# SPECTRALSEQUENCES

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The SPECTRALSEQUENCES package is a specialized tool built on top of PGF/TikZ for drawing spectral sequence charts. It provides a powerful, concise syntax for specifying the data of a spectral sequence, and then allows the user to print various pages of a spectral sequence, automatically choosing which subset of the classes, differentials, structure lines, and extensions to display on each page. It also handles most of the details of the layout. At the same time, SPECTRALSE-QUENCES is extremely flexible. It is closely integrated with TikZ to ensure that users can take advantage of as much as possible of its expressive power. It is possible to turn off most of the automated layout features and draw replacements using TikZ commands. SPECTRALSEQUENCES also has a carefully designed error reporting system intended to ensure that it is as clear as possible what is going wrong.

Many thanks to the authors of TikZ for producing such a wonderful package with such thorough documentation. I would have needed to spend a lot more time reading the TikZ code if the documentation weren't so excellent. I took ideas or code or both from tikzcd (part of the code for turning quotes into class or edge labels), PGFPLOTS (axes labels), and sseq (the grid types, the stack). I lifted a fair amount of code from TEXstack exchange. Thanks to Eva Belmont for tons of helpful suggestions, bug reports, and productive conversations. Talking to her has helped to clarify many design concepts for the package. Thanks to Eric Peterson for being a very early adopter and reporting many bugs. Also thanks to all my friends, family, and acquaintances listened to me talk about LATEX programming even though they probably found it dreadfully boring.

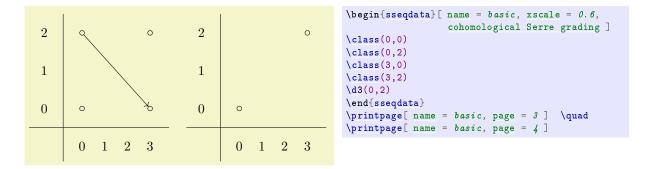
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# 1 Introduction

The SPECTRALSEQUENCES package consists of two main environments – the {sseqdata} environment, which specifies the data for a named spectral sequence, and the {sseqpage} environment, which prints a single page of a spectral sequence. The \printpage command is also available as a synonym for a {sseqpage} environment with an empty body.

Here is a basic example:



 $\begin{sseqdata}[name = basic, cohomological Serre grading] starts the declaration of the data of$ a spectral sequence named basic with cohomological Serre grading - that is, the page r differentials gor to the right and down <math>r - 1. Then we specify four classes and one page 3 differential, and we ask SPECTRALSEQUENCES to print the third and fourth pages of the spectral sequence. Note that on the fourth page, the source and target of the differential have disappeared.

# 1.1 Installation

In both MiKT<sub>E</sub>X and T<sub>E</sub>X Live installation should be automatic – your T<sub>E</sub>X distribution should automatically install the package the first time you include \usepackage{spectralsequences} in a document and compile it. However, in 2016, T<sub>E</sub>X Live made an incompatible change to their database, so no new packages will run on versions of T<sub>E</sub>X Live from before 2016. This includes SPECTRALSEQUENCES. If you have an old version of T<sub>E</sub>X Live, you can either perform a manual install, or, better, you should install an up to date version of T<sub>E</sub>X Live. If you want to do a manual install, see this T<sub>E</sub>X stack exchange post for instructions.

# 1.2 Memory Constraints

In a default  $T_EX$  install, PDFIAT<sub>E</sub>X has small static memory caps that prevent it from using more than about 60 megabytes of total ram. However, SPECTRALSEQUENCES and PGF/TikZ use a large amount of memory. For this reason, using PDFIAT<sub>E</sub>X with a default install, you cannot draw more than about 2500 classes across all of your diagrams (fewer if you include differentials, structure lines, and other features). There are a few solutions to this.

The easiest solution is to run LualATEX. LualATEX dynamically allocates memory and so is unlikely to run out of it. Using LualATEX on my computer, I can compile a document that draws two copies of a diagram with 20,000 classes in it (so a total of 40,000 classes). This takes about 50 seconds and 250 megabytes of ram. I expect any real-world use case will compile fine on a modern computer using LualATEX. This option has the advantage that any modern TEX install comes with a copy of LualATEX, and that LualATEX is the designated successor to PDFIATEX. It has the disadvantage that there are some incompatibilities between LualATEX and PDFIATEX so if your document depends on PDFIATEX-specific features, it might be a pain to switch to LualATEX.

Another option is to increase the static memory caps for  $PDFIAT_EX$ . See this  $T_EX$  stack exchange post for instructions on how to do this.

# 1.3 A warning about fragile macros

All the data in a SPECTRALSEQUENCES environment is stored and used later. As a result, most of the SPEC-TRALSEQUENCES commands currently cannot tolerate fragile macros. Unfortunately, it is impossible for SPEC-TRALSEQUENCES to warn you about this situation – if you use a fragile command in a place that it doesn't belong, the result will be an incomprehensible error message. If you are getting nonsense error messages, this might be why. The solution is to convert fragile macros into robust ones. Common examples of fragile macros include \widehat and \underline. My suggested solution to this is to add the following code to your preamble for each fragile macro (example given for \mathbb):

\let\oldwidehat\widehat
\protected\def\widehat{\oldwidehat}

# 2 Package Options and Environments

# Draft Mode

The drawings that SPECTRALSEQUENCES produces can be quite slow, especially if they are large. Draft mode skips drawing the content of the spectral sequence, but still takes up exactly the same amount of space in the document, so that you can deal with formatting issues. To active draft mode, load the package by saying \usepackage[draft]{spectralsequences}.

# $\begin{seqdata}[\langle options \rangle]$

```
\langle environment \ contents \rangle
```

#### \end{sseqdata}

The {sseqdata} environment is for storing a spectral sequence to be printed later. This environment is intended for circumstances where you want to print multiple pages of the same spectral sequence. When using the {sseqdata} environment, you must use the name option to tell SPECTRALSEQUENCES where to store the spectral sequence so that you can access it later.

 $\begin{sseqpage}[(options)]$ 

# $\langle environment \ contents \rangle$

\end{sseqpage}

This environment is used for printing a page of existing spectral sequence that was already specified using the  $\{sseqdata\}$  environment. The body of the environment adds local changes – classes, differentials, structure lines, extensions, and arbitrary TikZ options that are by default only printed on this particular page. The  $\{sseqpage\}$  environment can also be used to print a stand-alone page of a spectral sequence – that is, if you only want to print a single page of the spectral sequence, you can skip using the  $\{sseqdata\}$  environment.

# $\printpage[(options)]$

This command prints a single page of an existing spectral sequence as-is. This is equivalent to a {sseqpage} environment with an empty body.

# 3 The Main Commands

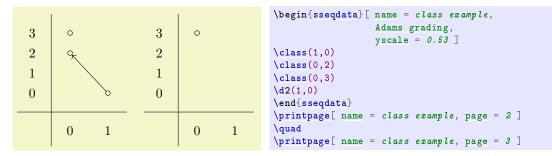
# $\class[\langle options \rangle](\langle x \rangle, \langle y \rangle)$

This places a class at (x,y) where x and y are integers. If multiple classes occur at the same position, SPECTRALSEQUENCES will automatically arrange them in a pre-specified pattern. This pattern may be altered using theclass pattern option.

		\begin{sseqpage}[ no axes, ymirror, yscale = 0.8 ]
0	00	class(0,0)
0		$class(1,0) \ class(1,0)$
	~ ~	$class(0,1) \ class(0,1) \ class(0,1)$
000	000	$class(1,1) \ class(1,1) \ class(1,1) \ class(1,1)$
		class(0,2) $class(0,2)$ $class(0,2)$ $class(0,2)$
000	88	$class(1,2) \ class(1,2) \ cla$
0 0	00	\end{sseqpage}

The effect of the  $\class$  command is to print a TikZ node on a range of pages. Any option that would work for a TikZ  $\class$ ,  $\class$ , and  $\class$ , and  $\class$ ,  $\class$ ,

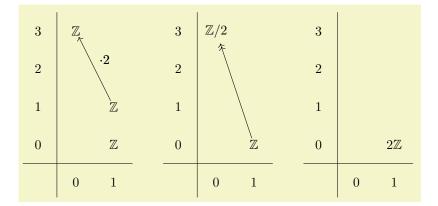
If a class is the source or the target of a differential on a certain page, then the page of the class is set to that page, and the class is only rendered on pages up to that number:



See the <u>class options</u> section for a list of the sort of options available for classes.

```
\label{eq:lass_control} $$ \operatorname{control} (\langle x \rangle, \langle y \rangle, \langle n \rangle) \\ \operatorname{control} (\langle classname \rangle) \\ \operatorname{control} (\langle classname \rangle) \\ \operatorname{control} (\langle classname \rangle) \\ \operatorname{control} (\langle chassname \rangle) \\ \operatorname{control}
```

After a class is the source or target of a differential, it disappears on the next page. However, some differentials are not injective or not surjective. Using the command  $\replaceclass$  causes a new symbol to appear on the page after a class supported or accepted a differential (or both). If there are multiple classes at the coordinate (x,y) you may specify which using an integer or a tag n. By default, this command will affect the first class placed in that position. You can also provide the class:name of a class. The variants  $\replacesource$  and  $\replacetarget$  replace the source and target respectively of the most recent differential.



```
\begin{sseqdata}[name = replace class example, Adams grading, classes = {draw = none } ]
\class["\mathbb{Z}"](0,3)
\class["\mathbb{Z}"](1,1)
\class["\mathbb{Z}"](1,0)
\d["\cdot 2"]2(1,1)
\replacetarget["\mathbb{Z}/2"] %\replaceclass["\mathbb{Z}/2"](0,3)
\d[-*]3(1,0)
\replacesource["2\mathbb{Z}"] %\replaceclass["2\mathbb{Z}"](1,0)
\end{sseqdata}
\printpage[ name = replace class example, page = 2 ] \qquad
\printpage[ name = replace class example, page = 3 ] \qquad
\printpage[ name = replace class example, page = 4 ]
```

Note that this will not restore any structure lines coming into or off of the class. If you want to restore all structlines on the class use **\replacestructlines**. If you want to selectively replace some of the structure lines, you must use **\structline** again (or use the structline:page option).

# \replacestructlines((source coordinate))

This command replaces all structlines touching a class that has been replaced using \replaceclass, \replacesource, or \replacetarget.



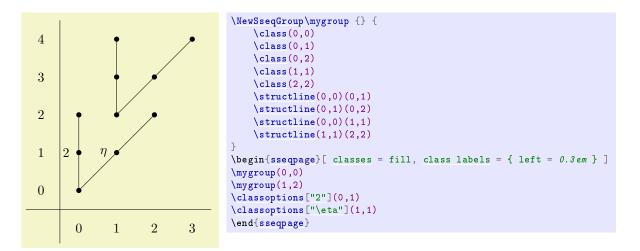
 $\classoptions[\langle options \rangle](\langle x \rangle, \langle y \rangle, \langle n \rangle) \\ \classoptions[\langle options \rangle](\langle classname \rangle) \\ \classoptions[\langle options \rangle] \class$ 

This adds options to an existing class. This can be used in a {sseqpage} environment to modify the appearance of a class for just one drawing of the spectral sequence, for instance to highlight it for discussion purposes.

If there are multiple classes at the coordinate (x,y) you may specify which using an integer or a tag n. By default, this command will affect the first class placed in that position. You can also provide the class:name of a class. If no coordinate is indicated at all, then \lastclass is used.

		I			\begin{sseqdata}[ name = class options example,
	1	•	•	••	classes = fill ]
	Т	•	•	••	class(2,1)
					$foreach x in {0,,2} foreach y in {0,1} {$
	0	•	•	•	$\class(x,y)$
	0		•	•	}
					\end{sseqdata}
		0	1	2	\begin{sseqpage}[ name = class options example,
			T	2	right clip padding = 0.6cm ]
					<pre>\classoptions[red](2,1,2) % Only is red on this page!</pre>
The red class is the problem					<pre>\node[ background ] at (0.3,-2.2)</pre>
					{\textup{The red class is the problem}};
					\end{sseqpage}

Another reason to use this is to give a label to one instance of a class that shows up in a loop or a command defined using \NewSseqGroup:



See the class options section for a list of the sort of options available for classes.

 $d[\langle options \rangle] \langle page \rangle$ 

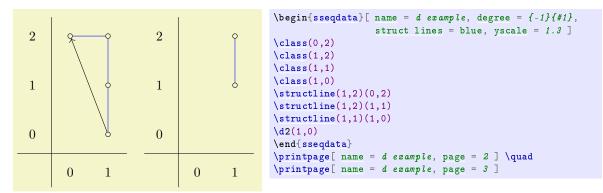
```
d[\langle options \rangle] \langle page \rangle (\langle x \rangle, \langle y \rangle, \langle source \ n \rangle, \langle target \ n \rangle)
```

```
d[\langle options \rangle] \langle page \rangle (\langle source name \rangle, \langle target n \rangle)
```

 $d[\langle options \rangle] \langle page \rangle (\langle source \ coordinate \rangle) (\langle target \ coordinate \rangle)$ 

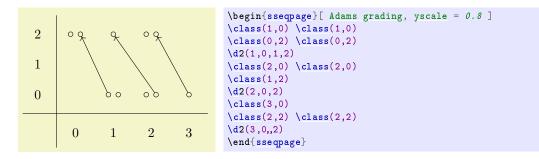
Calling  $d = \{age\}(\langle x \rangle, \langle y \rangle)$  creates a differential starting at  $(\langle x \rangle, \langle y \rangle)$  of length determined by the specified page. In order to use the d command like this, you must first specify the degree of the differentials as an option to the {sseqdata} or {sseqpage} environment. The degree indicates how far to the right and how far up a page r differential will go as a function of r. If there is a page r differential, on page r + 1, the source, target, and any structure lines connected to the source and target of the differential disappear. If no class is specified, the default is to use lastclass.

If there are multiple nodes in the source or target, you may specify which one the differential should go to using an index or tag for  $\langle source n \rangle$  or  $\langle target n \rangle$ . It is also possible to provide the name of the source coordinate and an optional target, or to separately provide the source and target coordinate, either as names or as  $(\langle x \rangle, \langle y \rangle, \langle n \rangle)$ . Using \d with explicit source and target coordinates works even if you did not provide a degree to the spectral sequence. If you did provide a degree, then SPECTRALSEQUENCES will check whether the difference between the source and target is appropriate for a differential of a given page, and if not it will throw an error. If this is undesirable, you can use the lax degree option.



If there are multiple nodes in the source or target coordinate, then there is a funny syntax for indicating which one should be the source and target:

\d\meta{page}\pars{\meta{x}, \meta{y}\opt{, \sourcen, \targetn}}



Negative indices will count from the most recent class in the coordinate (so the most recent is -1, the second most recent is -2, etc). You can also use a tag, which works better if the situation is complicated.



This command adds options to an existing differential, just like \classoptions except for differentials. Its syntax is identical to that of \d.

# $\[\langle coord \rangle ]$

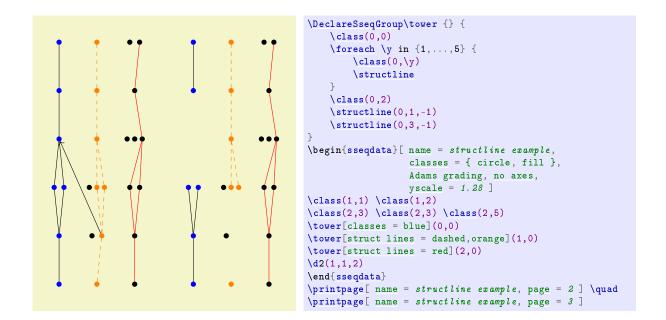
This command sets the indicated coordinate to die on the indicated page, but does not establish a target for the differential. This is useful if you want to draw your own differential using tikz (see \getdtarget) or if you are not drawing the class on the other side of the differential for clutter reasons. As usual, if no coordinate is provided, the default argument is \lastclass.

# $\timestyle (options)] ((source coordinate)) ((target coordinate))$

The \structline command creates a structure line from  $\langle source \ coordinate \rangle$  to  $\langle target \ coordinate \rangle$ . The source and target coordinates are either of the form  $(\langle x \rangle, \langle y \rangle, \langle n \rangle)$  or  $(\langle class \ name \rangle)$ . If there are multiple classes at (x, y), then  $\langle n \rangle$  specifies which of the classes at (x, y) the structure line starts and ends at - if n is positive, then it counts from the first class in that position, if n is negative, it counts backwards from the most recent. You can also use a tag for n. If the  $\langle target \ coordinate \rangle$  is omitted, then \lastclass is used, so that \structline(\sourcecoord) connects the most recent class to the specified coordinate. If both coordinates are omitted, then \lastclass and \lastclass1 are used, and so \structline with no arguments at all will connect the two most recent classes.

If the source or target of a structure line is hit by a differential, then on subsequent pages, the structure line disappears.

If the source or target has had multiple generations (i.e., they got hit and you used \replaceclass), then the \structline will only appear starting on the first page where the current generation of both the source and target are present. If this is undesirable, you can use the structline:page option or the to change it. Also, the structline will disppear the first time after this the source or target has a differential, but this can be changed with the \replacestructlines command.

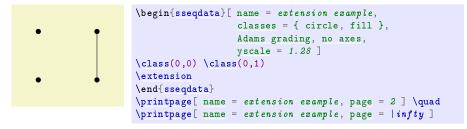


# 

This command adds options to an existing structure line, just like \classoptions except for structure lines. Its syntax is identical to \structline.

# 

The **\extension** command has an identical syntax to the **\structline** command and most of the same options. Instead of adding a structline, it adds an extension. The extensions are only shown on page  $\infty$  or page ranges ending at  $\infty$ .



# $\operatorname{conditions}[\langle options \rangle](\langle source \ coordinate \rangle)(\langle target \ coordinate \rangle)$

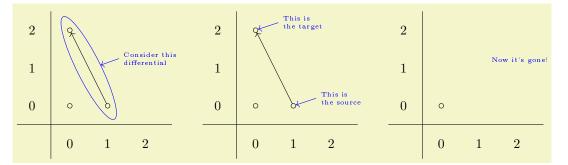
This command adds options to an existing extension. Its syntax is identical to \extension.

# $\circleclasses[\langle options \rangle](\langle source \ coordinate \rangle)(\langle target \ coordinate \rangle)$

This command is a lot like \structline except that it puts a circle around the classes instead of connecting them with a line. It might take a certain amount of fiddling with options to get \circleclasses to produce good results. There is no \circleclassesoptions command because it doesn't seem necessary.

\draw \path \node \clip

Any code that would work in a {tikzpicture} environment will also work unchanged in a {sseqdata} or {sseqpage} environment, with a few minor differences. This is a very flexible way to add arbitrary background or foreground features to the spectral sequence:



```
\begin{sseqdata}[ name = tikz example, Adams grading, math nodes = false,
                  tikz primitives = { blue, font = \tiny, <- }, circle classes = tikz primitive style,
                  x range = \{0\}\{2\}, x axis extend end = 2em ]
\class(0,0)
\class(1,0)
\class(0.2)
d2(1,0)
\end{sseqdata}
\begin{sseqpage}[ name = tikz example ]
\circleclasses[ name path = myellipse, inner sep = 3pt, ellipse ratio = 1.6 ] (1,0) (0,2)
\path[ name path = myline ] (1.3,1.25) -- (0.6,1);
\draw[ name intersections = { of = myellipse and myline } ]
      (intersection-1) to (1.3,1.25) node[ right, text width = 1.6cm ] {Consider this differential};
\end{sseqpage} \qquad
\begin{sseqpage}[ name = tikz example ]
\det x = 1 ] (0,0)  to (0.6,0.2)  node [ right, text width = 1.1 cm ] {This is the source};
\draw[ yshift = 2 ] (0,0) to (0.6,0.2) node[ right, text width = 1.1cm ] {This is the target};
\end{sseqpage} \qquad
\begin{sseqpage}[ page = 3, name = tikz example ]
circleclasses[ inner sep = 3pt, ellipse ratio = 1.6 ] (1,0)(0,2)
\node[ right, font = \tiny ] at (1.2,1.2) {Now it's gone!};
\end{sseqpage}
```

# 4 Options for the main commands

# 4.1 Universal options

The following options work with all of the drawing commands in this package, including  $\lass, \d$ , and  $\structline$ , their friends  $\replaceclass, \classoptions, \doptions, and \replacestructlines, as well as with TikZ primitives.$ 

```
 \begin{array}{l} \textbf{xshift} = \langle integer \rangle \\ \textbf{yshift} = \langle integer \rangle \\ \end{array}
```

Shifts by integer values are the only coordinate changes that are allowed to be applied to \class, \d, \structline, their relatives, or to a {scope} environment that contains any of these commands. These shift commands help with reusing code. For instance:



This code segment is very useful so SPECTRALSEQUENCES has the command \NewSseqGroup which to make code like this more convenient. The following code produces the same output as above:

```
\NewSseqGroup\examplegroup {} {
    \class(2,0)
    \class(0,1)
    \d2(0,1)
}
\begin{sseqpage}
\examplegroup(0,0)
\examplegroup(0,1)
\examplegroup(1,0)
\examplegroup(1,1)
\end{sseqpage}
```

A word of warning: the behavior of xshift in SPECTRALSEQUENCES is incompatible with the normal behavior of xshift in TikZ. For some reason, sayingxshift = 1 in TikZ does not shift the coordinate (0,0) to the coordinate (1,0) – instead it shifts by 1pt. In SPECTRALSEQUENCES, sayingxshift = 1 moves the coordinate (0,0) to the coordinate (1,0). This includes TikZ primitives: saying\draw[xshift = 1] (0,0) -- (1,0); inside a {sseqdata} or {sseqpage} environment is the same as saying \draw(1,0) -- (2,0); despite the fact that this is not the case in the {tikzpicture} environment.

#### Colors

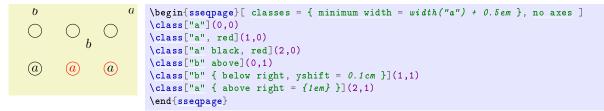
These come from the  $\mathbb{P}T_{E}X$  color package via  $\mathrm{Ti}kZ$ , so see the color package documentation for more information.

	\begin{sseqpage}[ classes = {fill, inner sep = 0.4em},
	no axes, scale = 1.3 ]
	class[red](0,0)
	\class[blue](1,0)
	\class[green](2,0)
	\class[cyan](0,1)
	\class[magenta](1,1)
	\class[yellow](2,1)
	\class[blue!50!red](0,2) % a 50-50 blend of blue and red
	\class[green!30!yellow](1,2) % 30% green, 70% yellow
<b>— — —</b>	<pre>\class[blue!50!black](2,2)</pre>
	\end{sseqpage}
	. цог

 $\langle text \rangle \langle options \rangle$ 

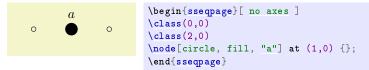
Specify a label for a class, a differential, or a structure line. This uses the TikZ quotes syntax. If the label text includes an equal sign or comma, you need to enclose the entire label in braces, e.g.,  $class["{x =y}"](0,0)$ . The options include anything you might pass as an option to a TikZ node, including arbitrary coordinate transforms, colors, opacity options, shapes, fill, draw, etc. The behavior is a little different depending on whether you use it on a class or on a differential or structure line.

For a class, the  $\langle text \rangle$  is placed in the position inside the node by default – in effect, the  $\langle text \rangle$  becomes the label text of the node (so saying \class["label text"](0,0) causes a similar effect to saying\node at (0,0) {label text};). There are other position options such asleft, above left, etc which cause the label text to be placed in a separate node positioned appropriately. If the placement is above, left, etc, then any option that you may pass to a TikZ node will also work for the label, including general coordinate transformations. If the placement is "inside", then the only relevant  $\langle options \rangle$  are those that alter the appearance of text, such as opacity and color.



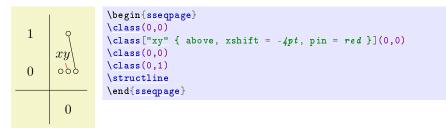
You can adjust the default behavior of class labels using the labels style option or its relatives class labels, inner class labels orouter class labels. Note that it is also possible to give a label to a \node this way, although the behavior is slightly different. In particular, the label defaults

to the **above** position instead of going in the **\node** text by default. Also, this won't respect the various label style options like **labels**, etc.

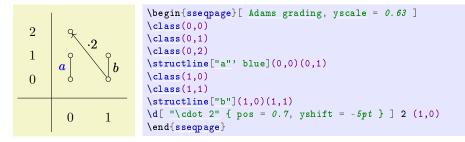


**pin** =  $\langle style \rangle$ 

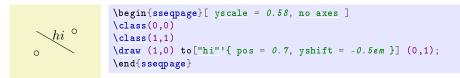
The pin key makes SPECTRALSEQUENCES draw a line connecting the label to the relevant class, which can provide necessary clarification in dense diagrams. The pin key itself can take options which adjust the way that the line is drawn:



For either a \structline or a \class the label normally goes on the right side of the edge. The special option ' makes it go in the opposite position from the default. I imitated the label handling in the tikzcd package, so if you use tikzcd, this should be familiar.



You can use the style options labels, edge labels, differential labels, and struct line labels to adjust the styling of edge labels. For instance, if you would prefer for the labels to default to the left hand side of the edge rather than the right hand side, you could say edge labels = {auto = left}. You can also use quotes to label edges drawn with TikZ primitives:



# description

The description key, stolen from tikzcd, places the label on top of the edge. In order to make this option work correctly, if the background coolor is not the default white, you must inform SPECTRALSEQUENCES about this using the key background color =  $\langle color \rangle$ . In this document, the background color is called *graphicbackground*.

$\begin{bmatrix} \mathbf{a} & \mathbf{a'} \end{bmatrix} \begin{bmatrix} \mathbf{b} & \mathbf{c} \\ & \mathbf{c} \\ & \mathbf{b} \end{bmatrix}$	<pre>\begin{sseqpage}[ no axes, background color = graphicbackground ] \foreach \x in {0,1,2} \foreach \y in {0,1} {     \class(\x,\y) } \structline["a" red](0,0)(0,1) \structline["a"";blue,"b"{yshift = 1em}](1,0)(1,1) \structline["c" description](2,0)(2,1)</pre>
	\end{sseqpage}

# 4.2 Options for $\class$

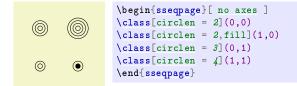
Because the main job of the  $\class$  command is to print a TikZ  $\node$  on the appropriate pages of the spectral sequence, most options that would work for a TikZ node also work for the commands  $\class$ ,  $\replaceclass$ , and  $\classoptions$ . Here are a few that you might care about:

# A $\operatorname{Ti} k \mathbb{Z}$ shape

If you give the name of a TikZ shape, the class node will be of that shape. The standard TikZ shapes are circle and rectangle. SPECTRALSEQUENCES defines two new shapes:

## circlen = $\langle n \rangle$

This draws *n* concentric circles. It's intended for indicating a  $\mathbb{Z}/p^n$  summand. For large values of *n* the result isn't all that appealing.

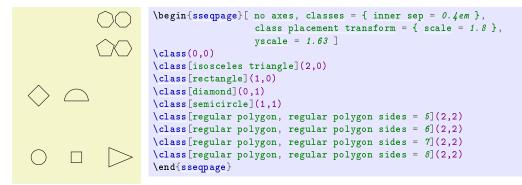


# newellipse

```
ellipse ratio = \langle ratio \rangle
```

This shape is used for \circleclasses. It's a variant on the ellipse shape that gives more control over the ellipse's aspect ratio.

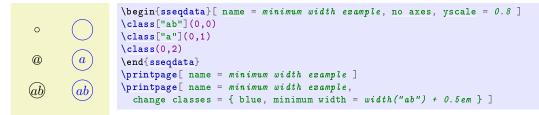
There are many more TikZ shapes in the shapes library, which you can load using the command  $\star{shapes}$ . The following are some examples:



See the TikZ manual for more information.

```
minimum width = (dimension)
minimum height = (dimension)
minimum size = (dimension)
inner sep = (dimension)
outer sep = (dimension)
```

These options control the size of a node. This is typically useful to make the size of nodes consistent independent of the size of their label text. For instance:



#### **name** = $\langle node \ name \rangle$

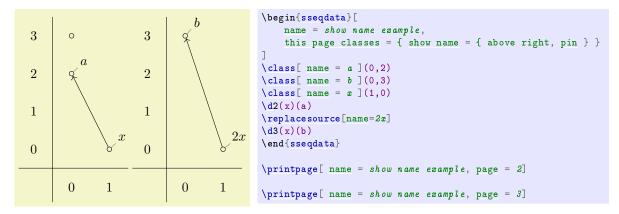
The **\class** command makes a TikZ node on appropriate pages. You can refer to this node using TikZ commands by using its coordinates. Using the class:name option, you can give the node a name, which you can use to refer to the class. Using names creates more readable code. The show name option can be used to display the names of classes. You can modify the names of classes systematically using the options class name prefix, class name postfix, and class name handler.

Named classes are immune to coordinate transformations. For example, in the following code, xshift does not apply to the nodes specified by (id) and (eta) but does apply to the coordinate specified by (1,1):



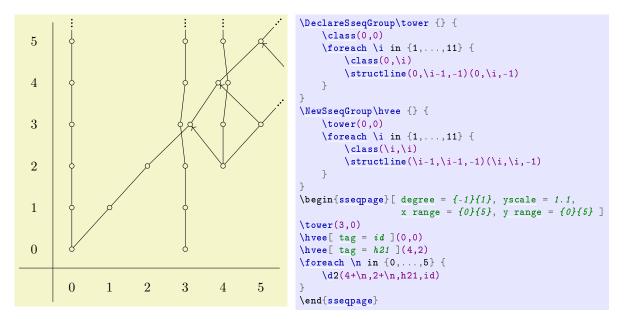
# **show name** = $\langle label options \rangle$

This option is like saying "class name"\marg{label options} if the class has a name, and does nothing if the class has no name. If the class has multiple names, only the most recent is used. This is particularly useful with class styles, . For instance, by saying this page classes = { show name = above } you can display names of all of the sources and targets of differentials on each page.



 $tag = \langle tag \rangle$ 

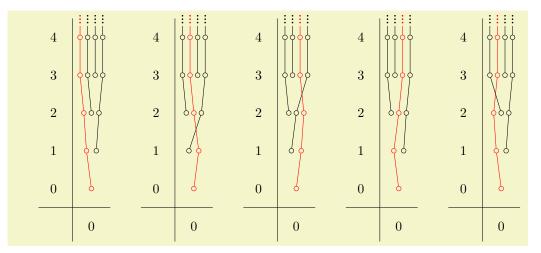
This key adds a tag to the current class. Tags are used for identifying which of multiple classes in the same position you are referring to. They are useful when you have groups of related classes and want a family of differentials connecting them. For instance:



We want each differential to go from the h21 vee to the id vee, independent of which classes are in the same position of the two vees. The easy way to accomplish this is by giving tags to each of the two vees.

# **insert** = $\langle integer \rangle$

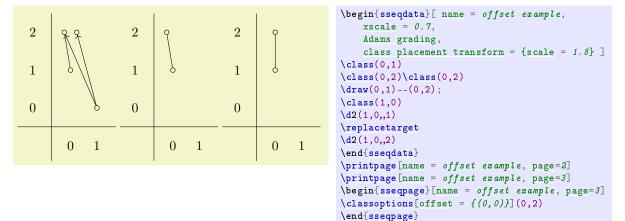
If there are multiple classes in the same position, this option allows you to insert classes later into earlier positions. This is intended to help you put logically related classes next to each other. If the integer is positive, it inserts the class in the specified position, and if the integer is negative, it counts backwards from the end. Providing 0 is the same as omitting the option entirely. Values larger in absolute value than the total number of classes are truncated. Consider:



```
\DeclareSseqGroup \tower {} {
    \class(0.0)
    \DoUntilOutOfBounds {
        \class(\lastx,\lasty+1)
        \structline
    }
}
\begin{sseqdata}[ name = insert-example, y range = {0}{4}, class pattern = linear ]
\det(0,2)
\det(0.3)
\forall tower(0,1)
\end{sseqdata}
\qquad
\begin{sseqpage}[ name = insert-example ]
\tower[red, classes = { insert = 1 } ](0,0)
\end{sseqpage}
\qquad
\begin{sseqpage}[ name = insert-example ]
\tower[red, classes = { insert = 2 } ](0,0)
\end{sseqpage}
\qquad
\begin{sseqpage}[ name = insert-example ]
\tower[red, classes = { insert = 3 } ](0,0)
\end{sseqpage}
\qquad
\begin{sseqpage}[ name = insert-example ]
\tower[red, classes = { insert = -2 } ](0,0)
\end{sseqpage}
\qquad
\begin{sseqpage}[ name = insert-example ]
\tower[red, classes = { insert = -3 } ](0,0)
\end{sseqpage}
```

## **offset** = {( $\langle x \ offset \rangle, \langle y \ offset \rangle$ )}

By default, a class uses the offset specified by **class pattern**. Occasionally this is undesirable. In this case, you can specify the offset for a particular class by hand. For example if the sum of two classes is hit by a differential, it looks better for the class replacing them to be centered:



# tooltip = $\langle text \rangle$

This key generates a "tooltip" over the given class. That is, if you hover your mouse over it, a little window will popup with the tooltip text. This is particularly useful to give the coordinates or names of classes in large charts where it may be hard to tell from looking at the picture what position the class is in, or there may not be room to supply names to classes.

The tooltip is made using the \pdftooltip command from the pdfcomment package. The pdfcomment package generates two extra auxiliary files, so it is not included by default. In order to use the tooltip option, you have to use the tooltips package option (e.g., load SPECTRALSEQUENCES with

 $\spackage[tooltips]$ {spectralsequences}). This cannot handle math, but it will print math expressions into TEX input form. Not all pdf viewers will display the tooltip correctly. If this concerns you, the command  $\spackage[tooltip is used to produce the tooltip, and you can redefine it as any other command that takes <math>\spackage[tooltip{{text}}{{tooltip text}}}$  and produces a tooltip. For instance, on this stack exchange post, there is code that supposedly produces tooltips that work with Evince. I have not tested whether it works by itself or whether it works with my package, but you could. You could potentially figure out how to get math to work in tooltips too – if you find a satisfactory method, please let me know.

Here's an example:

1	0	0	<pre>\begin{sseqpage}[classes = {tooltip = {( xcoord,  ycoord)}}] \class(0,0) \class(0,1) \class(1,0)</pre>
0	0	0	<pre>\class(1,1) \end{sseqpage}</pre>
	0	1	

There's another example at the beginning of the section on the class stack.

# page = $\langle page \rangle$ -- $\langle page max \rangle$ generation = $\langle generation \rangle$ -- $\langle generation max \rangle$

These options only work in \classoptions. The page option gives a range of pages for which the options apply to. If only one page is specified, it is the minimum page and the option applies to all larger pages.

```
      1
      2
      4

      o
      •
      o

      o
      •
      o

      (a)
      •
      o

      (b)
      •
      •

      (c)
      •
      •

      (c)</
```

A "generation" of a class is the interval from one call of \class or \replaceclass to the page on which it next supports or is hit by a differential. By default the \classoptions command adds options only to the most recent generation of the class in a {sseqdata} environment, or on the generation appropriate to the current page in a {sseqpage} environment. Using the generation option allows you to provide a single generation or range of generations of the class that the options should apply to. The first generation is generation 0, and the most recent generation is generation -1. Larger negative values count backwards.

3 2 1 0	0	3 2 1 0	0	3 2 1 0	0 9	3 2 1 0	Ŷ	3 2 1 0	•
	0 1		0 1		0 1		0 1		0 1

```
\begin{sseqdata}[ name = page_example2, Adams grading, xscale = 0.6, yscale = 0.5 ]
class(0,2) class(1,0)
d2(1.0)
\replace source
\class(0,3)
d3(1,0)
\replace source
\classoptions[fill, red](1,0) % (a) applies to most recent (last) generation.
\end{sseqdata}
\printpage[ name = page_example2, page = 1 ] % generation 0 of (1,0), not styled
\quad
\begin{sseqpage}[ name = page_example2, page = 1, keep changes ]
classoptions[fill, blue](1,0) % (b) applies to the generation present on page 1, that is, generation 0.
\end{sseqpage} \quad
% generation 0 of (1,0), so class is blue from (b)
\printpage[ name = page_example2, page = 2 ] \quad
% generation 1 of (1,0), class is not styled
\printpage[ name = page_example2, page = 3 ] \quad
% generation 2 of (1,0), class is red from (a)
\printpage[ name = page_example2, page = 4 ]
  3
                       3
                                             3
                                                                  3
                                                                                       3
         0
                               0
                                                    0
                       \mathbf{2}
  \mathbf{2}
         0
                               0
                                             2
                                                                  2
                                                                                       \mathbf{2}
  1
                       1
                                             1
                                                                  1
                                                                                       1
  0
                       0
                                             0
                                                                  0
                                                                                       0
         0
            1
                               0
                                                    0
                                                                         0
                                                                                              0
                                                                                                  1
                                  1
                                                       1
                                                                            1
\begin{sseqdata}[ name = page_example2, Adams grading, update existing ]
% (c) applies to all generations, overwrites (b) and (a):
classoptions[fill, red, generation = 0 - -1](1,0)
\end{sseqdata}
\printpage[ name = page_example2, page = 1 ]% generation 0 of (1,0), so class is red
\quad
\begin{sseqpage}[ name = page_example2, page = 1, keep changes ]
\classoptions[fill, blue](1,0) % (d) applies to the generation present on page 1, that is, generation 0.
\end{sseqpage} \quad
% generation 0 of (1,0), class is blue from (d)
\printpage[ name = page_example2, page = 2 ] \quad
% generation 1 of (1,0), class is red from (c)
\printpage[ name = page_example2, page = 3 ]
\quad
\printpage[ name = page_example2, page = 4 ] % generation 2 of (1,0), class is red from (c)
```

\xcoord \ycoord

These commands represent the x and y coordinate of the current class when used in class options. The only use I have for them is in the tooltip option, but maybe there is some other purpose for them.

# 4.3 Options for d, structline, and extension

Because the main job of the d, structline, and extension commands is to print an edge on the appropriate pages of the spectral sequence, most TikZ options that you could apply to a TikZ "to" operator (as in/draw (x1,y1) to (x2,y2);) can be applied to d, structline, and extension. Some such options are as follows:

```
source anchor = \langle anchor \rangle
target anchor = \langle anchor \rangle
```

Because you can't use the normal TikZ mechanism for specifying the source and target anchors, SPEC-TRALSEQUENCES has these two keys for \d and \structline:

```
\begin{sseqpage}[ no axes, yscale = 1.24 ]
\foreach \x in {0,1} \foreach \y in {0,1} {
    \class(\x,\y)
}
\structline(0,0)(0,1)
\structline[ source anchor = north west, target anchor = -30 ](1,0)(1,1)
\end{sseqpage}
```

# shorten > = \langle distance \rangle shorten < = \langle distance \rangle</pre>

These behave exactly like the corresponding options from TikZ, shortening the end and beginning of the edge respectively. Note that you can lengthen the edge by shortening by a negative amount.

Dash patterns:

See the TikZ manual for a complete explanation of the dash pattern related options. Some examples:

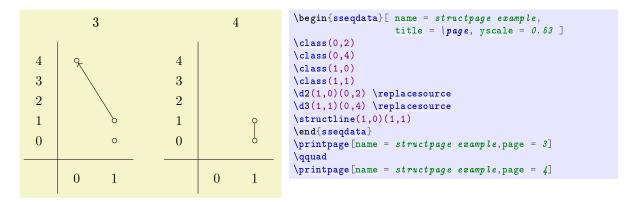
```
>begin{sseqpage}[ no axes, yscale = 1.6 ]
>foreach \x in {0,1,2} \foreach \y in {0,1} {
        \class(\x,\y)
}
}
a a a \structline[densely dotted](0,0)(0,1)
>structline[dashed, red, "a"](1,0)(1,1)
>structline[dash dot, red, "a" black](2,0)(2,1)
>end{sseqpage}
```

```
bend left = \langle angle \rangle
bend right = \langle angle \rangle
in = \langle anchor \rangle
out = \langle anchor \rangle
```

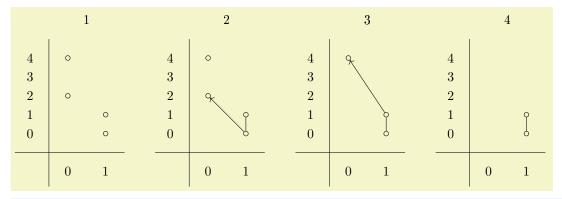
```
\begin{sseqpage}[no axes,yscale = 1.6]
\foreach \x in {0,1,2} \foreach \y in {0,1} {
    \class(\x,\y)
}
\structline[bend left = 20](0,0)(0,1)
\structline[bend right = 20](1,0)(1,1)
\structline[in = 20, out = north](2,0)(2,1)
\end{sseqpage}
```

**page** =  $\langle page \rangle - \langle page max \rangle$ 

This key is only for \structline and \structlineoptions. By default, the \structline command only adds a structure line starting on the page where the most recent generation of the source or target is born:



By specifying a page number, you can adjust which page the \structline starts on:



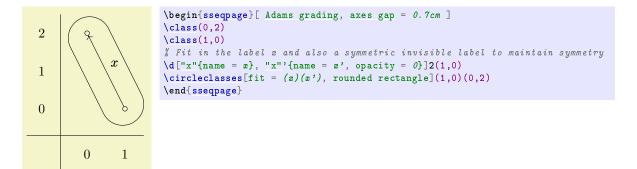
```
\begin{sseqdata}[ name = structpage example2, title = |page, yscale = 0.5 ]
\class(0,2)
\class(0,4)
\class(1,0)
\class(1,1)
d2(1,0)(0,2) \replacesource
d3(1,1)(0,4) \replacesource
\structline[page = 2](1,0)(1,1)
\end{sseqdata}
\printpage[ name = structpage example2, page = 1 ]
\qquad
\printpage[ name = structpage example2, page = 2 ]
\qquad
\printpage[ name = structpage example2, page = 3 ]
\qquad
\printpage[ name = structpage example2, page = 4 ]
```

Similarly, for \structlineoptions you can specify a minimum page on which to apply the options, or a range of pages.

# 4.4 Options for \circleclass

 $fit = \langle coordinates \ or \ nodes \rangle$ 

The  $\circleclasses$  command uses the TikZ fitting library. Sometimes it's desirable to make the resulting node fit extra things, for example a label. It doesn't necessarily end up looking great though.



#### rounded rectangle

You can put a shape as an option and it will change the shape of the node drawn by \circleclasses. Any shape will do, but I think that an ellipse or rounded rectangle are the only particularly appealing options.

#### ellipse ratio = $\langle ratio \rangle$

# (initially 1.2)

By default, the shape drawn by \circleclasses is a "newelipse" which is a custom defined shape that respects the option elipse ratio which roughly controls how long and skinny versus short and fat the ellipse is. If you find that the ellipse is too long, try a larger value of this option, and conversely if it's too fat try a smaller value. If no value is satisfactory, try out the rounded rectangle shape. (This is stolen from the following stack exchange answer: https://tex.stackexchange.com/a/24621.)

```
class style
permanent cycle style
transient cycle style
this page class style
differential style
struct line style
```

See the corresponding entry in the TikZ primitives section.

# **page** = $\langle page \rangle - \langle page max \rangle$

By default, the ellipse will be drawn on the same set of pages that a structure line between the two classes would be drawn on. This specifies a range of pages for the ellipse to be drawn. Note that unlike with structure lines, you can instruct \circleclasses to draw the shape even on pages where one or both of the classes that it is fitting are dead.

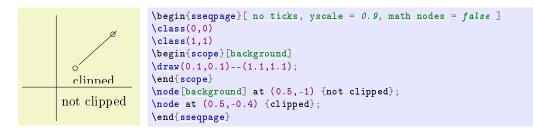
# 4.5 Options for TikZ primitives

#### background

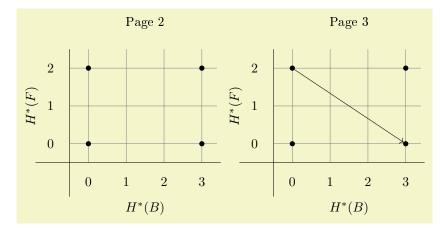
This key instructs SPECTRALSEQUENCES to put the current TikZ primitive in the background. The way that the spectral sequence is printed is as follows:

- The title, axes, axes ticks, and axes labels are printed (the appropriate steps are skipped when the no title, no axes, no ticks, or no labels keys are used or if no title or axes labels are provided).
- The TikZ background paths are printed.
- The clipping is inserted (unless the no clip key is used).
- All foreground elements (classes, differentials, structure lines, and normal TikZ paths) are printed.

In particular, this means that foreground TikZ paths can be clipped by the standard clipping, but background paths that are outside of the clipping expand the size of the TikZ picture.

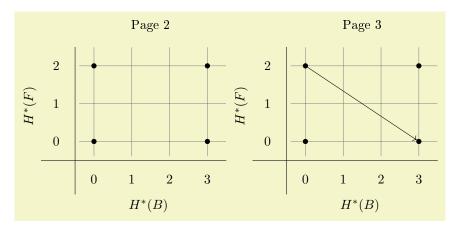


Here is an example where TikZ labels with the background key are used to add labels and a grid. Note that this styling is easier to make using the title, x label, y label, and grid options.



\begin{sseqdata}[ name = tikz background example, cohomological Serre grading, classes = fill ]
\begin{scope}[background]
\node at (\xmax/2,\ymax+1.2) {\textup{Page \page}};
\node at (\xmax/2,-1.7) {H^\*(B)};
\node[rotate = 90] at (-1.5,\ymax/2) {H^\*(F)};
\draw[step = 1cm, gray, very thin] (\xmin-0.5,\ymin-0.5) grid (\xmax+0.4,\ymax+0.5);
\end{scope}
\class(0,0)
\class(0,2)
\class(0,2)
\class(0,2)
\class(0,2)
\end{sseqdata}
\printpage[name = tikz background example, page = 2]
\printpage[name = tikz background example, page = 3]

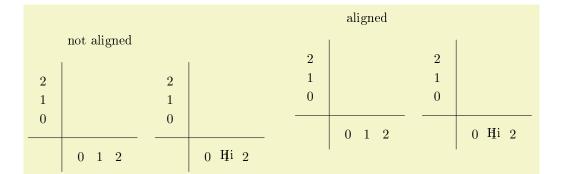
For this particular use case, it's probably better to use title, x label, and y label:



But if you need more flexible labeling, you'll likely want to use tikz primitives with background. See example\_KF3.tex for an instance where this key is useful.

One useful tip is that you can ensure consistent bounding boxes between different diagrams using

# \path[background] (smallest x, smallest y) -- (largest x, largest y);:



```
\begin{sseqdata}[ name = boundingboxex, x range = {0}{2}, y range = {0}{2}, scale = 0.5 ]
\end{sseqdata}
\printpage[ name = boundingboxex, title = not aligned ]
\quad
\printpage[ name = boundingboxex, x label = Hi ]
\quad
\begin{sseqpage}[ name = boundingboxex, keep changes, title = aligned ]
\path[background] (\xmin,\ymin-4) -- (\xmax,\ymax+2);
\end{sseqpage}
\quad
\printpage[ name = boundingboxex, x label = Hi, title = {} ]
```

page constraint =  $\langle predicate \rangle$ page constraint or =  $\langle predicate \rangle$ 

This places a constraint on the pages in which the TikZ primitive is printed. This predicate should look something like (\page <= 4) && (\page >= 3). The predicate is anded together with any previous predicates, so that you can use this as an option for a {scope} and again for the individual TikZ primitive.

(coordinate)

```
(\langle coordinate 1 \rangle) \cdots (\langle coordinate n \rangle)
```

This command can only be used with page constraint. Saying

```
page constraint = {\pars{\meta{x},\meta{y}\opt{,}\oarg{index}}}}
```

will print the TikZ primitive only on pages where the specified class is alive. Saying

```
page constraint = {(n \in (n \in 1)) \dots (n \in 1)}
```

is equivalent to

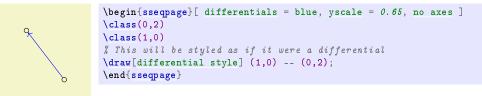
page constraint = {\isalive\pararg{coordinate 1} && ... && \isalive\pararg{coordinate n}}
Writing

```
\draw[page constraint = {\isalive(1,0)(2,2)}](1,0)--(2,2);
```

is the same as structline(1,0)(2,2), except that you can't later use structlineoptions on it (and it won't have the struct lines style applied).

```
c lass style
permanent cycle style
transient cycle style
this page class style
differential style
struct line style
```

These classes apply the styling of the corresponding element to your TikZ commands.



See \getdtarget for a more natural example.

# 5 Miscellaneous Commands

# 5.1 Settings

 $\seqset{\langle keys \rangle}$ 

The \sseqset command is for adjusting the global options for all spectral sequences in the current scope, or for applying options to the rest of the current spectral sequence. For instance, if most of the spectral sequences in the current document are going to be Adams graded, you can say\sseqset{Adams grading} and all future spectral sequences in the current scope will have Adams grading (unless you specify a different grading explicitly). As another example, \sseqset{no axes} will suppress axes from spectral sequences in the current scope. Note that defaults only apply to new {sseqdata} environments or to unnamed {sseqpage} environments; they won't apply to existing spectral sequences.

You can also use \sseqset to create styles to be used in spectral sequences.

```
.global sseq style = \langle keys \rangle
.global sseq append style = \langle keys \rangle
.sseq style = \langle keys \rangle
.sseq append style = \langle keys \rangle
```

These handlers create reusable styles to be used in spectral sequences. If this style is a set of global options, then use the .global sseq style handler, whereas if it is supposed to be applied to individual features (classes, differentials, structure lines, circle classes, and tikz primitives) then use the .sseq style handler.



# $\SeqErrorToWarning\langle error-name \rangle$

Turns the error with the given name into a warning. An error message will start by saying spectralsequences error: "error-name". This is the name you need to put into this command.

#### \begin{quiet}

(environment contents)
\end{quiet}

This environment quiets error messages that occur inside of it. SPECTRALSEQUENCES is pretty good at error recovery, and so most of commands will fail gracefully and do nothing if their preconditions aren't met. If there are any parsing errors in the body of the {quiet} environment, prepare to see low level internal error messages. You might also run into bugs in SPECTRALSEQUENCES – the error recovery code hasn't been that carefully tested. If you do get low level error messages, remember to comment out the {quiet} environment before trying to debug.

This is particularly useful for code reuse commands. Sometimes there is a source of long differentials that only applies to classes that haven't already supported shorter differentials. Sometimes there should be a structure line if a certain class exists, but it might not exist. In these cases, the {quiet} environment will help you out. See also \DrawIfValidDifferential, which is a variant of \d that behaves as if it were inside a {quiet} environment.

# 5.2 Code reuse commands

#### foreach

This command is from TikZ and works in pretty much the same way in SPECTRALSEQUENCES, though with slightly better variants. The \foreach command is very flexible and has a lot of variants. The basic usage is\foreach x in {\meta{xmin},...,\meta{xmax}} \marg{loop body} which will execute \meta{loop body} with x set to each value between  $\langle xmin \rangle$  and  $\langle xmax \rangle$  inclusive. If you want a step greater than 1, try

\foreach \x in {\meta{xmin}, \meta{xmin}+\meta{xstep},..., \meta{xmax}}\marg{loop body}. If you need to do multiple loops with a common body, you can just stack the \foreach commands:

$\frac{3}{2}$	0	0	0	0	<pre>\begin{sseqpage}[ xscale = 0.5, x tick step = 2 ] \foreach \x in {0,2,,6} \foreach \y in {0,,3}{         \class(\x,\y) } \end{sseqpage}</pre>
1	0	0	0	0	
0	0	0	0	0	
	0	2	4	6	

You can also loop through tuples, for instance:

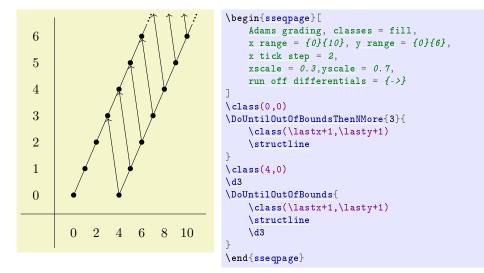


See the last example for normalize monomial for a better example of this usage.

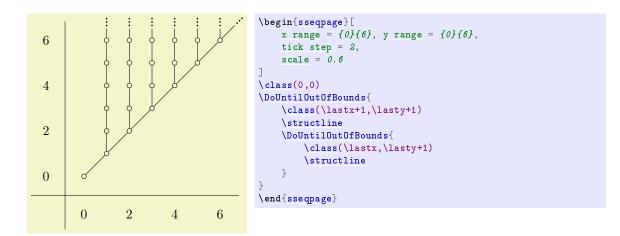
There are tons of other things you can do with foreach, though I haven't yet found need for them in combination with SPECTRALSEQUENCES. See the TikZ manual for more details.

# \Do{{iterations}}{loop body} \DoUntilOutOfBounds{loop body} \DoUntilOutOfBoundsThenNMore{{extra iterations}}{loop body} \iteration

The one use case that foreach doesn't cover all that well is if you want the loop to always repeat until the features you are drawing go off the page. This is what DoUntilOutOfBoundsThenNMore are for. These help ensure that if you change the range of your chart, infinite families will automatically be drawn correctly without the need to adjust a bunch of loop bounds. The purpose of DoUntilOutOfBoundsThenNMore is for towers that are receiving a differential. If your spectral sequence is Adams graded, and a tower is receiving a  $d_r$  differential from another tower, you should use  $DoUntilOutOfBoundsThenNMore{r}$ :



You can also nest \DoUntilOutOfBounds reasonably:



One important difference between \foreach and the \Do family of commands is that \Do has no effect on the stack. This is in order to ensure that they nest properly.

Note that if you are using these commands and you are planning to draw several pictures of the chart with restricted range, you need to specify a range for the {sseqdata} that contains all of the ranges of pages that you want to draw. If you then want to set a smaller default range, specify the smaller range the first time you use {sseqpage} or \printpage to draw the spectral sequence, and include the keep changes key.

The \Do command is less general than \foreach; the purpose is to provide a syntax for stack-based looping that is similar to \DoUntilOutOfBounds but with a fixed range. So \Do{n}\marg{loop body} repeats  $\langle loop \ body \rangle$  n times. The assumption is that the loop body draws something relative to the position of the \lastclass.

If you need to know how many iterations one of these three commands has gone through, this is stored in the variable *\iteration*.

# $\label{eq:large} $$ \eqref{argspec} $$ \eqref{arg$

The xparse package provides these very powerful commands for defining macros. They are used internally to the SPECTRALSEQUENCES package to define class, d, etc. To help you create variants of these commands, I will record here the argument specifications for each of them. See the xparse manual for a better explanation and more information.

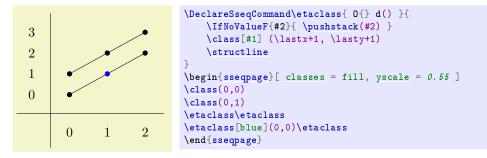
To make a command like  $\class$ , you can use the argument specification  $O{}r()$ . The argument type  $O{\langle default \rangle}$  stands for a bracket delimited optional argument with default value  $\langle default \rangle$ . In this case, we've specified the default to be empty. r() stands for a "required" argument delimited by ( and ). In the command definition, access the optional argument with #1 and the coordinate with #2.

$\#1 = \{\text{key} = \text{value}\}; \ \#2 = \{x, y\}$	<pre>\DeclareDocumentCommand\demo{ 0{} r() }         { \#1 = \textcolor{purple}{\{#1\}};</pre>
$\#1=\{\};\#2=\{1,2,3\}$	<pre>\#2 = \textcolor{purple}{\{#2\}} } \hbox{\demo[key = value](x,y)}</pre>
	<pre>\bigskip \hbox{\demo(1,2,3)}</pre>

If you want to separate out the coordinates into different arguments, you can use  $0{}u(u,u)$ . The argument type u stands for "until" and scans up until the next instance of the given character. So in this case, #1 is of argument type 0 which is an option list, #2 corresponds to the u( which is a throw-away argument, then #3 corresponds to u, and contains the x coordinate, and #4 corresponds to u) and contains the y coordinate. Note however that this will not match balanced parenthetical expressions.

You can specify an optional argument delimited by parentheses using d(). Use the commands \IfNoValueTF, \IfNoValueT, and \IfNoValueF to test whether the user provided a value.

An example where this is actually useful:



The  $\$  and  $\$  argument specification  $0{r()r()}$ .

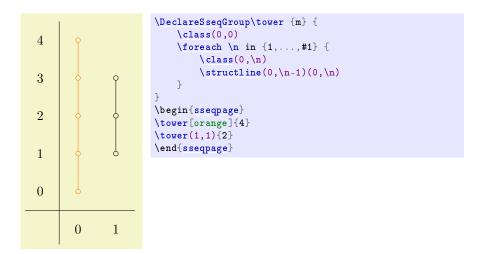
 $#1 = {hi}; #2 = {x,y}; #3 = {x',y'}$  $#1 = {}; #2 = {x,y,2}; #3 = {x',y',-1}$ 

```
\DeclareDocumentCommand\demo{ 0{} r() r() }
    { \#1 = \textcolor{purple}{\{#1\}};
    \#2 = \textcolor{purple}{\{#2\}};
    \#3 = \textcolor{purple}{\{#3\}} }
\hbox{\demo[hi](x,y)(x',y')}
\bigskip
\hbox{\demo(x,y,2)(x',y',-1)}
```

These are similar to \NewSseqCommand and \DeclareSseqCommand except that the commands defined take an optional square bracket delimited options list, followed by an optional parenthesis delimited (x,y) pair and wraps the body of the code in

```
\begin{scope}[xshift = \meta{xcoord}, yshift = \meta{ycoord}, options].
```

For instance:



Here we define a command which takes an options list, a coordinate, and a single mandatory argument. The options are applied to all the classes and structlines, the coordinate shifts the origin, and the mandatory argument is the length of the tower.

 $SseqCopyPage (command) {(spectral sequence name)} {(page)}$ 

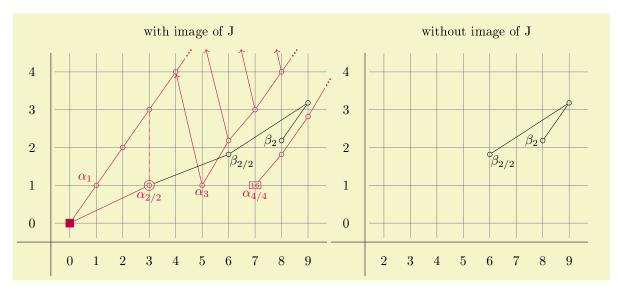
This defines  $\langle command \rangle$  to print all of the classes and structlines on page  $\texttt{meta{page}}$  of the spectral sequence named $\texttt{meta{spectral sequence name}}$ , throwing out differentials and tikz primitives. The resulting command has syntax as if you had used DeclareSseqGroup with no extra arguments – that is, it takes an optional options list, which are passed to a scope, and an optional coordinate pair.

# 5.3 Families

SPECTRALSEQUENCES has a concept of "class families" that can be drawn or suppressed as a group, and that can have styling options applied to them as a group.

# $SseqNewFamily{\langle family name \rangle}$

This makes a new family with name  $\langle family name \rangle$ . The effect of this is to define global options  $\meta{family name}$  style which apply options to all classes in the family, draw  $\meta{family name}$  which causes the family to be drawn, and no  $\meta{family name}$  which suppresses the family (drawing is the default behavior of course). It also defines an option  $\meta{family name}$  which puts a feature into the family – so it can be used as an option to any of the normal commands like  $\class, \d, \structline, etc and to a scope.$ 



```
\SseqNewFamily{imJ}
\begin{sseqdata}[
    name=ANSS-S_2, Adams grading,
    class labels = {below}, label distance = -1pt,
    class placement transform = {rotate = 90, scale = 2},
   differentials = blue,
   x range = \{0\}\{9\}, y range = \{0\}\{4\},
   xscale = 0.7, grid = go
% Image of J classes
\begin{scope}[imJ]
\class[rectangle,fill,inner sep=3pt](0,0)
\DoUntilOutOfBoundsThenNMore{3}{\etaclass}
\classoptions["\alpha_1" above left](1,1)
\class["\alpha_{2/2}", circlen = 2](3,1)
\structline(0,0) \structline[dashed](3,3)
\class["\alpha_3"](5,1) \d3\relax
\DoUntilOutOfBounds{ \etaclass \d3 }
class["alpha_{4/4}", rectangle, "16" {font = \tiny, inside, inner sep = 1pt](7,1)
\DoUntilOutOfBoundsThenNMore{3}{\etaclass}
\end{scope}
% Other classes
class["beta_{2/2}" {below right=-4pt}, insert = 1](6,2)
\structline(3,1)
\class["\beta_{2}" left](8,2)
\etaclass\structline(6,2,2) % This is a *nu
\end{sseqdata}
\printpage[ name = ANSS-S_2, title = with image of J, imJ style = purple]
\printpage[name = ANSS-S_2, no imJ, x range={2}{9}, title = without image of J]
```

# 5.4 Utilities

 $SseqParseInt (macro) {(integer expression)}$ 

Stores the result of evaluating an integer expression into  $\langle macro \rangle$ . An integer expression consists of +, -, \*, /, parentheses, and macros that expand to more of the same. The exact rules regarding what is a valid expression are pretty much what you would expect. Note that juxtaposition is a syntax error, not multiplication, so 2(1+1) is invalid, you must say 2\*(1+1).

This tests if an expression is the empty expression. This is mainly useful for giving systematic labels to things.

Test whether a class of the given description exists. The description can be any valid coordinate, including a named coordinate. If the coordinate is not valid, this will return false.

```
\Gamma \left( page \right) \left( \left( coordinate \right) \right) \left( \left( true \ code \right) \right)
```

```
\Gamma_{qage} (\langle coordinate \rangle) \{\langle false \ code \rangle\}
```

Test whether a class is alive on the given page. If the class doesn't exist, this will return false.

```
\label{eq:lighted} $$ IfOutOfBoundsTF(\langle coordinate \rangle) {\langle true \ code \rangle} {\langle false \ code \rangle} \\ IfOutOfBoundsT(\langle coordinate \rangle) {\langle true \ code \rangle} $$
```

```
\formula for four definition for the second secon
```

```
\IfInBoundsT(\langle coordinate \rangle) \{\langle true \ code \rangle\}
```

```
\figure{} \fig
```

Test whether a class is in bounds or out of bounds. If no such class exists, returns false.

```
\label{eq:linear} $$ If ValidDifferentialTF(page)((coordinate))((target coordinate)){(true code)}{(false code)} $$
```

 $\IfValidDifferentialT(page)((coordinate))((target coordinate)){(true code)}$ 

 $\If ValidDifferentialF(page)((coordinate))((target coordinate)) {(false code)}$ 

 $\DrawIfValidDifferentialF[\langle options \rangle] \langle page \rangle (\langle coordinate \rangle) (\langle target \ coordinate \rangle) {\langle false \ code \rangle}$ 

 $\label{eq:linear} $$ DrawIfValidDifferential[(options)](page)((coordinate))((target \ coordinate)) {(false \ code)} }$ 

Test whether a differential is valid. There are many possible reasons for a differential to not be valid – the source or target class could not exist, the target could not be in the correct grading, etc. If any error would be generated if you supplied the same arguments to \d, this tests false. Otherwise, this tests true. The command \DrawIfValidDifferental draws the differential if it is valid, whereas \DrawIfValidDifferentalT draws the differential and executes the true code if it is valid, \DrawIfValidDifferentalF draws the differential or executes false code if it isn't valid, etc.

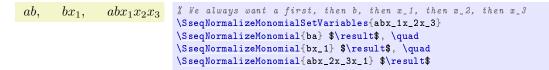
# \SseqNormalizeMonomial

This command simplifies a monomial by combining like variables and removing bases that are raised to the 0th power, removing exponents of 1, removing 1's, and replacing the empty monomial with 1. The variables are sorted by first occurrence, use \SseqNormalizeMonomialSetVariables to set a different sort order. It outputs its result into \result. This command is specifically meant to be used as a value for class label handler or class name handler. See the example in the documentation for class label handler for a realistic example. The exponents must be integers or else it will misbehave.

```
\begin{array}{cccc} 1, & x^2y, & x_2^4 \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\
```

# \SseqNormalizeMonomialSetVariables

This command takes an undelimited list sets up \SseqNormalizeMonomial to sort the variables in the input in the specified order. This is useful for consistency, and particularly important for when you use it to name classes. For example:



# \SseqAHSSNameHandler

This command expects an argument of the form\meta{monomial}[\meta{integer expression}] and defines \result to be m[n] where m is the result of applying \SseqNormalizeMonomial to the monomial, and n is the result of evaluation the integer expression plus any yshift that is present. This is intended for use with in drawing Atiyah Hirzebruch spectral sequences. See class name handler for an example of the calculation of  $KO^*\mathbb{RP}^8$ .

# 5.5 Coordinate parsers and related

```
\parsecoordinate \ (\ coordinate \)
```

This command parses the coordinate and puts the triple (x,y,n) into  $\langle macro \rangle$ . It also puts the components of the coordinate into macros, for instance if  $\langle macro \rangle$  is  $\langle coord$ , then  $\langle xcoord will contain$  the x coordinate,  $\langle ycoord will contain$  the y coordinate, and  $\langle ncoord will contain$  the index. The coordinate can be anything that would be valid to use in a differential or structure line; this is the macro that is used internally to handle coordinates.

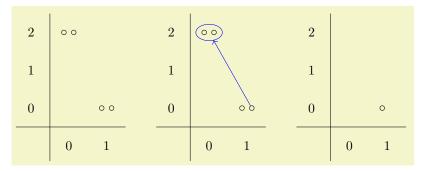
# 

Sets  $\langle macro \rangle$  equal to the coordinates of the target position of a length  $\langle page \rangle$  differential starting at  $\langle source \ coordinate \rangle$ . This helps to make commands that draw fancy differentials.

# $\parsedifferential (page)((differential coordinate))((differential target))$

This has the same weird syntax of \d, except that you are required to put braces around the page (if it has multiple digits) and you are required to provide at least one coordinate (you have to say \parsedifferential{2}(\lastclass) for instance). This command is similar in effect to saying both \parsecoordinate\source\meta{source coordinate} and \parsecoordinate\target\meta{target coordinate} but it handles determination of the target coordinate for you.

For instance, consider the following example, suggested by Catherine Ray:



```
\% O{} U( r() is the arg-spec for d, O{} U( r() mm looks like d with one extra mandatory arguments
parsedifferential{#2}(#3)(#4)
                                                 % Store the target position in \target
                                                % give names to the three classes
    \nameclass{source}(\sourcecoord, \nsource)
    \nameclass{target1}(\targetcoord,\ntarget)
    \nameclass{target2}(\targetcoord,#5)
%
    \circleclasses[ differential style, name path = circ,
                    #1, page = #2-#2]
                    (target1)(target2)
                                                % Circle the classes, use differential style
%
    % record source and targets as hit.
    \kill#2(source) \kill#2(target1) \kill#2(target2)
%
    \path(target1)--(target2)
                coordinate[midway](midpt); % put a coordinate in the center of the two classes
    \path[name path = lin] (source) -- (midpt); % save path from start to midpoint
%
    \label{eq:linear} \label{eq:linear} \label{eq:linear} \label{eq:linear} draw line in "differential style" from start to intersection point of circ and lin
    \draw[ differential style, #1, page constraint= { \page == #2 },
           name intersections = { of = circ and lin } ]
                (source) -- (intersection-1);
\begin{sseqdata}[ name = cathex, Adams grading, differentials = { blue } ]
class(0,2) class(0,2)
class(1,0) class(1,0)
twods2(1,0,-1,1){2}
\end{sseqdata}
\printpage[ name = cathex, page = 1 ]
\qquad
\printpage[ name = cathex, page = 2 ]
\qquad
\printpage[ name = cathex, page = 3 ]
```

 $\mbox{nameclass}(\langle name \rangle) (\langle coordinate \rangle)$ 

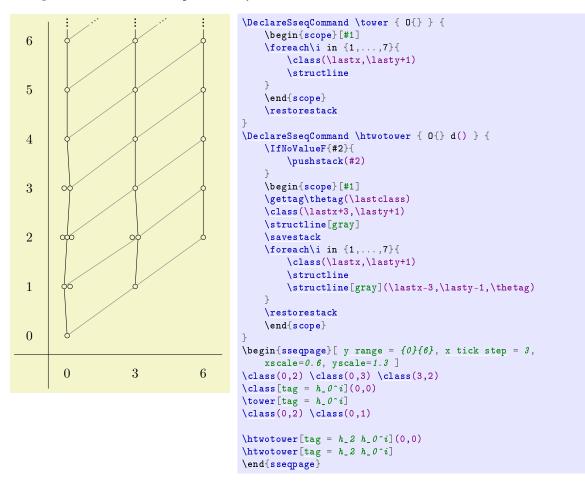
The \nameclass command gives a name to a class. It's similar to saying \doptions[name =  $\langle name \rangle$ ], but faster. It's also similar to saying \pushstack( $\langle coordinate \rangle$ ). Giving temporary names to coordinates that you are going to use repeatedly makes the code easier to read and is faster (though this only matters in very large charts). See \getdtarget for an example.

# $\tagclass{\langle tag \rangle}(\langle coordinate \rangle)$

The  $\tagclass command gives a tag to a class. It's similar to saying <math>\doptions[tag = \langle name \rangle]$ , but faster. See example\_tmfmayss.tex for a use case for this.

# $\gettag (macro) ((coordinate))$

The \gettag command finds the most recent tag applied to the coordinate and stores it into \cmdarg{macro}. This is useful for connecting groups of nodes. For example, consider the following code, inspired by example\_tmfmayss.tex.



# 5.6 The class stack

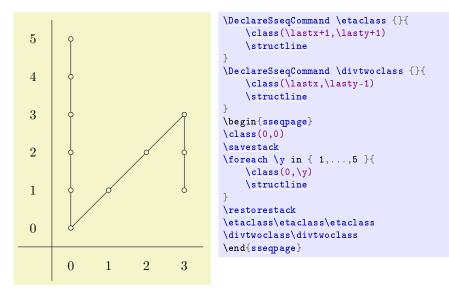
The class stack is a linked list of the classes in the order that they are produced that SPECTRALSEQUENCES maintains. Whenever you use the \class or \replaceclass command, the class you added is pushed onto the stack.

The following commands are used to access the stack:

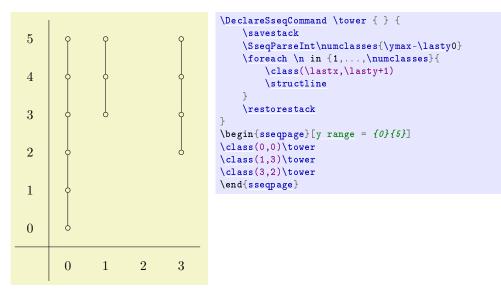
 $\begin{array}{l} \texttt{lastx} \langle n \rangle \\ \texttt{lasty} \langle n \rangle \end{array}$ 

# $\lastclass\langle n \rangle$

The commands  $\lastx$  and  $\lasty$  evaluate to the x and y position, respectively, of the *n*th class on the stack. If n = 0 you can leave it off. The command  $\lastclass$  evaluates to the coordinate of the most recent class on the stack. This is useful for writing turtle-style code:



You can use \lastx and \lasty in other contexts than in the body of a SPECTRALSEQUENCES command, most notably inside \SseqParseInt (they also work correctly when used inside of \pgfmathparse and its siblings). For instance, consider the following tower command:



 $\begin{substack}(\langle coordinate \rangle) \end{substack}$ 

This adds a class to the top of the stack. The coordinate is specified using the same syntax as a coordinate for \structline or \replaceclass.

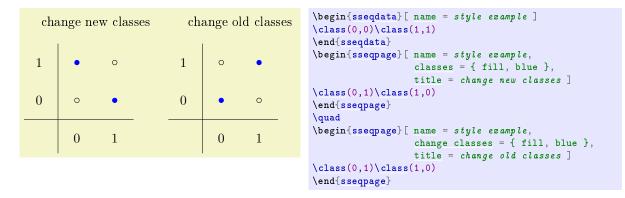
# \savestack

#### \restorestack

This saves and reverts the stack. Saves nest. Most frequently, you will want to use these at the start and end of a command.

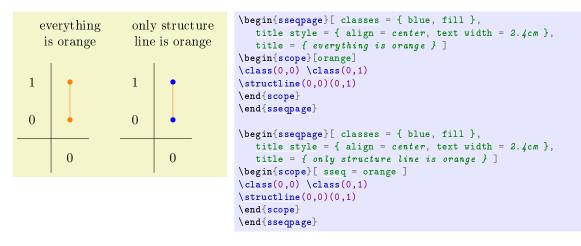
# 6 Styles

The SPECTRALSEQUENCES package has a large number of styles which control the appearance of specific components (e.g., classes, differentials, or structure lines) of a spectral sequence. Each style has two corresponding keys: classes and change classes. Saying classes =  $\{\langle keys \rangle\}$  adds the keys to the list of options used to style every future class, whereaschange classes =  $\{\langle keys \rangle\}$  only makes sense in a {sseqpage} environment, and temporarily overwrites the list of options. Note that change classes only applies to classes that existed before the current page, and that even with the keep changes option, the change classes options are local to the current page. Compare:



You can modify these styles outside of a spectral sequence or inside it using \sseqset, you can modify them as options to the {sseqdata} and {sseqpage} environments, or you can modify them as arguments to the {scope} environment.

In cases where the same drawing feature is affected by multiple of these styles, the more specific style takes precedence. For instance, for a class that is the source or target of a differential on the current page, the precedence order from lowest to highest goes: sseq style, class style,transient cycle style, this page cycle style, and then any options from scopes in the order they appear, and any local options (the options that come right with the class, e.g., \class[local options](x,y)). If you don't want the options to your scopes to override more specific styles, use sseq:



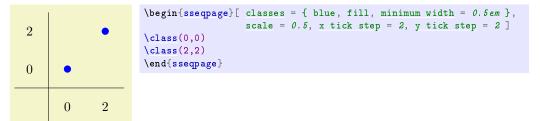
Throughout, "class" and "cycle" are synonyms.

```
sseqs = {\langle keys \rangle}
change sseqs = {\langle keys \rangle}
sseq = {\langle keys \rangle}
change sseq = {\langle keys \rangle}
```

This passes options to all features in all future spectral sequences in the current scope. Note that for many global options you can set a default directly by saying \sseqset{key = \marg{value}} and this is in some cases preferable.

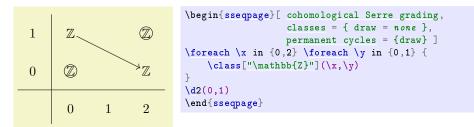
2 1 0	2 1 0		<pre>% Applies to both of the following sseqs: \sseqset{ sseqs = { blue, scale = 0.5 } } \begin{sseqpage} \foreach \x in {0,1} \foreach \y in {0,1,2} { \class(\x,\y) } \end{sseqpage} \begin{sseqpage}[ Adams grading, classes = fill ] \foreach \x in {0,1,2} \foreach \y in {0,1,2} {</pre>
		I	\class(\x,\y) } \d2(1,0) \d2(2,0) \end{sseqpage}

```
classes = {\langle keys \rangle}
cycles = {\langle keys \rangle}
change classes = {\langle keys \rangle}
change cycles = {\langle keys \rangle}
```



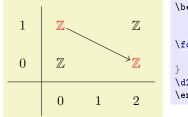
permanent classes = { $\langle keys \rangle$ } permanent cycles = { $\langle keys \rangle$ } change permanent classes = { $\langle keys \rangle$ } change permanent cycles = { $\langle keys \rangle$ }

These options change the appearance of all permanent cycles (e.g., those classes which never support or are hit by a differential). For instance, we can circle the permanent cycles automatically. In the following example, note that because permanent cycles is more specific than classes, thepermanent cycles = {draw} command takes precedence over theclasses = {draw = none} command and the permanent cycle nodes are drawn.



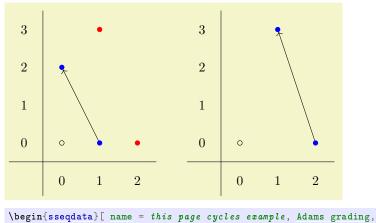
```
transient classes = {\langle keys \rangle}
transient cycles = {\langle keys \rangle}
change transient classes = {\langle keys \rangle}
change transient cycles = {\langle keys \rangle}
```

These options change the appearance of all transient cycles (e.g., those classes which eventually support or are hit by a differential). Again, this takes precedence over the **classes** option.



```
this page classes = {\langle keys \rangle}
this page cycles = {\langle keys \rangle}
change this page classes = {\langle keys \rangle}
change this page cycles = {\langle keys \rangle}
```

These options change the appearance of all cycles which support or are hit by a differential on this page. Any class that is hit on the current page is also a transient cycle, and so **this page classes** takes precedence overtransient cycles.



```
transient cycles = { red, fill }, this page cycles = { blue } ]
\class(0,0)
\class(0,2) \class(1,0)
\class(1,3) \class(2,0)
\d2(1,0) \d3(2,0)
\end{sseqdata}
\printpage[ name = this page cycles example, page = 2 ] \qquad
\printpage[ name = this page cycles example, page = 3 ]
```

```
edges = {\langle keys \rangle}
differentials = {\langle keys \rangle}
struct lines = {\langle keys \rangle}
change edges = {\langle keys \rangle}
change differentials = {\langle keys \rangle}
change struct lines = {\langle keys \rangle}
```

The edges key applies to both differentials and structure lines. The differentials and struct lines keys both take precedence over edges.

```
this page struct lines = {\langle keys \rangle}
change this page struct lines = {\langle keys \rangle}
```

This style applies to structure lines whose source or target is hit on the current page. It takes precedence over struct lines.

tikz primitives = { $\langle keys \rangle$ } change tikz primitives = { $\langle keys \rangle$ }

Applies to all TikZ primitives.

```
labels = {\langle keys \rangle}
change labels = {\langle keys \rangle}
```

This style applies to labels on classes, differentials, and structure lines. All the more specific label styles take precedence over it.

```
class labels = {\langle keys \rangle}
inner class labels = {\langle keys \rangle}
outer class labels = {\langle keys \rangle}
change class labels = {\langle keys \rangle}
change inner class labels = {\langle keys \rangle}
change outer class labels = {\langle keys \rangle}
```

Inner class labels specifically applies to class labels that are inside the node, outer class labels specifically applies to ones outside it:

```
b
    (a) (a) (c)
    (begin{sseqpage}[ no axes, classes = { inner sep = 1pt },
        label distance = 2pt,
        outer class labels = { red },
        inner class labels = { red },
        inner class labels = { blue } ]
        \class["a", "b" above](0,0)
        \class["a", "c" right](1,0)
        \end{sseqpage}
```

```
edge labels = {\langle keys \rangle}
differential labels = {\langle keys \rangle}
struct line labels = {\langle keys \rangle}
change edge labels = {\langle keys \rangle}
change differential labels = {\langle keys \rangle}
change struct line labels = {\langle keys \rangle}
```

## 6.1 Style-like options

The options are not styles, but can be modified in the same set of places (namely, anywhere):

#### label distance = $\langle dimension \rangle$

This sets the default distance from a class to an outer label. There are also variants like above label distance corresponding to above, below, left, right, above left, above right, below left, and below right.

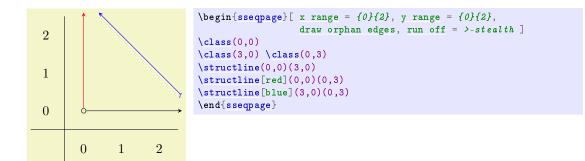
```
run off = \langle start tip \rangle - \langle end tip \rangle
```

```
run off struct lines = \langle start tip \rangle - \langle end tip \rangle
run off differentials = \langle start tip \rangle - \langle end tip \rangle
```

(initially  $\dots \dots$ ) (initially  $\dots \dots$ )

Change the default behavior of run off edges for either all edges, just structure lines, or just differentials respectively. Local arrowhead options override this.

If an edge runs off the edge of the clipping, SPECTRALSEQUENCES automatically add an arrowhead to indicate that the edge continues. This option controls which arrow head is added if the start or end of an edge runs off the page.



class label handler =  $\langle function \rangle$ 

The value of class label handler is a function that is applied to all labels before displaying them. It should put its output into \result. This is intended to help with code reusability. Because these handlers may crash or have annoying side-effects on some input, you may want to toggle the value of this command on and off. To turn this off for the rest of the current spectral sequence you can say \sseqset{class label handler = {}}. You can also use the class label handler key in a {scope}.

The main function SPECTRALSEQUENCES provides for use here is  $SseqNormalizeMonomial{#1}$ . This makes it convenient to translate expressions with polynomial labels. You can write your own handlers if your  $T_EX$  programming skills are sufficient. Let me know if there are any other functions that you want here, and if you implement them yourself, please send me your implementation. Here is an example of a function that evaluates an arithmetic expression:

1		21)	<pre>\begin{sseqpage}[     class label handler = { \SseqParseInt\result{#1} } ]</pre>
0	2		\class["1+1"](0,0) \class["1+2*(1+3*(4-1))"](1,1) \end{sseqpage}
	0	1	

Here's an example using \SseqNormalizeMonomial:

3	$lpha^3$	$lpha^3 y$	$lpha^3 y^2$	$lpha^3y^3$	<pre>\NewSseqGroup \test {m} {     \class["1#1"](0,0)     \class["\alpha#1"](0,1)     \["#1"1"1"1"1"1"1"1"1"1"1"1"1"1"1"1"1"1"1</pre>
2	$lpha^2$	$y\alpha^2$	$\alpha^2 y^2$	$y^3 lpha^2$	\class["y#1"](1,0) \class["\alpha y#1"](1,1) }
1	α	$\alpha y$	$lpha y^2$	$lpha y^3$	<pre>\begin{sseqpage}[     class label handler = { \SseqNormalizeMonomial{#1} },     classes = { draw = none }, class labels = { font = \small } ]</pre>
0	1	y	$y^2$	$y^3$	<pre> \test[red](2,0){y^2} \test[orange](2,2){\alpha^2y^2} \test[blue](0,0){\slube22}</pre>
	0	1	2	3	<pre>\test[blue](0,2){\alpha^2} \end{sseqpage}</pre>

Here is another example which demonstrates a useful idiom for drawing Serre spectral sequences. For a more complete example, see example\_KF3n.tex. Note the use of braces in  $\{Sq^1\iota_2\}$ . Without braces, SseqNormalizeMonomial will simplify  $Sq^1xSq^2x$  into  $S^2q^3x^2$ , which is obviously undesirable, so the correct way to input this is  $\{Sq^1x\}\{Sq^2x\}$ . Unfortunately, foreach strips a pair of braces from its arguments, so you need to put two pairs of braces.

4	$x^2$		$x^2\iota_2$	$x^2 S q^1 \iota_2$	$x^2 \iota_2^2$	<pre>\begin{sseqpage}[     xscale = 1.4,     classes = { draw = none },     class label handler = {\SseqNormalizeMonomial{#1}} ]</pre>
3	$\alpha x$		$\alpha x \iota_2$	$\alpha x Sq^1 \iota_2$	$\alpha x \iota_2^2$	foreach x/xlabel in
2	x		$x\iota_2$	$xSq^1\iota_2$	$x\iota_2^2$	<pre>{ 0/1, 2/\iota_2, 3/{{Sq^1\iota_2}}, 4/\iota_2^2 } \foreach \y/\ylabel in { 0/1, 1/\alpha, 2/x, 3/\alpha x, 4/x^2 } {</pre>
1	α		$\alpha \iota_2$	$\alpha Sq^1\iota_2$	$\alpha \iota_2^2$	<pre>\class["\ylabel\xlabel"] (\x,\y) }</pre>
					2	\end{sseqpage}
0	1		$\iota_2$	$Sq^1\iota_2$	$\iota_2^2$	
	0	1	2	3	4	

#### class name handler = $\langle function \rangle$

The value of class name handler is a function that is applied to all names before using them. It should put its output into \result. The main functions intended for use here are \SseqAHSSNameHandler and \SseqNormalizeMonomial, though you can make your own. This is applied both when you name the class, as in \class[name=a](\meta{coordinate}) and when you refer to a class by name, as in \structline(a)(b). One advantage if you are using \SseqNormalizeMonomial is that you can ensure that xy and yx refer to the same class:

$\left  \begin{array}{c} \circ^{-} xy^2 \\ \circ^{-} xy \end{array} \right _{\circ^{-}} xy \circ$	<pre>\SseqNormalizeMonomialSetVariables{xy} \begin{sseqpage}[ class name handler = \SseqNormalizeMonomial</pre>
 0 1	<pre>\structline(yx)(yyx) \end{sseqpage}</pre>

The next page is an example drawing the Atiyah Hirzebruch spectral sequence computing  $KO^*\mathbb{R}P^8$ .

```
class name prefix = \langle prefix \rangle
class name postfix = \langle postfix \rangle
```

These keys add respectively a prefix or a postfix to all names of all classes in the scope. This is applied both when you name the class, as in \class[name=a](\meta{coordinate}) and when you refer to a class by name, as in \structline(a)(b). The prefix and postfix are added to the command before the class name handler is applied, so if you say name=\meta{the name} then the name actually given to the class is the value of \result after saying

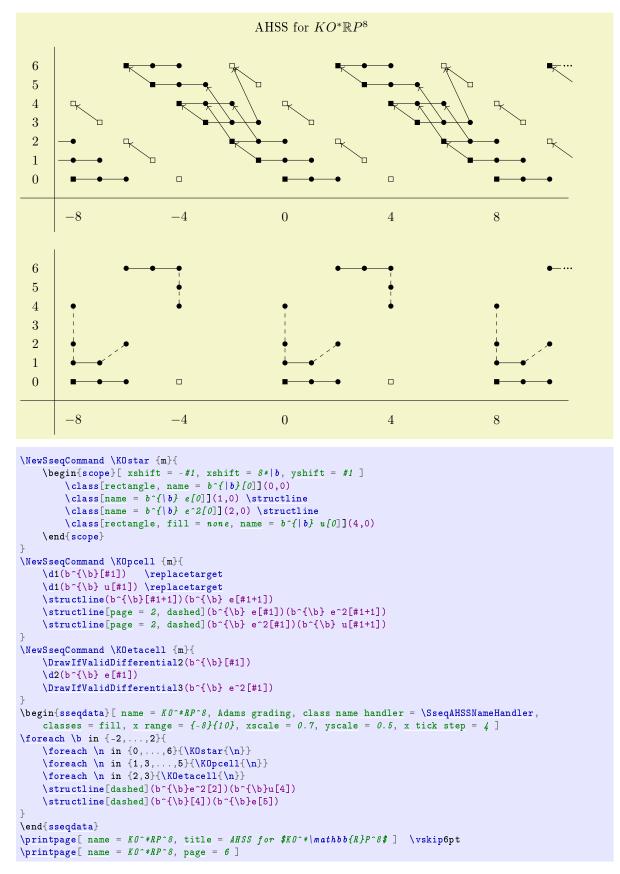
\classnamehander{\meta{name prefix}\meta{the name}\meta{name postfix}}

# 7 Global Options

These options can only be set at the beginning of a {sseqdata} or {sseqpage} environment. When it makes sense, you can also set a default value using \sseqset. Generally, these options either modify the plot style or the logic for the spectral sequence.

**name** =  $\langle sseq \ name \rangle$ 

This option must be used with the {sseqdata} environment where it indicates the name of the spectral sequence, which will be used with the {sseqpage} environment or \printpage command to draw the



An AHSS using class name handler =  $\SeqAHSSNameHandler$  :

spectral sequence. The name used in a {sseqdata} environment must be new unless the environment is used with the update existing key in which case the {sseqdata} environment will add to the existing spectral sequence. It is optional when used with {sseqpage}, and if included the name given must be the name of an existing spectral sequence.

#### **page** = $\langle page \ number \rangle - \langle page \ max \rangle$ (initially 0)

This key is for {sseqpage} and \printpage. It specifies which page of the spectral sequence is to be printed. On page r, all \classes that are not hit by differentials on pages less than r will be printed, as well as all \structlines whose source and target classes are both printed on page r, and all differentials of length exactly r. The special value page = 0 prints all classes, differentials, and structure lines but no extensions. The special value page=\infty will draw the infinity page with extensions.

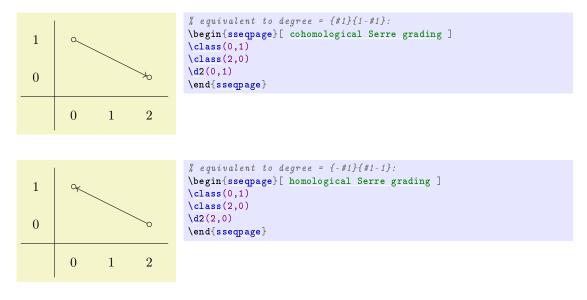
If you use this key with a range, e.g., page=2--5, then all differentials in that range of lengths will be drawn, so in the example differentials of length greater than or equal to 2 and less than or equal to 5 are drawn. The larger number only changes which differentials are drawn, classes and structlines are drawn as if the page was the small endpoint of the range. If you use 0 for the  $\langle page max \rangle$ , then all differentials longer than  $\langle page number \rangle$  will be drawn, e.g., page=5---0 draws all differentials of length at least 5, but no extensions. Using page=5---infty will draw all differentials of length at least 5 and also all extensions whose endpoint classes are in the final generation on page 5.

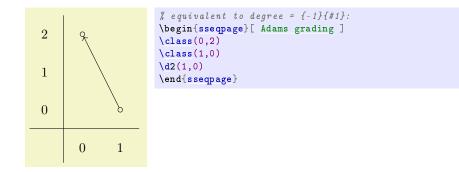
#### degree = { $\langle x \ degree \rangle$ }{ $\langle y \ degree \rangle$ } cohomological Serre grading homological Serre grading Adams grading

Specifies the degree of differentials. The  $\langle x \ degree \rangle$  and  $\langle y \ degree \rangle$  should both be mathematical expressions in one variable #1 that evaluate to integers on any input. They specify the x and y displacement of a page #1 differential. In practice, they will be linear expressions with #1 coefficient 1, -1, or 0.

The degree option must be given before placing any differentials. It can be specified at the beginning of the {sseqdata} environment, at the beginning of the {sseqpage} environment if it is being used as a standalone page, or as a default by saying \sseqset{degree = \marg{x degree}\marg{y degree}} or \sseqset{Adams grading} outside of the {sseqdata} and SPECTRALSEQUENCES environments.

You can make a named grading convention by saying  $sseqset{mygrading/.sseq grading = {<math>x degree$ }}. Then later passingmy grading to a spectral sequence is equivalent to sayingdegree =  $marg{x degree} marg{y degree}$ . The following grading conventions exist by default:

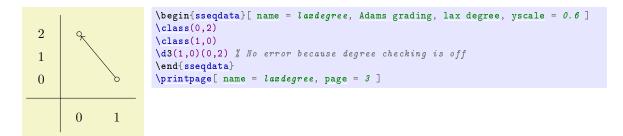




# strict degree

### lax degree

If the degree is strict, then LATEX will throw an error if you try to specify a differential that doesn't have the proper grading. The degree is strict by default.



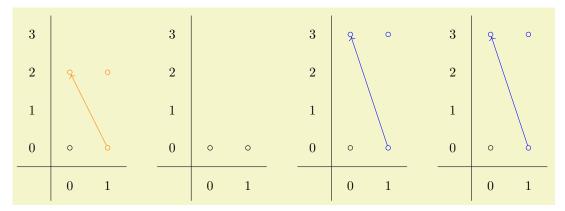
#### update existing

This key is only for the {sseqdata} environment. It specifies that the current {sseqdata} environment is adding data to an existing spectral sequence. If you don't pass this key, then giving a {sseqdata} environment the same name as a different {sseqdata} environment will cause an error. This is intended to help you avoid accidentally reusing the same name.

#### keep changes = $\langle boolean \rangle$

#### (default true) (initially false)

This option is only for the {sseqpage} environment, and only works when a name is provided. This option specifies that all of the commands in the current {sseqpage} environment should be carried forward to future pages of the same named spectral sequence. For example:



```
\begin{sseqdata}[ name = keep changes example, Adams grading, y range = {0}{3}]
\class(0.0)
\class(1,0)
\end{sseqdata}
\begin{sseqpage}[ name = keep changes example, sseq = orange ]
\class(0,2)
\class(1.2)
\classoptions[orange](1,0)
d2(1,0)
\end{sseqpage} \qquad
\printpage[ name = keep changes example, page = 2 ] \qquad
\begin{sseqpage}[ name = keep changes example, sseq = blue, keep changes ]
\class(0.3)
\class(1,3)
\classoptions[blue](1,0)
d3(1.0)
\end{sseqpage} \qquad
\printpage[ name = keep changes example, page = 3 ]
```

Note that the orange classes and differential do not persist because the keep changes option is not set in the first {sseqpage} environment, but the blue classes and differential do, since the keep changes option is set in the second {sseqpage} environment.

#### no differentials draw differentials

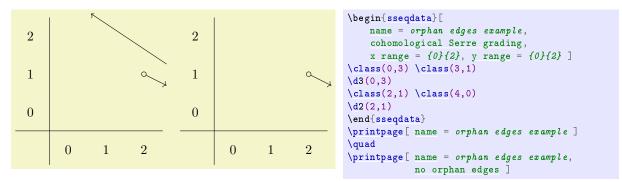
# The option no differentials suppresses all of the differentials on the current page, whereas draw differentials causes the page appropriate differentials to be drawn. This is useful for explaining how the computation of a spectral sequence goes, or if you want to display one of the edges of the spectral sequence, like in example\_KF3n.tex.

#### no struct lines draw struct lines

The option **no struct lines** suppresses all of the structure lines on the current page, whereas the option **draw struct lines** causes the page appropriate structure lines to be drawn.

#### no orphan edges draw orphan edges

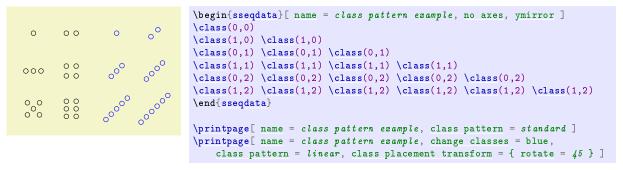
An edge is an "orphan" if both its source and target lie off the page. By default these are drawn, but with the option no orphan edges they are not. If the option no orphan edges has been set, draw orphan edges undoes it.



#### class pattern = $\langle class \ pattern \ name \rangle$

(initially standard)

This key specifies the arrangement of multiple classes at the same coordinate. The default value is standard.



You can add new class patterns using \SseqNewClassPattern:

 $SseqNewClassPattern{\langle class pattern name \rangle}{\langle offsets \rangle}$ 

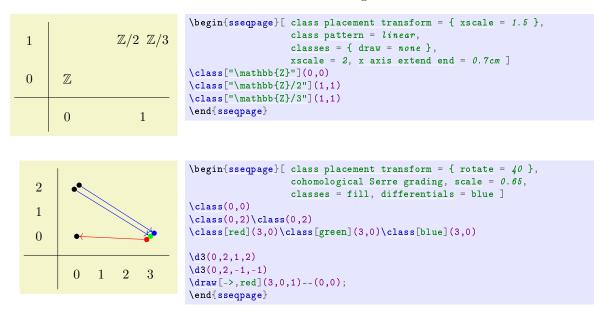
Creates a new class pattern. For example, the linear class pattern is created using the command:

```
\SseqNewClassPattern{linear}{
    (0,0);
    (-0.13,0)(0.13,0);
    (-0.2,0)(0,0)(0.2,0);
    (-0.3,0)(-0.1,0)(0.1,0)(0.3,0);
    (-0.4,0)(-0.2,0)(0,0)(0.2,0)(0.4,0);
    (-0.5,0)(-0.3,0)(-0.1,0)(0.1,0)(0.3,0)(0.5,0);
}
```

For instance the third row indicates that if there are three classes at the position (x,y) they should be printed at (x-0.2,y), (x,y), and (x+0.2,y). You can give as many rows as you like; SPECTRALSEQUENCES will throw an error if there are more classes in any position than the maximum number that your class pattern can handle – for instance, the linear class pattern can handle up to six classes based on this definition.

#### class placement transform = { $\langle transform \ keys \rangle$ } add class placement transform = { $\langle transform \ keys \rangle$ }

The option class placement transform allows the user to specify a TikZ coordinate transform to adjust the relative position of multiple nodes in the same (x, y) position. The class placement transform key overrides the previous value of transformations, the add class placement transform just adds the new transformation to the end of the list. This coordinate transform can only involve rotation and scaling, no translation. Specifying a scaling factor helps if the nodes are too large and overlap. In some cases a rotation makes it easier to see which class is the target of a differential.



With multiple large class labels, the best option is to arrange the classes vertically:

2	$ \begin{array}{c} \iota_2 P^1 \iota_3 \\ \\ \iota_2 \iota_3 \beta \iota_3 \end{array} $	$\iota_2 \beta P^1 \iota_3$ $\iota_2 P^1 \beta \iota_3$ $\iota_2 (\beta \iota_3)^2$	<pre>\begin{sseqpage}[ classes = {draw = none }, xscale = 2, yscale=1.55,</pre>
1			<pre>\class["\iota_2\iota_3\beta\iota_3"](7,2)</pre>
			\class["\iota_2P^1\iota_3"](7,2)
	$P^1\iota_3$	$\beta P^1 \iota_3$	$class["(beta\iota_3)^2"](8,0)$
0	F 13	$P^1 \beta \iota_3$	<pre>\class["P^1\beta\iota_3"](8,0)</pre>
0	$\iota_3\beta\iota_3$		<pre>\class["\beta P^1\iota_3"](8,0)</pre>
	03/203	$(eta\iota_3)^2$	$class["\iota_2(\beta\iota_3)^2"](8,2)$
			<pre>\class["\iota_2P^1\beta\iota_3"](8,2)</pre>
	7	8	$\class["\iota_2\beta P^1\iota_3"](8,2)$
			\end{sseqpage}

math nodes =  $\langle boolean \rangle$ 

(default true) (initially true)

This key instructs SPECTRALSEQUENCES to put all labels in math mode automatically.

## 7.1 Global coordinate transformations

Of the normal TikZ coordinate transformations, only the following can be applied to a SPECTRALSEQUENCES chart:

```
scale = \langle factor \rangle

xscale = \langle factor \rangle

yscale = \langle factor \rangle

xmirror

ymirror
```

Scale the chart by  $\langle factor \rangle$ . Under normal circumstances, you can tell TikZ to mirror a chart by saying, for instance, xscale = -1, but SPECTRALSEQUENCES needs to be aware that the chart has been mirrored in order to draw the axes correctly. Thus, if you want to mirror a spectral sequence, use the xmirror and ymirror options as appropriate.

**rotate** =  $\langle angle \rangle$ 

It probably won't look great if you pick an angle that isn't a multiple of 90 degrees.

#### 7.2 Plot options and axes style

x range =  $\{\langle x \min \rangle\} \{\langle x \max \rangle\}$ y range =  $\{\langle y \min \rangle\} \{\langle y \max \rangle\}$ 

These options set the x range (respectively y range) to be a specific interval. By default, if no range is specified then the range is chosen to fit all the classes. If an x range is specified but no y range, then the y range is chosen to fit all the classes that lie inside the specified x range, and vice versa. The values must be integers - if you want to extend the x axis a noninteger amount, try using x axis start extend or x axis end extend.

```
range check standard (default)
range check sideways
range check off
```

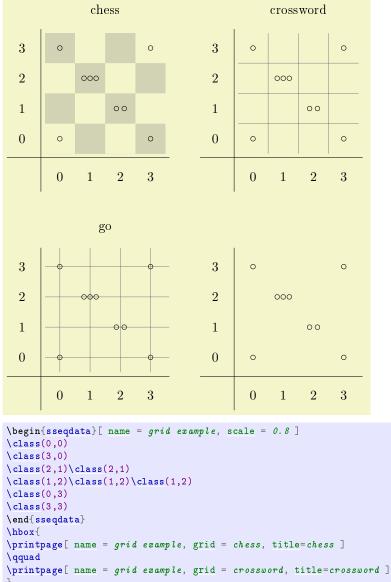
These options control the range checking behavior.

By default SPECTRALSEQUENCES will try to compute whether the chart fits onto the page (without causing overfull boxes). The computation isn't perfectly accurate and it assumes that the entire page is available for the chart to use up, so for instance if the chart is indented because of \textindent or not at the top of the page, this might give overly large values. Also, the values computed aren't perfectly accurate.

If the range check is not desirable, you can use range check off. If the diagram is being placed onto the page rotated 90 degrees, then use range check sideways. Inside of a {sideways} environment from the rotating package, this is the default.

grid = (grid type)
grid color = (color)
grid step = (positive integer)
x grid step = (positive integer)
y grid step = (positive integer)

Makes SPECTRALSEQUENCES draw a grid. The grid types and a significant part of the code that produces them were stolen from the sseq package.



```
\printpage[ name = grid example, grid = chess, title=chess ]
\qquad
\printpage[ name = grid example, grid = crossword, title=cros
}
\vskip20pt
\hbox{
\printpage[ name = grid example, grid = go, title=go ]
\qquad
\printpage[ name = grid example, grid = none ]
```

It is possible to make your own grid type by defining the command \sseq@grid@yourgridname to draw a grid.

It is a known problem that acrobat reader displays grids very dark and thick. This is caused by the enhance thin lines "feature" of Acrobat reader. You can turn it off globally by going into the acrobat reader preferences window and unchecking the "Enhance thin lines" checkbox in the "Rendering" section. Unfortunately, there is no way to instruct Acrobat Reader to not apply this feature to a particular document. This has apparently been annoying graphic designers for over a decade.

The grid color option changes the color of the grid; the default value is **gray**. The grid step keys change the grid step.

```
title = \langle text \rangle
title style = \langle keys \rangle
x label = \langle text \rangle
y label = \langle text \rangle
x label style = \langle keys \rangle
y label style = \langle keys \rangle
label style = \langle keys \rangle
```

This make chart labels.



Note that if you make multiple versions of the same chart and some of the charts have labels and others don't, they might not align the way you want. An easy solution to this is to use  $\path[background]$  (min x, min y) -- (max x, max y); where the coordinates are below and to the left, respectively above and to the right, of everything else drawn in any picture. This makes the bounding boxes for all of the pictures the same size, so that they line up even if the exact collection of things drawn changes. See the example at the end of the background key for an illustration of this.

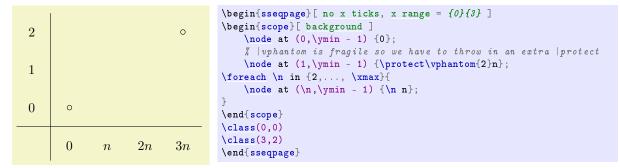
no title draw title no x label no y label no labels draw x label draw y label draw labels

Suppress or unsuppress the title, x label, y label, or both x and y labels, respectively.

no x ticks no y ticks no ticks draw x ticks draw y ticks draw ticks

Suppress axes ticks (the numbers next to the axes). Only matters if axes are drawn. You can make your own ticks using TikZ inside a  $\{scope\}$  environment with the background key. For instance,

you might want to label the axes as 0, n, 2n, ... You can achieve this as follows: (you can also use x tick handler).



х	tick	step	= $\langle positive \ integer \rangle$	
у	tick	step	= $\langle positive \ integer \rangle$	
ti	ick st	cep =	$\langle positive \ integer \rangle$	

Sets the interval between labels.

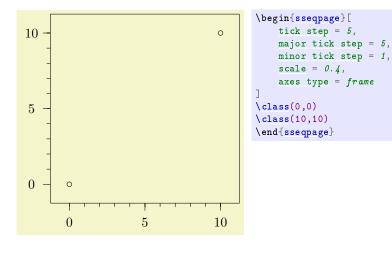
x tick offset = $\langle integer \rangle$	(initially 0)
y tick offset = $\langle integer \rangle$	(initially 0)
tick offset = $\langle integer \rangle$	(initially 0)

Sets the label offset – by default the ticks will always be the set of numbers that are 0 mod  $\langle tick \ step \rangle$ . Change it so that the ticks are the set of numbers that are  $\langle tick \ offset \rangle \mod \langle tick \ step \rangle$ .

(initially 1)
(initially 1)
(initially 1)

<b>x major tick step =</b> $\langle nonnegative integer \rangle$	(initially 0)
y major tick step = $\langle nonnegative \ integer \rangle$	(initially 0)
major tick step = $\langle nonnegative \ integer \rangle$	
x minor tick step = $\langle nonnegative \ integer \rangle$	(initially 0)
y minor tick step = $\langle nonnegative \ integer \rangle$	(initially 0)
minor tick step = $\langle nonnegative \ integer \rangle$	

If these are nonzero, they control the placement of tick marks on the axes. The value 0 prevents tick marks from being drawn. Uses x tick offset as an offset.



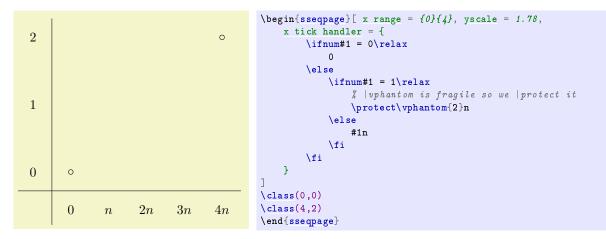
x tick style = { $\langle keys \rangle$ } y tick style = { $\langle keys \rangle$ } tick style = { $\langle keys \rangle$ }

Change the tick style:

1			0	<pre>\begin{sseqpage}[ tick style = { blue, font = \tiny } ] \class(0,0) \class(2,1) \end{sseqpage}</pre>
0	0			
	0	1	2	

x tick handler = $\langle function \rangle$	(initially #1)
y tick handler = $\langle function \rangle$	(initially #1)
tick handler = $\langle function \rangle$	(initially #1)

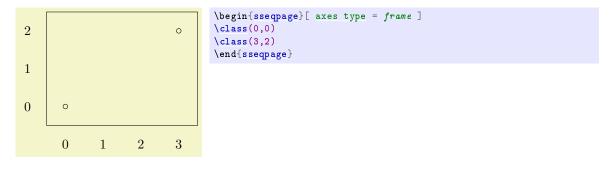
The value for x tick handler should be a function that takes in the current x value and outputs the appropriate tick. Correspondingly withy tick handler. The tick handler key sets both.



#### 7.3 Layout

x axis type = $\langle type \rangle$ y axis type = $\langle type \rangle$ axes type = $\langle type \rangle$	(initially border) (initially border) (initially border)
no x axis	
no y axis	
no axes	

The  $\langle type \rangle$  is either border, center, frame, or none. no axes is a shorthand for axes type=none. The border type is the default and puts the axes on the bottom and left of the picture. The center type by default places the axes to pass through (0,0); this can be modified using the x axis origin and y axis origin keys. See example\_KRAHSS.tex and example\_KUHFPSS.tex for examples where this is used. The frame type draws a frame around the entire chart:



x axis origin =  $\langle x \ value \rangle$ 

(initially 0)

y axis origin = $\langle y \ value \rangle$	(initially 0)
If you use <b>axes type = center</b> , these keys change the position of the axes. Ot	therwise, they are ignored.
x axis gap = $\langle dimension \rangle$ y axis gap = $\langle dimension \rangle$ axes gap = $\langle dimension \rangle$	(initially 0.5cm) (initially 0.5cm) (initially 0.5cm)
x tick gap = $\langle dimension \rangle$ y tick gap = $\langle dimension \rangle$	(initially 0.5cm) (initially 0.5cm)
<pre>x axis extend start = \langle dimension \rangle y axis extend start = \langle dimension \rangle x axis extend end = \langle dimension \rangle y axis extend end = \langle dimension \rangle x axis tail = \langle dimension \rangle y axis tail = \langle dimension \rangle </pre>	(initially 0.5cm) (initially 0.5cm) (initially 0.5cm) (initially 0.5cm) (initially 0.9cm) (initially 0.9cm)
x axis clip padding = $\langle dimension \rangle$ y axis clip padding = $\langle dimension \rangle$	(initially 0.1cm) (initially 0.1cm)
<pre>right clip padding = \langle dimension \rangle left clip padding = \langle dimension \rangle top clip padding = \langle dimension \rangle bottom clip padding = \langle dimension \rangle </pre>	(initially 0.1cm) (initially 0.1cm) (initially 0.1cm) (initially 0.1cm)

custom clip =  $\langle clip \ path \rangle$ 

Give a custom clipping. The clipping specified must be in the form of a valid TikZ path, for instance clip (0,0) rectangle (10,10);. This clipping is also applied to any grid and is used to draw ellipses on appropriate differentials or structure lines that go out of bounds and to determine whether a differential or structure line is an "orphan". It is not applied to any background elements, which is important because these are often used for axes labels and such that should lie outside of the clipping region. Weird things can happen with out of range edges if you provide an oddly shaped path.

#### $clip = \langle boolean \rangle$

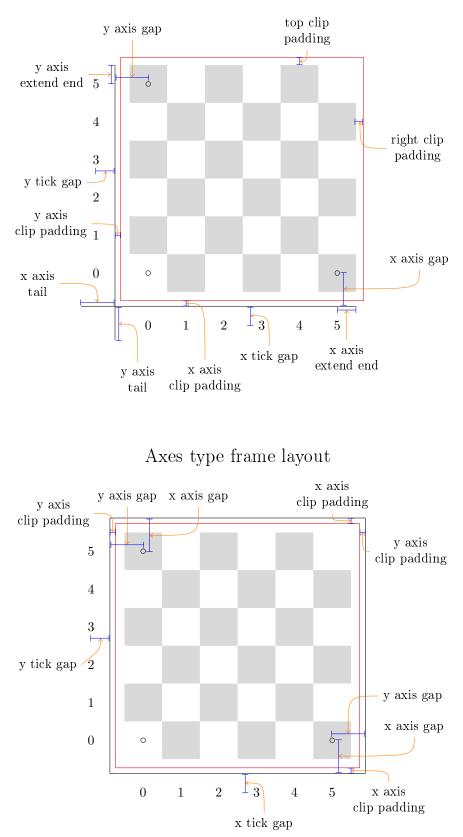
If this is false the spectral sequence chart won't be clipped. I'm not really sure why you would want that, but there might be some use case. Setting this to be false is not fully supported, and it's possible that weird things will happen with some of the edges that go out of range.

rotate labels =  $\langle boolean \rangle$ 

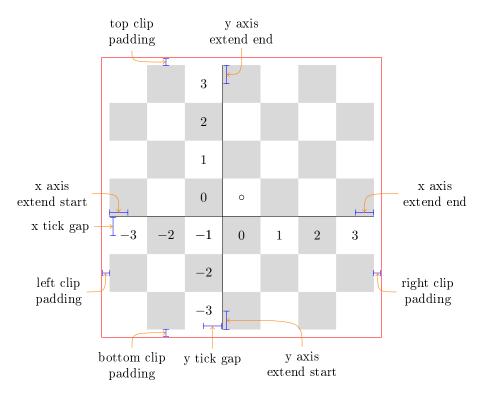
#### (default true) (initially false)

(default true) (initially true)

If you use rotate = 90 but also want the labels rotated (so that the whole chart is sideways) use this key.



# Axis type border layout



# Axes type center layout