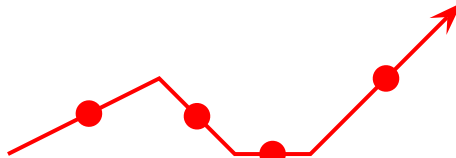
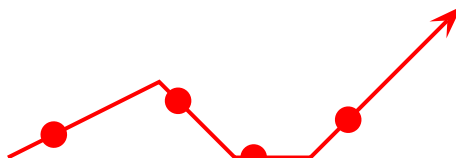
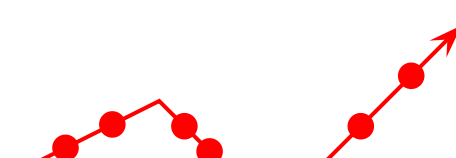


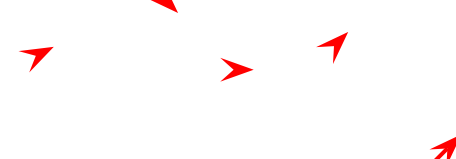

```
\begin{pspicture}(2,2)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=->]{|<->|}(2,1)
\end{pspicture}
```

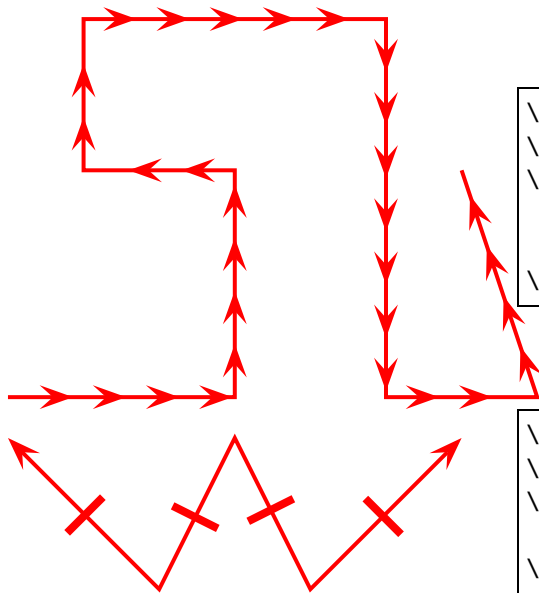


```
\begin{pspicture}(2,2)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=-|||]{|-|}(2,1)
\end{pspicture}
```



```
\begin{pspicture}(2,2)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=->,ArrowInsideNo=2]{->}(2,1)
\end{pspicture}
```

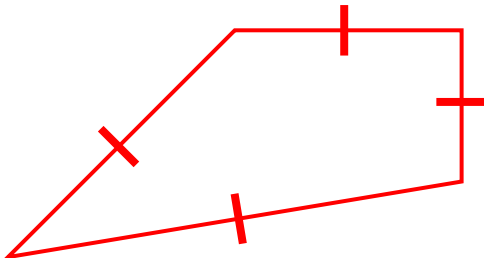
	<pre> \begin{pspicture}(2,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=->,ArrowInsideNo=2,ArrowInsideOffset =0.1]{->}(2,1) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=-*]{->}(0,0)(2,1)(3,0) (4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=-*,ArrowInsidePos =0.25]{->}(0,0)(2,1)(3,0)(4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=-*,ArrowInsidePos=0.25, ArrowInsideNo=2]{->}% (0,0)(2,1)(3,0)(4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=->, ArrowInsidePos =0.25]{->}% (0,0)(2,1)(3,0)(4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[linestyle=none,ArrowInside=->, ArrowInsidePos=0.25]{->}% (0,0)(2,1)(3,0)(4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true} \psline[ArrowInside=-<, ArrowInsidePos =0.75]{->}% (0,0)(2,1)(3,0)(4,0)(6,2) \end{pspicture} </pre>
	<pre> \begin{pspicture}(6,2) \psset{arrowscale=2,ArrowFill=true, ArrowInside=-*} \psline(0,0)(2,1)(3,0)(4,0)(6,2) \psset{linestyle=none} \psline[ArrowInsidePos=0](0,0)(2,1)(3,0) (4,0)(6,2) \psline[ArrowInsidePos=1](0,0)(2,1)(3,0) (4,0)(6,2) \end{pspicture} </pre>



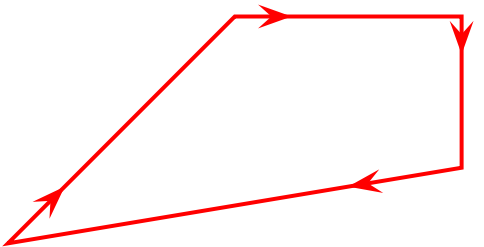
```
\begin{pspicture}(6,5)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=->,ArrowInsidePos
=20](0,0)(3,0)%
(3,3)(1,3)(1,5)(5,5)(5,0)(7,0)(6,3)
\end{pspicture}
```

```
\begin{pspicture}(6,2)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=-|]{<->}(0,2)(2,0)(3,2)
(4,0)(6,2)
\end{pspicture}
```

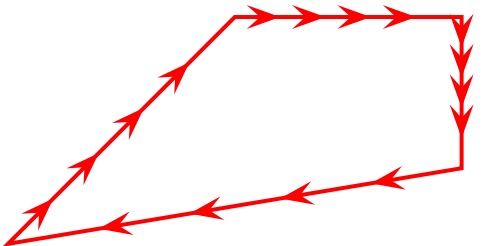
\pspolygon



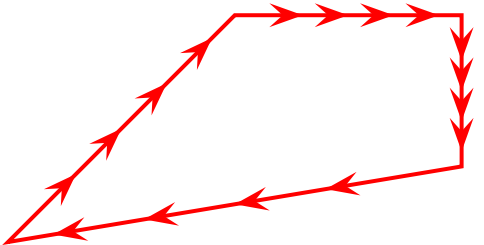
```
\begin{pspicture}(6,3)
\psset{arrowscale=2}
\pspolygon[ArrowInside=-|](0,0)(3,3)(6,3)
(6,1)
\end{pspicture}
```



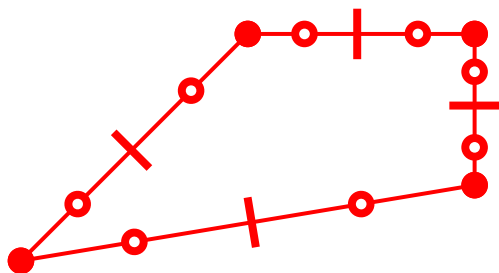
```
\begin{pspicture}(6,3)
\psset{arrowscale=2}
\pspolygon[ArrowInside=->,ArrowInsidePos
=0.25](0,0)(3,3)(6,3)(6,1)
\end{pspicture}
```



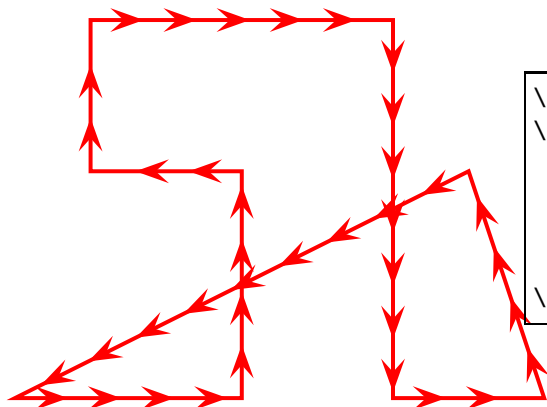
```
\begin{pspicture}(6,3)
\psset{arrowscale=2}
\pspolygon[ArrowInside=->,ArrowInsideNo=4](0,0)(3,3)(6,3)(6,1)
\end{pspicture}
```



```
\begin{pspicture}(6,3)
\psset{arrowscale=2}
\pspolygon[ArrowInside=->,ArrowInsideNo=4,%
ArrowInsideOffset=0.1](0,0)(3,3)(6,3)(6,1)
\end{pspicture}
```

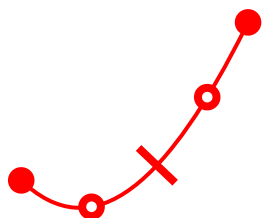


```
\begin{pspicture}(6,3)
\psset{arrowscale=2}
\pspolygon[ArrowInside=-|](0,0)(3,3)(6,3)
(6,1)
\psset{linestyle=none,ArrowInside=-*}
\pspolygon[ArrowInsidePos=0](0,0)(3,3)(6,3)
(6,1)
\pspolygon[ArrowInsidePos=1](0,0)(3,3)(6,3)
(6,1)
\psset{ArrowInside=-o}
\pspolygon[ArrowInsidePos=0.25](0,0)(3,3)
(6,3)(6,1)
\pspolygon[ArrowInsidePos=0.75](0,0)(3,3)
(6,3)(6,1)
\end{pspicture}
```

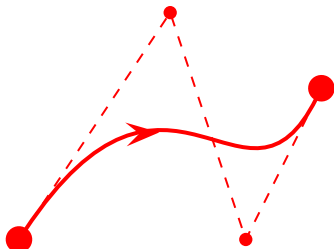


```
\begin{pspicture}(6,5)
\psset{arrowscale=2}
\pspolygon[ArrowInside=->,ArrowInsidePos
=20]%(
(0,0)(3,0)(3,3)(1,3)(1,5)(5,5)(5,0)(7,0)
(6,3)
\end{pspicture}
```

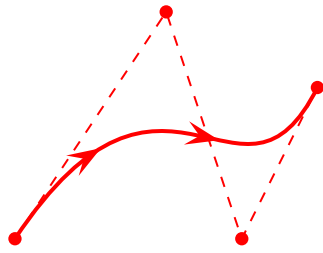
\psbezier



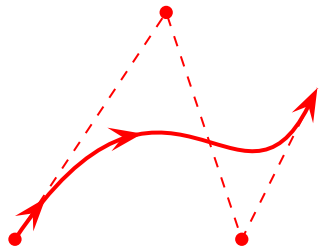
```
\begin{pspicture}(3,3)
\psset{arrowscale=2}
\psbezier[ArrowInside=-|](0,1)(1,0)(2,1)(3,3)
\psset{linestyle=none,ArrowInside=-o}
\psbezier[ArrowInsidePos=0.25](0,1)(1,0)(2,1)(3,3)
\psbezier[ArrowInsidePos=0.75](0,1)(1,0)(2,1)(3,3)
\psset{linestyle=none,ArrowInside=-*}
\psbezier[ArrowInsidePos=0](0,1)(1,0)(2,1)(3,3)
\psbezier[ArrowInsidePos=1](0,1)(1,0)(2,1)(3,3)
\end{pspicture}
```



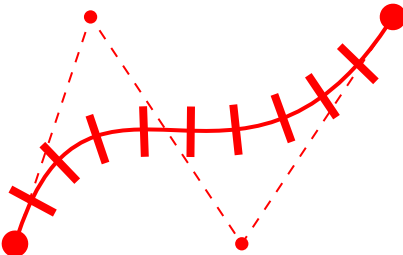
```
\begin{pspicture}(4,3)
\psset{arrowscale=2}
\psbezier[ArrowInside=->,showpoints]%
  {*-}(0,0)(2,3)(3,0)(4,2)
\end{pspicture}
```



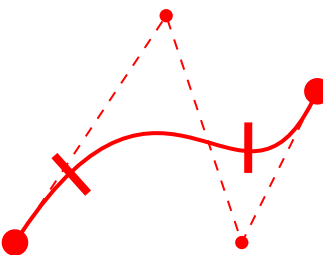
```
\begin{pspicture}(4,3)
\psset{arrowscale=2}
\psbezier[ArrowInside=->,showpoints=true,
  ArrowInsideNo=2](0,0)(2,3)(3,0)(4,2)
\end{pspicture}
```



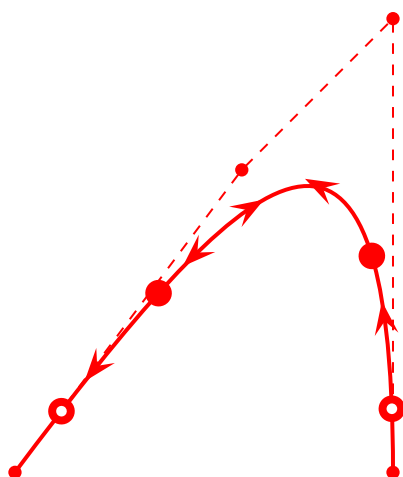
```
\begin{pspicture}(4,3)
\psset{arrowscale=2}
\psbezier[ArrowInside=->,showpoints=true,
  ArrowInsideNo=2,ArrowInsideOffset=-0.2]{->}(0,0)(2,3)(3,0)(4,2)
\end{pspicture}
```



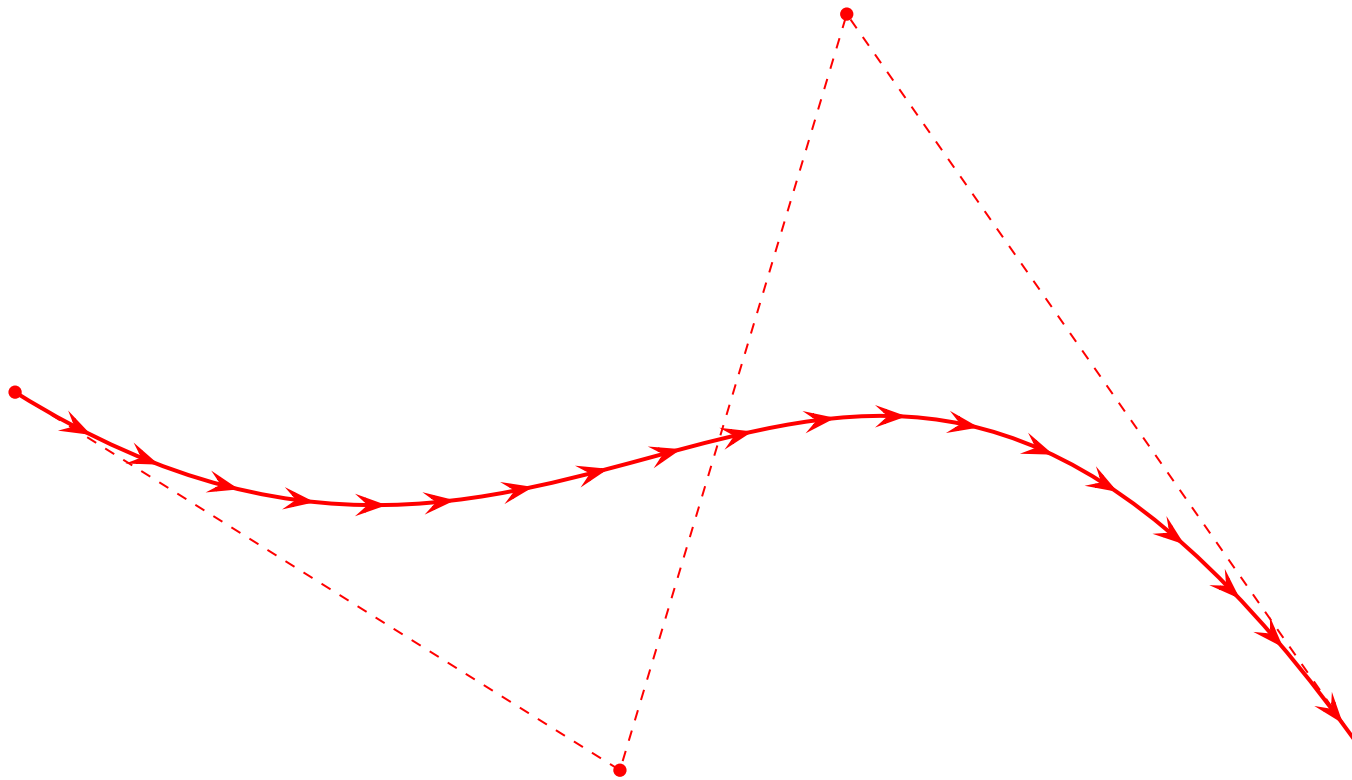
```
\begin{pspicture}(5,3)
\psset{arrowscale=2}
\psbezier[ArrowInsideNo=9,ArrowInside=-|,%
  showpoints=true]{*-}(0,0)(1,3)(3,0)(5,3)
\end{pspicture}
```



```
\begin{pspicture}(4,3)
\psset{arrowscale=2}
\psset{ArrowInside=-|}
\psbezier[ArrowInsidePos=0.25,showpoints=true]
  {*-}(2,3)(3,0)(4,2)
\psset{linestyle=none}
\psbezier[ArrowInsidePos=0.75](0,0)(2,3)(3,0)(4,2)
\end{pspicture}
```



```
\begin{pspicture}(5,6)
\psset{arrowscale=2}
\pnode(3,4){A}\pnode(5,6){B}\pnode(5,0){C}
\psbezier[ArrowInside=->,%
  showpoints=true](A)(B)(C)
\psset{linestyle=none,ArrowInside=-<}
\psbezier[ArrowInsideNo=4](0,0)(A)(B)(C)
\psset{ArrowInside=-o}
\psbezier[ArrowInsidePos=0.1](0,0)(A)(B)(C)
\psbezier[ArrowInsidePos=0.9](0,0)(A)(B)(C)
\psset{ArrowInside=-*}
\psbezier[ArrowInsidePos=0.3](0,0)(A)(B)(C)
\psbezier[ArrowInsidePos=0.7](0,0)(A)(B)(C)
\end{pspicture}
```

```
\begin{pspicture}(-3,-5)(15,5)
\psbezier[ArrowInside=19,%
  ArrowInside=->,ArrowFill=false,%
  showpoints=true]{->}(-3,0)(5,-5)(8,5)(15,-5)
\end{pspicture}
```

\pcline

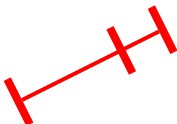
These examples need the package `pst-node`.



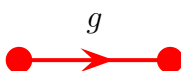
```
\begin{pspicture}(2,1)
\psset{arrowscale=2}
\pcline[ArrowInside=->](0,0)(2,1)
\end{pspicture}
```



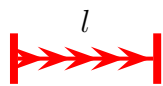
```
\begin{pspicture}(2,1)
\psset{arrowscale=2}
\pcline[ArrowInside=->]{<->}(0,0)(2,1)
\end{pspicture}
```



```
\begin{pspicture}(2,1)
\psset{arrowscale=2}
\pcline[ArrowInside=-|,ArrowInsidePos=0.75]{|-|}(0,0)(2,1)
\end{pspicture}
```



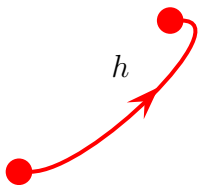
```
\psset{arrowscale=2}
\pcline[ArrowInside=->,ArrowInsidePos=0.65]{*-}(0,0)(2,0)
\naput[labelsep=0.3]{\large$g$}
```



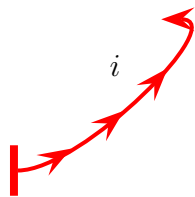
```
\psset{arrowscale=2}
\pcline[ArrowInside=->,ArrowInsidePos=10]{|-|}(0,0)(2,0)
\naput[labelsep=0.3]{\large$l$}
```

`\pccurve`

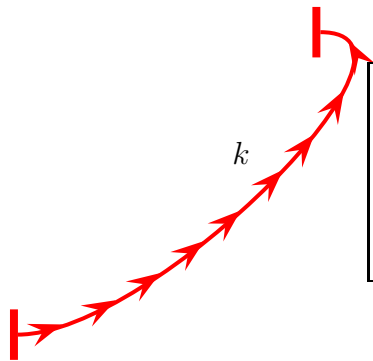
These examples also need the package `pst-node`.



```
\begin{pspicture}(2,2)
\psset{arrowscale=2}
\pccurve[ArrowInside=->,ArrowInsidePos=0.65,showpoints=true]
  {*-}(0,0)(2,2)
\naput[labelsep=0.3]{\large$h$}
\end{pspicture}
```



```
\begin{pspicture}(2,2)
\psset{arrowscale=2}
\pccurve[ArrowInside=->,ArrowInsideNo=3,showpoints=true]
  {|->}(0,0)(2,2)
\naput[labelsep=0.3]{\large$i$}
\end{pspicture}
```

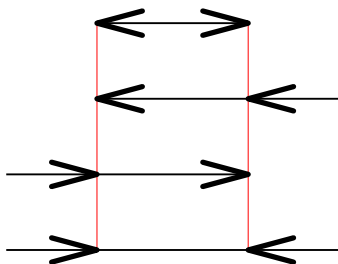


```
\begin{pspicture}(4,4)
\psset{arrowscale=2}
\pccurve[ArrowInside=->,ArrowInsidePos=20]{|-|}(0,0)
  (4,4)
\naput[labelsep=0.3]{\large$k$}
\end{pspicture}
```

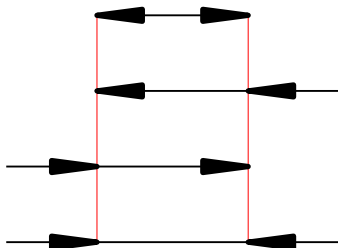
28.8. Special arrows v-V,t-T, and f-F

Possible optional arguments are

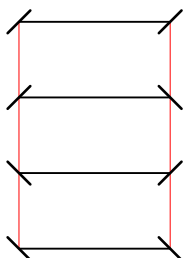
name	meaning
veearrowlength	default is 3mm
veearrowangle	default is 30
veearrowlinewidth	default is 0.35mm
filledveearrowlength	default is 3mm
filledveearrowangle	default is 15
filledveearrowlinewidth	default is 0.35mm
tickarrowlength	default is 1.5mm
tickarrowlinewidth	default is 0.35mm



```
\psset{unit=5mm}
\begin{pspicture}(4,6)
  \psset{dimen=middle,arrows=c-c,
    arrowscale=2,linewidth=.25mm}
  \psline[linecolor=red,linewidth=.05mm](0,0)(0,6)
  \psline[linecolor=red,linewidth=.05mm](4,0)(4,6)
  \psline{v-v}(0,6)(4,6)
  \psline{v-V}(0,4)(4,4)
  \psline{V-v}(0,2)(4,2)
  \psline{V-V}(0,0)(4,0)
\end{pspicture}
```



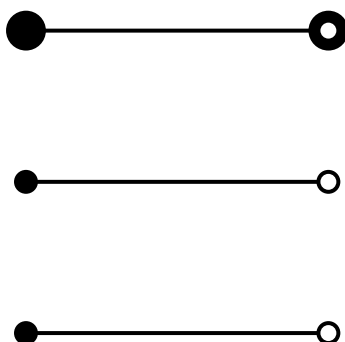
```
\psset{unit=5mm}
\begin{pspicture}(4,6)
  \psset{dimen=middle,arrows=c-c,
    arrowscale=2,linewidth=.25mm}
  \psline[linecolor=red,linewidth=.05mm](0,0)(0,6)
  \psline[linecolor=red,linewidth=.05mm](4,0)(4,6)
  \psline{f-f}(0,6)(4,6)
  \psline{f-F}(0,4)(4,4)
  \psline{F-f}(0,2)(4,2)
  \psline{F-F}(0,0)(4,0)
\end{pspicture}
```



```
\psset{unit=5mm}
\begin{pspicture}(4,6)
  \psset{dimen=middle,arrows=c-c,linewidth=.25mm}
  \psline[linecolor=red,linewidth=.05mm](0,0)(0,6)
  \psline[linecolor=red,linewidth=.05mm](4,0)(4,6)
  \psline{t-t}(0,6)(4,6)
  \psline{t-T}(0,4)(4,4)
  \psline{T-t}(0,2)(4,2)
  \psline{T-T}(0,0)(4,0)
\end{pspicture}
```

28.9. Special arrow option arrowLW

Only for the arrowtype o and * it is possible to set the arrowlinewidth with the optional keyword arrowLW. When scaling an arrow by the keyword arrowScale the width of the borderline is also scaled. With the optional argument arrowLW the line width can be set separately and is not taken into account by the scaling value.



```
\begin{pspicture}(4,6)
\psline[arrowscale=3,arrows=-o](0,5)(4,5)
\psline[arrowscale=3,arrows=-o,
arrowLW=0.5pt](0,3)(4,3)
\psline[arrowscale=3,arrows=-o,
arrowLW=0.3333\pslinewidth](0,1)(4,1)
\end{pspicture}
```

29. Ticks and other marks along a curve

29.1. Quick overview

The macros described below allow you to place tick and other marks along an arbitrary parametric curve with placement rules similar to those used by \psaxes in the pst-plot package. You have to define a metric function along the curve to govern tick placement. That function can be a specified function of x, y which should increase along the curve, or it can be an function whose increment is a specified positive function of x, y, dx, dy, ds where the last term is the arc-length element that you could specify alternately as $dx \text{ dup mul } dy \text{ dup mul add sqrt}$.

In addition, a new command \Put is proposed, expanding as appropriate to \rput or \uput. Its syntax is

```
\Put * [Options] {<ref>} (<position>) {<stuff>}
```

where the optional * blanks the background, the optional [Options] may be used to specify a rotation using any form acceptable to \SpecialCoord (eg, $\text{rot}=45$ or $\text{rot}=\{(1,1)\}$ or $\text{rot}=(P)$, and *ref* takes one of two forms: (a) a refpt such as B1, in which case \rput is called; (b) a polar form of offset (eg, 7pt;30, or ;(P) — in the latter case, \pslabelsep is substituted for the missing radius), in which case a modified form of \uput is called. The idea of \Put is to allow position, ref and rot to be specified in any of the forms acceptable to \SpecialCoord and to do so with the same output no matter what form is used. The cost of this consistency is that \Put can lead to results that differ from \uput in some special cases.

29.2. Details

Suppose you have drawn a parametric curve using `\psparametricplot`, and you wish to indicate some points on the curve using tick-marks like those on the axes. This is a two-step process, the first of which serves to define at the PostScript level a number of data arrays containing information about the curve. Those arrays are used in the second step to compute tick positions and draw the ticks. The first step is to run the macro `\pscurvepoints`. For example,

```
\pscurvepoints[plotpoints=20]{0}{6}{t t t mul 12 div}{Pt}%
```

makes a virtual (ie, data only—nothing is rendered) polyline with 20 vertices approximating the curve $x(t) = t, y(t) = t^2/12, 0 \leq t \leq 6$. The last argument `Pt` is the root name given to the data arrays. PostScript arrays will be created with the following names: `Pt.X`, `Pt.Y` for the coordinates of the vertices, `PtDelta.X`, `PtDelta.Y` for the increments between the vertices (using, eg, `PtDelta.X[2]=Pt.X[2]-Pt.X[1]`) and `PtNormal.X`, `PtNormal.Y` for a vector normal to `PtDelta.X`, `PtDelta.Y` in the visual, not mathematical, sense. (Both senses are the same if the scales on the axes are identical.) The Normal is always constructed so as to point “upward” (ie, to your left) as you traverse the curve in the positive direction. The PostScript variable `unitratio` provides the ratio of the unit on the y axis to that on x axis, and `unitratiosq` is its square. All of these PostScript objects are stored in the main `pstricks` dictionary `tx@Dict` which should be automatically made available when using many `pstricks` macros. If `gs` returns you an error message like

```
Error: /undefined in Pt.X
```

then you may need to enclose the offending PostScript code within a block of the form

```
tx@Dict begin ... end
```

so that the dictionary is made available.

With this preparation, the main tick-making macro may be run. For example,

```
\pspolylineticks{Pt}{ dx dy add 3 div }{1}{2}%
```

looks for data arrays made using `\pscurvepoints` with the root name `Pt`. The next argument, `dx dy add 3 div`, specifies the (PostScript) function of increments that should be used to construct the metric. If the keyword `metricInitValue` is defined, eg, with `\psset{metricInitValue=2.5}`, it is used as the initial value of the metric, otherwise it is defined to be 0. In the previous example, the increment function is always positive, and care should be taken to guarantee this is so or the results will not be meaningful. (If we wanted to use arc-length, the function would have been `ds`, assuming equal scales on the axes.) The last two arguments determine the index of the first tick and the number of ticks. Tick numbering begins with index 0, so the example says to drop the first tick and draw the next 2 ticks. In this example, where all keywords take their default values, ticks are potentially located at values on the curve where the metric takes a positive integer value. In the arc-length example, the tick with index 0 is at the beginning of the curve, and subsequent ticks are at unit distance, measured along the curve. At

each index where a tick is drawn, a `\pnode` is created: In this example, you create nodes `PtTick1`, `PtTick2` on the curve where the ticks are located. This is handy for placing labels using, eg, `\Put`. In addition, PostScript data arrays (in this example, `PtTickN.X`, `PtTickN.Y` of the normals at these nodes are stored in the dictionary `TDict`. More importantly, the tangent and normal vectors at `PtTick0` etc are constructed as nodes with names `PtTangent0`, `PtNormal0` etc. See the last example below for typical usage.

The shape of the ticks is governed by the keywords `ticksize` (default value `-4pt 4pt`) and `tickwidth` (default value `.5\linewidth`.) With the default settings, ticks are drawn perpendicular the the curve extending `4pt` to each side. The line

```
\pspolylineticks[ticksize=-6pt 6pt]{Pt}{ dx dy add 3 div }{1}{2}%
```

would draw longer ticks than the default.

Placement of the ticks is governed by the keywords `Ds` and `Os`, whose meaning for the curve is similar to (but not the same as) the meanings of `Dx` and `Ox` with respect to the x axis. That is, if `Ds=2` and `Os=0`, ticks will be drawn where the metric takes values `0`, `2`, `4` and so on. More generally, ticks are placed where the metric takes value `Os`, `Os+Ds`, `Os+2*Ds`, ..., as long as those positions are on the curve. If `Os` has an empty value as a result, say, of `\psset{Os=}`, then `Os` is set internally to the initial metric value. If `Ds` has an empty value, it is set internally to the final metric value less the initial metric value, divided by `10`.

To draw major and minor ticks requires two passes—one to draw the minor ticks and then one to draw the major ticks.

Note that a ticks may be placed at arbitrary metric values on the curve by running the macro once for each point, like:

```
\pspolylineticks[ticksize=-6pt 6pt,Os=1.3]{Pt}{ dx dy add 3 div }{0}{1}%
\pspolylineticks[ticksize=-6pt 6pt,Os=2.4]{Pt}{ dx dy add 3 div }{0}{1}%
```

You may also dispense entirely with the tick and use the macro to generate a node sequence that can be used to place other graphic objects. For example:

```
\pspolylineticks[ticksize=0pt 0pt]{Pt}{ dx dy add 3 div }{0}{3}%
%This defines nodes PtTick0..PtTick2
\multido{\iA=0+1}{3}{\psdot(PtTick\iA)}
```

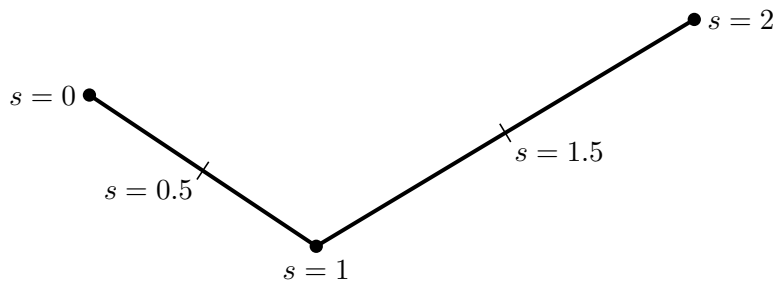
There is another way to define a metric function without using increments. If the keyword `metricFunction` is set to `true`, then the function you present as an argument to `\pspolylineticks` must be a function of x and y only, and must be designed to increase along the curve. It is useful only in those cases where, in essence, the increment function can be explicitly integrated. For example, in the elliptical motion of planets and comets around the sun, it is not hard to integrate the area function explicitly, and this provides a convenient metric, being proportional to time elapsed.

There is some useful information left in the log by these macros. They report the starting and ending values of the metric function, the the range of indices for the Tick related arrays.

29.3. Examples

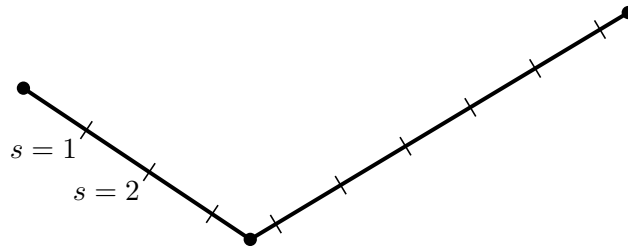
The examples in this section make use of very recent (as of May, 2010) versions of pstricks and related packages.

The first couple of examples are constructed entirely by hand, and have no interest other than to illustrate what is going on under the surface in the simplest case.



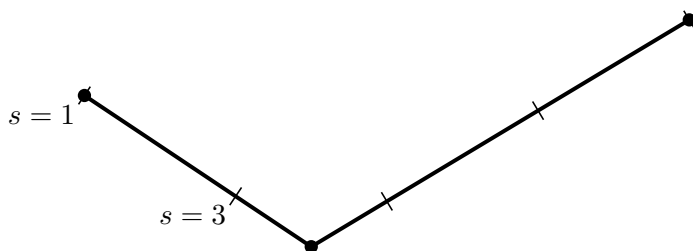
```
\begin{pspicture}(-1,-1)(10,4)
\psline[showpoints=true](1,2)(4,0)(9,3)%
\uput[180](1,2){$s=0$}%
\uput[-90](4,0){$s=1$}%
\uput[0](9,3){$s=2$}%
\makeatletter% need to use macro names containing @
\pstVerb{tx@Dict begin %the pstricks dictionary
% declare arrays of length 3 (indices 0,1,2) to hold points,
% differences and normals
/unitratiosq 1 def % yunit=xunit
/P.X [ 1 4 9 ] def %array of x coords
/P.Y [ 2 0 3 ] def %array of y coords
/PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
/PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
% normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
/PNormal.X [ 2 2 -3 ] def % index 0 =index 1
/PNormal.Y [ 3 3 5 ] def % index 0 = index 1
end }
\def\Ppointcount{2}
\makeatother
% make ticks using metric function with values 0,1,2
\pspolylineticks[0s=.5,Ds=1]{P}{1}{0}{2}
% ticks at s=0.5,1.5 (increment function =1)
\uput[-135](PTick0){$s=0.5$}%
\uput[-45](PTick1){$s=1.5$}%
\end{pspicture}
```

Now the same data, but with arc-length as metric. We change the last few lines:



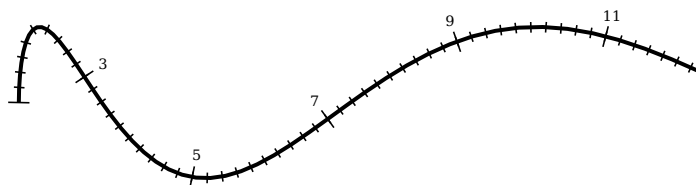
```
\begin{pspicture}(-1,-1)(10,4)
\psline[showpoints=true](1,2)(4,0)(9,3)%
%\uput[180](1,2){$s=0$}%
%\uput[-90](4,0){$s=1$}%
%\uput[0](9,3){$s=2$}%
\makeatletter% need to use macro names containing @
\pstVerb{tx@Dict begin %the pstricks dictionary
% declare arrays of length 3 (indices 0,1,2) to hold points,
% differences and normals
/unitratiosq 1 def % yunit=xunit
/P.X [ 1 4 9 ] def %array of x coords
/P.Y [ 2 0 3 ] def %array of y coords
/PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
/PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
% normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
/PNormal.X [ 2 2 -3 ] def % index 0 =index 1
/PNormal.Y [ 3 3 5 ] def % index 0 = index 1
end }
\def\Ppointcount{2}
\makeatother
% make ticks using metric function arc-length
\pspolylineticks[0s=1,Ds=1]{P}{ ds }{0}{9}
% ticks at s=1,2... (increment function = distance)
\uput[-135](PTick0){$s=1$}%
\uput[-135](PTick1){$s=2$}%
\end{pspicture}
```


Once again the same data, but with metric equal to the x coordinate. Change the last few lines to:



```
\begin{pspicture}(-1,-1)(10,4)
\psline[showpoints=true](1,2)(4,0)(9,3)%
%\uput[180](1,2){$s=0$}%
%\uput[-90](4,0){$s=1$}%
%\uput[0](9,3){$s=2$}%
\makeatletter% need to use macro names containing @
\pstVerb{tx@Dict begin %the pstricks dictionary
% declare arrays of length 3 (indices 0,1,2) to hold points,
% differences and normals
/unitratiosq 1 def % yunit=xunit
/P.X [ 1 4 9 ] def %array of x coords
/P.Y [ 2 0 3 ] def %array of y coords
/PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
/PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
% normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
/PNormal.X [ 2 2 -3 ] def % index 0 =index 1
/PNormal.Y [ 3 3 5 ] def % index 0 = index 1
end }
\def\Ppointcount{2}
\makeatother
% make ticks using metric function arc-length
\pspolylineticks[metricFunction,0s=1,Ds=2]{P}{ x }{0}{5}
% ticks at x=1,3,... , start at tick index 0, draw 5 ticks
% the tick at s=1 has index 0
% ticks at s=1,2... (increment function = distance)
\uput[-135](PTick0){$s=1$}%
\uput[-135](PTick1){$s=3$}%
\end{pspicture}
```

The next example is a smooth path where subticks are drawn first, followed by major ticks. The metric is arc-length with initial value $s = 1$.

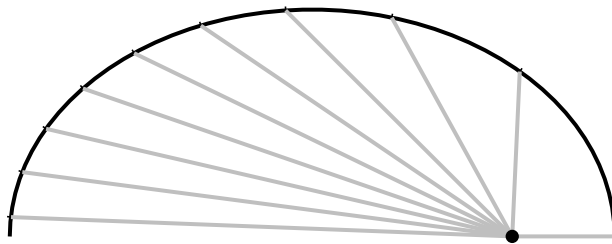


```
\begin{pspicture}(-1,-1)(10,4)
%\parametricplot[algebraic]{0}{9}{(t^2)/9 | 4*Ex(-t)*(1+t+(t^2)/2+(t^3)/6)}
\psparametricplot[algebraic]{0}{9}{t^2/9 | sin(t)+1}%
\pscurvepoints{0}{9}{(t^2)/9 | sin(t)+1}{P}%
% make ticks using arc-length metric
\pspolylineticks[metricInitValue=1,ticksize=-2pt 2pt,0s=1,Ds=.2]{P}{ ds }{1}{56}
%
\pspolylineticks[metricInitValue=1,0s=1,Ds=2]{P}{ ds }{0}{6}%
\multido{\iA=1+1,\iB=3+2}{5}{\Put{6pt;(PNormal\iA)}(PTick\iA){\tiny \iB}}
%\nodexn{(PTick\iA)+(10pt;(PNormal\iA))}{Q}\rput(Q){\tiny \iB}}%
%\multido{\iA=1+1,\iB=3+2}{5}{\uput{6pt}[(PNormal\iA)](PTick\iA){\iB}}%
% ticks at x=1,3,... , start at tick index 0, draw 5 ticks
% the tick at s=1 has index 0
% ticks at s=1,2... (increment function = distance)
\end{pspicture}
```

Suppose for the next example that we have an ellipse $x^2/a^2 + y^2/b^2 = 1$ ($a > b$) with eccentricity $\epsilon = (1 - b^2/a^2)^{1/2}$. With planetary motion in mind, a natural metric for the ellipse is the area swept out by the radial line from the focus $(\epsilon a, 0)$ starting from $(a, 0)$ around to an arbitrary location (x, y) , where $y > 0$, as this quantity is proportional to the time elapsed since perihelion. A routine calculation gives the following formula:

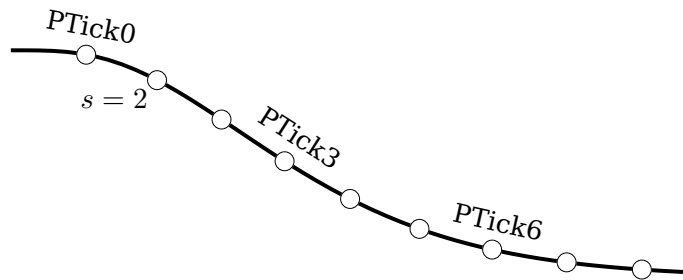
$$A = \frac{ab}{2} \arccos\left(\frac{x}{a}\right) - \frac{\epsilon ay}{2}.$$

Remembering that PostScript's `acos` gives its result in degrees, not radians, we have the following, drawn for the case $a = 4$, $b = 3$.



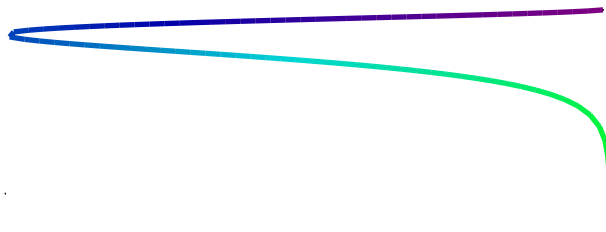
```
\begin{pspicture}(-4.5,-.5)(4.5,3.5)
\pstVerb{ /smajor 4 def /sminor 3 def % define semimajor, semiminor
/ecc 1 sminor smajor div dup mul sub sqrt def % compute eccentricity
/ab smajor sminor mul 2 div def %first coeff
/ea smajor ecc mul 2 div def }% second coeff
\psparametricplot[algebraic]{0}{3.142}{smajor*cos(t) | sminor*sin(t)}%
\pscurvepoints{0}{3.142}{smajor*cos(t) | sminor*sin(t)}{P}%
\pspolylineticks[metricFunction,Ds=2,ticksize=-1.5pt 0]{P}{ ab x smajor div acos
%
180 div PI mul mul ea y mul sub }{1}{9}%
\pnode(! ecc smajor mul 0){S}% focus
\psline[linecolor=lightgray](S)(!smajor 0)%
\multido{\i=1+1}{9}{\psline[linecolor=lightgray](S)(PTick\i)}
\psdot(S)
\end{pspicture}
```

The next examples works without visible ticks, using the macros to construct nodes at which other objects will be placed.



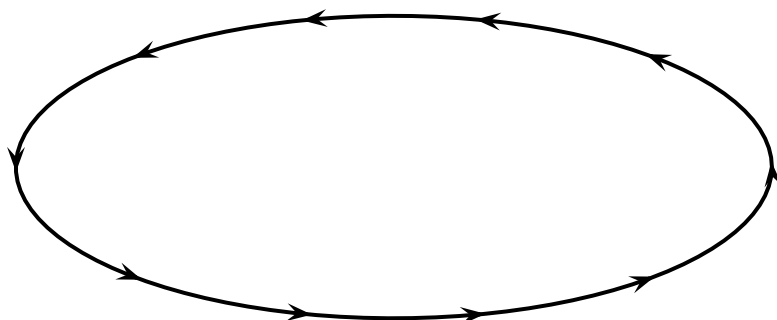
```
\begin{pspicture}(-1,-1)(10,4)
\psparametricplot[algebraic]{0}{9}{t| 3*Ex(-t)*(1+t+t^2/2+t^3/6)}
\pscurvepoints{0}{9}{t| 3*Ex(-t)*(1+t+t^2/2+t^3/6)}{P}%
\pspolylineticks[0s=1,Ds=1,ticks=0 0]{P}{ ds }{0}{9}%
\multido{\i=0+1}{9}{\psdot[dotscale=1.5,dotstyle=o](PTick\i)}%
% ticks at s=1,2,... , start at tick index 0, set 9 ticks
% the tick at s=1 has index 0
% ticks at s=1,2... (increment function = distance)
\multido{\i=0+3}{3}{\Put[rot=(PTangent\i)]{7pt;(PNormal\i)}(PTick\i){PTick\i}}%
\uput[-135](PTick1){$s=2$}%
\end{pspicture}
```

This variant also has no visible ticks, but makes a color gradient along the curve based on arc-length from the start.



```
\begin{pspicture}(-1,-1)(10,4)
\psparametricplot[plotpoints=200,linecolor=white]{0}{360}{ t cos 1 add 4 mul t 1
  add 20 div ln 2 div 1 add }
\pscurvepoints[plotpoints=200]{0}{360}{ t cos 1 add 4 mul t 1 add 20 div ln 2
  div 1 add }{P}%
\pspolylineticks[0s=0,Ds=.2,ticksiz=0 0]{P}{ ds }{0}{90}%
\definecolorseries{ctest}{hsb}{last}{green}{violet}
\resetcolorseries[88]{ctest}%
\multido{\iA=0+1,\iB=1+1}{87}{\psline[linewidth=2pt,linecolor=ctest!![\iB](PTick
  \iA)(PTick\iB)}%
\end{pspicture}
```

Here is another variant of this technique which allows arrows to be placed at locations on the curve where the metric takes particular values.



```
\begin{pspicture}(-1,-1)(10,4.5)
\psparametricplot[plotpoints=100]{0}{360}{t cos 1 add 5 mul t sin 1 add 2 mul}
\pscurvepoints[plotpoints=100]{0}{360}{t cos 1 add 5 mul t sin 1 add 2 mul}{P}%
\pspolylineticks[0s=0,Ds=2.3,ticksiz=0 0]{P}%
{ ds }{0}{10}% distance
\multido{\i=0+1}{10}{\psrline[arrows=->,arrowscale=1.5](PTick\i)(2pt;{(PTangent\i)}}}%
\end{pspicture}
```

30. Troubleshooting

If you get PostScript errors when you process your file, the most likely culprit is the function you specified to define the metric. There are some things to look out for:

- If `metricFunction`, the function you specify in PostScript code must involve only `x` and `y`, and must leave exactly one real value on the stack as a result of substituting specific values for `x` and `y`. The function must be strictly increasing on the curve.
- If `metricFunction=false` (the default), the function you specify in PostScript code must involve only the variables `x`, `y`, `dx`, `dy`, `ds` (where `ds` is defined to be the arc-length element `dx dup mul dy dup mul add sqrt`, and must leave exactly one strictly positive real value on the stack when specific values are substituted for those variables. The constant function 1 gives equal weight to each segment in the curve, so in effect it gives you the original parametrization, up to a constant factor.
- If the function you specify in `\parametricplot` and `\pscurvepoints` is algebraic, make sure you follow precisely the syntax it understands. In complex cases, PostScript may be the safer solution.
- It is unwise to use a different resolution for `\psparametricplot` and `\pscurvepoints`. The default value of `plotpoints=50` is marginal except for modest curve segments, and 200 should suffice for most smooth curves.

31. Transparent colors

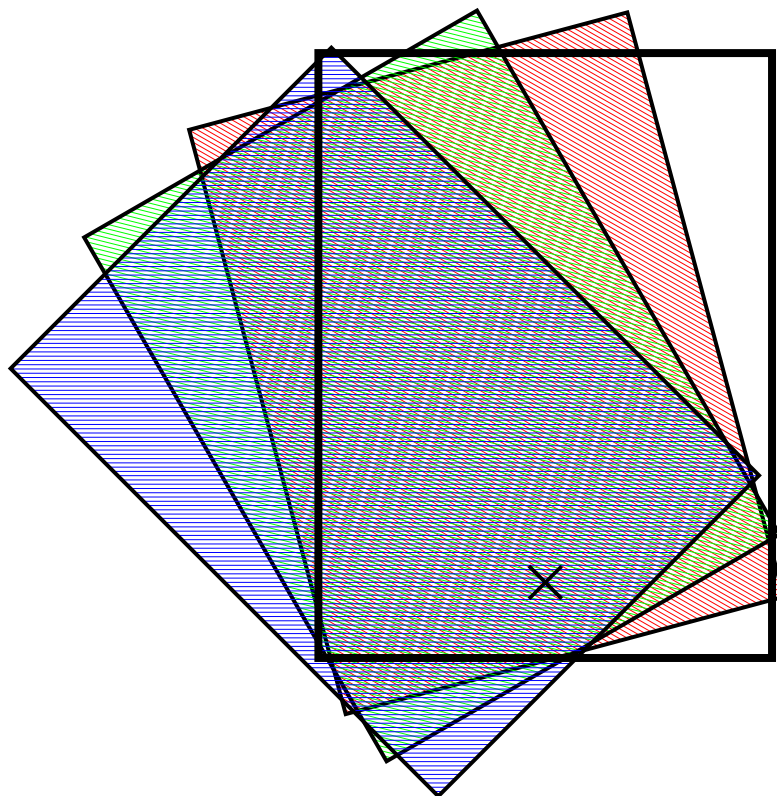
Transparency is now part of the main pstricks package. But pay attention, the names and syntax have changed and you need to run ps2pdf with the option `-dCompatibilityLevel=1.4`.

32. „Manipulating transparent colors“

pstricks-add supports real transparency and a simulated one with hatch lines:

```
\def\defineTColor{\@ifnextchar[{\defineTColor@i}{\defineTColor@i[]}}
\def\defineTColor@i[#1]#2#3{% transparency "Colors"
  \newsstyle{#2}{%
    fillstyle=vlines,hatchwidth=0.1\pslinewidth,
    hatchsep=1\pslinewidth,hatchcolor=#3,#1%
  }%
}
\defineTColor{TRed}{red}
\defineTColor{TGreen}{green}
\defineTColor{TBlue}{blue}
```

There are three predefined "transparent" colors TRed, TGreen, TBlue. They are used as PSTricks styles and not as colors:



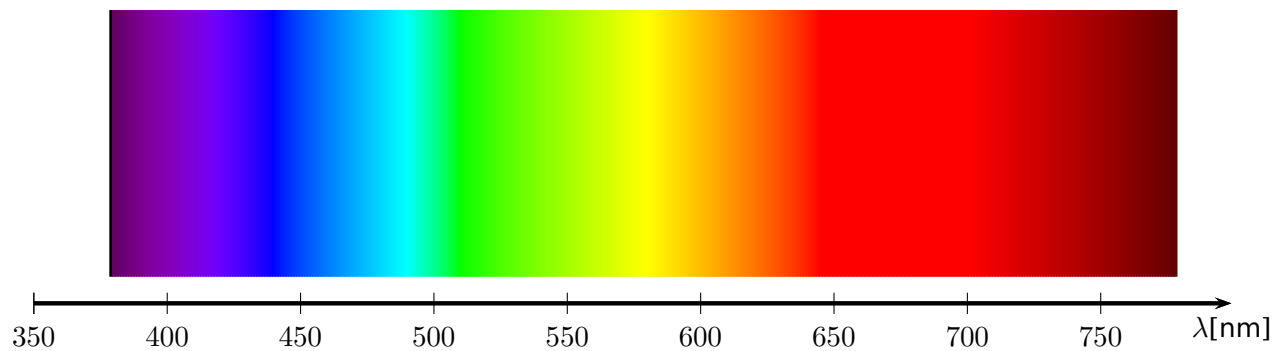
```
\begin{pspicture}(-3,-5)(5,5)
\psframe(-1,-3)(5,5) % objet de base
\psrotate(2,-2){15}{%
  \psframe[style=TRed](-1,-3)(5,5)}
\psrotate(2,-2){30}{%
  \psframe[style=TGreen](-1,-3)(5,5)}
\psrotate(2,-2){45}{%
  \psframe[style=TBlue](-1,-3)(5,5)}
\psframe[linewidth=3pt](-1,-3)(5,5)
\psdots[dotstyle=+,dotangle=45,dotscale=3](2,-2) % centre de la rotation
\end{pspicture}
```

33. Calculated colors

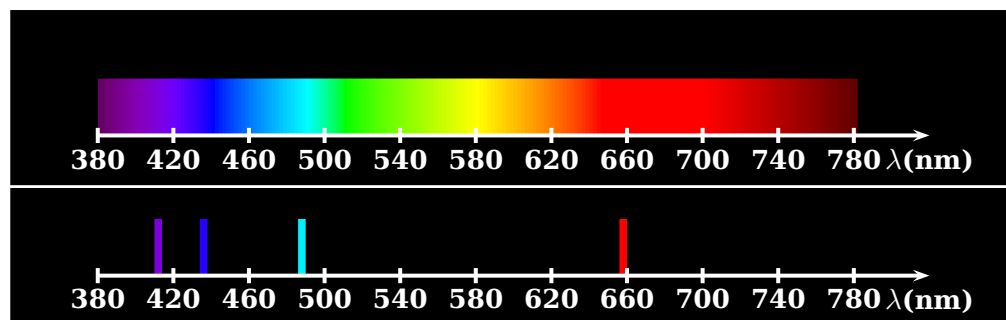
The xcolor package (version 2.6) has a new feature for defining colors:

```
\definecolor[ps]{<name>}{<model>}{< PS code >}
```

model can be one of the color models, which PostScript will understand, e.g. rgb. With this definition the color is calculated on the PostScript side.



```
\definecolor[ps]{bl}{rgb}{tx@addDict begin Red Green Blue end}%
\psset{unit=1bp}
\begin{pspicture}(0,-30)(400,100)
\multido{\iLAMBDA=0+1}{400}{%
\pstVerb{
\iLAMBDA\space 379 add dup /lambda exch def
tx@addDict begin wavelengthToRGB end
}%
\psline[linecolor=bl](\iLAMBDA,0)(\iLAMBDA,100)%
}
\psaxes[yAxis=false,0x=350,dx=50bp,Dx=50]{->}{-29,-10}(420,100)
\uput[-90](420,-10){$\lambda$[nm]}
\end{pspicture}
```



Spectrum of hydrogen emission (Manuel Luque)

```
\newcommand\Touch{%
\psframe[linestyle=none,fillstyle=solid,fillcolor=bl,dimen=middle](0.1,0.75)}
\definecolor[ps]{bl}{rgb}{tx@addDict begin Red Green Blue end}%
% Echelle 1cm <-> 40 nm
% 1 nm <-> 0.025 cm
\psframebox[fillstyle=solid,fillcolor=black]{%
\begin{pspicture}(-1,-0.5)(12,1.5)
\multido{\iLAMBDA=380+2}{200}{%
\pstVerb{
/lambda \iLAMBDA\space def
lambda
tx@addDict begin wavelengthToRGB end
}%
\rput(! lambda 0.025 mul 9.5 sub 0){\Touch}
}
}
```

```

\multido{\n=0+1,\iDiv=380+40}{11}{%
  \psline[linecolor=white](\n,0.1)(\n,-0.1)
  \uput[270](\n,0){\textbf{\white\iDiv}}
  \psline[linecolor=white]{->}(11,0)
  \uput[270](11,0){\textbf{\white$\lambda$(nm)}}
\end{pspicture}}

\psframebox[fillstyle=solid,fillcolor=black]{%
\begin{pspicture}(-1,-0.5)(12,1)
  \pstVerb{
    /lambda 656 def
    lambda
    tx@addDict begin wavelengthToRGB end
  }%
  \rput(! 656 0.025 mul 9.5 sub 0){\Touch}
  \pstVerb{
    /lambda 486 def
    lambda
    tx@addDict begin wavelengthToRGB end
  }%
  \rput(! 486 0.025 mul 9.5 sub 0){\Touch}
  \pstVerb{
    /lambda 434 def
    lambda
    tx@addDict begin wavelengthToRGB end
  }%
  \rput(! 434 0.025 mul 9.5 sub 0){\Touch}
  \pstVerb{
    /lambda 410 def
    lambda
    tx@addDict begin wavelengthToRGB end
  }%
  \rput(! 410 0.025 mul 9.5 sub 0){\Touch}
\multido{\n=0+1,\iDiv=380+40}{11}{%
  \psline[linecolor=white](\n,0.1)(\n,-0.1)
  \uput[270](\n,0){\textbf{\white\iDiv}}
  \psline[linecolor=white]{->}(11,0)
  \uput[270](11,0){\textbf{\white$\lambda$(nm)}}
\end{pspicture}}

```

Spectrum of hydrogen emission (Manuel Luque)

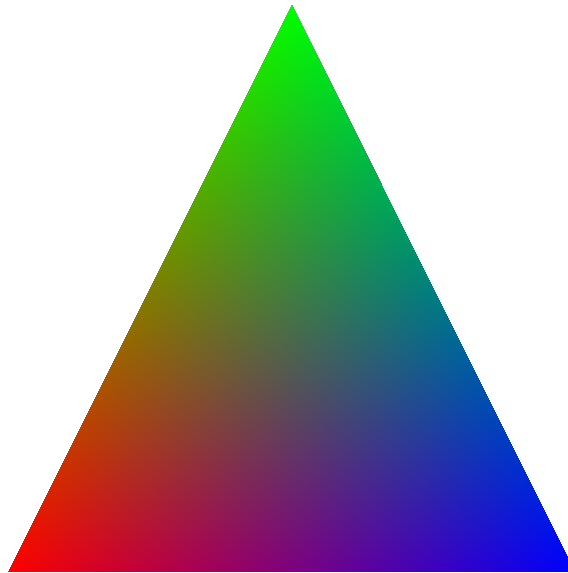
34. Gouraud shading

Gouraud shading is a method used in computer graphics to simulate the differing effects of light and colour across the surface of an object. In practice, Gouraud shading is used to achieve smooth lighting on low-polygon surfaces without the heavy computational requirements of calculating lighting for each pixel. The technique was first presented by Henri Gouraud in 1971.

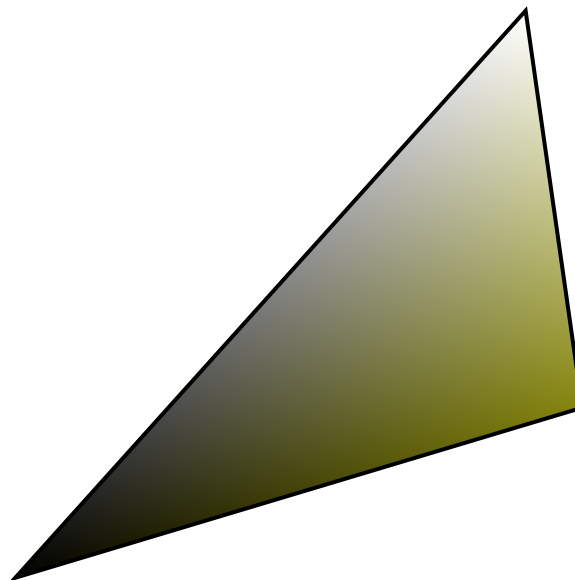
<http://www.wikipedia.org>

PostScript level 3 supports this kind of shading and it can only be seen with Acroread 7 or later. The syntax is easy:

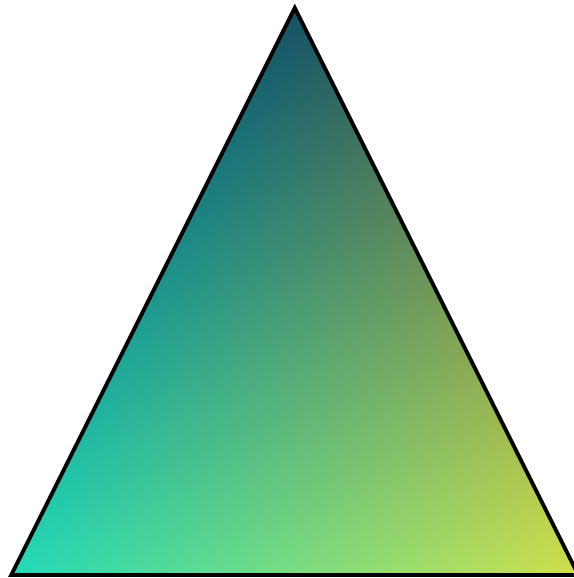
```
\psGTriangle(x1,y1)(x2,y2)(x3,y3){color1}{color2}{color3}
```



```
\begin{pspicture}(0,-.25)(10,10)
\psGTriangle(0,0)(5,10)(10,0){red}{green}{blue}
\end{pspicture}
```



```
\begin{pspicture}(0,-.25)(10,10)
\psGTriangle*(0,0)(9,10)(10,3){black}{white!50}{red!50!green!95}
\end{pspicture}
```



```
\begin{pspicture}(0,-.25)(10,10)
\psGTriangle*(0,0)(5,10)(10,0){-red!100!green!84!blue!86}
                                   {-red!80!green!100!blue!40}
                                   {-red!60!green!30!blue!100}
\end{pspicture}
```



```
\definecolor{rose}{rgb}{1.00, 0.84, 0.88}
\definecolor{vertpommeasmure}{rgb}{0.80, 1.0, 0.40}
\definecolor{fushia}{rgb}{0.60, 0.30, 1.0}
\begin{pspicture}(0,-.25)(10,10)
\psGTriangle(0,0)(5,10)(10,0){rose}{vertpommeasmure}{fushia}
\end{pspicture}
```

A. \resetOptions

Sometimes it is difficult to know what options, which are changed inside a long document, are different to the default ones. With this macro all options belonging to pst-plot can be reset. This refers to all options of the packages pstricks, pst-plot and pst-node.

B. PostScript

PostScript uses the stack system and the LIFO system, "Last In, First Out".

Table 4: Some primitive PostScript macros

<i>Function</i>	<i>Meaning</i>	
	<i>on stack before</i>	<i>→ after</i>
add	$x \ y$	$x + y$
sub	$x \ y$	$x - y$
mul	$x \ y$	$x \times y$
div	$x \ y$	$x \div y$
sqrt	x	\sqrt{x}
abs	x	$ x $
neg	x	$-x$
cos	x	$\cos(x)$ (x in degrees)
sin	x	$\sin(x)$ (x in degrees)
tan	x	$\tan(x)$ (x in degrees)
atan	$y \ x$	$\angle(\vec{Ox}; \vec{OM})$ (in degrees of $M(x, y)$)
ln	x	$\ln(x)$
log	x	$\log(x)$
array	n	v (of dimension n)
aload	v	$x_1 \ x_2 \ \dots \ x_n \ v$
astore	$x_1 \ x_2 \ \dots \ x_n \ v$	$[v]$
pop	x	-
dup	x	$x \ x$

C. List of all optional arguments for pstricks-add

Key	Type	Default
CMYK	boolean	true
intSeparator	ordinary	[none]
braceWidth	ordinary	[none]
bracePos	ordinary	[none]
braceWidthInner	ordinary	[none]
braceWidthOuter	ordinary	[none]
veearrowlength	ordinary	3mm
veearrowangle	ordinary	30
veearrowlinewidth	ordinary	0.35mm
filledveearrowlength	ordinary	3mm
filledveearrowangle	ordinary	15
filledveearrowlinewidth	ordinary	0.35mm
tickarrowlength	ordinary	1.5mm
tickarrowlinewidth	ordinary	0.35mm
hooklength	ordinary	3mm
hookwidth	ordinary	1mm
ArrowFill	boolean	true
nArrowsA	ordinary	2
nArrowsB	ordinary	2
nArrows	ordinary	2
ArrowInside	ordinary	[none]
ArrowInsidePos	ordinary	0.5
ArrowInsideNo	ordinary	1
ArrowInsideOffset	ordinary	0
Os	ordinary	0
Ds	ordinary	1
metricInitValue	ordinary	0
metricFunction	boolean	true
randomPoints	ordinary	1000
color	boolean	true
blName	command	
bcName	command	
brName	command	
clName	command	
ccName	command	
crName	command	
tlName	command	
tcName	command	
trName	command	
whichabs	ordinary	[none]
whichord	ordinary	[none]

Continued on next page

Continued from previous page

Key	Type	Default
plotfuncx	ordinary	[none]
plotfuncy	ordinary	[none]
expression	ordinary	[none]
buildvector	boolean	true
varsteptol	ordinary	[none]
adamsorder	ordinary	[none]
StepType	ordinary	[none]
Derive	ordinary	[none]
Tnormal	boolean	true
GetFinalState	boolean	true
filename	ordinary	[none]
saveData	boolean	true
Xoffset	ordinary	0pt
Yoffset	ordinary	0pt
XYoffset	ordinary	0pt
colorType	ordinary	0
chartStyle	ordinary	[none]
chartColor	ordinary	[none]
chartSep	ordinary	[none]
chartStack	ordinary	[none]
chartStackDepth	ordinary	[none]
chartStackWidth	ordinary	[none]
chartHeight	ordinary	[none]
userColor	ordinary	[none]
chartNodeI	ordinary	[none]
chartNode0	ordinary	[none]
markAngle	boolean	true

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