# The derivative package 

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The derivative package provides a set of commands which makes writing ordinary and partial derivatives of arbitrary order in a straight forward manner. Additionally, this package provides a set of commands to define variants of the aforementioned derivatives. A set of optional arguments along with lots of package options allow for easy and great flexibility over the derivative's format, such as where the function is positioned, point of evaluation, and switching between fraction styles. Moreover, the mixed order of the partial derivative and variants hereof is automatically computed. This package is written in the expl3 language and requires therefore the $\mathrm{LAT}_{\mathrm{E}} \mathrm{X} 3$ package bundles I3kernel and I3package. Additionally, the mleftright package is optional and provides the improved automatically scaling $\backslash m l e f t$ and \mright.

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This package started as a personal package a few years ago that I used in various projects．Firstly，it was written in $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ and $\mathrm{LA}_{\mathrm{E}} \mathrm{X}$ ，which gave rise to various errors as the complexity of the package grew larger and ended up as a spaghetti code．Therefore， the code was rewritten into the $\mathrm{LAT}_{\mathrm{EX}}$ 3 language and may now be easily maintained． Originally this package was written because there did not exist any great package for derivatives．It was first much later that I discovered the diffcoeff package，which does a good job．However，at this time，I had already written much of the code with no documentation．So I decided to write one and make it into a package for the public．

As a note on terminology，I use the wording infinitesimal abbreviated as inf for the operator symbols $d, \partial, \delta$ etc．that used in derivatives like $\frac{\mathrm{d} y}{\mathrm{~d} x}, \frac{\partial y}{\partial x}, \frac{\delta y}{\delta x}$ and in differentials like $\mathrm{d} x, \partial_{x}, \delta x$ ．In the description of macros and options，I often write $c s$－〈placeholder〉 to denote a comma－separated list of $\langle$ placeholder $\rangle$ ．For example，［〈cs－numbers $\rangle$ ］is used in the option section for math space keys to denote comma－separated list of numbers． It should also be noted that whenever an argument reads 〈keyvalue list〉，it means that it is a comma－separated list of keyvalue pairs．

## 1 Derivative

＊［〈keyval list $\rangle]\{\langle$ function $\rangle\} /\left\{\left\langle\right.\right.$ variables $\left.^{\prime}\right\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\} \_\left\{\left\langle\text {point }_{2}\right\rangle\right\}$
The partial derivative $\backslash p d v$ is defined with a set of mandatory and optional arguments that either typeset specific parts or changing the style of the derivative．In this package， the partial derivative is defined with an italic partial differential $\partial$ as
$\backslash$ DeclareDerivative $\{\backslash p d v\}\{\backslash$ partial\} [style-var=multiple, sep-inf-ord=1, delims－eval＝（），delims－eval－／＝（）］
＊The first argument of $\backslash p d v$ is an optional star that determines where the function is typeset；either in the numerator of the fraction or next to the fraction．Using the option switch－＊＝false，the function is typeset in the numerator when the star is absent，and next to the fraction when the star is present as shown below

$$
\begin{aligned}
\backslash \operatorname{pdv}\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2} f}{\partial x \partial y} \\
\backslash \operatorname{pdv} *\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2}}{\partial x \partial y} f
\end{aligned}
$$

The effect of the star＇s presence can be switched around using switch－＊＝true i．e．the equations in the above example are exchanged．
［〈keyval list $\rangle$ ］
Updated：v1．0

The second argument is optional and is written inside square brackets．This argument is used to set the options of the derivative using a key＝value semantic．For example the order of differentiation can be set via the order option

$$
\begin{aligned}
\backslash \operatorname{pdv}[\text { order }=\{2,3\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{5} f}{\partial x^{2} \partial y^{3}} \\
\backslash \operatorname{pdv}[\text { order }=\{\backslash \text { beta, } \mathrm{a}, \mathrm{n}+2 \mathrm{a}\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3 a+\beta+n} f}{\partial x^{\beta} \partial y^{a} \partial z^{n+2 a}} \\
\backslash \operatorname{pdv}\left[\text { order }=\left\{2, \mathrm{n}^{\wedge} 2, \mathrm{n}^{\wedge} 2-1\right\}\right]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{2 n^{2}+1} f}{\partial x^{2} \partial y^{n^{2}} \partial z^{n^{2}-1}} \\
& \Longrightarrow \frac{\partial^{n^{2}+3} f}{\partial x^{2} \partial y^{n^{2}} \partial z}
\end{aligned}
$$

The list of options that can be applied to derivatives can be found in section 3．2．
\｛〈function〉\} This is the first mandatory argument that typeset the function that is to be differentiated

$$
\begin{aligned}
\backslash \operatorname{pdv}\{\mathrm{f}(\mathrm{x}, \mathrm{y}, \mathrm{z})\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3} f(x, y, z)}{\partial x \partial y \partial z} \\
\backslash \operatorname{pdv}\left\{\mathrm{e}^{-} \mathrm{x} \backslash \sin (\mathrm{y}) \backslash \ln (\mathrm{z})\right\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3} e^{x} \sin (y) \ln (z)}{\partial x \partial y \partial z}
\end{aligned}
$$

The function is simply typeset in the numerator or next to the fraction.
/ The fourth argument is an optional slash written between the function and the variable arguments and determines which fraction style the derivative is typeset with, as described in section 3.2. Using the option switch-/=false and the package's default fractions, the derivative is typeset with $\backslash f r a c$ when the slash is absent, and $\backslash$ slashfrac ${ }^{1}$ when the slash is present, as shown below

$$
\begin{aligned}
\backslash \operatorname{dv}\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2} f}{\partial x \partial y} \\
\backslash \operatorname{pdv}\{\mathrm{f}\} /\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \partial^{2} f / \partial x \partial y
\end{aligned}
$$

As for the star argument, the effect of the slash's presence can be switched around using switch-/=true i.e. the equations in the above example are exchanged.
\{〈variables〉\} This is the second and final mandatory argument, which purpose is to typeset the variable in which the function is differentiated with respect to. The variables are given in a comma-separated list e.g. $\{x, y, z\}$

$$
\begin{aligned}
\backslash \operatorname{pdv}\{\mathrm{f}\}\{\mathrm{x}\} & \Longrightarrow \frac{\partial f}{\partial x} \\
\backslash \operatorname{pdv}\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2} f}{\partial x \partial y}
\end{aligned}
$$

This is the last optional argument that specifies the point(s) of evaluation or variables held constant. It is an e-type argument in the xparse language and is given by e\{_ $\left.{ }^{\wedge}\right\}$. This means that the subscript _ and superscript ^ accepts an argument given in braces. Moreover, the order of _ and ~ is independent as shown below

$$
\begin{aligned}
\backslash \operatorname{pdv}\{f\}\{\mathrm{x}, \mathrm{y}\}_{-}\left\{\left(\mathrm{x}_{-} 1, \mathrm{y}_{-} 1\right)\right\} & \Longrightarrow\left(\frac{\partial^{2} f}{\partial x \partial y}\right)_{\left(x_{1}, y_{1}\right)} \\
\backslash \operatorname{pdv}\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} \_\left\{\left(\mathrm{x}_{-} 2, \mathrm{y}_{-} 2\right)\right\} & \Longrightarrow\left(\frac{\partial^{2} f}{\partial x \partial y}\right)^{\left(x_{2}, y_{2}\right)} \\
\backslash \operatorname{pdv}\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} \_\left\{\left(\mathrm{x}_{-} 1, \mathrm{y}_{-} 1\right)\right\} \sim\left\{\left(\mathrm{x}_{-} 2, \mathrm{y}_{-} 2\right)\right\} & \Longrightarrow\left(\frac{\partial^{2} f}{\partial x \partial y}\right)_{\left(x_{1}, y_{1}\right)}^{\left(x_{2}, y_{2}\right)} \\
\backslash \operatorname{pdv\{ f\} \{ \mathrm {x},\mathrm {y}\} \wedge \{ (\mathrm {x}_{-}2,\mathrm {y}_{-}2)\} \} \{ (\mathrm {x}_{-}1,\mathrm {y}_{-}1)\} } & \Longrightarrow\left(\frac{\partial^{2} f}{\partial x \partial y}\right)_{\left(x_{1}, y_{1}\right)}^{\left(x_{2}, y_{2}\right)}
\end{aligned}
$$

The subscript argument is commonly used as the point of evaluation or variables held constant. If needed, the superscript argument may be used for the second point of evaluation.

[^0]
### 1.1 Other derivatives

This package offers five other derivatives: Ordinary derivative \odv, material derivative $\backslash m d v$, functional derivative $\backslash f d v$, the average rate of change \adv and the Jacobian $\backslash j d v$. A unique feature of this package, is that you can define your own derivatives as described in section 4.1.
\odv $*[\langle$ keyval list $\rangle]\{\langle$ function $\rangle\} /\{\langle$ variables $\rangle\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\} \sim\left\{\left\langle\right.\right.$ point $\left.\left._{2}\right\rangle\right\}$
In this package, the ordinary derivative is defined with an upright lowercase $d$ as

```
\DeclareDerivative{\odv}{\mathrm{d}}
\DeclareDerivative{\odv}{\symup{d}}
```

because it is used by many nowadays books

$$
\frac{\mathrm{d} f}{\mathrm{~d} x}=\lim _{h \rightarrow 0}\left(\frac{f(x+h)-f(x)}{h}\right)
$$

However it can always be changed with the style-inf key.
*[〈keyval list $\rangle]\{\langle$ function $\rangle\} /\{\langle$ variables $\rangle\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\}^{\wedge}\left\{\left\langle\right.\right.$ point $\left.\left._{2}\right\rangle\right\}$
The material derivative is used in some branches of physics e.g. thermodynamic, fluid dynamic etc. It is only natural for a physics student as me to define such a variant, that used an upright uppercase D. In this package, the material derivative is defined as

```
\DeclareDerivative{\mdv}{\mathrm{D}}
\DeclareDerivative{\mdv}{\symup{D}}
```

In physics, the material derivative is defined by

$$
\frac{\mathrm{D} \varphi(\mathbf{r}, t)}{\mathrm{D} t}:=\frac{\partial \varphi(\mathbf{r}, t)}{\partial t}+\dot{\mathbf{r}} \cdot \nabla \varphi(\mathbf{r}, t)
$$

\fdv $*[\langle$ keyval list $\rangle]\{\langle$ function $\rangle\} /\left\{\left\langle\right.\right.$ variables $\left.^{\prime}\right\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\}$ - $\left\{\left\langle\right.\right.$ point $\left.\left._{2}\right\rangle\right\}$
The functional derivative is used in the calculus of variation and uses a lowercase delta. With the package's default settings, it will use an italic delta. In this package, the functional derivative is defined as

```
\DeclareDerivative{\fdv}{\delta}
```

In physics, it is for example used in the Lagrange equation or in the derivation of the Hartree-Fock equation

$$
\frac{\delta I}{\delta q_{\alpha}}=\frac{\partial L}{\partial q_{\alpha}}-\frac{\mathrm{d}}{\mathrm{~d} t} \frac{\partial L}{\partial \dot{q}_{\alpha}}=0, \quad \frac{\delta \mathcal{L}}{\delta \psi_{n}^{*}}=\hat{F}\left|\psi_{n}\right\rangle-\epsilon_{n}\left|\psi_{n}\right\rangle=0,
$$

respectively.
*[ $\langle$ keyval list $\rangle]\{\langle$ function $\rangle\} /\{\langle$ variables $\rangle\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\} \_\left\{\left\langle\text {point }_{2}\right\rangle\right\}$
The average rate of change is defined to use an upright uppercase delta with the packages default settings. In this package, the average rate of change is defined as
pdfTEX

$\operatorname{pdf} \mathrm{TE}_{\mathrm{E}} \mathrm{X}$
X GIEX $^{2}$, LuateX
$\operatorname{pdf} T_{E} \mathrm{X}, \mathrm{X}_{\mathrm{G}} \mathrm{TE}_{\mathrm{E}} \mathrm{X}$, Lua $_{\mathrm{E}} \mathrm{X}$

```
\DeclareDerivative{\adv}{\Delta}
```

$\operatorname{pdf} T_{E} \mathrm{X}, \mathrm{X}_{\mathrm{G}} \mathrm{T}_{\mathrm{E}} \mathrm{X}, \operatorname{Lua}_{\mathrm{E}} \mathrm{X}$

The average rate of change is used to determine the slope of a straight line

$$
\frac{\Delta y}{\Delta x}=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}
$$

$\backslash j \mathrm{dv} \quad *[\langle$ keyval list $\rangle]\{\langle$ function $\rangle\} /\{\langle$ variables $\rangle\} \_\left\{\left\langle\text {point }_{1}\right\rangle\right\} \wedge\left\{\left\langle\right.\right.$ point $\left.\left._{2}\right\rangle\right\}$
Updated: v1.0 The Jacobian is defined to use an italic partial differential with the package's default settings. Also a pair of parentheses is automatically inserted around the function and variable. In this package, the Jacobian is defined as

## \DeclareDerivative\{\jdv\}\{\partial\}[fun=true, var=1]

which gives

$$
\frac{\partial(f, g, h)}{\partial(x, y, z)}
$$

## 2 Differentials

## \odif

＊［〈keyval list $\rangle$ ］$\{\langle$ variables $\rangle\}$
New：v1．0 The differential \odif using an lowercase d is defined with a set of mandatory and optional arguments that either typeset specific parts or changing the style of the differential．It is defined as

```
\DeclareDifferential{\odif}{\mathrm{d}}
\DeclareDifferential{\odif}{\symup{d}}
```

$\operatorname{pdf} \mathrm{TE}_{\mathrm{E}} \mathrm{X}$
$\mathrm{X}_{\mathrm{H}_{\mathrm{E}} \mathrm{T}} \mathrm{X}, \mathrm{Lua} \mathrm{T}_{\mathrm{E}} \mathrm{X}$
＊The first argument of \odif is an optional star that determines the notation style of the differential．Using the option switch－＊＝false，the variables and orders are typeset in a subscript and superscript respectively when the star is present．When the star is absent，then the macros associated infinitesimal is placed in front of each variable as shown below

$$
\begin{aligned}
\operatorname{lodif}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \mathrm{d} x \mathrm{~d} y \mathrm{~d} z \\
\operatorname{\backslash odif} *\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \mathrm{d}_{x, y, z}
\end{aligned}
$$

The effect of the star＇s presence can be switched around using switch－＊＝true i．e．the equations in the above example are exchanged，as described in section 3．2．
［〈keyval list $\rangle$ ］The second argument is optional and is written inside square brackets．This argument is used to set the options of the differential using a key＝value semantic．

$$
\begin{aligned}
&\text { \odif [order }=\{\mathrm{n}, 3\}]\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} \Longrightarrow \\
& \mathrm{d}^{n} x \mathrm{~d}^{3} y \mathrm{~d} z \\
& \text { \odif }[\text { sep-var-inf }=0]\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} \Longrightarrow \\
& \mathrm{d} x \mathrm{~d} y \mathrm{~d} z \\
& \text { \odif*[sep-var-var=0] }\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} \Longrightarrow
\end{aligned} \mathrm{d}_{x y z} \quad l
$$

The list of options that can be applied to differential can be is found in section 3.3
\｛〈variables $\}$ \}
This is the mandatory argument，which purpose is to typeset the variables，as shown below

$$
\begin{aligned}
\text { \odif }\{\mathrm{x}\} & \Longrightarrow \mathrm{d} x \\
\backslash \operatorname{odif}\left\{\mathrm{~s}_{1} 1, \mathrm{~s}_{-} 2 \ldots, \mathrm{~s} \_\mathrm{n}\right\} & \Longrightarrow \mathrm{d} s_{1} \mathrm{~d} s_{2} \ldots \mathrm{~d} s_{n}
\end{aligned}
$$

## 2．1 Other differentials

This package offers four other differentials：partial differential \pdif，uppercase D \mdif，delta \fdif and Delta \adif．A unique feature of this package，is that you can define your own differential as described in section 4．2．
\pdif $*[\langle$ keyval list $\rangle]\{\langle$ variables $\rangle\}$
The partial differential \pdif is typically used as a shorthand notation for the partial derivative．In this package it is defined as

```
\DeclareDifferential{\pdif}{\partial}[style-notation=single,
style-notation-*=mixed]
```

The non-star and star version gives

$$
\begin{aligned}
\partial_{x, y, z}^{i, j, k} & :=\frac{\partial^{i+j+k}}{\partial x^{i} \partial y^{j} \partial z^{k}} \\
\partial_{x}^{i} \partial_{y}^{j} \partial_{z}^{k} & :=\frac{\partial^{i+j+k}}{\partial x^{i} \partial y^{j} \partial z^{k}}
\end{aligned}
$$

respectively.
\mdif $\quad *[\langle$ keyval list $\rangle]\{\langle$ variables $\rangle\}$
Another commonly used shorthand notation for various derivatives is the differential with a uppercase D. In this package it is defined with a upright D as

```
\DeclareDifferential{\mdif}{\mathrm{D}}[style-notation=single,
style-notation-*=mixed]
\DeclareDifferential{\mdif}{\symup{D}}[style-notation=single,
style-notation-*=mixed]
```

$\operatorname{pdfT} \mathrm{X}$
$\mathrm{X}_{\underline{G}} \mathrm{~T}_{\mathrm{E}} \mathrm{X}, \mathrm{LuaT}_{\mathrm{E}} \mathrm{X}$

The non-star and star version gives

$$
\begin{array}{r}
\mathrm{D}_{x, y, z}^{i, j, k} \\
\mathrm{D}_{x}^{i} \mathrm{D}_{y}^{j} \mathrm{D}_{z}^{k}
\end{array}
$$

respectively.
\fdif $*[\langle$ keyval list $\rangle]\{\langle$ variables $\rangle\}$
When working with functional derivatives another differential is frequently encountered. This differential uses a delta symbol and is defined as

## \DeclareDifferential\{\fdif\}\{\delta\}

For example an expression like

$$
\delta J=\int_{a}^{b} \frac{\partial L}{\partial f} \delta f(x)+\frac{\partial L}{\partial f^{\prime}} \frac{\mathrm{d}}{\mathrm{~d} x} \delta f(x) \mathrm{d} x
$$

is frequently encountered.
\adif $*[\langle$ keyval list $\rangle]\{\langle$ variables $\rangle\}$
To wrap it up, a differential for differences is defined as

```
\DeclareDifferential{\adif}{\Delta}
```

```
pdfTEX, XGTEX, LuaTEX
```

For example

$$
\Delta E=E_{2}-E_{1}
$$

## 3 Package options

This package accepts its options using the well－known key＝value syntax．The keys are divided into categories，for which each key have its associated category as a prefix．
\｛〈command $\rangle\}$［〈keyval list $\rangle$ ］
Updated：v1．0
The \derivset is meant to set the default values for derivatives and differentials options in the preamble．It can be used in the document but this is what the new［〈keyval list）］arguments are for in the derivative and differential commands．
$\{\langle$ command $\rangle\}$ A mandatory argument that determines which command the key＝value pairs is assigned to，where the allowed 〈commands〉 are the derivatives and differentials defined by the package and you，see sections 4.1 and 4.2 for more information．The special value all is also allowed，which gives access to the options that applies to all derivatives and differentials．
［〈keyval list $\rangle$ ］This optional argument accepts its input as a comma－separated list of key＝value pairs． Leaving out［〈keyval list $\rangle$ ］sets the options to the package＇s default settings for the chosen $\{\langle$ command $\rangle\}$ ．E．g．\derivset $\{\backslash o d v\}$ sets the options for the ordinary derivative to the packages default settings．

## 3．1 Categories

This section seeks to give a detailed description of each category．
－The style－$\langle\ldots\rangle$ keys sets either the font style or the fraction style of $\langle\ldots\rangle$ ．The font styles \mathnormal／\symnormal and \mathrm／\symup are commonly used in literat－ ure．The fraction style can be either \frac，\dfrac，\tfrac，\sfrac ${ }^{\mathrm{R}}, \backslash \mathrm{slashfrac}{ }^{1}$ or any command with two mandatory arguments．
－The delims－$\langle\ldots$.$\rangle keys sets the delimiters used around the \langle\ldots$. ．．．．The Rule of Two applies here：＇Always two there are，no more，no less．A left and a right delimiter＇． The allowed delimiters are those that can be scaled with \left，\big etc．
－The scale－〈．．．〉 keys sets the size of the $\langle\ldots\rangle$＇．．s delimiters．The values big，Big， bigg，and Bigg are self－explanatory and internally a left and right version are used e．g．\bigl and \bigr．The value none inserts the delimiters（except periods） unscaled．While the value auto scales the delimiters automatically using \left } and $\backslash$ right．
－The sep $-\langle\ldots\rangle-\langle\ldots\rangle$ keys inserts their value between $\langle\ldots\rangle$ and $\langle\ldots$. ．．．．If the value is a comma－separated list of up to three numbers（e．g．$\{x, y, z\}$ ）it will be converted into the syntax \muskip $x$ mu plus y mu minus z mu and inserted．All other values are used as they were given．
－The switch $-\langle.$.$\rangle keys serves to change an argument＇s behaviour by swapping the$ effect of an optional character＇s presence．
－The sort－〈．．．〉 keys deals with the sorting algorithm behind the mixed order，where you can choose the sorting method that suits you best．
－The miscellaneous keys does not fit into any of the above categories and no longer have the prefix misc

Note．A value with superscripted $\mathrm{U}, \mathrm{P}$ and R refers to a unicode engine i．e． $\mathrm{LuaT}_{\mathrm{E}} \mathrm{X}$ and $\mathrm{X}_{-1} \mathrm{~T}_{\mathrm{E}} \mathrm{X}, \mathrm{pdf} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ and requires package，respectively．Additionally，some keys have two versions；with and without－／at the end．These keys are related to the slash argument． If switch－／＝false then the keys with and without－／are used when the slash argument is present and absent，respectively．Setting switch－／＝true then these keys are used in the opposite cases of the slash argument＇s presence．

## 3．2 Derivative options

The options in this subsection are available for derivatives defined by the package and you with the commands in section 4．1．

## Style

style－inf
Updated：v1．0

〈math－font－style〉〈infinitesimal〉
d
Sets the derivative＇s infinitesimal including font style．This change was necessary to allow multiple font styles，e．g．style－inf＝\mathbf $\{\backslash \operatorname{mathrm\{ d\} \} .~The~default~font~style~}$ is d．If an upright font is preferred then $\backslash$ mathrm $^{\mathrm{P}}$ and $\backslash$ symup $^{\mathrm{U}}$ could be used，or if an italic font then $\backslash$ mathnormal ${ }^{\mathrm{P}}$ and $\backslash$ symit $^{\mathrm{U}}$ ．
fraction〉 \frac
The derivative uses the fraction set by this key whenever switch－／＝false and the slash argument is absent．The key＇s default value is the usual fraction $\backslash f r a c$ ．
style－frac－／〈fraction〉 \slashfrac
The derivative uses the fraction set by this key whenever switch－／＝false and the slash argument is present．The key＇s default value is a text－styled fraction \slashfrac ${ }^{1}$ i．e． on the form $\partial^{2} f / \partial x \partial y$ ．
style－var
single，multiple
single
This option determines how the derivative treats its variables and some features．The variable argument is treated as a single variable when single is used．Moreover the mixed order is set equal to the first order given in order＝$\langle$ order $\rangle$ which by default is 1 ． The variable argument is treated as a comma separated list of variables with multiple similarly to a partial derivative．Moreover the mixed order is automatically calculated from the list of orders given in order＝$=\langle$ order $\rangle$ ．

## Scaling

scale－eval
auto，none，big，Big，bigg，Bigg
auto
This key sets the size of the delimiters used for the point of evaluation．This scaling is used whenever switch－／＝false and the slash argument is absent．The key＇s default value is set to scale the delimiters automatically．
scale－eval－／ auto，none，big，Big，bigg，Bigg
auto
This key sets the size of the delimiters used for the point of evaluation．This scaling is used whenever switch－／＝false and the slash argument is present．The key＇s default value is set to scale the delimiters automatically．

```
    scale-fun
auto，none，big，Big，bigg，Bigg
auto
```

This key sets the size of the delimiters used around the function．The scaling is used whenever fun＝true is used．The key＇s default value is set to scale the delimiters automatically．
scale－var auto，none，big，Big，bigg，Bigg auto
This key sets the size of the delimiters used around the variable．The scaling is used whenever var＝true is used．The key＇s default value is set to scale the delimiters automatically．
scale－frac auto，none，big，Big，bigg，Bigg auto
This key sets the size of the delimiters used for around the fraction．This scaling is used whenever switch－／＝false，the slash argument is absent and frac＝true is used． The key＇s default value is set to scale the delimiters automatically．

## scale－frac－／

auto，none，big，Big，bigg，Bigg
auto
This key sets the size of the delimiters used for around the fraction．This scaling is used whenever switch－／＝false，the slash argument is present and frac＝true is used． The key＇s default value is set to scale the delimiters automatically．

## Delimiters

delims－eval
$\langle$ left delimiter〉〈right delimiter〉
．\rvert
This key sets the left and right delimiters used to indicate the point of evaluation．These delimiters are inserted whenever switch－／＝false and the slash argument is absent．The key＇s default left and right delimiters are a left and a right parenthesis，respectively．
delims－eval－／

〈left delimiter〉〈right delimiter〉
．\rvert
This key sets the left and right delimiters used to indicate the point of evaluation．These delimiters are inserted whenever switch－／＝false and the slash argument is present． The key＇s default left and right delimiters are a left and a right parenthesis，respectively．
delims－fun
$\langle$ left delimiter〉$\langle$ right delimiter〉
（ ）
This key sets the left and right delimiters used around the function and these are inserted whenever fun＝true is used．The key＇s default left and right delimiters are a left and a right parenthesis，respectively．
This key sets the left and right delimiters used around the variable and these are inserted whenever var＝true is used．The key＇s default left and right delimiters are a left and a right parenthesis，respectively．
delims－frac＜left delimiter〉〈right delimiter〉
This key sets the left and right delimiters used around the fraction in the derivative e．g． $\left(\frac{\partial}{\partial x}\right) y$ ．These delimiters are inserted whenever switch－／＝false，the slash argument is absent and frac＝true is used．The key＇s default left and right delimiters are a left and a right parenthesis，respectively．
delims－frac－／〈left delimiter〉〈right delimiter〉
This key sets the left and right delimiters used around the fraction in the derivative e．g． $(\partial / \partial x) y$ ．These delimiters are inserted whenever switch－／＝false，the slash argument is present and frac＝true is used．The key＇s default left and right delimiters are a left and a right parenthesis，respectively．

## Math spacing

The options in this subsection inserts extra horizontal math space．The below equation illustrates where the space is inserted for each option

$$
\begin{array}{ccc}
\frac{\partial}{\partial x}\langle\text { frac-fun }\rangle & \frac{\partial\langle\text { inf-fun }\rangle}{\partial\langle\text { inf-var }\rangle x} & \frac{\partial^{2} f}{\partial x_{\langle\text {var-inf }\rangle} \partial y} \\
\frac{\partial^{\text {(inf-ord }\rangle} 2}{} \frac{x^{\text {(var-ord }\rangle} 2}{} & \frac{\partial^{3}\langle\text { ord-fun }\rangle}{\partial x^{2}\langle\text { ord-inf }\rangle} \partial y & \left(\frac{\partial f}{\partial x}\right)_{\langle\text {eval-sb }\rangle x_{1}}^{\langle\text {eval-sp }\rangle x_{2}}
\end{array}
$$

where it have been split into six to give a better overview．Here $\langle.$.$\rangle means the value$ given to the option sep－$\langle\ldots\rangle$ ．Some of the math spaces shown above are only used when style－var＝multiple．Additionally，when the option style－var＝single is used then the following math space is used in the denominator

$$
\frac{\partial(f, g)}{\partial(x\langle\mathrm{var}-\mathrm{var}\rangle y)}
$$

where the Jacobian have been used as an example．

Sets the math space that is inserted in the infinitesimal＇s power left to the mixed order in the numerator．It is only inserted when the mixed order is different from 1 ．The key＇s default value is 0 mu ．

This key sets the math space that is inserted between the infinitesimal and the function when the mixed order is equal to 1 ．The space is only inserted when a non－blank function is printed in the numerator．The key＇s default value is 0 mu ．

This key sets the math space that is inserted between the infinitesimal＇s order and the function when the mixed order is different from 1 ．The space is only inserted when a non－blank function is printed in the numerator．The key＇s default value is 0 mu ．
$\frac{\text { sep－frac－fun }}{\text { New：v1．0 }}$
$\langle$ cs－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
This key sets the math space that is inserted between the fractional part of the derivative and the function．The space is only inserted when a non－blank function is printed next to the derivative．The key＇s default value is 0 mu ．
sep－inf－var $\langle c s-n u m b e r\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\} \quad 0$
This key sets the math space that is inserted between the infinitesimal and the following variable．The space is only inserted when a non－blank variable is given．The key＇s default value is 0 mu ．
sep－var－ord 〈cs－number〉，\｛〈mspace $\rangle\}$ ，\｛〈delimiter $\rangle\}$
This key sets the math space that is inserted in a variable＇s power left to the order． The space is only inserted when the order is different from 1 ．The key＇s default value is 0 mu ．
sep－var－inf $\langle c s-n u m b e r\rangle,\{\langle m s p a c e\rangle\},\{\langle$ delimiter $\rangle\}$ \mathop $\} \backslash!$
They key sets the math space that is inserted between a variable and the following infinitesimal．The space is only inserted when the variable＇s order is equal to 1 ．It is only inserted when more than one non－blank variables are given．The key＇s default value is $\backslash$ mathop $\} \backslash!$ ．
sep－ord－inf $\langle$ cs－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\} \quad \backslash m a t h o p\{ \} \backslash!$
They key sets the math space that is inserted between a variable and the following infinitesimal．The space is only inserted when the variable＇s order is different from 1．It is only inserted when more than one non－blank variables are given．The key＇s default value is $\backslash$ mathop $\} \backslash!$ ．
sep－var－var
$\langle$ cs－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
New：v1．0 They key sets the math space that is inserted between two variables．The space is only inserted when the style－var＝single is used．and when more than one non－blank variables are given．The key＇s default value is a comma．
sep－eval－sb 〈cs－number〉，\｛〈mspace $\rangle$ ，\｛〈delimiter $\rangle\} 0$
This key sets the math space that is inserted in the evaluation subscript left to the point of evaluation．The space is only inserted when a non－blank subscript is given． The key＇s default value is 0 mu ．
sep－eval－sp 〈cs－number〉，\｛〈mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
This key sets the math space that is inserted in the evaluation superscript left to the point of evaluation．The space is only inserted when a non－blank superscript is given． The key＇s default value is 0 mu ．

## Switches

The effect of the star argument's presence can be switched with the value true. That is, the function is typeset next to the fraction when the star is absent and in the numerator when the star is present. As an example, compare below where the option is turned on (true) and off (false)

$$
\begin{aligned}
\backslash \mathrm{pdv}[\text { switch-*=false }]\{\mathrm{y}\}\{\mathrm{x}\} & \Longrightarrow \frac{\partial y}{\partial x} \\
\backslash \mathrm{pdv}[\text { switch-*=true }]\{\mathrm{y}\}\{\mathrm{x}\} & \Longrightarrow \frac{\partial}{\partial x} y
\end{aligned}
$$

respectively. The key's default value is false.
true, false
false
The effect of the slash argument's presence can be switched with the value true. That is, the derivative is typeset with the fraction set by style-frac-/ when the slash is absent and with the fraction set by style-frac when the slash is present. As an example, compare below where the option is turned on (true) and off (false)

$$
\begin{aligned}
\text { \pdv[switch-/=false] }\{\mathrm{y}\}\{\mathrm{x}\} & \Longrightarrow \frac{\partial y}{\partial x} \\
\backslash \operatorname{pdv}[\text { switch-/=true] }\{\mathrm{y}\}\{\mathrm{x}\} & \Longrightarrow \partial y / \partial x
\end{aligned}
$$

respectively. The key's default value is false.

## Sort

The keys given in this subsection will be briefly described here and a in-depth description will be given in section 5 .
sort-method
Updated: v1.0
abs, number, sign, symbol
sign, symbol, abs
This key sets the sorting method behind the mixed order using build-in algorithms. The symbolic terms in the mixed order are sorted by their sign, symbolic length, numerical value and absolute value by the sign, symbol, number and abs algorithms, respectively. The key takes its input as a comma-separated list of values, accepting up to three values e.g.

$$
\begin{aligned}
\backslash \mathrm{pdv}[\text { sort-method=sign, order=\{c+kn,-b+2a\}] }\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{c+k n+2 a-b} f}{\partial x^{c+k n} \partial y^{-b+2 a}} \\
\backslash \operatorname{pdv}[\text { sort-method=\{sign, symbol\}, order=\{c+kn,-b+2a\}]\{f\}\{x,y\}} & \Longrightarrow \frac{\partial^{k n+c+2 a-b} f}{\partial x^{c+k n} \partial y^{-b+2 a}} \\
\backslash \operatorname{pdv}[\text { sort-method=\{sign,symbol, abs\}, order}=\{c+\mathrm{kn},-\mathrm{b}+2 \mathrm{a}\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{k n+2 a+c-b} f}{\partial x^{c+k n} \partial y^{-b+2 a}}
\end{aligned}
$$

are all valid inputs. Note how the terms are ordered differently with different methods. This key is further described in section 5.1. The key's default value uses the three algorithms sign, symbol, abs.
auto, first, last, symbolic auto
This key determines where the numerical term ${ }^{2}$ is placed in the mixed order. The numerical term will always be placed as the first with first and as the last term with last in the mixed order. While auto will automatically determine where to place the numerical term depending on the sign of the first symbolic term. This is shown below

$$
\begin{array}{ll}
\backslash p d v[\text { sort-numerical=first, order }=\{\mathrm{n}, 2\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2+n} f}{\partial x^{n} \partial y^{2}} \\
\backslash \mathrm{pdv}[\text { sort-numerical=last, order }=\{-\mathrm{n}, 2\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{-n+2} f}{\partial x^{-n} \partial y^{2}}
\end{array}
$$

where the value auto would have placed the numerical term opposite in both equations. The value symbolic treats the numerical term as a symbolic term with symbolic length equal zero and is thus sorted alongside with all other terms

$$
\backslash \text { pdv [sort-numerical=symbolic, order=\{2+n,-a\}] }\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} \quad \Longrightarrow \frac{\partial^{n+2-a} f}{\partial x^{2+n} \partial y^{-a}}
$$

The key is further described in section 5.2, and its default value is auto.

The sorting algorithm abs sorts the terms by their absolute value in a descending manner. If the value true is used, then the terms will be sorted in an ascending manner instead. See section 5.3 for more information.

The sorting algorithm number sorts the terms by their numerical value in a descending manner. If the value true is used, then the terms will be sorted in an ascending manner instead. See section 5.3 for more information.

The sorting algorithm sign sorts the terms by their numerical sign where the positive terms are placed before the negative terms. The value true will reverse this ordering such that the negative terms are placed before the positive terms. See section 5.3 for more information.

The sorting algorithm symbol sorts the terms by their symbolic length in a descending manner. If the value true is used, then the terms will sorted in an ascending manner instead. See section 5.3 for more information.

[^1]
## Miscellaneous

New：v1．0
true，false
false
Adds or remove delimiters around the function．

$$
\begin{aligned}
\backslash \operatorname{pdv}[\text { fun=false }]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3} f}{\partial x \partial y \partial z} \\
\backslash \mathrm{pdv}[\text { fun=true }]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3}(f)}{\partial x \partial y \partial z} \\
\backslash \operatorname{pdv}[\mathrm{fun}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3}(f)}{\partial x \partial y \partial z}
\end{aligned}
$$

Without setting the option to a value is equivalent to setting it to true as seen above．
$\qquad$ true，false
false
$\overline{\text { New：v1．0 Adds or remove delimiters around the fractional part of the derivative．}}$

$$
\begin{aligned}
\backslash \mathrm{pdv}[\text { frac }=\mathrm{false}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow \frac{\partial^{3} f}{\partial x \partial y \partial z} \\
\backslash \mathrm{pdv}[\text { frac=true }]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow\left(\frac{\partial^{3} f}{\partial x \partial y \partial z}\right) \\
\backslash \mathrm{pdv} *[\mathrm{frac}=\operatorname{true}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow\left(\frac{\partial^{3}}{\partial x \partial y \partial z}\right) f \\
\backslash \mathrm{pdv}[\text { frac }]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}\} & \Longrightarrow\left(\frac{\partial^{3} f}{\partial x \partial y \partial z}\right)
\end{aligned}
$$

Without setting the option to a value is equivalent to setting it to true as seen above．

Adds or remove delimiters around the variable．The value all adds delimiters around all variables and none removed all delimiters．However，if only some variables needs delimiters then $\langle$ cs－numbers〉 can be used e．g．var $=\{1,3\}$ adds delimiters around the first and third variable

$$
\begin{aligned}
\backslash \mathrm{pdv}[\text { var=none }]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}\} & \Longrightarrow \frac{\partial^{4} f}{\partial x \partial y \partial z \partial t} \\
\backslash \mathrm{pdv}[\mathrm{var}=\{1,3\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}\} & \Longrightarrow \frac{\partial^{4} f}{\partial(x) \partial y \partial(z) \partial t} \\
\backslash \mathrm{pdv}[\mathrm{var}=\mathrm{all}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}\} & \Longrightarrow \frac{\partial^{4} f}{\partial(x) \partial(y) \partial(z) \partial(t)} \\
\backslash \operatorname{pdv}[\mathrm{var}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}\} & \Longrightarrow \frac{\partial^{4} f}{\partial(x) \partial(y) \partial(z) \partial(t)}
\end{aligned}
$$

Without setting the option to a value is equivalent to setting it to all as seen above．
order $\{\langle$ cs-orders $\rangle\}$
ord Sets the order of differentiation for each variable as a comma separated list of values.

The mixed order is automatically calculated from the orders of differentiation set by order $=\{\langle$ orders $\rangle\}$. In cases where it fails or another form is preferred, the calculated mixed order can be overwritten with this option.

### 3.3 Differential options

The options in this subsection are available for differentials defined by the package and you with the commands in section 4.2. All options in this section were introduced in v1. 0 .

## Style

style-inf
Updated: v1.0
style-notation
style-notation-*
single, multiple, mixed
single
Sets the differential's notation when the star argument is present (given switch-*=false). The key's default value is single.

## Scaling

auto, none, big, Big, bigg, Bigg
auto
Sets the size of the delimiters used around the variable when the star argument is absent (given switch-*=false). The scaling is used whenever var=true is used. The key's default value is set to scale the delimiters automatically.

Sets the size of the delimiters used around the variable when the star argument is present（given switch－＊＝false）．The scaling is used whenever var＝true is used．The key＇s default value is set to scale the delimiters automatically．

## Delimiters

delims－var
〈left delimiter〉〈right delimiter〉
Sets the left and right delimiters used around the variable when the star argument is absent（given switch－＊＝false）．The delimiters are inserted when var＝true is used． The key＇s default delimiters are a left and right parenthesis，respectively．
＜left delimiter〉〈right delimiter〉
Sets the left and right delimiters used around the variable when the star argument is present（given switch－＊＝false）．The delimiters are inserted when var＝true is used． The key＇s default delimiters are a left and right parenthesis，respectively．

## Math spacing

The options in this subsection inserts extra horizontal math space．Below，illustrates where the space is inserted for each option

$$
\begin{array}{cc}
\partial\langle\text { inf-var }\rangle x\langle\text { var-inf }\rangle & \langle y
\end{array} \quad\langle\text { begin }\rangle \partial x\langle\text { end }\rangle
$$

where it have been split into four to give a better overview．
sep－begin $\langle c s$－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\} \quad \backslash m a t h o p\{ \} \backslash!$
Sets the math space that is inserted to the left of the first differential．The key＇s default value is $\backslash$ mathop $\} \backslash!$ ．
sep－inf－ord $\langle$ cs－number $\rangle$ ，\｛〈mspace $\rangle\}$ ，\｛〈delimiter $\rangle\}$
This key sets the math space that is inserted in the infinitesimal＇s power left to the order．It is only inserted when the mixed order is different from 1．The key＇s default value is 0 mu ．
sep－inf－var
$\langle c s-n u m b e r\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
This key sets the math space that is inserted between the infinitesimal and the following variable．The space is only inserted when the order is equal to 1when a non－blank variable is given．The key＇s default value is 0 mu ．
sep－ord－var
$\langle c s$－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
This key sets the math space that is inserted between the infinitesimal＇s power and the following variable．The space is only inserted when the order is different from 1 and a non－blank variable is given．The key＇s default value is 0 mu ．

They key sets the math space that is inserted between a variable and the following infinitesimal．It is only inserted when more than one non－blank variables are given． The key＇s default value is $\backslash$ mathop $\} \backslash!$ ．
$\langle$ cs－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
Sets the math space that is inserted between two variables．The space is only inserted when style－var＝single and more than one non－blank variables are given．The key＇s default value is a comma．
sep－ord－ord $\langle$ cs－number $\rangle$ ，\｛〈mspace $\rangle\}$ ，\｛〈delimiter $\rangle\}$
Sets the math space that is inserted between two orders．The space is only inserted when style－var＝single and more than one non－blank orders are given．The key＇s default value is a comma．
sep－end $\langle c s$－number $\rangle,\{\langle$ mspace $\rangle\},\{\langle$ delimiter $\rangle\}$
Sets the math space that is inserted to the right of the last differential．The key＇s default value is 0 ．

## Switches

The effect of the star argument＇s presence can be switched with the value true．As an example，compare below where the option is turned on（true）and off（false），

```
\odif[switch-*=false]{x,y,z,t} }\Longrightarrow\textrm{d}x\textrm{d}y\textrm{d}z\textrm{d}
\odif[switch-*=true]{x,y,z,t} }\Longrightarrow\mp@subsup{\textrm{d}}{x,y,z,t}{
```

The key＇s default value is false．

## Miscellaneous

none，all，〈cs－numbers〉
Adds or remove delimiters around the variable．The value all adds delimiters around all variables and none removed all delimiters．However，if only some variables needs delimiters then $\langle$ cs－numbers $\rangle$ can be used e．g．var＝\｛1，3\} adds delimiters around the first and third variable

$$
\begin{aligned}
\text { \odif [var=none] }\{\mathrm{x}, \mathrm{y}, \mathbf{z}, \mathrm{t}\} & \Longrightarrow \mathrm{d} x \mathrm{~d} y \mathrm{~d} z \mathrm{~d} t \\
\text { \odif[var=\{1,3\}] }\{\mathrm{x}, \mathrm{y}, \mathbf{z}, \mathrm{t}\} & \Longrightarrow \mathrm{d}(x) \mathrm{d} y \mathrm{~d}(z) \mathrm{d} t \\
\text { \odif[var=all] }\{\mathrm{x}, \mathrm{y}, \mathbf{z}, \mathrm{t}\} & \Longrightarrow \mathrm{d}(x) \mathrm{d}(y) \mathrm{d}(z) \mathrm{d}(t) \\
\text { \odif[var] }\{\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}\} & \Longrightarrow \mathrm{d}(x) \mathrm{d}(y) \mathrm{d}(z) \mathrm{d}(t)
\end{aligned}
$$

Without setting the option to a value is equivalent to setting it to all as seen above．
order \｛〈cs－orders $\rangle\}$
ord Sets the differentiation order of each variable．

### 3.4 All derivatives and differentials

The options in this subsection are applied to all derivatives and differential because some options should be consisting regardless of the derivative and differential. The options are accessed using \derivset\{all\}[〈key=value〉]. mleftmright requires the mleftright package, which makes this package use $\backslash m l e f t$ and \mright instead.

## 4 Defining variants

This section goes into detail with how to define derivative and differential variants based on the package＇s internal commands，as mentioned earlier．The derivative package provides a $\operatorname{LAT}_{\mathrm{E}} \mathrm{X} 2_{\varepsilon}$ way of defining the derivatives．

## 4．1 Derivative variant

\NewDerivative
\RenewDerivative \ProvideDerivative \DeclareDerivative

〈control－sequence〉
\｛〈infinitesimal $\rangle\}$
［〈key＝value〉］
\NewDifferential
\RenewDifferential \ProvideDifferential \DeclareDifferential

〈control－sequence〉 $\{\langle$ infinitesimal $\rangle\}[\langle$ key $=$ value $\rangle]$
This family of commands are used to define a derivative variant with the macro name 〈control－sequence〉．Moreover，the new derivative will use \｛〈infinitesimal〉\} as its infinitesimal and inherit the package＇s default settings given in section 3．2，but they may be overwritten with $[\langle k e y=v a l u e\rangle]$ ．The difference between them is as follows：
－\NewDerivative is similar to \NewDocumentCommand of the xparse package and will issue an error if 〈control－sequence〉 has already been defined．
－\RenewDerivative is similar to \RenewDocumentCommand of the xparse package and will issue an error if＜control－sequence〉 has not previously been defined．
－\ProvideDerivative is similar to \ProvideDocumentCommand of the xparse package and will define 〈control－sequence〉 if it does not have an existing definition．It will not issue any errors．
－\DeclareDerivative is similar to \DeclareDocumentCommand of the xparse package and will always define the 〈control－sequence〉 with the new definition regardless of whether it already exists．

The first argument is the macro name of the derivative that is to be defined．
The second argument makes the derivative＜control－sequence〉 use \｛〈infinitesimal $\rangle\}$ as its infinitesimal．It is equivalent to setting style－inf $=\{\langle$ infinitesimal $\rangle\}$ ．
The optional argument accepts its input as a comma－separated list of key＝value pairs，which overrides the package＇s default options for the keys given．The derivative〈control－sequence〉 will use the package＇s default settings if the argument is left out．

## 4．2 Differential variant

〈control－sequence〉 $\{\langle$ infinitesimal $\rangle\}[\langle$ key $=$ value $\rangle]$
This family of commands are used to define a differential variant with the macro name 〈control－sequence〉．Moreover，the new derivative will use \｛〈infinitesimal〉\} as its infinitesimal and inherit the package＇s default options given in section 3．3，but they may be overwritten with $[\langle k e y=v a l u e\rangle]$ ．The difference between them is as follows：
－\NewDifferential is similar to \NewDocumentCommand of the xparse package and will issue an error if 〈control－sequence〉 has already been defined．
－$\backslash$ RenewDifferential is similar to \RenewDocumentCommand of the xparse package and will issue an error if 〈control－sequence〉 has not previously been defined．
－\ProvideDifferential is similar to \ProvideDocumentCommand of the xparse package and will define 〈control－sequence〉 if it does not have an existing definition．It will not issue any errors．
－\DeclareDifferential is similar to \DeclareDocumentCommand of the xparse package and will always define the＜control－sequence〉 with the new definition regardless of whether it already exists．

〈control－sequence〉 The first argument is the macro name of the differential that is to be defined．
\｛〈infinitesimal $\rangle\}$ While the second argument makes the differential $\langle$ control－sequence $\rangle$ use $\{\langle$ infinitesimal $\rangle\}$ as its infinitesimal．It is equivalent to setting style－inf＝\｛〈infinitesimal $\rangle\}$ ．
$[\langle k e y=v a l u e\rangle]$ The optional argument accepts its input as a comma－separated list of key＝value pairs，which overrides the package＇s default options for the keys given．The derivative〈control－sequence〉 will use the package＇s default settings if the argument is left out．

## 5 The mixed order

### 5.1 Sorting algorithms

A unique feature of this package is that the sorting method behind the mixed order may be changed using built-in algorithms and there are currently four available: abs, number, sign and symbol. The algorithms have been chosen such that it the terms in the mixed order may be arranged in many ways with as few algorithms as possible to suit your liking. A sorting method may consist of up to three algorithms which are applied in layers.

- The sorting algorithm sign separates the positive and negative terms, and puts the positive terms before the negative terms in the mixed order. The option sort-sign-reverse=true reverses ordering is reversed such that the negative terms appear before the positive terms.
- The sorting algorithm symbol separates the terms by their symbolic length, where the terms are sorted in a descending manner according to their length. The option sort-symbol-reverse=true sorts the terms in a ascending manner instead.
- The sorting by abs separates the terms by their absolute value, where the terms are ordered in a descending manner. The option sort-abs-reverse=true sorts the terms in an ascending manner instead.
- The sorting by number separates the terms by their numerical value, where the terms are ordered in a descending manner. The option sort-number-reverse=true sort the terms in an ascending manner instead.

When using the option sort-method=\{...\}, the number of algorithms determines the number of layers e.g. sort-method=\{sign, symbol\} is a sorting method with two layers, where the algorithms sign and symbol are applied in layer 1 and layer 2, respectively. E.i the sign algorithm splits the terms into two groups, one with positive terms and one with negative terms. Then the symbol algorithm will sorts the terms within each groups according to the terms symbolic length. The mixed order is then formed by combining these two groups.

### 5.1.1 Examples

The examples below are uses partial derivatives with order $=\{3 \mathrm{a}-3 \mathrm{hh}-2 \mathrm{~b}, 4 \mathrm{c}+4 \mathrm{gg}+2 \mathrm{ff}$, $-5 d-5 e e\}$ and a close up view of the mixed order. Square brackets are used to indicate grouping of terms and the text below a group refers to the algorithm applied. Here the words positive and negative, long and short, and big and low refers to the sign, symbol, and abs algorithms, respectively. A row of square brackets represents a layer.
The packages default sorting method is sort-method=\{sign,symbol,abs\} which is used below. The sign algorithm separate the positive and negative terms in the first layer. While in the second layer, the terms are separated by symbol length etc.

$$
\frac{\partial^{4 g g+2 f f+4 c+3 a-5 e e-3 h h-5 d-2 b} f}{\partial x^{3 a-3 h h-2 b} \partial y^{4 c+4 g g+2 f f} \partial z^{-5 d-5 e e}}
$$

as expected. Interchanging sign and symbol from the previous example i.e sortmethod=\{symbol, sign, abs\}, then the symbol and sign algorithms are now applied in the first and second layer, respectively. The result is shown below

$$
\begin{aligned}
& \frac{\partial^{4 g g+2 f f-5 e e-3 h h+4 c+3 a-5 d-2 b} f}{\partial x^{3 a-3 h h-2 b} \partial y^{4 c+4 g g+2 f f} \partial z^{-5 d-5 e e}}
\end{aligned}
$$

where a clear difference is seen between the above two examples.
The above two examples used 3-layer sorting methods but as mentioned earlier, the sorting method can also be constructed with one and two algorithms i.e. 1-layer and 2-layer sorting methods. A sorting method with two layers could be constructed as sort-method=\{sign,symbol\} and the terms are ordered by sign and then symbolic length. In this case, there is not a third layer

$$
\begin{gathered}
\frac{\partial^{4 g g+2 f f+3 a+4 c-3 h h-5 e e-2 b-5 d} f}{\partial x^{3 a-3 h h-2 b} \partial y^{4 c+4 g g+2 f f} \partial z^{-5 d-5 e e}} \\
\underbrace{4 g g+2 f f}_{\text {positive }}+\underbrace{3 a+4 c}_{\text {long }}-\underbrace{3 h h-5 e e-}_{\text {nert }}-\underbrace{2 b-5 d}_{\text {long }}
\end{gathered}
$$

The last example shows a 1-layer sorting method given as sort-method=symbol which gives the result

$$
\begin{gathered}
\frac{\partial^{-3 h h+4 g g+2 f f-5 e e+3 a-2 b+4 c-5 d} f}{\partial x^{3 a-3 h h-2 b} \partial y^{4 c+4 g g+2 f f} \partial z^{-5 d-5 e e}} \\
-3 h h+4 g g+2 f f-5 e e+\underbrace{3 a-2 b+4 c-5 d}_{\text {long }}
\end{gathered}
$$

as expected.

### 5.2 The numerical term

With the symbolic part of the mixed order treated, it is time to look at the numerical term ${ }^{2}$ which have a symbolic of zero. For this reason it is treated differently than the symbolic terms.

The numerical term can be placed either at the beginning or at the end of the mixed order with the values first and last, respectively. The package can also determine where to place the numerical term with the value auto. Compare below

$$
\text { sort-numerical=auto: } \quad \frac{\partial^{\beta+2} f}{\partial x^{\beta} \partial y^{2}} \quad \frac{\partial^{\beta-2} f}{\partial x^{\beta} \partial y^{-2}} \quad \frac{\partial^{2-\beta} f}{\partial x^{-\beta} \partial y^{2}} \quad \frac{\partial^{-2-\beta} f}{\partial x^{-\beta} \partial y^{-2}}
$$

$$
\begin{array}{rcccc}
\text { sort-numerical=first: } & \frac{\partial^{2+\beta} f}{\partial x^{\beta} \partial y^{2}} & \frac{\partial^{-2+\beta} f}{\partial x^{\beta} \partial y^{-2}} & \frac{\partial^{2-\beta} f}{\partial x^{-\beta} \partial y^{2}} & \frac{\partial^{-2-\beta} f}{\partial x^{-\beta} \partial y^{-2}} \\
\text { sort-numerical=last: } & \frac{\partial^{\beta+2} f}{\partial x^{\beta} \partial y^{2}} & \frac{\partial^{\beta-2} f}{\partial x^{\beta} \partial y^{-2}} & \frac{\partial^{-\beta+2} f}{\partial x^{-\beta} \partial y^{2}} & \frac{\partial^{-\beta-2} f}{\partial x^{-\beta} \partial y^{-2}} \\
\text { sort-numerical=symbolic: } & \frac{\partial^{\beta+2} f}{\partial x^{\beta} \partial y^{2}} & \frac{\partial^{\beta-2} f}{\partial x^{\beta} \partial y^{-2}} & \frac{\partial^{2-\beta} f}{\partial x^{-\beta} \partial y^{2}} & \frac{\partial^{-\beta-2} f}{\partial x^{-\beta} \partial y^{-2}}
\end{array}
$$

These three options should satisfy every needs.

### 5.3 Reversing the sort algorithm

The reverse keys serves to reverse the ordering of the terms by the sorting algorithms. This allows for even greater flexibility over the sorting method. So if the default ordering of an algorithm is not wished it may be reversed with the corresponding reverse key. For example, the sign algorithm places the positive terms before the negative terms, but is opposite with sort-sign-reverse=true. The reverse keys in action are shown below (sort-method= $\langle 1$ algorithm only $\rangle$ is also used to better show off the reverse functionality)

$$
\begin{array}{rcrl}
\text { sort-abs-reverse=false: } & \frac{\partial^{-3 b+2 a} f}{\partial x^{2 a} \partial y^{-3 b}} \quad \text { sort-abs-reverse=true : } & \frac{\partial^{2 a-3 b} f}{\partial x^{2 a} \partial y^{-3 b}} \\
\text { sort-number-reverse=false: } & \frac{\partial^{2 a-3 b} f}{\partial x^{2 a} \partial y^{-3 b}} \quad \text { sort-number-reverse=true : } & \frac{\partial^{-3 b+2 a} f}{\partial x^{2 a} \partial y^{-3 b}} \\
\text { sort-sign-reverse=false: } & \frac{\partial^{a-b} f}{\partial x^{a} \partial y^{-b}} & \text { sort-sign-reverse=true : } & \frac{\partial^{-b+a} f}{\partial x^{a} \partial y^{-b}} \\
\text { sort-symbol-reverse=false: } & \frac{\partial^{a b+c} f}{\partial x^{a b} \partial y^{c}} & \text { sort-symbol-reverse=true: } & \frac{\partial^{c+a b} f}{\partial x^{a b} \partial y^{c}}
\end{array}
$$

### 5.4 Mixed order override

In cases where the mixed order fails to be calculated or another form is preferred, then the mixed order override can be used

$$
\begin{aligned}
\backslash \mathrm{pdv}[\text { order }=\{\mathrm{n}+3 \mathrm{k}, \mathrm{n}-\mathrm{k}\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2 n+2 k} f}{\partial x^{n+3 k} \partial y^{n-k}} \\
\backslash \operatorname{pdv}[\text { order }=\{\mathrm{n}+3 \mathrm{k}, \mathrm{n}-\mathrm{k}\}, \operatorname{mixed}-\text { order }=\{2(\mathrm{n}+\mathrm{k})\}]\{\mathrm{f}\}\{\mathrm{x}, \mathrm{y}\} & \Longrightarrow \frac{\partial^{2(n+k)} f}{\partial x^{n+3 k} \partial y^{n-k}}
\end{aligned}
$$

## 6 Miscellaneous

## 6．1 Slashfrac

\slashfrac［〈scale $]$ \｛ $\langle$ numerator $\rangle\}\{\langle$ denominator $\rangle\}$
A text－styled fraction i．e．$a / b$ ，is commonly used in text－mode．While \slashfrac\｛a\}\{b\} is certainly longer to write than $a / b$ ，which only requires three keystrokes，but for the implementation of text－styled derivatives a macro for it is needed．
［〈scale〉］The optional argument is the scaling parameter for the slash and takes the inputs as shown below．Leaving out［〈scale $\rangle$ ］sets the scaling parameter to auto

$$
\begin{array}{rll}
\text { \slashfrac[auto] \{y_f\}\{x\} } & \Longrightarrow & y_{f} / x \\
\text { \slashfrac[none] \{y_f\}\{x\} } & \Longrightarrow & y_{f} / x \\
\text { \slashfrac[big] \{y_f\}\{x\} } & \Longrightarrow & y_{f} / x \\
\text { \slashfrac[Big] \{y_f\}\{x\} } & \Longrightarrow & y_{f} / x \\
& & y_{f} / x \\
\text { \slashfrac[bigg]\{y_f\}\{x\} } & \Longrightarrow & y_{f} / x \\
& &
\end{array}
$$

This argument is subject to change，see consideration 7．2（ii）for more information．
\｛〈numerator $\rangle\}$ Typesets the fraction＇s numerator．
\｛〈denominator $\rangle\}$ Typesets the fraction＇s denominator．

## 7 To do

Entries marked with $\checkmark$ will be implemented in a future release specified in the entry. Entries marked with $\times$ will not be implemented.

### 7.1 Future implementation

The list describes what will be added to the package in a later release.
(i) Implement the option to turn off the sorting of the terms in the mixed order. This could be made as a draft / final option.
$\checkmark \times$ Conclusion: There could be an draft/final option for the package. But what is should turn off/on is harder to say.

### 7.2 Future considerations

The list describes what might be changed or added to the package in a later release.
(i) It can become rather cumbersome to read a derivative with a very long function. To ease this up, I am considering to add a switch that exchange the variable and the function arguments. But this might be against the $\mathrm{LAT}_{\mathrm{E}} \mathrm{X}$ way of using arguments, which is the reason it have not been done and I would like feedback on it.
(ii) I am considering making the optional argument of \slashfrac into a $[\langle k e y=v a l u e\rangle]$ argument with something like scale=\{〈scaling $\rangle$.
$\checkmark$ Conclusion: I want an key-value implementation like this in the future, but it will not be added in the next release.

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## Change history

 -07-21 Beta| v0.95b |
| ---: |
| $2019-09-21$ <br> Beta |
| v0.96 |
| 2019-12-22 |
| Beta |

- First release of the package. The package is currently in a beta version.
- Please ignore this version, since it contained the wrong .sty and .pdf files : (.
- Removed the single token restriction of the infinitesimal since it made no sense.
- Fixed the documentation errors and typos.
- Minor fixes to the code.
- Contains the correct .sty and .pdf files :).
- One minor code fix
- Fixed the double superscript issue for higher order derivative when the variable contained a superscript.
- Fixed the argument specifier of \__deriv_scale_big:nnnn when it was used (it was used with :nnnm).
- Fixed a bug concerning the subscript argument due to recent changes to the xparse package dated 2020-05-14 (the fix works with earlier versions of xparse as well).
- Added new options for derivatives
- Added new values for existing options
- Added new commands to write differentials
- Changed usage of style-inf
- Changed the order argument to an option argument
- Changed default values for some options
- Changed math space keys to accept more general inputs
- Changed \derivset to define default options
- Merged the codes for ordinary and partial derivatives
- Removed the mixed order argument
- Removed the options 'misc-add-delims' and 'misc-remove-delims'
- Replaced the commands in section 5 with new ones. Old ones no longer works.
- Code clean-up and optimization
- Fixed code errors
- Fixed Documentation errors
- Enhanced support for preventing options effecting nested derivatives/differentials
- Changed the option sep-end default value because it caused issues
- Fixed code errors due to changes introduced in version 1.0 to the option style-inf
- Fixed documentation errors


[^0]:    ${ }^{1}$ which is a macro defined by the package, see section 6.1 for more information.

[^1]:    ${ }^{2}$ The numerical term is the sum of all the orders that does not contain any symbols but solely consist of numbers.

